





$$\boxed{A \rightarrow B}$$

\equiv

$$(A \wedge B) \vee (\neg A \wedge B) \vee (\neg A \wedge \neg B)$$

↓ defn of \rightarrow

$$\neg A \vee B$$

↓ double neg

$$\neg A \vee \neg \neg B$$

↓ De Morgan

$$\neg(A \wedge \neg B)$$

$$(A \wedge B) \vee (\neg A \wedge B) \vee \neg(A \vee B)$$

↓ De Morgan

↑
↓ NOT ASSOCIATIVE

↓ COMMUTATIVE \vee

$$(A \wedge B) \vee \neg(A \vee B) \vee (\neg A \wedge B)$$

↓ defn in

$$(A \wedge B) \vee ((A \vee B) \rightarrow (\neg A \wedge B))$$

↓ De Morgan
→ distributive

$$(\neg A \wedge B)$$

$$\neg \neg (A \wedge B)$$



$$\neg (\neg A \vee \neg B)$$

$$(\neg \neg A \wedge B)$$

$$(\neg \neg A \wedge \neg \neg B)$$

$$\neg (\neg A \vee \neg B)$$

distribute

$$(A \wedge B) \vee (\overline{A} \wedge B) \vee (\overline{A} \wedge \overline{B})$$

~~_____~~ ← ~~_____~~

$$(A \wedge B) \vee (\overline{A} \wedge (B \vee \overline{B}))$$

↑
T

$$(A \wedge B) \vee (\overline{A} \wedge T)$$

Given

def of imp

commutative \vee

simplification (Backwards)

\wedge introduction

unsimplify

$$A \rightarrow B$$

$$\neg A \vee B$$

$$B \vee \neg A$$

$$T \wedge (B \vee \neg A)$$

$$(A \vee \neg A) \wedge (B \vee \neg A)$$

$$(\neg A \vee A) \wedge (B \vee \neg A)$$

$$(\neg A \vee A) \wedge (\neg A \vee B)$$

$$\neg A \vee (A \wedge B)$$

$$(A \wedge B) \vee \neg A$$

$$(A \vee \neg A) \wedge (B \vee \neg A)$$

$$T \wedge (B \vee \neg A)$$

$$B \vee \neg A$$

$$\neg A \vee B$$

$$A \rightarrow B$$