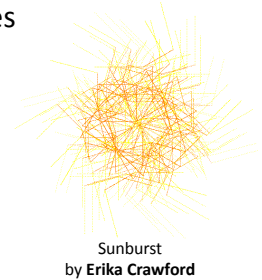


## Lecture 15: Running Practice



## Menu

- Any Questions from Last Week?
- Exam 1
- Practice Analyzing Procedures
- Finest Fractalists



## Exam 1

- Handed out at end of Friday's class, due at the beginning of Wednesday's class
- Open non-human resources except for Scheme interpreters but no help from other people
- Covers everything through this Wednesday including:
  - Lectures 1-16, Course Book Chapters 1-8, PS 1-4
- Sample exams from previous years: if you can do well on Spring 2009 Exam 1, you should do well on our Exam 1 (of course, questions will be different!)
- Review Session, Wednesday 6:30 in Olsson 001

## Running Time Practice

From ps3:

```
(define (flatten-commands ll)
  (if (null? ll) ll
      (if (is-system-command? (car ll))
          (cons (car ll) (flatten-commands (cdr ll)))
          (flat-append (car ll) (flatten-commands (cdr ll))))))
```

What is the asymptotic running time of **flatten-commands**?

First: determine running times of all the procedures applied in flatten-commands.

## Flatten Running Time

From ps3:

```
(define (flatten-commands ll)
  (if (null? ll) ll
      (if (is-system-command? (car ll))
          (cons (car ll) (flatten-commands (cdr ll)))
          (flat-append (car ll) (flatten-commands (cdr ll))))))
```

First: determine running times of all the procedures applied in flatten-commands.

**null?**, **car**, **cons**, **cdr** – we already know there are constant time

What about **is-system-command**?

## is-system-command?

```
(define (is-system-command? lcommand)
  (or (is-forward? lcommand)
      (is-rotate? lcommand)
      (is-offshoot? lcommand)))
```

**or** is a special form:

OrExpression ::= (**or** MoreExpressions)

To evaluate (**or** Expr<sub>1</sub> MoreExpressions):

1. Evaluate Expr<sub>1</sub>.
2. If it evaluates to a non-false value, that is the value of the or expression. None of the other sub-expressions are evaluated. Otherwise, the value of the or-expression is the value of (**or** MoreExpressions)

The value of (**or**) is **false**.

## is-system-command?

```
(define (is-system-command? lcommand)
  (or (is-forward? lcommand)
      (is-rotate? lcommand)
      (is-offshoot? lcommand)))
```

**is-system-command?** has constant running time: it involves applications of at most three constant time procedures.

```
(define (is-forward? lcommand)
  (eq? (car lcommand) 'f))
```

```
(define (is-rotate? lcommand)
  (eq? (car lcommand) 'r))
```

```
(define (is-offshoot? lcommand)
  (eq? (car lcommand) 'o))
```

Each of these procedures has constant running time: they involve only applications of constant time procedures **eq?** and **car**.

## Flatten Running Time

From ps3:

```
(define (flatten-commands ll)
  (if (null? ll) ll
      (if (is-system-command? (car ll))
          (cons (car ll) (flatten-commands (cdr ll)))
          (flat-append (car ll) (flatten-commands (cdr ll))))))
```

First: determine running times of all the procedures applied in flatten-commands.

**null?**, **car**, **cons**, **cdr**, and **is-system-command?** are constant time

## Running Time Practice

Remember: we care about the size of the input.  
Introduce variables:

```
(define (flat-append lst ll)
  (if (null? lst) ll
      (cons (car lst) (flat-append (cdr lst) ll))))
```

$N_1$  = number of elements in first input list (lst)  
 $N_2$  = number of elements in second input list (ll)

What is the asymptotic running time of **flat-append**?

Other than the recursive call, each execution is constant time:

**null?**, **car**, **cons**, **cdr**, are constant time

How many recursive calls are there?

$N_1$  (the number of elements in the first input list)

What is the running time?

The asymptotic running time of flat-append is in  $\theta(N_1)$  where  $N_1$  is the number of elements in the first input.

Note: **flat-append** is the same as **list-append**! (Stupid to define this as a separate procedure and name it **flat-append**.)

## Flatten Running Time

```
(define (flatten-commands ll)
  (if (null? ll) ll
      (if (is-system-command? (car ll))
          (cons (car ll) (flatten-commands (cdr ll)))
          (flat-append (car ll) (flatten-commands (cdr ll))))))
```

First: determine running times of all the procedures applied in flatten-commands.

**null?**, **car**, **cons**, **cdr**, and **is-system-command?** are constant time  
**flat-append** has running time in  $\theta(N_1)$  where  $N_1$  is the number of elements in the first input.

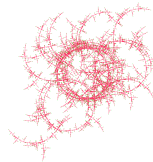
Second: determine running time for each application **except** for recursive call.

Need to consider both paths:

```
(if (is-system-command? (car ll))
    (cons (car ll) (flatten-commands (cdr ll)))
    (flat-append (car ll) (flatten-commands (cdr ll))))
```

## Paths to Flattening

```
(if (is-system-command? (car ll))
    (cons (car ll) (flatten-commands (cdr ll)))
    (flat-append (car ll) (flatten-commands (cdr ll))))
```



Each recursive call involves  $\theta(P)$  work where  $P$  is the number of elements in (car ll).  
Each recursive call reduces the number of elements in ll by one.

Teamwork by  
Rose Cunnion and  
Lucy Raper

For input list that is all lists of length  $P$ :  
**flatten-commands** has running time in  $\theta(QP)$  where  $Q$  is the number of sub-lists (of length  $P$ ) in the input list.

to be continued Wednesday...

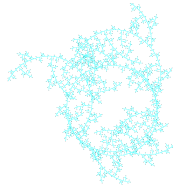
## Fractal Finalists

Blowin' in the Wind

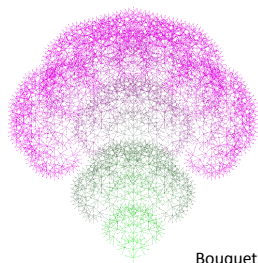


1

TwistOnTiffany's

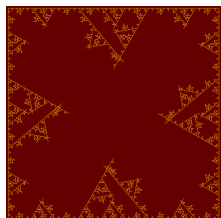


2



3

Bouquet



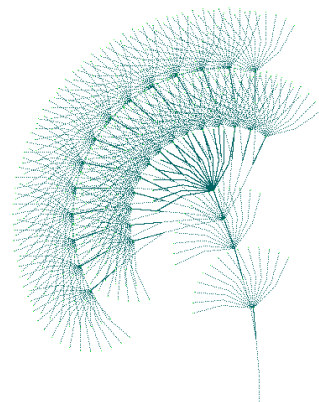
4 CrissCross



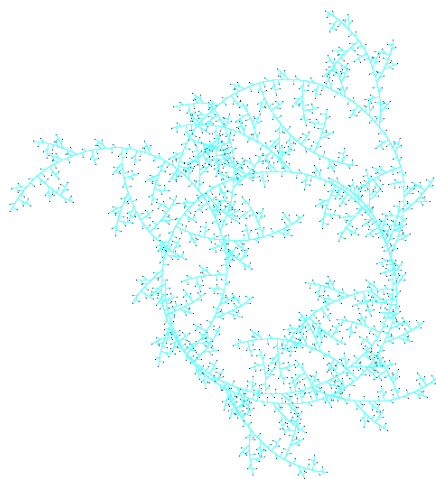
5 Ascension



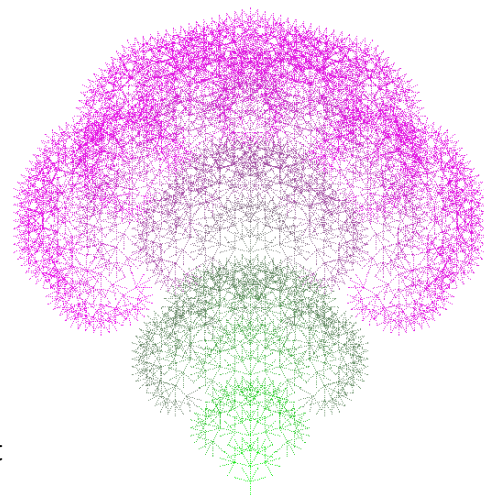
6 August Wheat



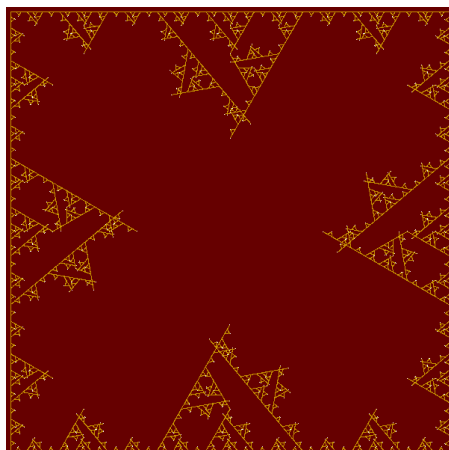
Blowin' in the Wind



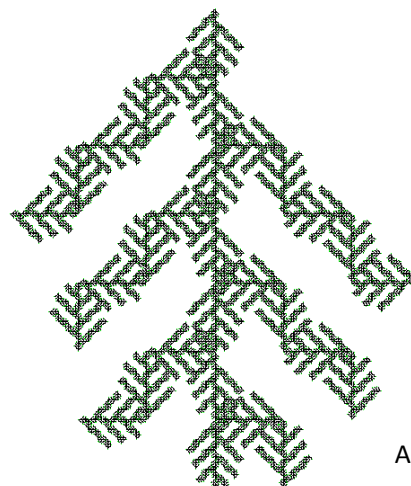
TwistOnTiffany's



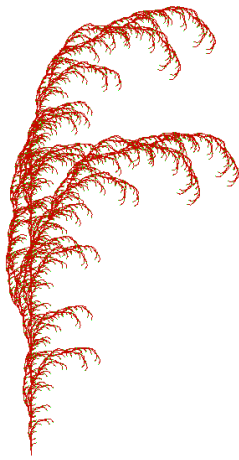
Bouquet



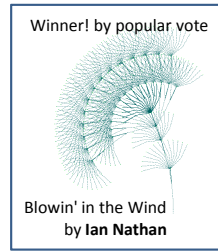
CrissCross



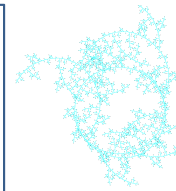
Ascension



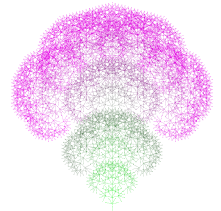
August Wheat



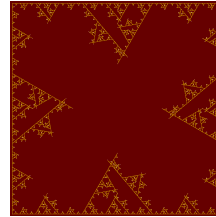
Blowin' in the Wind  
by Ian Nathan



TwistOnTiffany's  
by Brittney Blanks



Bouquet  
by Richard McPherson



CrissCross  
by Trygve Loken and Andrew Crute



Ascension  
by Siddharth Rajagopalan



August Wheat  
by Melissa Bailey

## Charge

- PS4 is due Wednesday
- Exam 1 is out Friday, due next Wednesday
- Exam Review, Wednesday 6:30 in Olsson 001

## Returning PS3

