



# Power Distribution Scheduling for Electric Vehicles in Wireless Power Transfer Systems

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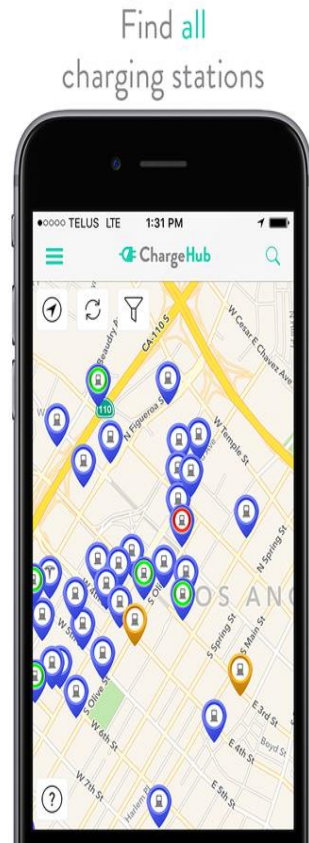
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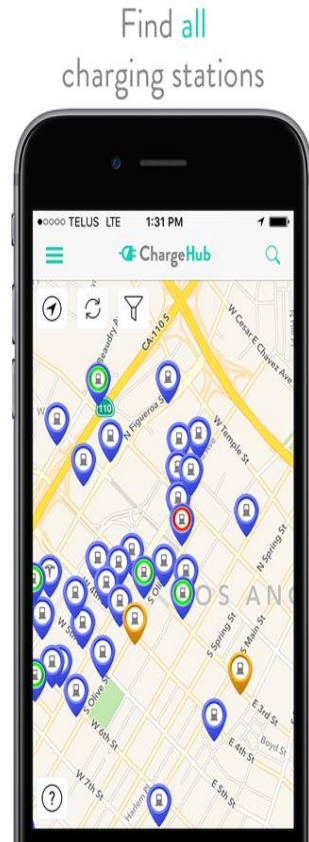
## How does the ANTIQUE way of charging serve Electric Vehicles (EVs)?



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Find all  
charging stations



**Range Anxiety**



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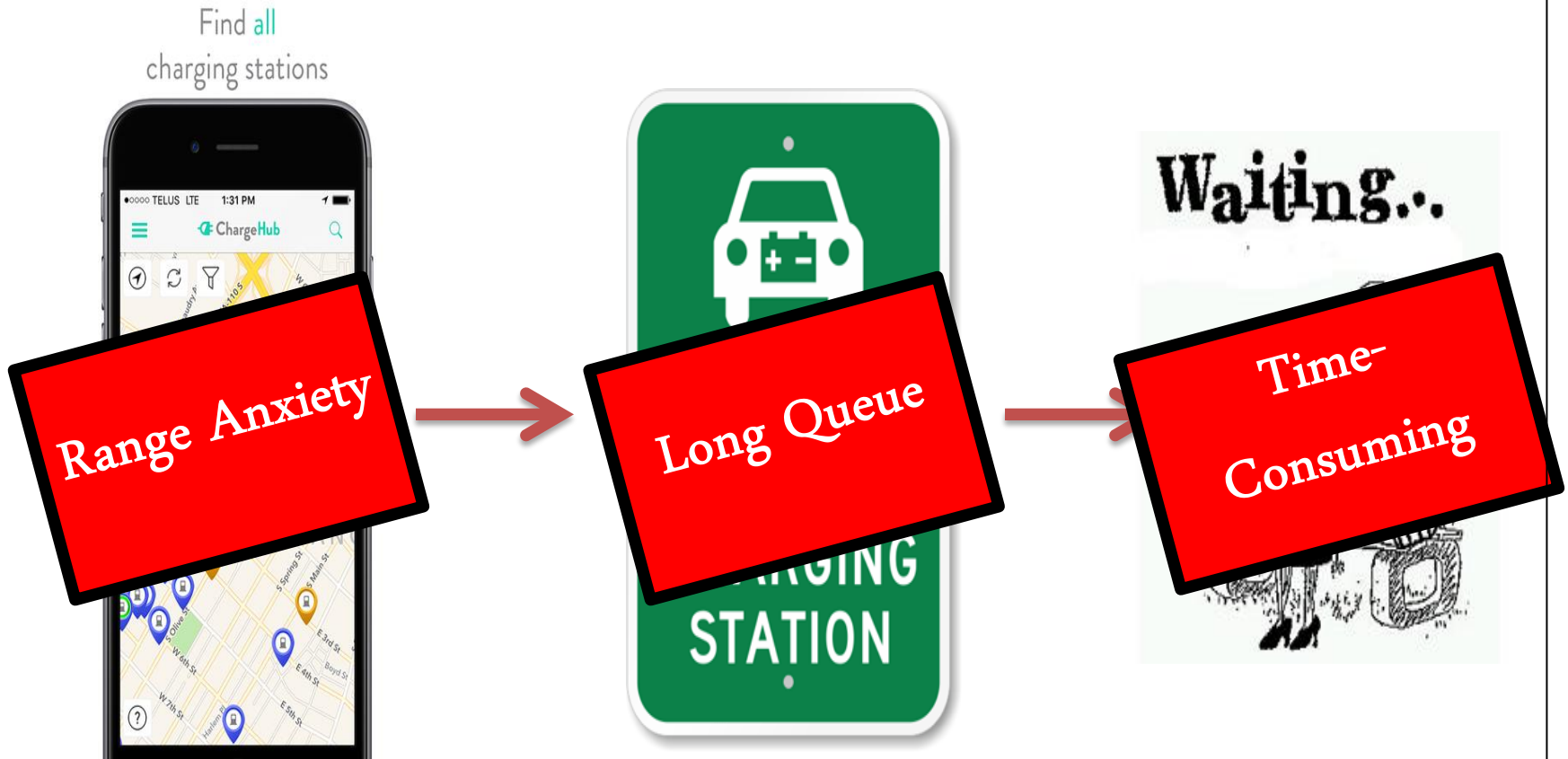
**Range Anxiety**



**Long Queue**

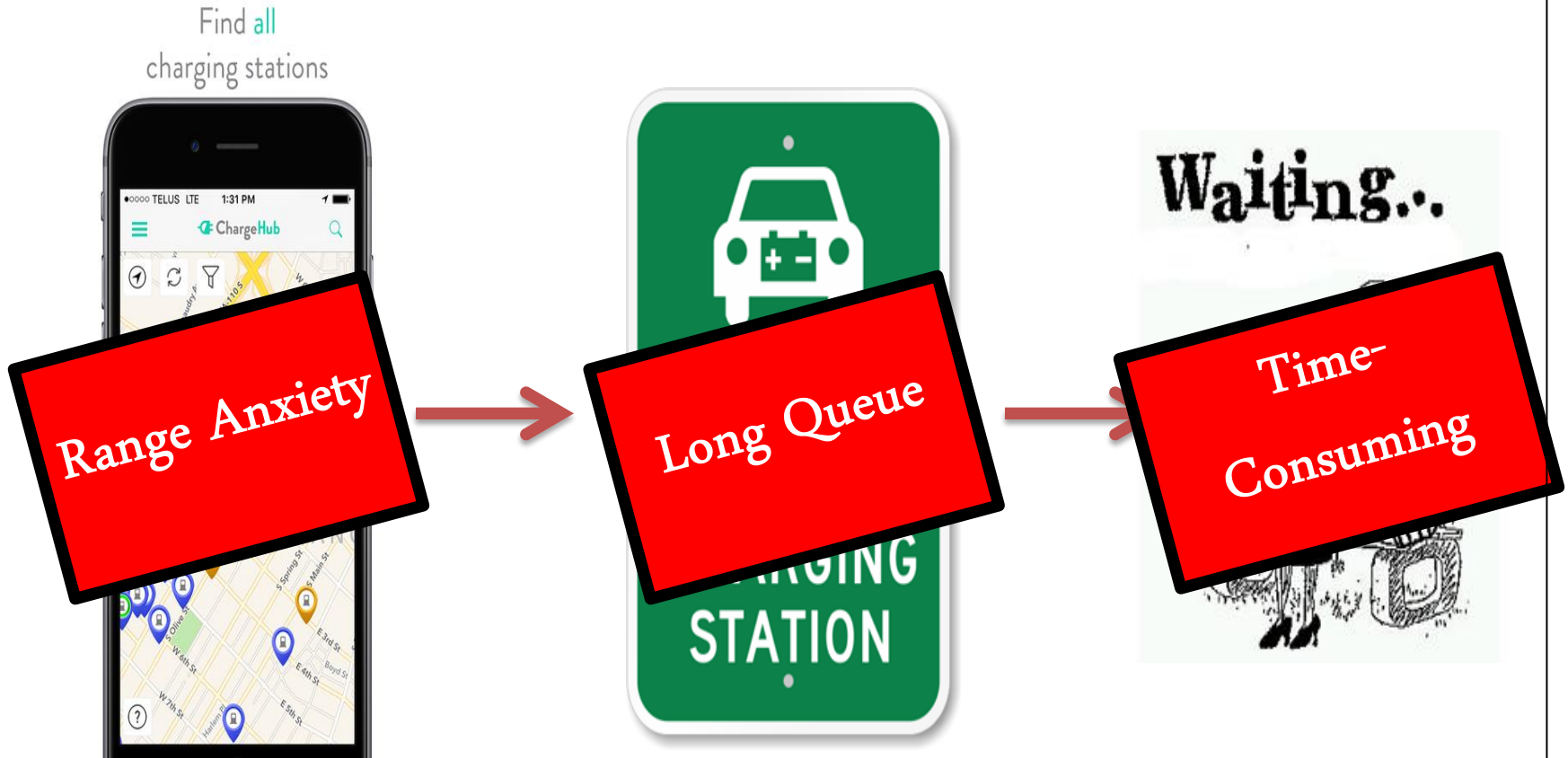


## How does the ANTIQUE way of charging serve EVs?





## How does the ANTIQUE way of charging serve EVs?



Fail to maintain State-of-Charge (SoC)

## Charge vehicles in motion



## Charge vehicles in motion



Long Queue



## Charge vehicles in motion



Long Queue



Time-Consuming



## Charge vehicles in motion



Long Queue



Time-Consuming



Range Anxiety



## Charge vehicles in motion



Long Queue



Time-Consuming



Range Anxiety

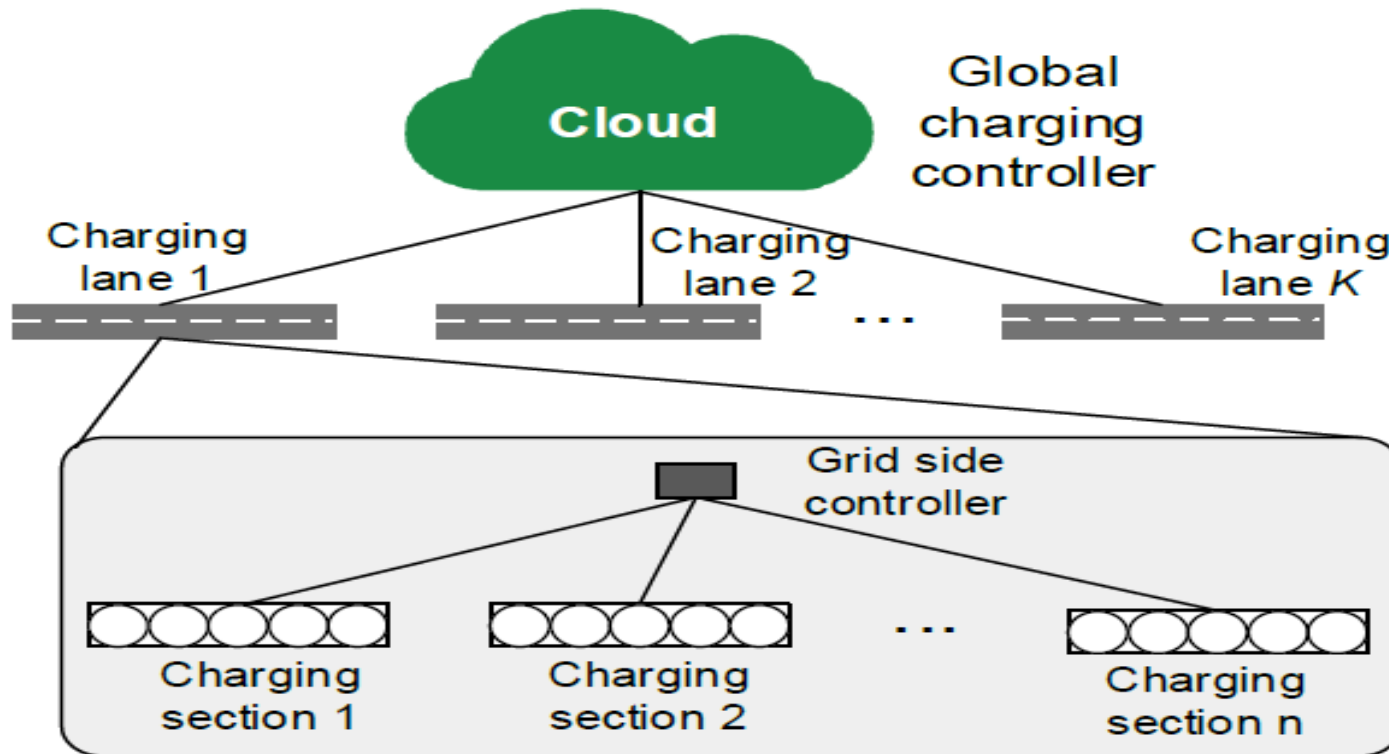


Maintain SoC



# Background & Motivation

The wireless power transfer (WPT) system architecture

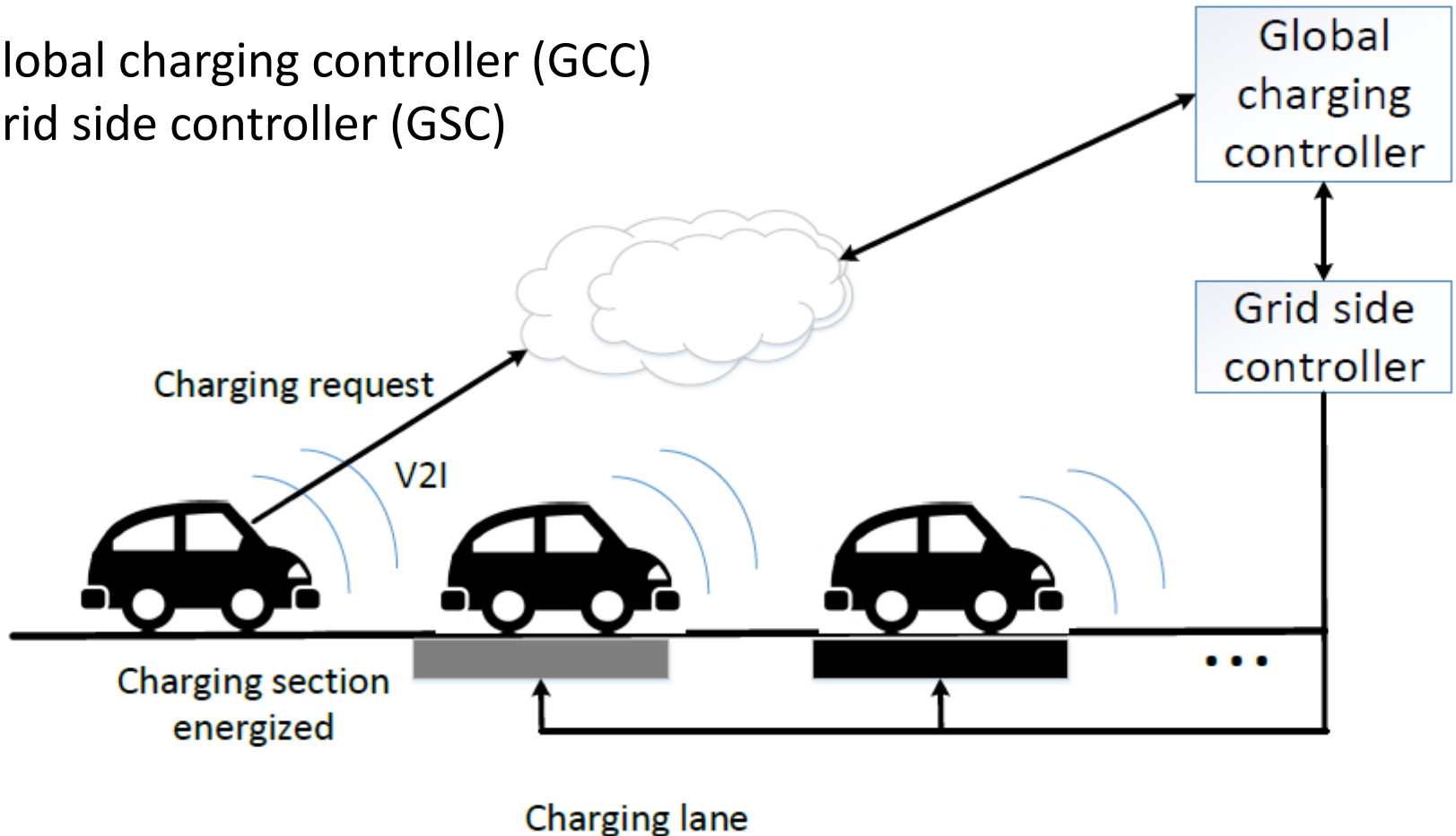


# Introduction

## The wireless power transfer (WPT) system architecture

Global charging controller (GCC)

Grid side controller (GSC)

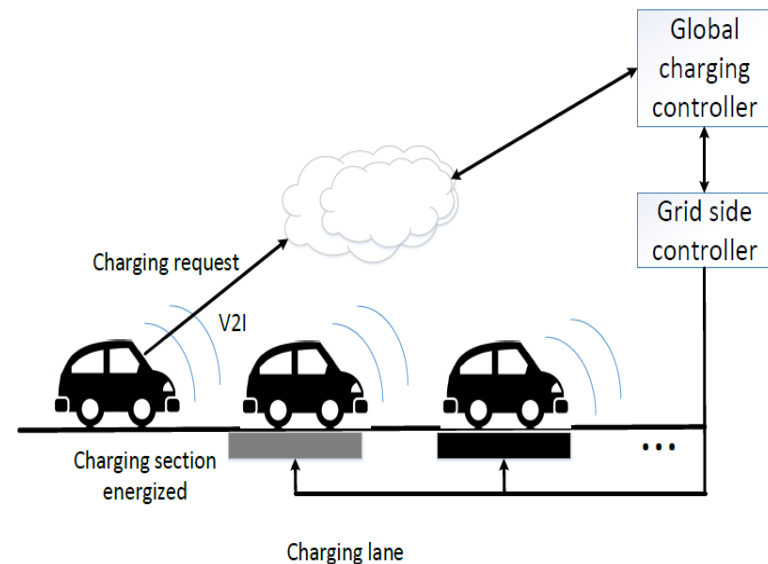




# Introduction

## The scenario we consider

1. We consider a WPT system in a highway scenario where vehicles follow a similar velocity.
2. When there are multiple vehicles on a charging lane simultaneously, the charging infrastructure needs to meet the needs of all the vehicles at the same time.





# Introduction

## Challenge

There has been no effort devoted  
to handling this challenge

# Introduction

## Related work

### **Study on the WPT systems and EV techniques**

1. Analyze the existing technologies in the WPT systems
  - [Li, JESTPE 2015]
2. Examine the technical aspects and charging topology of in-motion wireless power charging of EVs
  - [Onar, APEC 2011]

### **Implementation of the WPT systems for EVs**

1. Design of optimized core structure and electric components
  - [Shin, Trans. IE 2014]
2. General design requirements and analysis of WPT systems
  - [Yilmaz, ITEC 2012]
3. Dynamic models to identify the maximum pickup
  - [Lee, Trans. PE 2015]

# Introduction

## Three problems to be formulated

- i. SOC-B: balancing the state of charge (SOC) of the EVs
- ii. Power-B: balancing the amount of stored power of the EVs
- iii. Power-M: minimizing the total power charged

## Solution

1. i)-ii) are convex: **use the subgradient method to solve the problems.**
2. iii) is a linear programming problem: can be solved by the simplex method. **We also design a greedy algorithm to solve the problem.**

# Power Distribution Scheduling

## EV Traffic Model we consider

1. A discrete time system where time =  $1, 2, \dots$
2.  $n$  charging sections  $c_1, c_2, \dots, c_n$  in a charging lane
3.  $m$  heterogeneous EVs  $\{1, 2, \dots, m\}$  based on the EVs' current stored energy in the batteries
4. The maximum capacity of the GSC is  $A$
5. The maximum power that each charging section  $j$  can provide is  $a_j$

# Power Distribution Scheduling

The SOC-B problem: balancing the SOC of the EVs

**Goal:** to distribute the power to each charging section  $j$  in each time slot  $t$ ,  $x_j(t)$ , to guarantee all the EVs can finish their trips and the SOC of all the EVs are balanced when they leave the charging lane.

# Power Distribution Scheduling

The SOC-B problem: balancing the SOC of the EVs

## Problem formulation

Objective function: minimize the variance of SOC

Constraints:

- 1) the sum of the allocated power of all the charging sections  $\leq$  the maximum power provided by the GSC;
- 2) the power allocated to each charging section  $j$  cannot exceed the maximum power provided by charging section  $j$ ;
- 3) the SOC of each EV should be enough to move to the next charging section or the destination;

The problem is **convex**.

**Solution:** The subgradient method



# Power Distribution Scheduling

**The Power-B problem: Balancing the amount of the stored power of the EVs**

**Objective:** to balance the absolute amount of stored power of all the Evs when the EVs leave the charging lane.

## Problem formulation

**Objective function:** minimize the variance of energy stored

**Constraints:** has the same constraints as the problem to balance the SOC of EVs.

The problem is **convex**.

**Solution:** The subgradient method

# Power Distribution Scheduling

The Power-M problem: minimizing the total power charged

**Objective:** to minimize the total power charged by all the charging sections in the charging lane.

## Problem formulation

**Objective function:** minimize the total power charged by all the charging sections in the charging lane.

**Constraints:** has the same constraints as the previous two problems.

The problem is a linear programming (LP) problem, and hence can be solved directly using the **simplex method**.

# Power Distribution Scheduling

The Power-M problem: minimizing the total power charged

## Greedy algorithm

**for each** charging section  $j$  at time slot  $t$  do

**if** charging section  $j$  is the last charging section

**then** charge each EV  $i$  with power

$$x_j(t) = \max\{p'_{\text{req},i} + P_{\text{trac},i}^j - z_i(t), 0\}$$

// Provide enough power to reach the destination

**else** charge each EV  $i$  with power

$$x_j(t) = \max\{p'_{\text{th},i} + P_{\text{trac},i}^j - z_i(t), 0\}$$

// Provide enough power to reach the next

charging section

**Theorem:** The greedy algorithm can achieve the optimal solution.

# Experiment

## Simulation settings

1. Both MatLab and Simulation for Urban MObility (SUMO);
2. The number of EVs is varied from 10 to 50;
3. The number of charging sections is set to 10;
4. Each EV's SOC is set randomly in  $[0.4, 0.8]$  when entering a charging lane;
5. 3 types of EVs were considered (Nissan Leaf, Toyota Prius, and Chevy Volt);
6. The power capacity of the GSC is randomly chosen from  $[40-100]$ Kw;
7. The simulation takes 20 times;

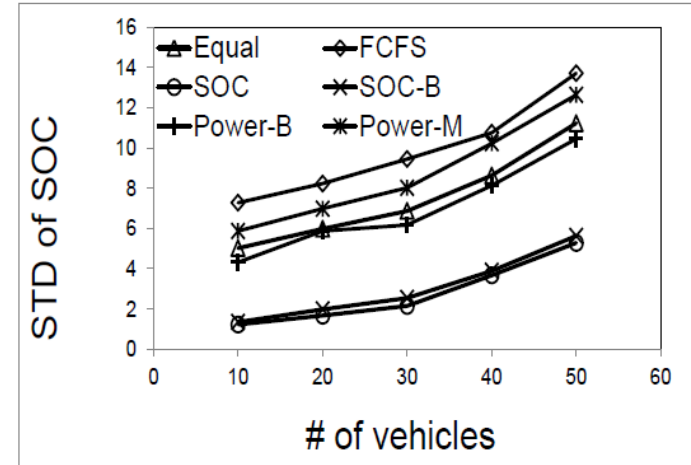
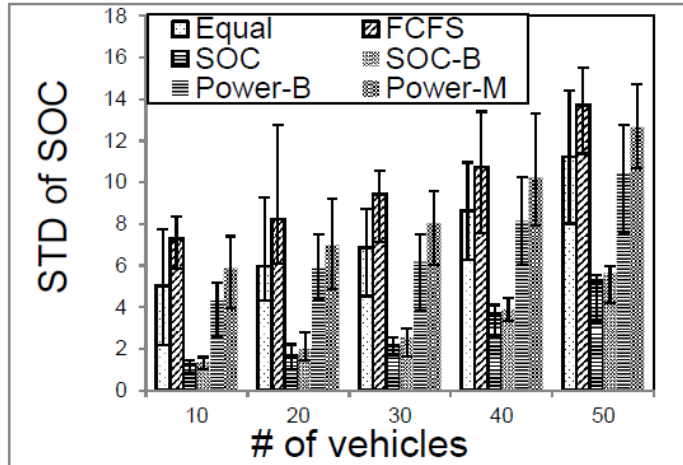
## Compared methods

1. Equal sharing method (Equal).
2. First come first serve method (FCFS).
3. State of charge method (SOC).

# Experiment

## Simulation results

### Balancing the SOC of the EVs

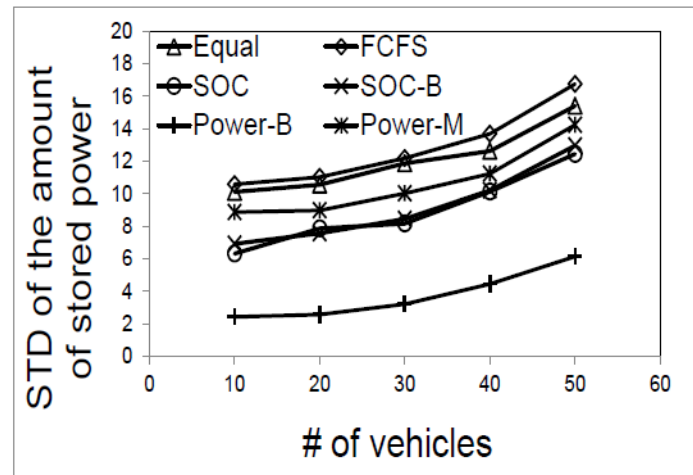
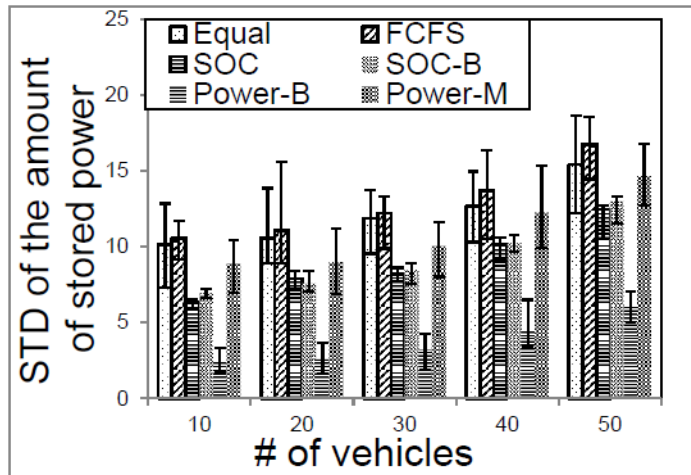


**Observation:** the standard deviation of SOC follow  
 $SOC \approx SOC-B < Power-B < Equal < Power-M < FCFS$

# Experiment

## Simulation results

### Balancing the Amount of the Stored Power of the EVs



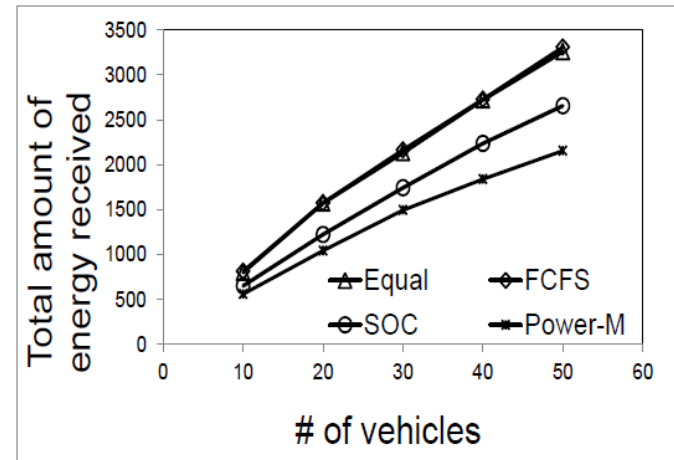
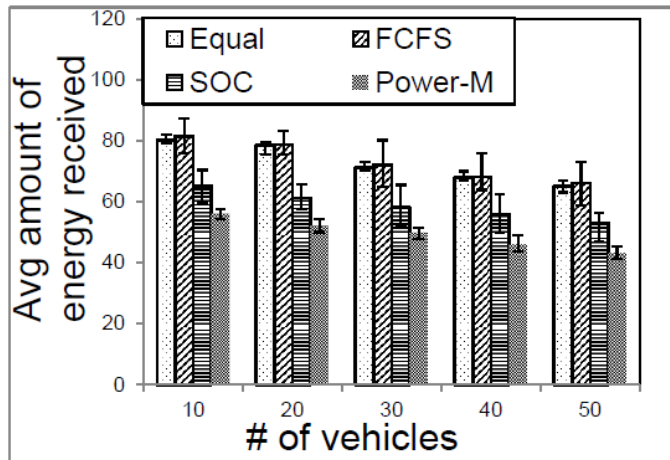
**Observation:** the standard deviation of EVs' stored power follows

$$\text{Power-B} < \text{SOC} \approx \text{SOC-B} < \text{Power-M} < \text{Equal} < \text{FCFS}$$

# Experiment

## Simulation results

### Minimizing the Amount of Total Power Charged



**Observation:** Fuel consumption follows:  
 $\text{Power-M} < \text{SOC} < \text{Equal} \approx \text{FCFS}$

## Conclusions

1. We studied the power distribution scheduling problems, SOC-B, Power-B, and Power-M, to enable the EVs to receive enough power to reach their destinations and meanwhile achieve a goal.
2. We showed SOC-B and Power-B are convex, which can be solved using the subgradient method. We also designed a greedy algorithm to achieve the optimal solution for Power-M.
3. We conducted extensive experiments to confirm that our solutions are effective in achieving their goals.

## Future work

We will consider different velocities and velocity variation of vehicles in general roads



# QUESTIONS ?

*Thank you!*

*Questions & Comments?*

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