September 23 Slides Elizabeth Orrico

Agenda

Videos not playing

Predicate video

Predicate examples

Soft Intro to Quantifiers

About Domain...

Good to have in your back pocket

"if p, then q"
"if p, q"
"p is sufficient for q"
"q if p"
"q when p"
"a necessary condition for p is q"
"q unless ¬p"

"p implies q" "p only if q" "a sufficient condition for q is p" "q whenever p" "q is necessary for p" "q follows from p" "q provided that p"

Predicates and First-Order Logic

We can only do so much with atomic propositions. To say more interesting things, like:

All files that are larger than 1,000 blocks are to be moved to backup provided that they have not been referenced within the last 100 days and that they are not system files.

We need more.

Predicates and First-Order Logic

We can only do so much with atomic propositions. To say more interesting things, like:

- All files that are larger than 1,000 blocks are to be moved to backup provided that they have not been referenced within the last 100 days and that they are not system files.
- All system files that are either source code or have not been referenced with the last 300 days are to be moved to backup.
- Any user file that is larger than 10,000 blocks is to be compressed irrespective of the most recent reference date.

Predicates

[FOL stands for First Order Logic]

https://youtu.be/hq2VUc7isw8?list=PL_onPhFCkV QjXugm0ak5NYEeFL-OGcYj5&t=4

Predicates

- "A function that evaluates to True or False"
- "A proposition missing the noun(s)"
- "A proposition template"

Determine the predicate and the arguments of the following:

"Sam loves Diane"



"Sam loves Diane" Formalizes to L(Sam, Diane)

$$\frac{1}{x} \quad \text{loves} \quad = \ L(x, y)$$

$$\frac{1}{x} \quad \frac{1}{y} = L(x, y)$$

"Sam loves Diane" = L(Sam, Diane) "Diane doesn't love Sam" = ¬L(Diane, Sam) "I Love Lucy" = ????

$$\frac{1}{x} \quad \frac{1}{y} = L(x, y)$$

"Sam loves Diane" = L(Sam, Diane)
"Diane doesn't love Sam" = ¬L(Diane, Sam)
"I Love Lucy" = L(me, Lucy)
"Everyone Loves Raymond" = ????



"Sam loves Diane" = L(Sam, Diane) "Diane doesn't love Sam" = ¬L(Diane, Sam) "I Love Lucy" = L(me, Lucy)

"Everybody Loves Raymond" = $\forall x L(x, Raymond)$

Universal Quantifier (\forall)

∀ = "for all" or "given any"
It expresses that a propositional function can be satisfied by
every member of the domain

Domain: People L(x, y) = x loves y

∀x L(x, Raymond) means ???

Universal Quantifier (\forall)

∀ = "for all" or "given any"
 It expresses that a propositional function can be satisfied by
 every member of the domain.

Domain: People L(x, y) = x loves y

∀x L(x, Raymond) means "For all people x, each one loves Raymond" "Given any person x, that person loves Raymond" "Every person loves Raymond"



"Everybody Loves Raymond" = ∀x L(x, Raymond)
"Everybody does not love Chris" = ????

Domain: People L(x, y) = *x loves y* **"Everybody does not love Chris"**

How could I rephrase this?

Domain: People L(x, y) = x loves y "Everybody does not love Chris"

How could I rephrase this?

"For all people, each one does not love Chris" "There does not exist one person who loves Chris"

Domain: People L(x, y) = x loves y"Everybody does not love Chris" How could I formalize this? "For all people, each one does not love Chris" $\forall x \neg L(x, Chris)$

¬(∀x L(x, Chris)) = ???

Domain: People L(x, y) = x loves y "Everybody does not love Chris"

How could I formalize this?

"For all people, each one does not love Chris" ∀x ¬L(x, Chris)

Domain: People L(x, y) = *x loves y* **"Everybody does not love Chris"**



How could I formalize this?

"There does not exist one person who loves Chris"

Existential Quantifier (3)

Ξ = "there exists", "there is at least one", or "for some" It expresses that a propositional function can be satisfied by at least one member of the domain.

Domain: People L(x, y) = x loves y

¬ ∃ x L(x, Chris) means "There does not exist one person who loves Chris"

Existential Quantifier (3)

∃ = "there exists", "there is at least one", or "for some"
It expresses that a propositional function can be satisfied by
at least one member of the domain.

Domain: People L(x, y) = x loves y

¬ ∃ x L(x, Chris) means "There does not exist one person who loves Chris"

(might also see ∄)

\exists and \forall

Domain: People L(x, y) = x loves y

 $\neg \exists x L(x, Chris)$ means "There does not exist one person who loves Chris" $\forall x \neg L(x, Chris)$ means "For all people, each one does not love Chris"

 $\neg \exists x L(x, Chris) \equiv \forall x \neg L(x, Chris)$

Another Example

$$Q(x) = (x^2 \ge x)$$

Q(4) = <mark>???</mark>

Q(-3) = <mark>???</mark>

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$$Q(x) = (x^2 \ge x)$$

Q(4) = <mark>???</mark>

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To the whiteboard for why domain matters!