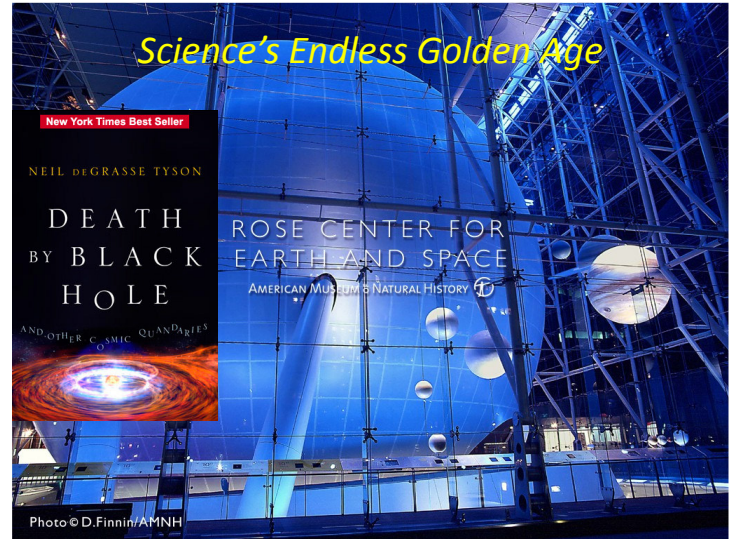




## Lecture 26: Sex, Religion, and Politics

University of  
Virginia  
cs1120 Fall 2009  
David Evans



“If you’re going to use your computer to simulate some phenomenon in the universe, then it only becomes interesting if you change the scale of that phenomenon by at least a factor of 10. ... For a 3D simulation, an increase by a factor of 10 in each of the three dimensions increases your volume by a factor of 1000.”

What is the asymptotic running time for simulating the universe?

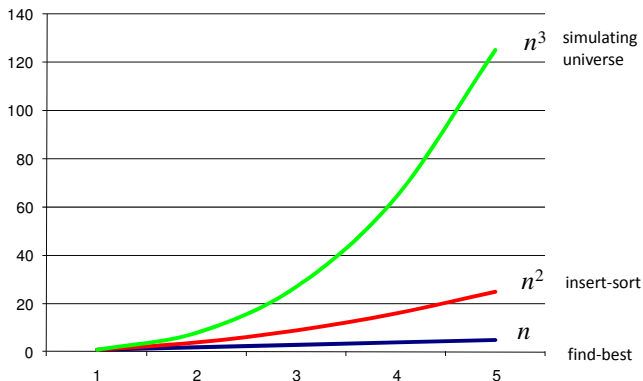
## Simulating the Universe

Work scales linearly with volume of simulation: scales cubically with scale

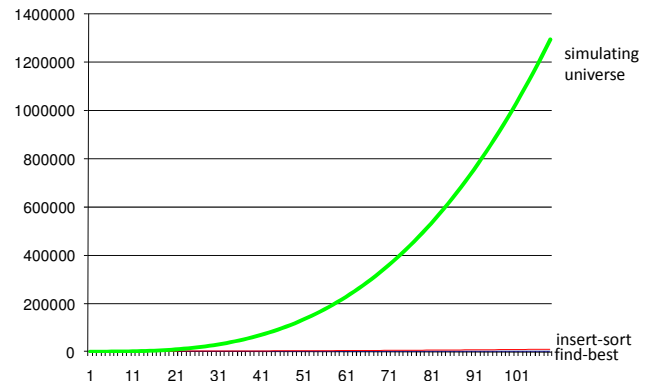
$$\Theta(n^3)$$

When we double the scale of the simulation, the work octuples! (Just like oceanography octopi simulations)

## Orders of Growth



## Orders of Growth



## Astrophysics and Moore's Law

- Simulating universe is  $\Theta(n^3)$
- Moore's "law": computing power doubles every 18 months
- Dr. Tyson: to understand something new about the universe, need to scale by 10x

How long does it take to know *twice* as much about the universe?

## Knowledge of the Universe

```
import math

# 18 months * 2 = 12 months * 3
yearlyrate = math.pow(4, 1.0/3.0) # cube root

def computing_power(nyears):
    if nyears == 0: return 1
    else: return yearlyrate * computing_power(nyears - 1)

def simulation_work(scale):
    return scale ** 3

def knowledge_of_universe(scale):
    return math.log(scale, 10) # log base 10
```

## Knowledge of the Universe

```
def computing_power(nyears):
    return yearlyrate ** nyears

def simulation_work(scale):
    return scale ** 3

def knowledge_of_universe(scale):
    return math.log(scale, 10) # log base 10

def relative_knowledge_of_universe(nyears):
    scale = 1
    while simulation_work(scale + 1) <= 1000 * computing_power(nyears):
        scale = scale + 1
    return knowledge_of_universe(scale)
```

## While Loop

**Statement ::= while Expression: Block**

```
x = 1
res = 0
while x < 100:
    res = res + x
print res
```

```
(define (while pred body)
  (if (pred)
      (begin
        (body)
        (while pred body))))

(define x 1)
(define sum 0)
(while (lambda () (< x 100))
  (lambda ()
    (set! sum (+ sum x))
    (set! x (+ x 1))))
```

## Knowledge of the Universe

```
def computing_power(nyears):
    return yearlyrate ** nyears

def simulation_work(scale):
    return scale ** 3

def knowledge_of_universe(scale):
    return math.log(scale, 10) # log base 10

def relative_knowledge_of_universe(nyears):
    scale = 1
    while simulation_work(scale + 1) <= 1000 * computing_power(nyears):
        scale = scale + 1
    return knowledge_of_universe(scale)
```

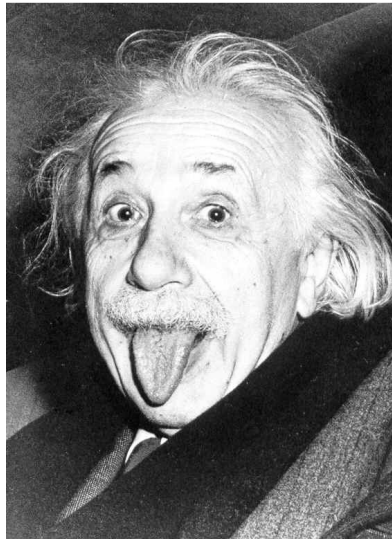
(Note: with a little bit of math, could compute this directly using a log instead.)

```
>>> relative_knowledge_of_universe(0)
1.0
>>> relative_knowledge_of_universe(1)
1.0413926851582249
>>> relative_knowledge_of_universe(2)
1.1139433523068367
>>> relative_knowledge_of_universe(10)
1.6627578316815739
>>> relative_knowledge_of_universe(15)
2.0
>>> relative_knowledge_of_universe(30)
3.0064660422492313
>>> relative_knowledge_of_universe(60)
5.0137301937137719
>>> relative_knowledge_of_universe(80)
6.351644238569782
```

Will there be any *mystery* left in the Universe when you die?

Only two things are infinite, the universe and human stupidity, and I'm not sure about the former.

Albert Einstein



## The Endless Golden Age

- Golden Age – period in which knowledge/quality of something doubles quickly
- At any point in history, half of what is known about astrophysics was discovered in the previous 15 years!
  - Moore’s law today, but other advances previously: telescopes, photocopiers, clocks, agriculture, etc.

Accumulating 4% per year => doubling every 15 years!

### Endless/Short Golden Ages

**Endless golden age:** at any point in history, the amount known is twice what was known 15 years ago

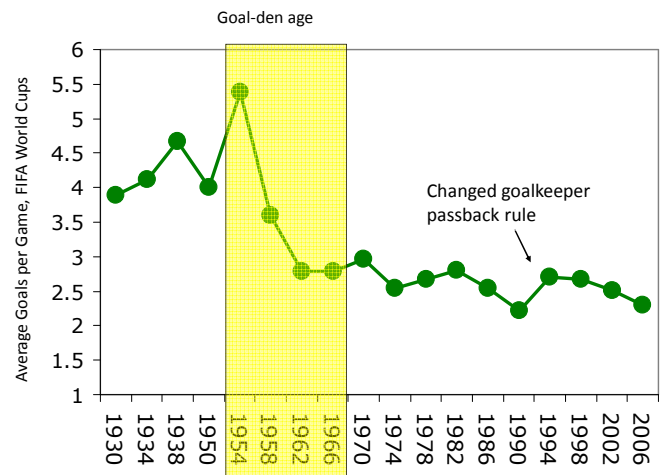
Continuous exponential growth:  $\Theta(k^n)$

$k$  is some constant (e.g., 1.04),  $n$  is number of years

**Short golden age:** knowledge doubles during a short, “golden” period, but only improves linearly most of the time

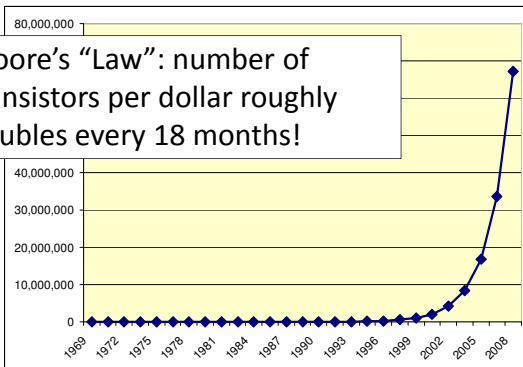
Mostly linear growth:  $\Theta(n)$

$n$  is number of years

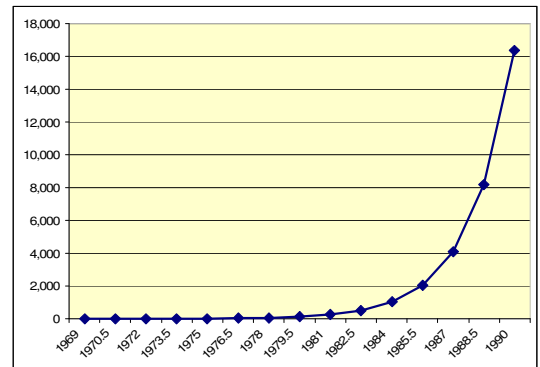


## Computing Power 1969-2008 (in Apollo Control Computer Units)

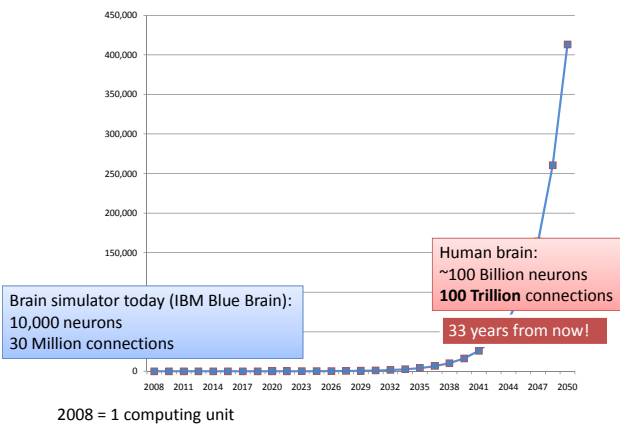
Moore’s “Law”: number of transistors per dollar roughly doubles every 18 months!



## Computing Power 1969-1990 (in Apollo Control Computer Units)



## Computing Power 2009-2050?



## More Moore's Law?

"Any physical quantity that's growing exponentially predicts a disaster, you simply can't go beyond certain major limits."  
Gordon Moore (2007)

Current technologies are already slowing down...

An analysis of the history of technology shows that technological change is exponential, contrary to the common-sense 'intuitive linear' view. So we won't experience 100 years of progress in the 21st century-it will be more like 20,000 years of progress (at today's rate). The 'returns,' such as chip speed and cost-effectiveness, also increase exponentially. There's even exponential growth in the rate of exponential growth. Within a few decades, machine intelligence will surpass human intelligence, leading to the Singularity — technological change so rapid and profound it represents a rupture in the fabric of human history. The implications include the merger of biological and non-biological intelligence, immortal software-based humans, and ultra-high levels of intelligence that expand outward in the universe at the speed of light.

Ray Kurzweil

but advances won't come from more transistors with current technologies...new technologies, algorithms, parallelization, architectures, etc.

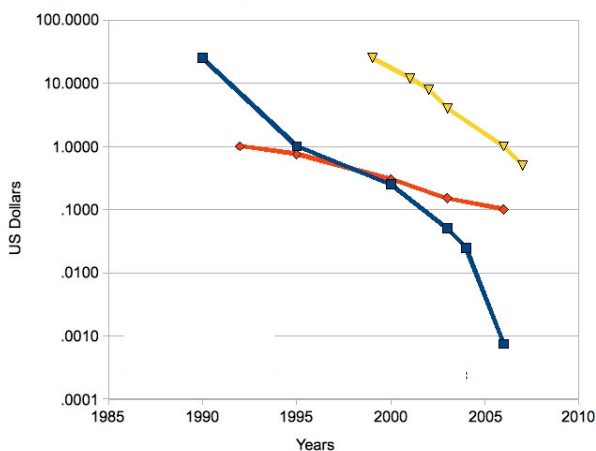
## The Real Golden Rule?

Why do fields like astrophysics, medicine, biology and computer science have "endless golden ages", but fields like

- music (1775-1825)
- rock n' roll (1962-1973)\*
- philosophy (400BC-350BC?)
- art (1875-1925?)
- soccer (1950-1966)
- baseball (1925-1950?)
- movies (1920-1940?)

have short golden ages?

\* or whatever was popular when you were 16.



## Golden Ages or Golden Catastrophes?

## PS4, Question 1e

**Question 1:** For each  $f$  and  $g$  pair below, argue convincingly whether or not  $g$  is (1)  $O(f)$ , (2)  $\Omega(f)$ , and (3)  $\Theta(g)$  ...

- (e)  $g$ : the federal debt  $n$  years from today,  
 $f$ : the US population  $n$  years from today

## Malthusian Catastrophe

Reverend Thomas Robert Malthus, *Essay on the Principle of Population*, 1798

“The great and unlooked for discoveries that have taken place of late years in natural philosophy, the increasing diffusion of general knowledge from the extension of the art of printing, the ardent and unshackled spirit of inquiry that prevails throughout the lettered and even unlettered world, ... have all concurred to lead many able men into the opinion that we were touching on a period big with the most important changes, changes that would in some measure be decisive of the future fate of mankind.”



Source: The Warren J. Samuels Portrait Collection at Duke University

## Malthus' Postulates

“I think I may fairly make two postulata.

- First, that food is necessary to the existence of man.
- Secondly, that the passion between the sexes is necessary and will remain nearly in its present state.

These two laws, ever since we have had any knowledge of mankind, appear to have been fixed laws of our nature, and, as we have not hitherto seen any alteration in them, we have no right to conclude that they will ever cease to be what they now are...”

## Malthus' Conclusion

“Assuming then my postulata as granted, I say, that the power of population is indefinitely greater than the power in the earth to produce subsistence for man.

Population, when unchecked, **increases in a geometrical ratio**. Subsistence **increases only in an arithmetical ratio**. A slight acquaintance with numbers will show the immensity of the first power in comparison of the second.”

## Malthusian Catastrophe

- Population growth is geometric:  $\Theta(k^n)$  ( $k > 1$ )
- Food supply growth is linear:  $\Theta(n)$

What does this mean as  $n \rightarrow \infty$ ?

$$\text{Food per person} = \text{food supply} / \text{population} \\ = \Theta(n) / \Theta(k^n)$$

As  $n$  approaches infinity, food per person approaches zero!

## Malthus' Fallacy



## Malthus' Fallacy

He forgot how he started:

“The great and unlooked for discoveries that have taken place of late years in natural philosophy, the increasing diffusion of general knowledge from the extension of the art of printing, the ardent and unshackled spirit of inquiry that prevails throughout the lettered and even unlettered world...”

# Golden Age of Food Production

Agriculture is an “endless golden age” field: production from the same land increases as  $\sim \Theta(1.02^n)$

Increasing knowledge of farming, weather forecasting, plant domestication, genetic engineering, pest repellants, distribution channels, preservatives, etc.

# Growing Corn



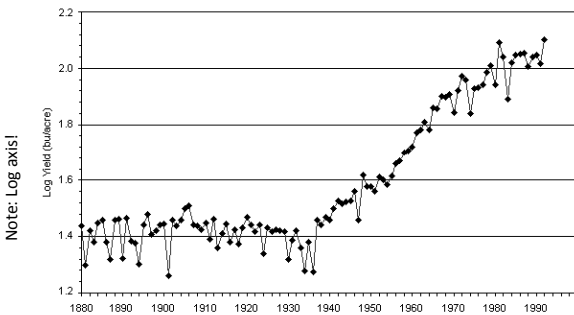
1906: < 1,000 pounds per acre



2006: 10,000 pounds per acre

Michael Pollan's *The Omnivore's Dilemma*

# Corn Yield



<http://www.agbioforum.org/v2n1/v2n1a10-ruttan.htm>

# Green Revolution



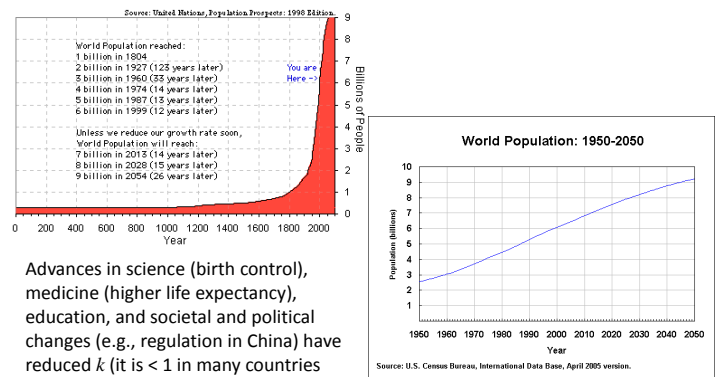
Norman Borlaug (1914-2009)

“At a time when doom-sayers were hopping around saying everyone was going to starve, Norman was working. He moved to Mexico and lived among the people there until he figured out how to improve the output of the farmers. So that saved a million lives. Then he packed up his family and moved to India, where in spite of a war with Pakistan, he managed to introduce new wheat strains that quadrupled their food output. So that saved another million. You get it? But he wasn't done. He did the same thing with a new rice in China. He's doing the same thing in Africa -- as much of Africa as he's allowed to visit.

When he won the Nobel Prize in 1970, they said he had saved a billion people. That's BILLION! BUH! That's Carl Sagan BILLION with a "B"! And most of them were a different race from him. Norman is the greatest human being, and you probably never heard of him.”

Penn Jillette (*Penn & Teller*)

# Malthus was wrong about #2 Also

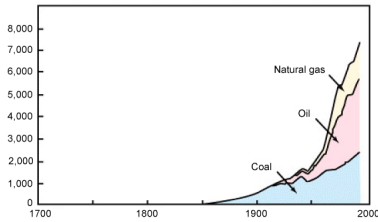


Advances in science (birth control), medicine (higher life expectancy), education, and societal and political changes (e.g., regulation in China) have reduced  $k$  (it is < 1 in many countries now!)

## Upcoming Malthusian Catastrophes?

- Human consumption of fossil fuels grows as  $\Theta(k^n)$  (fairly large  $k$  like 1.08?)
- Available fuel is constant (?)

Fig. 3: Trends in World Fossil Fuel Consumption  
(Million tons oil equivalent)



Source: Environment Agency's "White Paper on the Environment" (1998)  
[http://www.wpa.mest.go.jp/hakuryo/book/hpqa200001/hpqa200001\\_2\\_006.html](http://www.wpa.mest.go.jp/hakuryo/book/hpqa200001/hpqa200001_2_006.html)

## PS4, Question 1e

$g$ : the federal debt  $n$  years from today,  
 $f$ : the US population  $n$  years from today

Debt increases:

Spending – Revenues

this varies, but usually positive

+ Interest on the previous debt (exponential)

$$= \Theta(k^n)$$

Population increase is not exponential:

rate continues to decrease

=> as  $n$  increases, debt per person approaches infinity!

This will *eventually* be a problem, but growth analysis doesn't say *when*.

## “Cornucopian View”

Few resources are really finite

All scientific things have endless golden ages

Knowledge accumulates

Knowledge makes it easier to acquire more

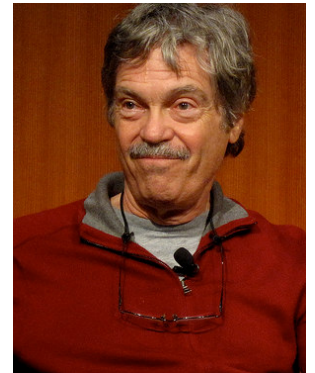
(We hope) Human ingenuity and economics and politics will continue solve problems before they become catastrophes

No one will sell the last gallon of gas for \$2.45

## “Kay”-sian View

The best way to predict the future is to invent it.

— Alan Kay



## Charge

- When picking majors, pick a short golden age field that is about to enter its short golden age
  - This requires vision and luck!
- Play it safe by picking an endless golden age field (CS is a good choice for this!)
- Wednesday: History of Object-Oriented Programming; Interpreters