BLACK HOLE COMPUTER may sound absurd but is proving to be a useful conceptual tool for researchers studying cosmology and fundamental physics. And if physicists are able to create black holes in particle accelerators—as some predict will be possible within a decade—they may actually observe them perform computation.
In keeping with the spirit of the age, researchers can think of the laws of physics as computer programs and the universe as a computer.

BY SETH LLOYD AND Y. JACK NG

BLACK HOLE COMPUTERS

What is the difference between a computer and a black hole? This question sounds like the start of a Microsoft joke, but it is one of the most profound problems in physics today. Most people think of computers as specialized gizmos: streamlined boxes sitting on a desk or fingernail-size chips embedded in high-tech coffeepots. But to a physicist, all physical systems are computers. Rocks, atom bombs and galaxies may not run Linux, but they, too, register and process information. Every electron, photon and other elementary particle stores bits of data, and every time two such particles interact, those bits are transformed. Physical existence and information content are inextricably linked. As physicist John Wheeler of Princeton University says, “It from bit.”
Black holes might seem like the exception to the rule that everything computes. Inputting information into them presents no difficulty, but according to Einstein’s general theory of relativity, getting information out is impossible. Matter that enters a hole is assimilated, the details of its composition lost irretrievably. In the 1970s Stephen Hawking of the University of Cambridge showed that when quantum mechanics is taken into account, black holes do have an output: they glow like a hot coal. In Hawking’s analysis, this radiation is random, however. It carries no information about what went in. If an elephant fell in, an elephant’s worth of energy would come out—but the energy would be a hodgepodge that could not be used, even in principle, to re-create the animal.

That apparent loss of information poses a serious conundrum, because the laws of quantum mechanics preserve information. So other scientists, including Leonard Susskind of Stanford University, John Preskill of the California Institute of Technology and Gerard ’t Hooft of the University of Utrecht in the Netherlands, have argued that the outgoing radiation is not, in fact, random—that it is a processed form of the matter that falls in [see “Black Holes and the Information Paradox,” by Leonard Susskind; SCIENTIFIC AMERICAN, April 1997]. This past summer Hawking came around to their point of view. Black holes, too, compute.

Black holes are merely the most exotic example of the general principle that the universe registers and processes information. The principle itself is not new. In the 19th century the founders of statistical mechanics developed what would later be called information theory to explain the laws of thermodynamics. At first glance, thermodynamics and information theory are worlds apart: one was developed to describe steam engines, the other to optimize communications. Yet the thermodynamic quantity called entropy, which limits the ability of an engine to do useful work, turns out to be proportional to the number of bits registered by the positions and velocities of the molecules in a substance. The invention of quantum mechanics in the 20th century put this discovery on a firm quantitative foundation and introduced scientists to the remarkable concept of quantum information. The bits that make up the universe are quantum bits, or “qubits,” with far richer properties than ordinary bits.

Analyzing the universe in terms of bits and bytes does not replace analyzing it in conventional terms such as force and energy, but it does uncover new and surprising facts. In the field of statistical mechanics, for example, it unknotted the paradox of Maxwell’s demon, a contraption that seemed to allow perpetual motion. In recent years, we and other physicists have been applying the same insights to cosmology and fundamental physics: the nature of black holes, the fine-scale structure of spacetime, the behavior of cosmic dark energy, the ultimate laws of nature. The universe is not just a giant computer; it is a giant quantum computer. As physicist Paola Zizzi of the University of Padova says, “It from qubit.”

**When Gigahertz Is Too Slow**

The confluence of physics and information theory flows from the central maxim of quantum mechanics: at bottom, nature is discrete. A physical system can be described using a finite number of bits. Each particle in the system acts like the logic gate of a computer. Its spin “axis” can point in one of two directions, thereby encoding a bit, and can flip over, thereby performing a simple computational operation.

The system is also discrete in time. It takes a minimum amount of time to flip a bit. The exact amount is given by a theorem named after two pioneers of the physics of information processing, Norman Margolus of the Massachusetts Institute of Technology and Lev Levitin of Boston University. This theorem is related to the Heisenberg uncertainty principle, which describes the inherent trade-offs in measuring physical quantities, such as position and momentum or time and energy. The theorem says that the time it takes to flip a bit, \( t \), depends on the amount of energy you apply, \( E \). The more energy you apply, the shorter the time can be. Mathematically, the rule is \( t \geq h/4E \), where \( h \) is Planck’s constant, the main parameter of quantum theory. For example, one type of experimental quantum computer stores bits on protons and uses magnetic fields to flip them. The operations take place in the minimum time allowed by the Margolus-Levitin theorem.

From this theorem, a huge variety of conclusions can be drawn, from limits on the geometry of spacetime to the computational capacity of the universe as a whole. As a warm-up, consider the limits to the computational power of ordinary matter—in this case, one kilogram occupying the volume of one liter. We call this device the ultimate laptop.

Its battery is simply the matter itself, converted directly to energy per Einstein’s famous formula \( E = mc^2 \). Putting all this energy into flipping bits, the computer can do \( 10^{51} \) operations per second, slowing down gradually as the

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**Overview/Cosmic Computers**

- Merely by existing, all physical systems store information. By evolving dynamically in time, they process that information. The universe computes.
- If information can escape from black holes, as most physicists now suspect, a black hole, too, computes. The size of its memory space is proportional to the square of its computation rate. The quantum-mechanical nature of information is responsible for this computational ability; without quantum effects, a black hole would destroy, rather than process, information.
- The laws of physics that limit the power of computers also determine the precision with which the geometry of spacetime can be measured. The precision is lower than physicists once thought, indicating that discrete “atoms” of space and time may be larger than expected.
What is a computer? That is a surprisingly complex question, but whatever precise definition one adopts, it is satisfied not just by the objects people commonly call “computers” but also by everything else in the world. Physical objects can solve a broad class of logic and mathematics problems, although they may not accept input or give output in a form that is meaningful to humans. Natural computers are inherently digital: they store data in discrete quantum states, such as the spin of elementary particles. Their instruction set is quantum physics.

### INPUT
- **ORDINARY LAPTOP**
  - Speed: $10^{10}$ hertz
  - Memory: $10^{10}$ bits
  - A keyboard and associated circuitry encode information as voltage pulses in a wire.

### COMPUTATION
- **ORDINARY LAPTOP**
  - The pulses interact, guided by devices such as transistors, which perform logical operations such as NOT.

### OUTPUT
- **ORDINARY LAPTOP**
  - The pulses, having been processed, are translated into meaningful patterns of light.

### ULTIMATE LAPTOP
- Speed: $10^{15}$ hertz
- Memory: $10^{30}$ bits
- Consisting of one kilogram of hot plasma in a one-liter box, this device accepts data encoded as particle positions, velocities and spins.

### ULTIMATE LAPTOP
- The particles interact. Collisions can be arranged to perform operations such as NOT; a collision can cause particles to flip.

### OUTPUT
- **ULTIMATE LAPTOP**
  - As particles leave the volume, their properties can be measured and translated. The system slowly winds down as its energy degrades.

### BLACK HOLE
- Speed: $10^{10}$ hertz
- Memory: $10^{10}$ bits
- This black hole consists of one kilogram in a volume $10^{-27}$ meter in radius. Data and instructions are encoded in matter and dropped in.

### BLACK HOLE
- On their descent, particles interact much as in the ultimate laptop, except that gravity also plays a role. The governing laws are not yet understood.

### OUTPUT
- **BLACK HOLE**
  - The hole emits radiation, named after physicist Stephen Hawking. New theories suggest that the radiation carries the computational output.
By preparing the material that falls into a black hole, A HACKER COULD PROGRAM IT to perform any desired computation.

FIRST LAW of quantum computation is that computation takes energy. The spin of a proton encodes a single bit, which can be inverted by applying a magnetic field. The stronger the field is—the more energy it applies—the faster the proton will flip.

**From Nanotech to Xenotech**

If any chunk of matter is a computer, a black hole is nothing more or less than a computer compressed to its smallest possible size. As a computer shrinks, the gravitational force that its components exert on one another becomes stronger and eventually grows so intense that no material object can escape. The size of a black hole, called the Schwarzschild radius, is directly proportional to its mass.

A one-kilogram hole has a radius of about \(10^{-27}\) meter. (For comparison, a proton has a radius of \(10^{-15}\) meter.) Shrinking the computer does not change its energy content, so it can perform \(10^{51}\) operations per second, just as before. What does change is the memory capacity. When gravity is insignificant, the total storage capacity is proportional to the number of particles and thus to the volume. But when gravity dominates, it interconnects the particles, so collectively they are capable of storing less information. The total storage capacity of a black hole is proportional to its surface area. In the 1970s Hawking and Jacob Bekenstein of the Hebrew University of Jerusalem calculated that a one-kilogram black hole can register about \(10^{16}\) bits—much less than the same computer before it was compressed.

In compensation, the black hole is a much faster processor. In fact, the amount of time it takes to flip a bit, \(10^{-35}\) second, is equal to the amount of time it takes light to move from one side of the computer to the other. Thus, in contrast to the ultimate laptop, which is highly parallel, the black hole is a serial computer. It acts as a single unit.

How would a black hole computer work in practice? Input is not problematic: just encode the data in the form of matter or energy and throw it down the hole. By properly preparing the material that falls in, a hacker should be able to program the hole to perform any desired computation. Once the material enters a hole, it is gone for good; the so-called event horizon demarcates the point of no return. The plummeting particles interact with one another, performing computation for a finite time before reaching the center of the hole—the singularity—and ceasing to exist. What happens to matter...
as it gets squished together at the singularity depends on the details of quantum gravity, which are as yet unknown.

The output takes the form of Hawking radiation. A one-kilogram hole gives off Hawking radiation and, to conserve energy, decreases in mass, disappearing altogether in a mere $10^{-21}$ second. The peak wavelength of the radiation equals the radius of the hole; for a one-kilogram hole, it corresponds to extremely intense gamma rays. A particle detector can capture this radiation and decode it for human consumption.

Hawking’s study of the radiation that bears his name is what overturned the conventional wisdom that black holes are objects from which nothing whatsoever can escape [see “The Quantum Mechanics of Black Holes,” by Stephen W. Hawking; SCIENTIFIC AMERICAN, January 1977]. The rate at which black holes radiate is inversely related to their size, so big black holes, such as those at the center of galaxies, lose energy much more slowly than they gobble up matter. In the future, however, experimenters may be able to create tiny holes in particle accelerators, and these holes should explode almost immediately in a burst of radiation. A black hole can be thought of not as a fixed object but as a transient congregation of matter that performs computation at the maximum rate possible.

**Escape Plan**

**THE REAL QUESTION** is whether Hawking radiation returns the answer of the computation or merely gibberish. The issue remains contentious, but most physicists, including Hawking, now think that the radiation is a highly processed version of the information that went into the hole during its formation. Although matter cannot leave the hole, its information content can. Understanding precisely how is one of the liveliest questions in physics right now.

Last year Gary Horowitz of the University of California at Santa Barbara and Juan Maldacena of the Institute for Advanced Study in Princeton, N.J., outlined one possible mechanism. The escape hatch is entanglement, a quantum phenomenon in which the properties of two or more systems remain correlated across the reaches of space and time. Entanglement enables teleportation, in which information is transferred from one particle to another with such fidelity that the particle has effectively been beamed from one location to another at up to the speed of light.

The teleportation procedure, which has been demonstrated in the laboratory, first requires that two particles be entangled. Then a measurement is performed on one of the particles jointly with some matter that contains information to be teleported. The measurement erases the information from its original location, but because of entanglement, that information resides in an encoded form on the second particle, no matter how distant it may be. The information can be decoded using the results of the measurement as the key [see “Quantum Teleportation,” by Anton Zeilinger; SCIENTIFIC AMERICAN, April 2000].

A similar procedure might work for black holes. Pairs of entangled photons materialize at the event horizon. One of the photons flies outward to become the Hawking radiation that an observer sees. The other falls in and hits the singularity together with the matter that formed the hole in the first place. The annihilation of the infalling photon acts as a measurement, transferring the information contained in the matter to the outgoing Hawking radiation.

The difference from laboratory teleportation is that the results of this “mea-
“Objects so dense that nothing, not even light, can escape”—this definition of black holes has become a cliché of newspaper articles and freshman astronomy lectures. But it is probably wrong. Physicists have argued since the mid-1970s that energy can leak out of a black hole, and most now think that information (which describes the form that the energy takes) can, too. These diagrams show a black hole from a hypothetical viewpoint outside spacetime.

CLASSICAL VIEW, based on prequantum physics, holds that a blob of matter falling through the hole’s outer rim—the event horizon—can neither escape nor send out its information. It hits the center of the hole—the singularity—where its mass is assimilated and its information lost.

HAWKING MODEL is a first stab at considering quantum effects. Pairs of virtual particles materialize at the event horizon [red and blue balls]. One member of each pair, like other matter, falls to the singularity. Its partner flies outward. The particle spins are random and do not carry any information about the infalling blob.

HOROWITZ-MALDACENA MODEL suggests that the outgoing particle carries away not just raw mass but also information. The particle is quantum-mechanically entangled with its infalling partner, which in turn gets entangled with the blob. The entanglement beams the blob’s information out.

SINGULARITY

MATTER

EVENT HORIZON

VIRTUAL-PARTICLE PAIR

QUANTUM TELEPORTATION

Past June one of us (Lloyd) showed that the Horowitz-Maldacena mechanism is robust; it does not depend on what exactly the final state is, as long as there is one. It still seems to lead to a small loss of information, however.

Other researchers have proposed escape mechanisms that also rely on weird quantum phenomena. In 1996 Andrew Strominger and Cumrun Vafa of Harvard University suggested that black holes are composite bodies made up of multidimensional structures called branes, which arise in string theory. Information falling into the black hole is stored in waves in the branes and can eventually leak out. Earlier this year Samir Mathur of Ohio State University and his collaborators modeled a black hole as a giant tangle of strings. This “fuzzyball” acts as a repository of the information carried by things that fall into the black hole. It emits radiation that reflects this information. Hawking, in his recent approach, has argued that quantum fluctuations prevent a well-defined event horizon from ever forming [see “Hawking a Theory,” by Graham P. Collins; News Scan, October]. The jury is still out on all these ideas.
The process of mapping the geometry of spacetime is a kind of computation, in which distances are gauged by transmitting and processing information. One way to do this is to fill a region of space with a swarm of Global Positioning System satellites, each containing a clock and a radio transmitter [see illustration on next page]. To measure a distance, a satellite sends a signal and times how long it takes to arrive. The precision of the measurement depends on how fast the clocks tick. Ticking is a computational operation, so its maximum rate is given by the Margolus-Levitin theorem: the time between ticks is inversely proportional to the energy.

The energy, in turn, is also limited. If you give the satellites too much energy or pack them too closely together, they will form a black hole and will no longer be able to participate in mapping. (The hole will still emit Hawking radiation, but that radiation has a wavelength the size of the hole itself and so is not useful for mapping features on a finer scale.) The maximum total energy of the constellation of satellites is proportional to the radius of the region being mapped.

Thus, the energy increases more slowly than the volume of the region does. As the region gets bigger, the cartographer faces an unavoidable trade-off: reduce the density of satellites (so they are spaced farther apart) or reduce the energy available to each satellite (so that their clocks tick more slowly). Either way, the measurement becomes less precise. Mathematically, in the time it takes to map a region of radius \( R \), the total number of ticks by all the satellites is \( R^3/l_P^2 \). If each satellite ticks precisely once during the mapping process, the satellites are spaced out by an average distance of \( R^{15/2}l_P^{2/3} \). Shorter distances can be measured in one subregion but only at the expense of reduced precision in some other subregion. The argument applies even if space is expanding.

This formula gives the precision to which distances can be determined; it is applicable when the measurement apparatus is just on the verge of becoming a black hole. Below the minimum scale, spacetime geometry ceases to exist. That level of precision is much, much bigger than the Planck length. To be sure, it is still very small. The average imprecision in measuring the size of the observable universe is about \( 10^{-15} \) meter. Nevertheless, such an imprecision might be detectable by precise distance-measuring equipment, such as future gravitational-wave observatories.

From a theorist’s point of view, the broader significance of this result is that it provides a new way to look at black holes. Ng has shown that the strange scaling of spacetime fluctuations with the cube root of distances provides a back-door way to derive the Bekenstein-Hawking formula for black hole memory. It also implies a universal bound for all black hole computers: the number of bits in the memory is proportional to the square of the computation rate. The proportionality constant is \( G\hbar c^5 \)—mathematically demonstrating the linkage between information and the theories of special relativity (whose defining parameter is the speed of light, \( c \)), general relativity (the gravitational con-
Computing Spacetime

Measuring distances and time intervals is a type of computation and falls under the same constraints that computers do. It turns out that measurement is a much more slippery process than physicists had thought.

Perhaps most significantly, the result leads directly to the holographic principle, which suggests that our three-dimensional universe is, in some deep but unfathomable way, two-dimensional. The maximum amount of information that any region of space can store seems to be proportional not to its volume but to its surface area [see “Information in the Holographic Universe,” by Jacob D. Bekenstein; SCIENTIFIC AMERICAN, August 2003]. The holographic principle is normally thought to arise from the unknown details of quantum gravity, yet it also follows directly from the fundamental quantum limits to the precision of measurement.

The Answer Is ... 42

The principles of computation can be applied not just to the most compact computers (black holes) and tiniest possible computers (spacetime foam) but also to the largest: the universe. The universe may well be infinite in extent, but it has existed a finite length of time, at least in its present form. The observable part is currently some tens of billions of light-years across. For us to know the results of a computation, it must have taken place within this expanse.

The above analysis of clock ticks also gives the number of operations that can have occurred in the universe since it began: 10^{123}. Compare this limit with the behavior of the matter around us—the visible matter, the dark matter and the so-called dark energy that is causing the universe to expand at an accelerated rate. The observed cosmic energy density is about 10^{-50} joule per cubic meter, so the universe contains 10^{72} joules of energy. According to the Margolus-Levitin theorem, it can perform up to 10^{106} operations per second, for a total of 10^{123} operations during its lifetime so far. In other words, the universe has performed the maximum possible number of operations allowed by the laws of physics.

To calculate the total memory capacity of conventional matter, such as atoms, one can apply the standard methods of statistical mechanics and cosmology. Matter can embody the most information when it is converted to energetic, massless particles, such as neutrinos or photons, whose entropy density is proportional to the cube of their temperature. The energy density of the par-
The universe has performed the maximum possible number of operations allowed by the laws of physics.

Particles (which determines the number of operations they can perform) goes as the fourth power of their temperature. Therefore, the total number of bits is just the number of operations raised to the three-fourths power. For the whole universe, that amounts to \(10^{92}\) bits. If the particles contain some internal structure, the number of bits might be somewhat higher. These bits flip faster than they intercommunicate, so the conventional matter is a highly parallel computer, like the ultimate laptop and unlike the black hole.

As for dark energy, physicists do not know what it is, let alone how to calculate how much information it can store. But the holographic principle implies that the universe can store a maximum of \(10^{123}\) bits—nearly the same as the total number of operations. This approximate equality is not a coincidence. Our universe is close to its critical density. If it had been slightly more dense, it might have undergone gravitational collapse, just like the matter falling into a black hole. So it meets (or nearly meets) the conditions for maxing out the number of computations. That maximum number is \(R^2/l_P^2\), which is the same as the number of bits given by the holographic principle. At each epoch in its history, the maximum number of bits that the universe can contain is approximately equal to the number of operations it could have performed up to that moment.

Whereas ordinary matter undergoes a huge number of operations, dark energy behaves quite differently. If it encodes the maximum number of bits allowed by the holographic principle, then the overwhelming majority of those bits have had time to flip no more than once over the course of cosmic history. So these unconventional bits are mere spectators to the computations performed at much higher speeds by the smaller number of conventional bits. Whatever the dark energy is, it is not doing very much computation. It does not have to. Supplying the missing mass of the universe and accelerating its expansion are simple tasks, computationally speaking.

What is the universe computing? As far as we can tell, it is not producing a single answer to a single question, like the giant Deep Thought computer in the science-fiction classic *The Hitchhiker's Guide to the Galaxy*. Instead the universe is computing itself. Powered by Standard Model software, the universe computes quantum fields, chemicals, bacteria, human beings, stars and galaxies. As it computes, it maps out its own spacetime geometry to the ultimate precision allowed by the laws of physics. Computation is existence.

These results spanning ordinary computers, black holes, spacetime foam and cosmology are testimony to the unity of nature. They demonstrate the conceptual interconnections of fundamental physics. Although physicists do not yet possess a full theory of quantum gravity, whatever that theory is, they know it is intimately connected with quantum information. It from qubit.

**MORE TO EXPLORE**


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**MATTER**

- Speed: \(10^{14}\) hertz
- Memory: \(10^{92}\) bits

**DARK ENERGY**

- Speed: \(>10^{-18}\) hertz
- Memory: <\(10^{123}\) bits