



$$\begin{matrix} 1 & 1 \\ 1 & 1 \end{matrix} \Rightarrow \neg(\begin{matrix} 1 & 1 \\ 1 & 1 \end{matrix})$$



$$a \wedge b \rightarrow \neg(c \wedge d)$$

$$a \wedge b \rightarrow \neg c \vee \neg d$$

$$\neg(a \wedge b) \vee \neg c \vee \neg d$$

$$\neg a \vee \neg b \vee \neg c \vee \neg d$$

$$d \rightarrow (\neg a \vee \neg b \vee \neg c)$$

$$d \rightarrow \neg(a \wedge b \wedge c)$$

HALT

is there some input that makes my alg
run forever?

one
↓
Proposition
fixed

alg runs forever on some input

P

every
↑
Predicates
cut

_____x runs forever on _____y

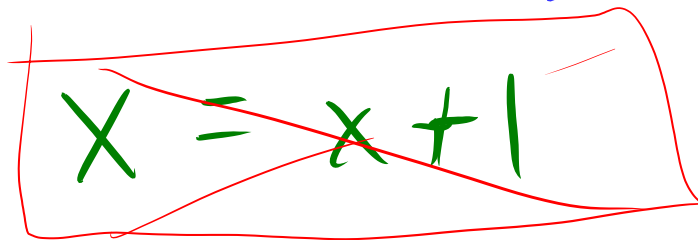
$P(x, y)$

Variables

- Code changeable named value

$$x = x + 1$$

- math unchanging unknown


$$~~x = x + 1~~$$

- Stats

my algorithm is faster than yours

_____ is faster than _____

my alg faster on input _____

_____ is faster than _____ on _____

_____ is _____ than _____ on _____

Types: Person

$L(x, y)$: $\text{---}_x \text{ loves } \text{---}_y$

m : Luther Tycheviorch

Everyone loves me $\overset{\text{bound}}{\uparrow}$

is there an x , $L(x, m) \wedge L(m, x)$
 $\underset{\text{unbound}}{\downarrow}$

$\forall x. L(x, m)$

$\exists x. L(x, m)$

$\neg \exists x. L(x, m)$

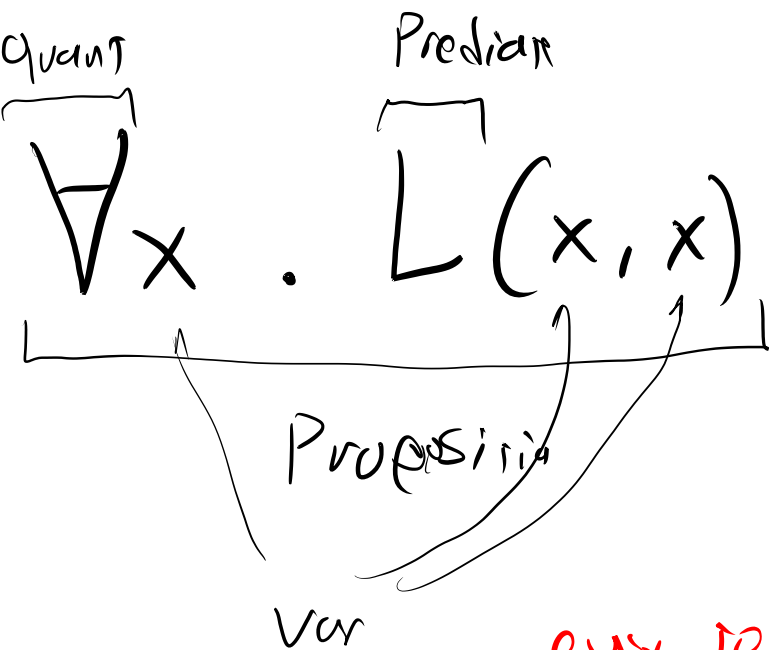
domain : set of all allowed values of variables

Variable
predicate

Quantifiers

 \forall

for all



easy to
disprove

 \exists

there exists

 $\exists x . L(x, x)$

easy to
prove

$$\forall x. P(x)$$

$$P(x_0) \wedge P(x_1) \wedge P(x_2) \wedge \dots \\ \dots P(x_{\text{last}})$$

$$\neg \forall x. P(x) \equiv \exists x. \neg P(x)$$

$$\neg \exists x. P(x) \equiv \forall x. \neg P(x)$$

$$\exists x. P(x)$$

$$P(x_0) \vee P(x_1) \vee P(x_2) \vee \dots \\ \dots P(x_{\text{last}})$$

$$\nexists \equiv \neg \exists$$