

A Brief History of Computing

Gabriel Robins

Department of

Computer Science

University of Virginia

www.cs.virginia.edu/robins

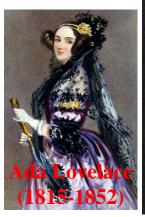


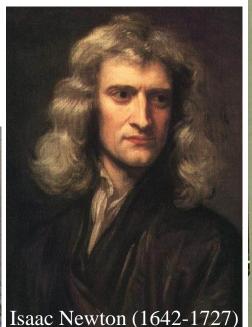


- Knowing the "big picture" is empowering
- Science and mathematics builds heavily on past
- Often the simplest ideas are the most subtle
- Most fundamental progress was done by a few
- We learn much by observing the best minds
- Research benefits from seeing connections
- The field of computer science has many "parents"
- We get inspired and motivated by excellence
- The giants can show us what is possible to achieve
- It is fun to know these things!

"Standing on the Shoulders of Giants"

- Aristotle, Euclid, Archimedes, Eratosthenes
- Abu Ali al-Hasan ibn al-Haytham
- Fibonacci, Descartes, Fermat, Pascal
- Newton, Euler, Gauss, Hamilton
- Boole, De Morgan
- Babbage, Ada Lovelace
- Venn, Carroll



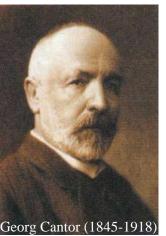




"Standing on the Shoulders of Giants"

- Cantor, Hilbert, Russell
- Hardy, Ramanujan, Ramsey
- Gödel, Church, Turing
- von Neumann, Shannon
- Kleene, Chomsky
- Hoare, McCarthy, Erdos
- Knuth, Backus, Dijkstra

Many others...







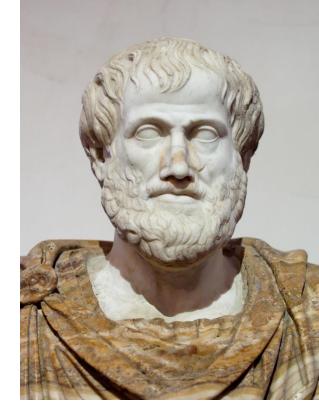


MAKING PHILOSOPHY ACCESSIBLE: POP-UP PLATO



Aristotle (384BC-322BC)

- Founded Western philosophy
- Student of Plato
- Taught Alexander the Great
- "Aristotelianism"
- Developed the "scientific method"
- One of the most influential people ever
- Wrote on physics, theatre, poetry, music, logic, rhetoric, politics, government, ethics, biology, zoology, morality, optics, science, aesthetics, psychology, metaphysics, ...
- Last person to know everything known in his own time!
- "Almost every serious intellectual advance has had to begin with an attack on some Aristotelian doctrine." – Bertrand Russell







APISTOTENHE



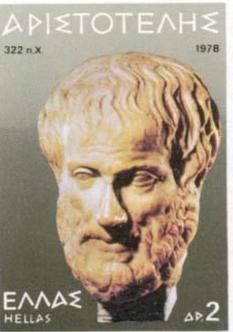


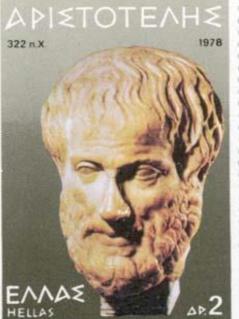




- Aristotle (384-322 B.C.)

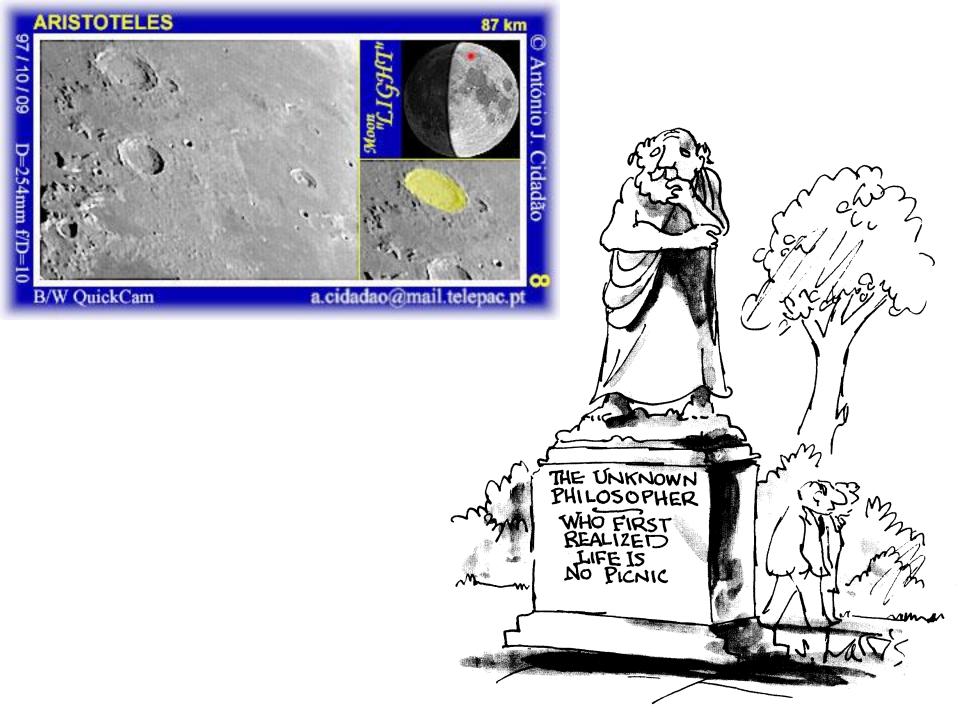














"The periodic table."

Euclid (325BC-265BC)

- Founder of geometry
 & the axiomatic method
- "Elements" oldest and most impactful textbook
- Unified logic & math
- Introduced rigor and "Euclidean" geometry
- Influenced all other fields of science:
 Copernicus, Kepler, Galileo, Newton,
 Russell, Lincoln, Einstein & many others



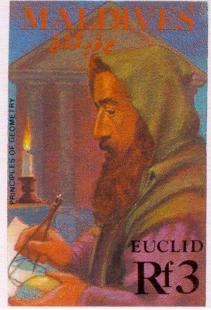


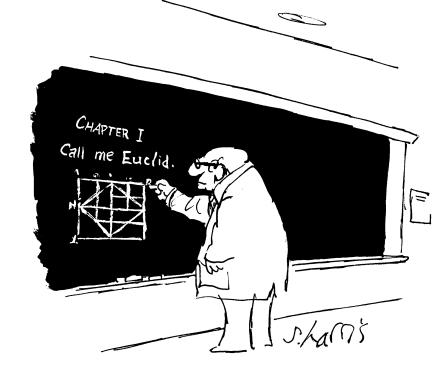




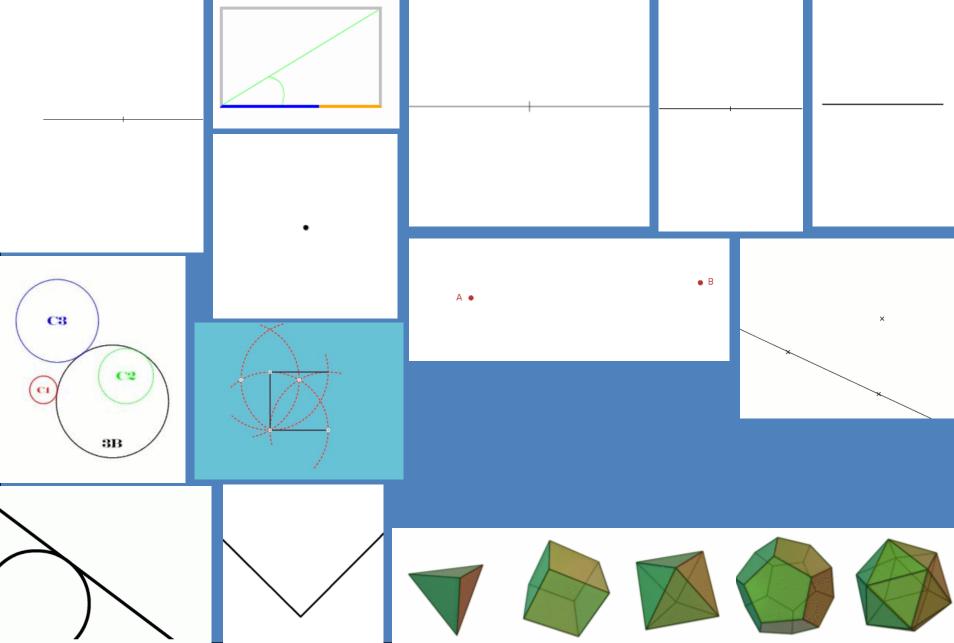








Euclid's Straight-Edge and Compass Geometric Constructions



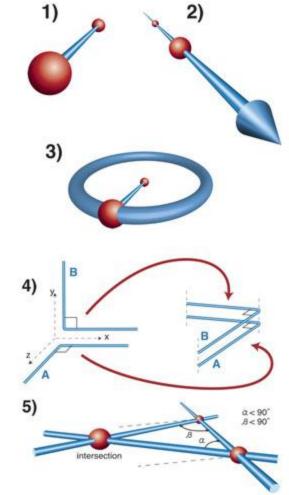
Euclid's Axioms

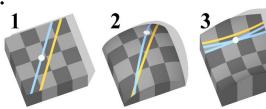
- 1: Any two points can be connected by exactly one straight line.
- 2: Any segment can be extended indefinitely into a straight line.
- 3: A circle exists for any given center and radius.
- 4: All right angles are equal to each other.
- 5: The parallel postulate: Given a line and a point off that line, there is exactly one line passing through the point, which does not intersect the first line.

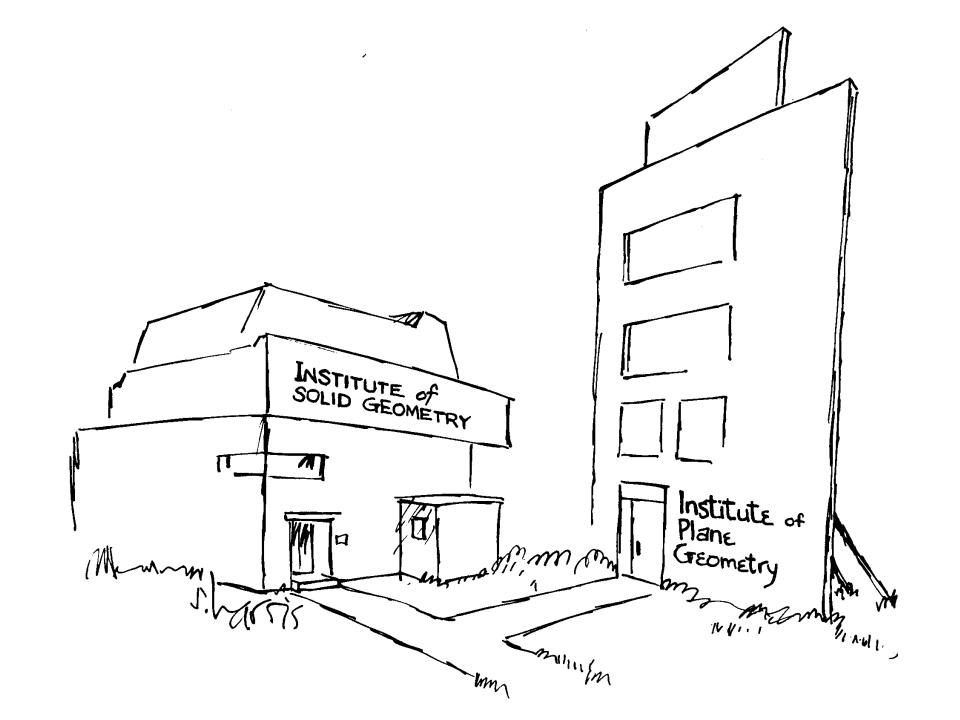
The first 28 propositions of Euclid's Elements were proven without using the parallel postulate!

Theorem [Beltrami, 1868]: The parallel postulate is independent of the other axioms of Euclidean geometry.

The parallel postulate can be modified to yield non-Euclidean geometries!

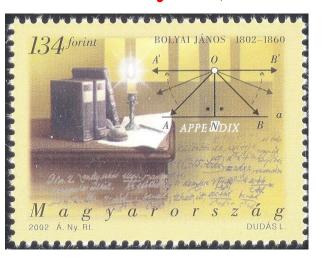






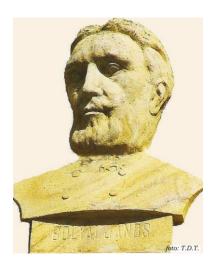
Founders of Non-Euclidean Geometry

János Bolyai (1802-1860)









Nikolai Ivanovich Lobachevsky (1792-1856)









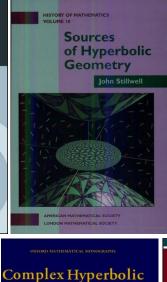


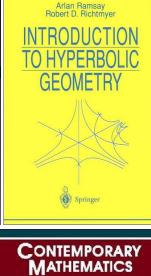
James W. Anderson



Hyperbolic Geometry





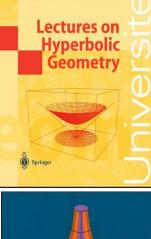


Complex Manifolds and Hyperbolic Geometry

Clifford J. Earle

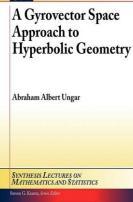
William J. Harvey Sev'ı n Recilias-Pishmish





Riccardo Benedetti

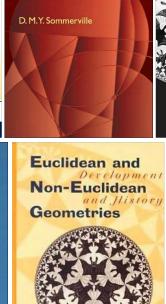
Carlo Petronio



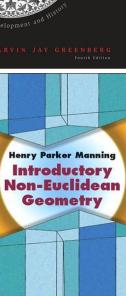
NON-EUCLIDEAN

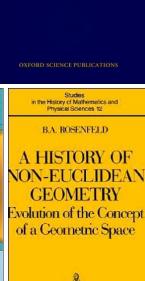
GEOMETRY

H. S. M. COXETER



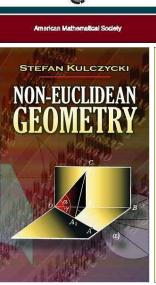
THE ELEMENTS OF NON-EUCLIDEAN GEOMETRY

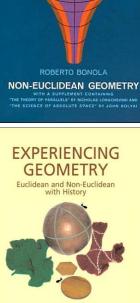




Springer-Verlag

Geometry



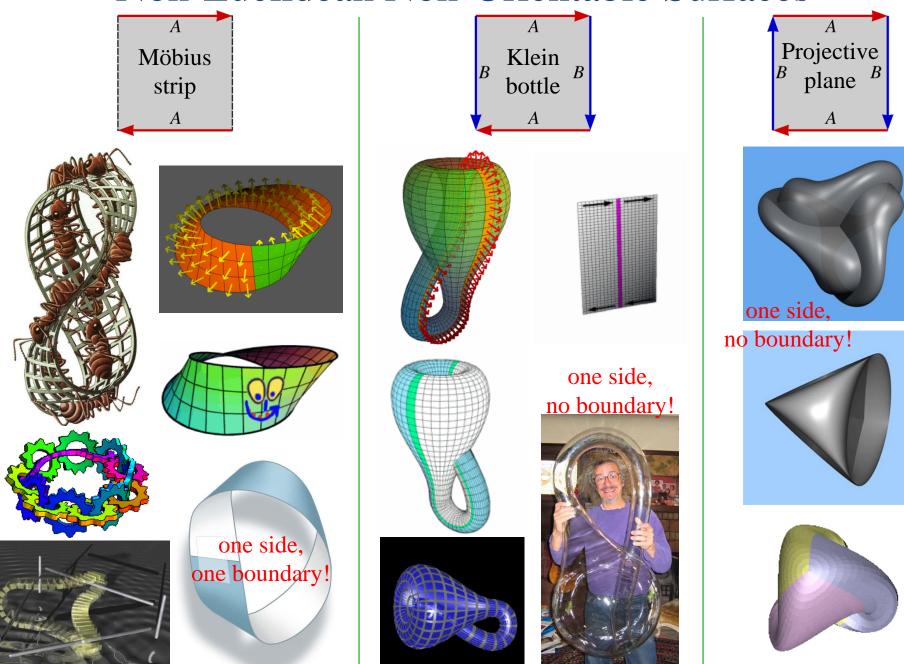


David W. Henderson Daina Taimina





Non-Euclidean Non-Orientable Surfaces

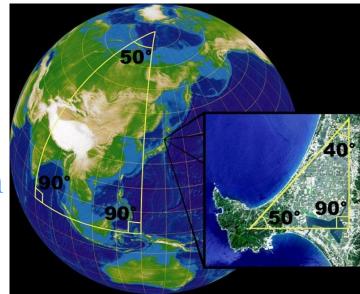


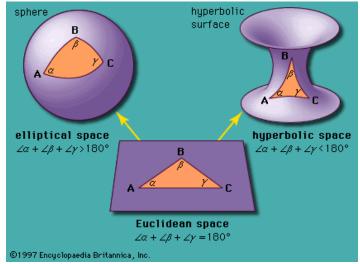
Non-Euclidean Geometries

Spherical / Elliptic geometry: Given a line and a point off that line, there are no lines passing through that point that do not

intersect the first line.

- Lines are geodesics "great circles"
- Sum of triangle angles is $> 180^{\circ}$
- Not all triangles have same angle sum
- Figures can not scale up indefinitely
- Area does not scale as the square
- Volume does not scale as the cube
- The Pythagorean theorem fails
- Self-consistent, and complete

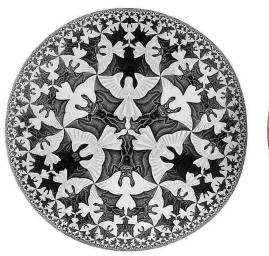


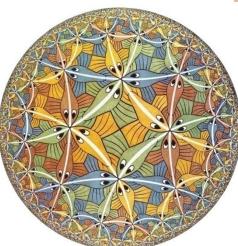


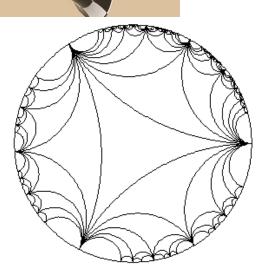
Non-Euclidean Geometries

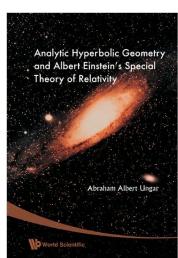
Hyperbolic geometry: Given a line and a point off that line, there are an infinity of lines passing through that point that do not intersect the first line.

- Sum of triangle angles is less than 180°
- Different triangles have different angle sum
- Triangles with same angles have same area
- There are no similar triangles
- Used in relativity theory

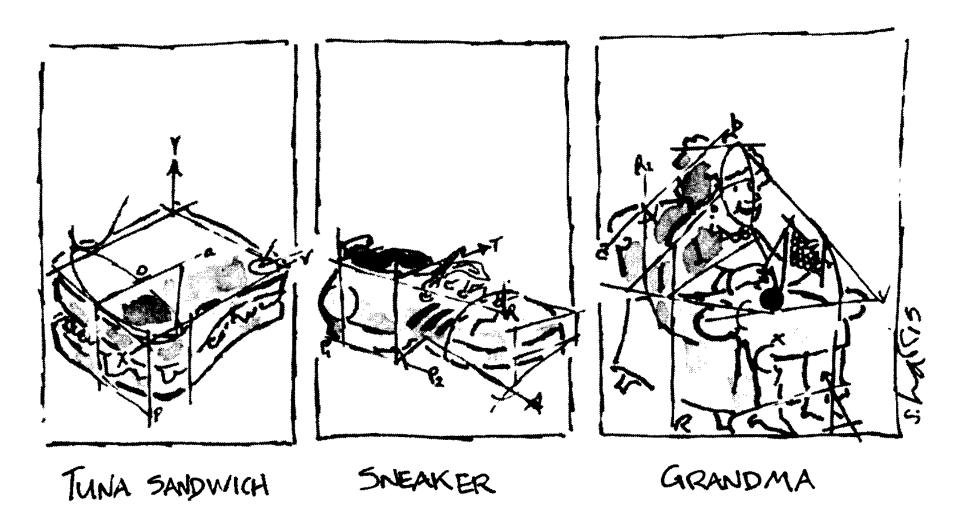






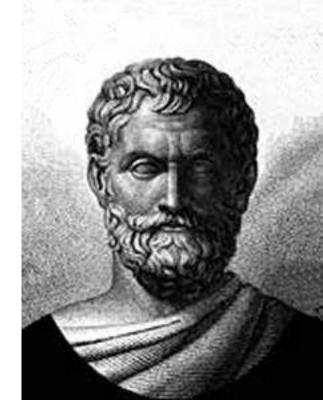


THE GEOMETRY OF EVERYDAY LIFE



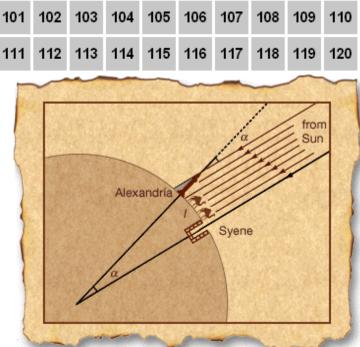
Eratosthenes (276BC-194BC)

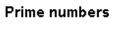
- Chief librarian at Library of Alexandria
- Measured the Earth's size (<1% error!)
- Calculated the Earth-Sun distance
- Invented latitude and longtitude
- Primes "Sieve of Eratosthenes"
- Chronology of ancient history
- Wrote on astronomy, geography, history, mathematics, philosophy, and literature

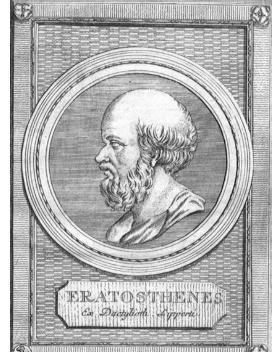


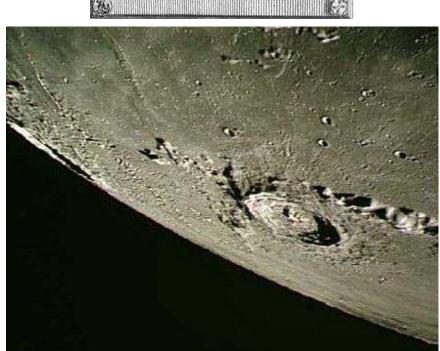
ж	2	3	X	5	×	7	X	9 <	蚀
11	32	13	14	矮	16	17	18	19	28
2 (22	23	24	2 5	26	27	28	29	3Q
31	3	38	34	35	36	37	38	39	40
41	4 2	43	*	45	46	47	48	49	5 0
¥	52	53	54	55	56	57	56	59	96
61	62	63	94	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
8 (8 2	83	84	85	3 6	87	88	89	90
91	9 2	3 8	94	95	96	97	98	99	1)00

	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100
101	102	103	104	105	106	107	108	109	110
111	112	113	114	115	116	117	118	119	120
					-		MA AND		







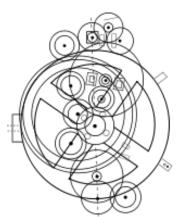


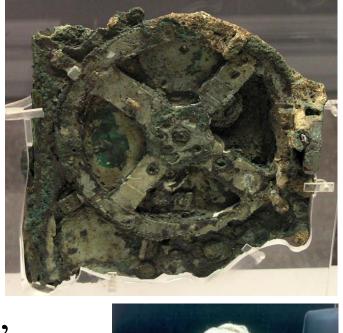
An Ancient Computer: The Antikythera

- Oldest known mechanical computer
- Built around 150-100 BCE!
- Calculates eclipses and astronomical positions of sun, moon, and planets
- Very sophisticated for its era
- Contains dozens of intricate gears
- Comparable to 1700's Swiss clocks
- Has an attached "instructions manual"
- Still the subject of ongoing research

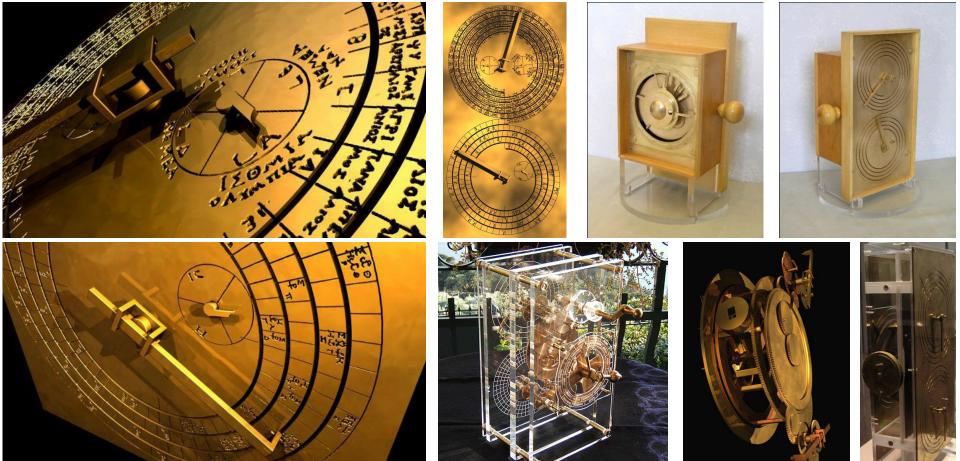




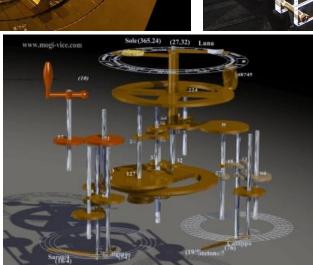




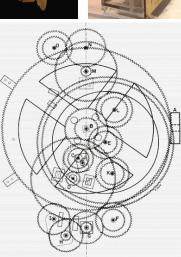


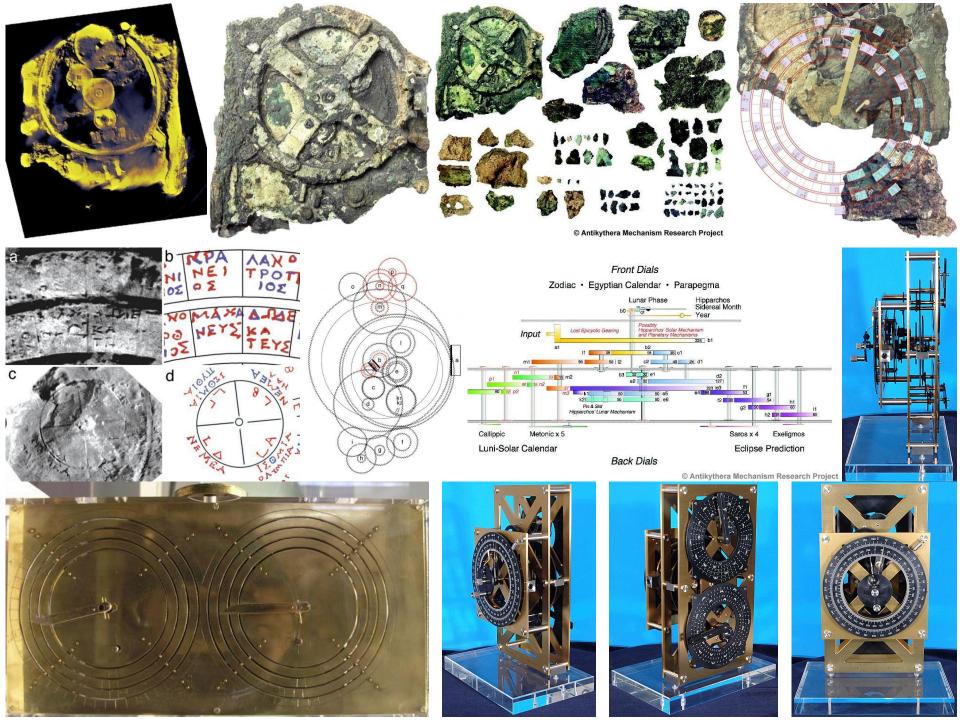


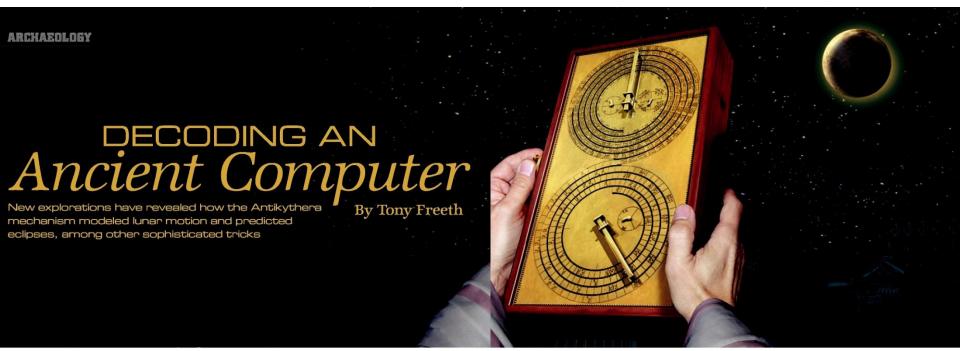












KEY CONCEPTS

- The Antikythera mechanism is a unique mechanical calculator from second-century B.C. Greece. Its sophistication surprised archaeologists when it was discovered in 1901. But no one had anticipated its true power.
- Advanced imaging tools have finally enabled researchers to reconstruct how the device predicted lunar and solar eclipses and the motion of the moon in the sky.
- Inscriptions on the mechanism suggest that it might have been built in the Greek city of Syracuse (now in modern Sicily), perhaps in a tradition that originated with Archimedes.

-The Editors

f it had not been for two storms 2,000 years apart in the same area of the Mediterranean, the most important technological artifact from the ancient world could have been lost forever.

The first storm, in the middle of the 1st century B.C., sank a Roman merchant vessel laden with Greek treasures. The second storm, in A.D. 1900, drove a party of sponge divers to shelter off the tiny island of Antikythera, between Crete and the mainland of Greece. When the storm subsided, the divers tried their luck for sponges in the local waters and chanced on the wreck. Months later the divers returned, with backing from the Greek government. Over nine months they recovered a hoard of beautiful ancient Greek objects—rare bronzes, stunning glassware, amphorae, pottery and jewelry—in one of the first major underwater archaeological excavations in history.

One item attracted little attention at first: an undistinguished, heavily calcified lump the size of a phone book. Some months later it fell apart, revealing the remains of corroded bronze gearwheels—all sandwiched together and with teeth just one and a half millimeters long—along with plates covered in scientific scales and Greek in plates covered in plates covered in plates c

scriptions. The discovery was a shock: until then, the ancients were thought to have made gears only for crude mechanical tasks.

Three of the main fragments of the Antikythera mechanism, as the device has come to be known, are now on display at the Greek National Archaeological Museum in Athens. They look small and fragile, surrounded by imposing bronze statues and other artistic glories of ancient Greece. But their subtle power is even more shocking than anyone had imagined at first.

I first heard about the mechanism in 2000. I was a filmmaker, and astronomer Mike Edmunds of Cardiff University in Wales contacted me because he thought the mechanism would make a great subject for a TV documentary. I learned that over many decades researchers studying the mechanism had made considerable progress, suggesting that it calculated astronomical data, but they still had not been able to fully grasp how it worked. As a former mathematician, I became intensely interested in understanding the mechanism myself.

Edmunds and I gathered an international collaboration that eventually included historians, astronomers and two teams of imaging experts. In the past few years our group has reconstructed how nearly all the surviving parts worked and what functions they performed. The mechanism calculated the dates of lunar and solar eclipses, modeled the moon's subtle apparent motions through the sky to the best of the available knowledge, and kept track of the dates of events of social significance, such as the Olympic Games. Nothing of comparable technological sophistication is known anywhere in the world for at least a millennium afterward. Had this unique specimen not survived, historians would have thought that it could not have existed at that time.

Early Pioneers

German philologist Albert Rehm was the first person to understand, around 1905, that the Antikythera mechanism was an astronomical calculator. Half a century later, when science historian Derek J. de Solla Price, then at the Institute for Advanced Study in Princeton, N.J., described the device in a Scientific American article, it still had revealed few of its secrets.

The device, Price suggested, was operated by turning a crank on its side, and it displayed its output by moving pointers on dials located on its front and back. By turning the crank, the user could set the machine on a certain date as indi-

cated on a 365-day calendar dial in the front. (The dial could be rotated to adjust for an extra day every four years, as in today's leap years.) At the same time, the crank powered all the other gears in the mechanism to yield the information corresponding to the set date.

A second front dial, concentric with the calendar, was marked out with 360 degrees and with the 12 signs representing the constellations of the zodiac [see box on pages 80 and 81]. These are the constellations crossed by the sun in its apparent motion with respect to the "fixed" stars—"motion" that in fact results from Earth's orbiting the sun—along the path called the ecliptic. Price surmised that the front of the mechanism probably had a pointer showing where along the ecliptic the sun would be at the desired date.

In the surviving fragments, Price identified the remains of a dozen gears that had been part of the mechanism's innards. He also estimated their tooth counts—which is all one can do given that nearly all the gears are damaged and incomplete. Later, in a landmark 1974 study, Price described 27 gears in the main fragment and provided improved tooth counts based on the first x-rays of the mechanism, by Greek radiologist Charalambos Karakalos.

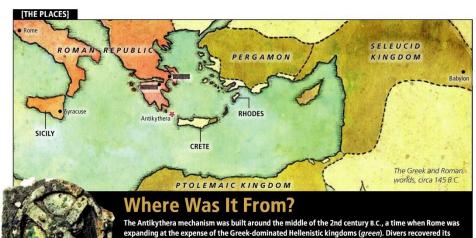
ANCIENT GREEKS knew how to calculate the recurring patterns of lunar eclipses thanks to observations made for centuries by the Babylonians. The Antikythera mechanism would have done those calculations for them—or perhaps for the wealthy Romans who could afford to own it. The depiction here is based on a theoretical reconstruction by the author and his collaborators.

76 SCIENTIFIC AMERICAN

© 2009 SCIENTIFIC AMERICAN, INC.

December 2009 Www.ScientificAmerican.com

© 2009 SCIENTIFIC AMERICAN, INC.



corroded remnants (including fragment at left) in A.D. 1901 from a shipwreck near the island of Antikythera. The ship sank around 65 B.C. while carrying Greek artistic treasures, perhaps from Pergamon to

Greek inventor Archimedes had lived there and may have left behind a technological tradition.

Rome. Rhodes had one of the major traditions of Greek astronomy, but the latest evidence points to a Corinthian origin. Syracuse, which had been a Corinthian colony in Sicily, is a possibility: the great

[THE AUTHOR]

Tony Freeth's academic background is in mathematics and mathematical logic (in which he holds a Ph.D.). His award-winning career as a filmmaker culminated in a series of documentaries about increasing crop yields in sub-Saharan Africa, featuring the late Nobel Peace Prize Laureate Norman Borlaug, Since 2000 Freeth has returned to an academic focus with research on the Antikythera mechanism. He is managing director of the film and television production company Images First, and he is now developing a film on the mechanism.



Tooth counts indicate what the mechanism calculated. For example, turning the crank to give a full turn to a primary 64-tooth gear represented the passage of a year, as shown by a pointer on the calendar dial. That primary gear was also paired to two 38-tooth secondary gears, each of which consequently turned by 64/38 times for every year. Similarly, the motion relayed from gear to gear throughout the mechanism; at each step, the ratio of the numbers of gear teeth represents a different fraction. The motion eventually transmitted to the pointers, which thus turned at rates corresponding to different astronomical cycles. Price discovered that the ratios of one of these gear trains embodied

Price, like Rehm before him, suggested that the mechanism also contained epicyclic gearing-gears spinning on bearings that are themselves attached to other gears, like the cups on a Mad Hatter teacup ride. Epicyclic gears extend the range of formulas gears can calculate beyond multiplications of fractions to additions and subtractions. No other example of epicyclic gearing is known to have existed in Western technology for another 1,500 years.

an ancient Babylonian cycle of the moon.

Several other researchers studied the mechanism, most notably Michael Wright, a curator at the Science Museum in London, in collaboration

with computer scientist Allan Bromley of the University of Sydney. They took the first threedimensional x-rays of the mechanism and showed that Price's model of the mechanism had to be wrong. Bromley died in 2002, but Wright persisted and made significant advances. For example, he found evidence that the back dials, which at first look like concentric rings, are in fact spirals and discovered an epicyclic mechanism at the front that calculated the phase of the moon.

Wright also adopted one of Price's insights, namely that the dial on the upper back might be a lunar calendar, based on the 19-year, 235lunar-month cycle called the Metonic cycle. This calendar is named after fifth-century B.C. astronomer Meton of Athens-although it had been discovered earlier by the Babylonians-and is still used today to determine the Jewish festival of Rosh Hashanah and the Christian festival of Easter. Later, we would discover that the pointer was extensible, so that a pin on its end could follow a groove around each successive turn of the spiral.

BladeRunner in Athens

As our group began its efforts, we were hampered by a frustrating lack of data. We had no access to the previous x-ray studies, and we did not even have a good set of still photographs.

Two images in a science magazine-x-rays of a goldfish and an enhanced photograph of a Babvlonian clay tablet-suggested to me new ways o get better data.

We asked Hewlett-Packard in California to perform state-of-the-art photographic imaging and X-Tek Systems in the U.K. to do three-dimensional x-ray imaging. After four years of careful diplomacy, John Seiradakis of the Aristotle University of Thessaloniki and Xenophon Moussas of the University of Athens obtained the required permissions, and we arranged for the imaging teams to bring their tools to Athens, a necessary step because the Antikythera mechanism is too fragile to travel.

Meanwhile we had a totally unexpected call from Mary Zafeiropoulou at the museum. She had been to the basement storage and found boxes of bits labeled "Antikythera." Might we be interested? Of course we were interested. We now had a total of 82 fragments, up from about 20.

The HP team, led by Tom Malzbender, assembled a mysterious-looking dome about five feet across and covered in electronic flashbulbs that provided lighting from a range of different angles. The team exploited a technique from the computer gaming industry, called polynomial exture mapping, to enhance surface details. Inscriptions Price had found difficult to read were now clearly legible, and fine details could be enhanced on the computer screen by controlling the reflectance of the surface and the angle of the lighting. The inscriptions are essentially an instruction manual written on the outer plates.

A month later local police had to clear the streets in central Athens so that a truck carrying the BladeRunner, X-Tek's eight-ton x-ray machine, could gain access to the museum. The BladeRunner performs computed tomography similar to a hospital's CT scan, but with finer detail. X-Tek's Roger Hadland and his group had specially modified it with enough x-ray power to penetrate the fragments of the Antikythera mechanism. The resulting 3-D reconstruction was wonderful: whereas Price could see only a puzzle of overlapping gears, we could now isolate layers inside the fragment and see all the fine details of the gear teeth.

Unexpectedly, the x-rays revealed more than 2,000 new text characters that had been hidden deep inside the fragments. (We have now identified and interpreted a total of 3,000 characters out of perhaps 15,000 that existed originally.) In Athens, Moussas and Yanis Bitsakis, also at the University of Athens, and Agamemnon Tselikas of the Center for History and Palaeography be-

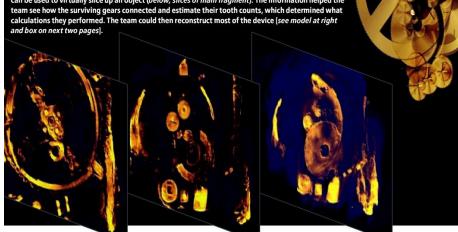
Historians would have thought that SOMETHING

SO COMPLEX could not have existed at the time.

[THE RECONSTRUCTION]

Anatomy of a Relic

Computed tomography—a 3-D mapping obtained from multiple x-ray shots—enabled the author and his colleagues to get inside views of the Antikythera mechanism's remnants. For example, a CT scan can be used to virtually slice up an object (below, slices of main fragment). The information helped the



78 SCIENTIFIC AMERICAN December 2009 www.ScientificAmerican.com SCIENTIFIC AMERICAN 79 @ 2000 CCIENTIFIC AMERICAN INC

gan to discover inscriptions that had been invisible to human eyes for more than 2,000 years. One translated as "... spiral subdivisions 235...," confirming that the upper back dial was a spiral describing the Metonic calendar.

[INSIDE THE ANTIKYTHERA MECHANISM]

EGYPTIAN

of a year.

CALENDAR DIAL

Displayed 365 days

Date pointer

Solar pointer

PLANETARY POINTERS (HYPOTHETICAL)

May have shown

the positions of

the planets on

the zodiac dial

FRONT-PLATE INSCRIPTIONS

Described the rising and setting times

of important stars throughout the year

Astronomical

Clockwork

ZODIAC DIAL

Showed the 12

constellations along the ecliptic, the

sun's path in the sky.

LUNAR POINTER

Showed the posi-

tion of the moon

with respect to the

constellations on

the zodiac dial.

Babylon System

Back at home in London, I began to examine the CT scans as well. Certain fragments were clearly all part of a spiral dial in the lower back. An estimate of the total number of divisions in the dial's four-turn spiral suggested 220 to 225.

The prime number 223 was the obvious contender. The ancient Babylonians had discovered that if a lunar eclipse is observed-something that can happen only during a full moon-usually a similar lunar eclipse will take place 223 full moons later. Similarly, if the Babylonians saw a solar eclipse—which can take place only during a new moon—they could predict that 223 new moons later there would be a similar one (although they could not always see it: solar eclipses are visible only from specific locations, and ancient astronomers could not predict them reliably). Eclipses repeat this way because every 223 lunar months the sun, Earth and the moon return to approximately the same alignment with respect to one another, a periodicity known as the Saros cycle.

Between the scale divisions were blocks of symbols, nearly all containing Σ (sigma) or H (eta), or both. I soon realized that Σ stands for Σ elphyn (selene), Greek for "moon," indicating a lunar eclipse; H stands for Hlloo (helios), Greek for "sun," indicating a solar eclipse. The Babylonians also knew that within the 223-month period, eclipses can take place only in particular months, arranged in a predictable pattern and separated by gaps of five or six months; the distribution of symbols around the dial exactly matched that pattern.

I now needed to follow the trail of clues into the heart of the mechanism to discover where this new insight would lead. The first step was to find a gear with 223 teeth to drive this new Saros dial. Karakalos had estimated that a large gear visible at the back of the main fragment had 222 teeth. But Wright had revised this estimate to 223, and Edmunds confirmed this. With plausible tooth counts for other gears and with the addition of a small, hypothetical gear, this 223-tooth gear could perform the required calculation.

But a huge problem still remained unsolved and proved to be the hardest part of the gearing to crack. In addition to calculating the Saros cyThis exploded view of the mechanism shows all but one of the 30 known gears, plus a few that have been hypothesized. Turning a crank on the side activated all the gears in the mechanism and moved pointers on the front and back dials: the arrows colored blue, red and yellow explain how the motion transmitted from one gear to the next. The user would choose a date on the Egyptian, 365-day calendar dial on the front or on the Metonic, 235-lunar-month calen-

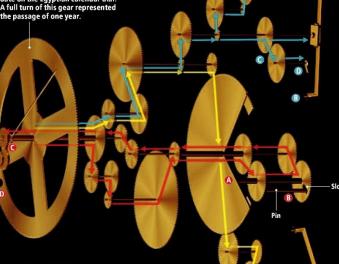
dar on the back and then read the astronomical predictions for that time—such as the position and phases of the moon—from the other dials. Alternatively, one could turn the crank to set a particular event on an astronomical dial and then see on what date it would occur. Other gears, now lost, may have calculated the positions of the sun and of some or all of the five planets known in antiquity and displayed them via pointers on the zodiac dial.

METONIC GEAR TRAIN

Calculated the month in the Metonic calendar, made of 235 lunar months, and displayed it via a pointer (a) on the Metonic calendar dial on the back. A pin (a) at the pointer's tip followed the spiral groove, and the pointer extended in length as it reached months marked on successive, outer twists. Auxiliary gears (a) turned a pointer (b) on a smaller dial indicating four-year cycles of Olympiads and other games. Other gears moved a pointer on another small dial (b), which may have indicated a 76-year cycle.

PRIMARY GEAR

When spun by the crank, it activated all other gears. It also directly moved a pointer that indicated the date on the Egyptian calendar dial. A full turn of this gear represented the passage of one year.

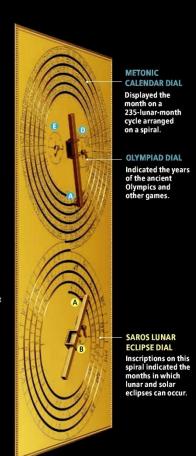


LUNAR GEAR TRAIN

A system that included epicyclic gears simulated variations in the moon's motion now know to stem from its changing orbital velocity. The epicyclic gears were attached to a larger gear (A like the cups on a Mad Hatter teacup ride. One gear turned the other via a pin-and-slot mechanism (B). The motion was then transmitted through the other gears and to the front of the mechanism. There, another epicyclic system (C) turned a half-black, half-white sphere (D) to show the lunar phases, and a pointer (E) showed the position of the mechanism.



Calculated the month in the 223-lunar-month Saros cycle of recurring eclipses. It displayed the month on the Saros dial with an extensible pointer $^{\circ}_{4}$, similar to the one on the Metonic dial. Auxiliary gears moved a pointer $^{\circ}_{4}$ on a smaller dial. That pointer made one third of a turn for each 223-month cycle to indicate that the corresponding eclipse time would be offset by eight hours.



cle, the large 223-tooth gear also carried the epicyclic system noticed by Price: a sandwich of two small gears attached to the larger gear in teacup-ride fashion. Each epicyclic gear also connected to another small gear. Confusingly, all four small gears appeared to have the same tooth count—50—which seemed nonsensical because the output would then be the same as the input.

After months of frustration, I remembered that Wright had observed that one of the two epicyclic gears has a pin on its face that engages with a slot on the other. His key idea was that the two gears turned on slightly different axes, separated by about a millimeter. As a consequence, the angle turned by one gear alternated between being slightly wider and being slightly narrower than the angle turned by the other gear. Thus, if one gear turned at a constant rate, the other gear's rate kept varying between slightly faster and slightly slower.

Ask for the Moon

Although Wright rejected his own observation, I realized that the varying rotation rate is precisely what is needed to calculate the moon's motion according to the most advanced astronomical theory of the second century B.C., the one often attributed to Hipparchos of Rhodes. Before Kepler (A.D. 1605), no one understood that orbits are elliptical and that the moon accelerates toward the perigee-its closest point to Earthand slows down toward the apogee, the opposite point. But the ancients did know that the moon's motion against the zodiac appears to periodically slow down and speed up. In Hipparchos's model, the moon moved at a constant rate around a circle whose center itself moved around a circle at a constant rate-a fairly good approximation of the moon's apparent motion. These circles on circles, themselves called epicycles, dominated astronomical thinking for the next 1,800 years.

There was one further complication: the apogee and perigee are not fixed, because the ellipse of the moon's orbit rotates by a full turn about every nine years. The time it takes for the body to get back to the perigee is thus a bit longer than the time it takes it to come back to the same point in the zodiac. The difference was just 0.112579655 turns a year. With the input gear having 27 teeth, the rotation of the large gear was slightly too big; with 26 teeth, it was slightly too small. The right result seemed to be about halfway in between. So I tried the impossible idea that the input gear had 26 ½ teeth. I pressed the key on my calculator, and it gave 0.112579655—

[A USER'S MANUAL]

How to Predict an Eclipse

Operating the Antikythera mechanism may have required only a small amount of practice and astronomical knowledge. After an initial calibration by an expert, the mechanism could provide fairly accurate predictions of events several decades in the past or future. The inscriptions on the Saros dial, coming at intervals of five or six months, corresponded to months when Earth, the sun and the moon come to a near alignment (and so represented potential solar and lunar eclipses) in a 223-lunar-month cycle. Once the month of an eclipse was known, the actual day could be calculated on the front dials using the fact that solar eclipses always happen during new moons and lunar eclipses during full moons.

exactly the right answer. It could not be a coincidence to nine places of decimals! But gears cannot have fractional numbers of teeth.

Then I realized that $26 \frac{1}{2} \times 2 = 53$. In fact. Wright had estimated a crucial gear to have 53 teeth, and I now saw that that count made everything work out. The designer had mounted the pin and slot epicyclically to subtly slow down the period of its variation while keeping the basic rotation the same, a conception of pure genius. Thanks to Edmunds, we also realized that the epicyclic gearing system, which is in the back of the mechanism, moved a shaft that turned inside another, hollow shaft through the rest of the mechanism and to the front, so that the lunar motion could be represented on the zodiac dial and on the lunar phase display. All gear counts were now explained, with the exception of one small gear that remains a mystery to this day.

Further research has caused us to make some modifications to our model. One was about a small subsidiary dial that is positioned in the back, inside the Metonic dial, and is divided into four quadrants. The first clue came when I read the word "NEMEA" under one of the quadrants. Alexander Jones, a New York University historian, explained that it refers to the Nemean Games, one of the major athletic events in ancient Greece. Eventually we found, engraved round the four sectors of the dial, most of "ISTHMIA," for games at Corinth, "PYTHIA," for games at Delphi, "NAA," for minor games at Dodona, and "OLYMPIA," for the most important games of the Greek world, the Olympics. All games took place every two or four years. Previously we had considered the mechanism to be Metonic dial

Date pointer

Solar pointer

FIND ECLIPSE MONTH

CALCULATE DAY

Begin by turning the crank to set the current month and year on the Metonic calendar. The lower pointer will turn to the corresponding month on the Saros (eclipse) dial.

Turn the crank to move time forward until the pointer on the Saros dial points to an eclipse inscription. The inscription will indicate month and time of the day (but not the day) of an eclipse and whether it will be solar or lunar. Adjust the crank until the lunar and solar pointers are aligned (for a solar eclipse) or at 180 degrees (for a lunar eclipse). The Egyptian calendar pointer will move correspondingly and indicate the day of the eclipse.

purely an instrument of mathematical astronomy, but the Olympiad dial—as we named it—gave it an entirely unexpected social function.

Twenty-nine of the 30 surviving gears calculate cycles of the sun and the moon. But our studies of the inscriptions at the front of the mechanism have also yielded a trove of information on the risings and settings of significant stars and of the planets. Moreover, on the "primary" gearwheel at the front of the mechanism remnants of bearings stand witness to a lost epicyclic system that could well have modeled the back-and-forth motions of the planets along the ecliptic (as well as the anomalies in the sun's own motion). All these clues strongly support the inclusion of the sun and of at least some of the five planets known in ancient times—Mercury, Venus, Mars, Jupiter and Saturn.

Wright built a model of the mechanism with epicyclic systems for all five planets. But his ingenious layout does not agree with all the evidence. With its 40 extra gears, it may also be too complex to match the brilliant simplicity of the rest of the mechanism. The ultimate answer may still lie 50 meters down on the ocean floor.

Eureka?

The question of where the mechanism came from and who created it is still open. Most of the cargo in the wrecked ship came from the eastern Greek world, from places such as Pergamon, Kos and Rhodes. It was a natural guess that Hipparchos or another Rhodian astronomer built the mechanism. But text hidden between the 235 monthly scale divisions of the Metonic calendar contradicts this view. Some of the month names

were used only in specific locations in the ancient Greek world and suggest a Corinthian origin. If the mechanism was from Corinth itself, it was almost certainly made before Corinth was completely devastated by the Romans in 146 B.C. Perhaps more likely is that it was made to be used in one of the Corinthian colonies in northwestern Greece or Sicily.

Sicily suggests a remarkable possibility. The island's city of Syracuse was home to Archimedes, the greatest scientist of antiquity. In the first century B.C. Roman statesman Cicero tells how in 212 Archimedes was killed at the siege of Syracuse and how the victorious Roman general, Marcellus, took away with him only one piece of plunder—an astronomical instrument made by Archimedes. Was that the Antikythera mechanism? We believe not, because it appears to have been made many decades after Archimedes died. But it could have been constructed in a tradition of instrument making that originated with the eureka man himself.

Many questions about the Antikythera mechanism remain unanswered—perhaps the greatest being why this powerful technology seems to have been so little exploited in its own era and in succeeding centuries.

In Scientific American, Price wrote:

It is a bit frightening to know that just before the fall of their great civilization the ancient Greeks had come so close to our age, not only in their thought, but also in their scientific technology.

Our discoveries have shown that the Antikythera mechanism was even closer to our world than Price had conceived.

MORE TO EXPLORE

An Ancient Greek Computer.
Derek J. de Solla Price in Scientific American, Vol. 200, No. 6, pages 60–67; June 1959.

Gears from the Greeks: The Antikythera Mechanism— A Calendar Computer from ca. 80 B.C. Derek de Solla Price in Transactions of the American Philosophical Society, New Series, Vol. 64, No. 7, pages 1–70: 1974.

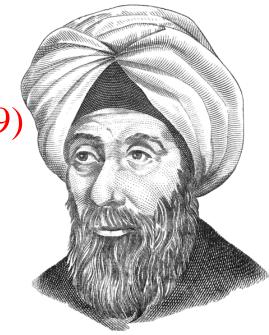
Decoding the Ancient Greek Astronomical Calculator Known as the Antikythera Mechanism. Tony Freeth et al. in *Nature*, Vol. 444, pages 587–591; November 30, 2006.

Calendars with Olympiad Display and Eclipse Prediction on the Antikythera Mechanism. Tony Freeth, Alexander Jones, John M. Steele and Yanis Bitsakis in Nature, Vol. 454, pages 614–617; July 31, 2008.

The Antikythera Mechanism Research Project: www. antikythera-mechanism.gr

Abu Ali al-Hasan ibn al-Haytham (965-1039)

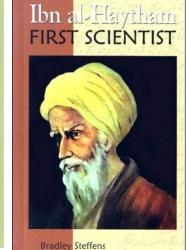
- AKA Alhazen or "The Physicist"
- Greatest scientist of the middle ages
- Contributed to mathematics, physics, optics, astronomy, anatomy, medicine, engineering, philosophy, psychology
- Pioneered the scientific method, modern optics and experimental physics
- Polymath: authored over 200 treatises, including influential "Book of Optics"
- Influenced Leonardo da Vinci, Bacon, Descartes, Kepler, Galileio and Newton







35



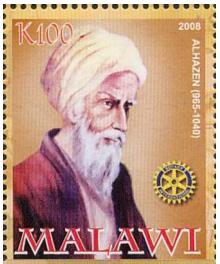






A L. H. A. Y. Z. E. N. O. P. I. I. G. A. L. H. A. Y. Z. E. N. O. P. I. I. G. A. L. H. A. Y. Z. E. N. O. P. I. I. G. A. L. H. A. Y. Z. E. N. O. P. I. I. G. A. L. H. A. Y. Z. E. N. O. P. I. I. G. A. L. H. A. Y. Z. E. N. G. A. L. H. A. Y. Z. E. L. H person all annual learness for the season to the contract of t







THE OLD SCIENTIFIC METHOD

Formulate a hypothesis.
Accumulate data.
Do extensive experimentation.



THE NEW SCIENTIFIC METHOD

Formulate a hypothesis. Patent it. Raise \$17 million.



Leonardo of Pisa (1170–1250)

- Better known as "Fibonacci"
- Considered the most talented mathematician of the middle ages
- Published (1202) "Liber Abaci" "The Book of Calculation"
- Introduced Hindu-Arabic positional number system in Europe
- Popularized Fibonacci sequence



1 1 2 3 5 8 13 21 34 55 89

European	0	1	2	3	4	5	6	7	8	9
Arabic-Indic		١	۲	٣	٤	٥	٦	٧	٨	٩
Eastern Arabic-Indic (Persian and Urdu)		١	۲	٣	۴	۵	ç	٧	٨	٩
Devanagari (Hindi)	o	?	२	ą	४	५	Ç	૭	2	९
Tamil		க	ഉ	<u>ъ</u>	சு		Эm	எ	Э	சூ

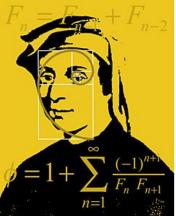
VMDCLXVI = 6666

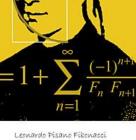
















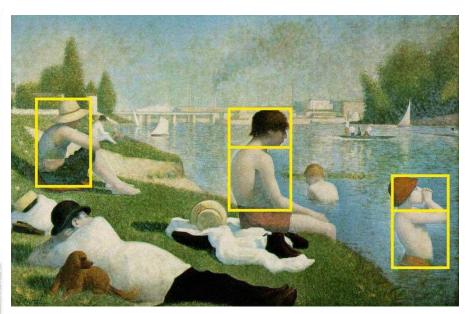
gemmar. Ale fe fo melepara + er quib'i uno mite duo pamant 4mmii gemmar in ico mele parta - coniclos. The fit parta y Tito mi हि. टम्प्याधित म्ह मेद्रावर माना क्रिक्ट मार्टिक मार्टिक माना ह टम्पेडि pm parta o gemmat alia parta o quill'additticii partif s fina ार्क क्षामा । इ र वृंताक mele, crafb pura 4 वृ geminam fuere र म्ह mie fi genpint i fo file fala & parapanant ofic fe i ferro mele 30kg क्यान = । की वृष्टि अववास्तर क्रमान । इत् कुलामार्के रिक्मिक दारे रे मिर ten mira ? + cu quib adduit parift : | q geminar ? comino mete. क्टरीकि क्रमान 4 4 ट्रम quib addur furif + + व geminat ? no Durat no mete ert रे मिंठ क्रमात ह - द्ये quib ते त्रे त्या प्रमानी क्रमानी क्रमानी a geminat i decimo ert ino parti i + et quib adduit runfit Out parif s o d gemmar i undecimo mefe: ert i po paria t 1 1 12 en qb 4 addine parife (1+ + q geminar in ultimo mele erne self turn 7 7 7 pror parta pepir fin par 7 pfaro loco 7 capite uni 21 im potet e moe ? hao margine quali boc opan fum f. q urmi Septi केमारी मार्गेम दर्श कि मार्थिक । दर्श र दर्मिम हे स्वतः नांदर्श दर्श वृक्तिकः निवा £ # मां त्यं वृत्ताकः नृपत् व्हां व्यान व्यान व्यान व्यान त्या पावेद्यान पावेदी milet cu z z 7 hum fou cuniclou fund moetics. +77 77 The pollet face pordine de ifiniat mile mefib. Home varior holer ff quoy pin - lost red hat driot seet unq riel न व्य און מושים ווים שווים שווים שווים שווים ליוף ליוף ליוף מווים שווים har oftet = - dert grundig hie. dode bot infinior i uni ere 12 4 वं मार्स टिक्ंमिर्न कार्ने सिमाल ठामेंक्य मीक्य मार्म horna. 1000 वा निमा म्ला र भे नेटिन र प क्ये नामां के ने नियमापुर ने पान के मार्गिया इतामे filma. erqua fi ermirit delos pmi ofi otes boics. = vemanebir में के अरे के कि कि का कार के कि का का कि का का का कि का कि का कि का rieg fort hoir temmebir omo hoi de iz Purfit fi tedfife " eriment ह 4 .f. में देश न्यूना boit pmi boit remanebe fo de रिमार्थमा के केमिर के कामार केमिर के में मिर्म केमा केमिर क penamebrico de 6 contentump deiff 12 pmi boit cu िर्देश हती । देवा करती । व्या मामार्गी कि एक्टेरे में द क विभागित विर्वार के वार्ष के कार्य है कि किल दिलार के विर्वार के वार्ष किल ्रेट्स क्षित्र व्यान है। देन तार स्वाम क्षित्र वृत्ता के मान वृत्ता क्रमार्थ क offimilet में क्लिकार वृत्तिक will क्लिक में में पर पहिल् व folus क्लिक ab hifqui folui ni polit cognolait mie v moim embent moetic भर अवेतर नामान कृतान हो त्या मांठ रेपा न्व्यान हो द्या मिलार द्यान निर्मात nuo firita ogen opini to lotubil eru affio. fi at lequal filit toel no post tohn cognofat ut the aftene Ta bin feor sto - ov से नियमितार का विभाग मार मार मार कार कार विभाग के नियम के नियम

The Fibonacci Quarterly

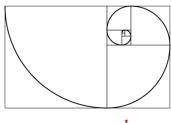






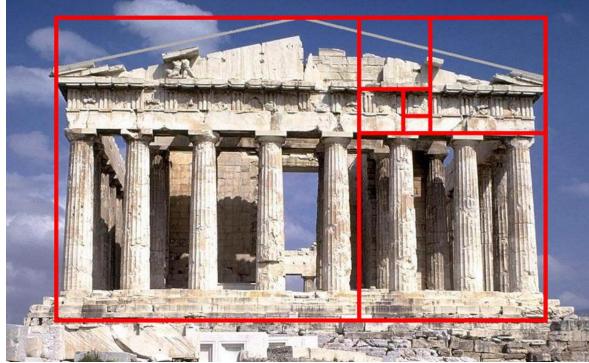


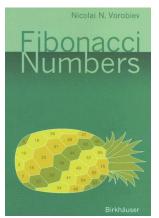


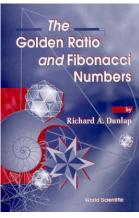


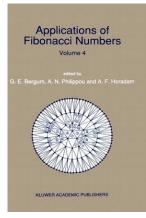
a+b a+b is to a as a is to b

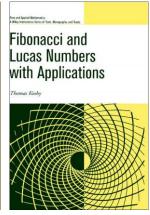


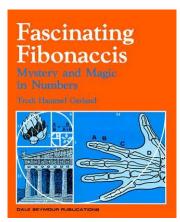


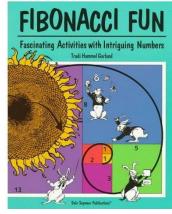


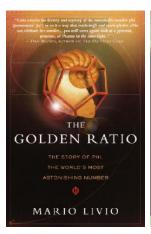




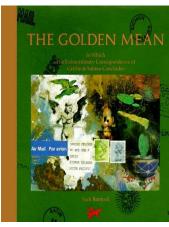


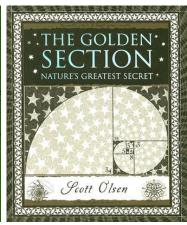


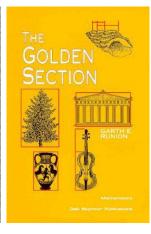


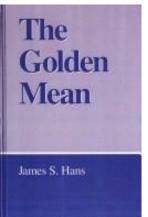


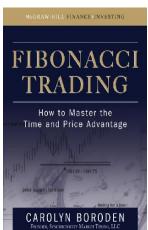


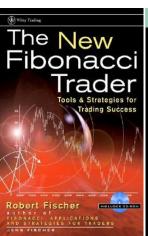


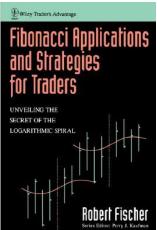




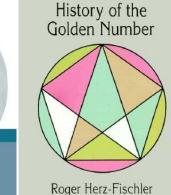




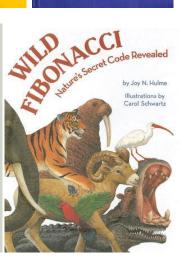








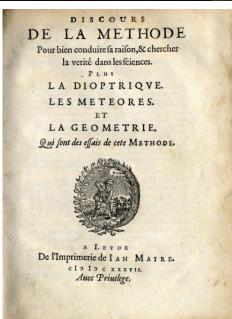
A Mathematical



René Descartes (1596-1650)

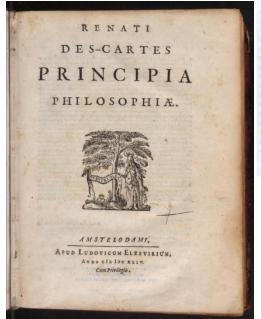
- Father of modern philosophy
- Invented Cartesian coordinates, analytic geometry, heuristics
- Characterized paradoxes & falacies
- Discovered momentum conservation
- Authored "Principia Philosophiae"
- Pioneered methodological skepticism "Cogito ergo sum" - "Je pense, donc je suis"
- "Discours de la Méthode" (1637) one of the most influential works in modern science
- Pioneered the scientific method & revolution "For it is not enough to have a good mind: one must use it well." - Descartes

















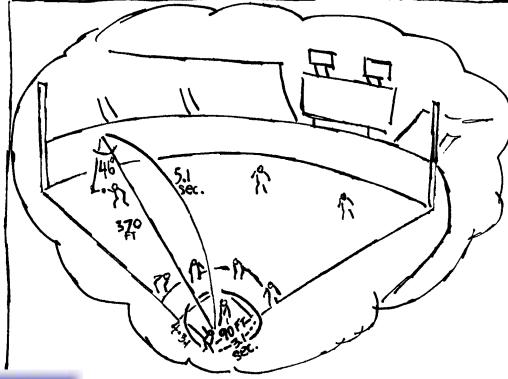








RENÉ DESCARTES EXPLAINS THE COORDINATE SYSTEM WHICH TIES TOGETHER ALGEBRA AND GEOMETRY





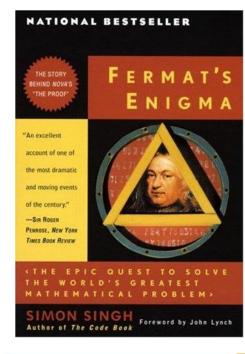


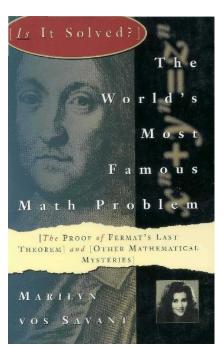
Pierre de Fermat (1601-1665)

- Father of modern number theory
- Lawyer, Parlement of Toulouse
- Laid groundwork for calculus
- Contributions to optics, probability, and analytic geometry
- Fermat numbers, primes, perfect #'s
- Descartes' Law of refraction
- Reponsible for many open problems
- "Fermat's Last Theorem" (1637-1995)
- Recognized "principle of least action" and "principle of least time" in physics
- Influenced Newton and Leibniz

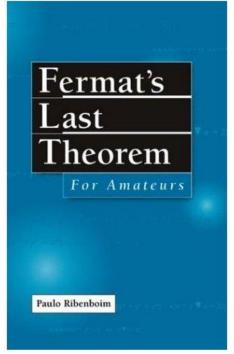


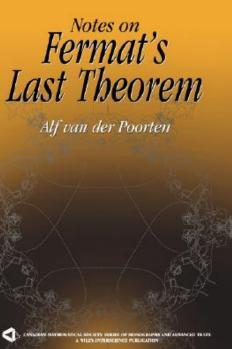


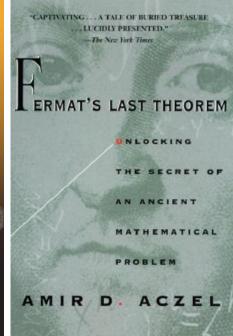


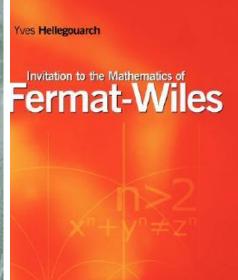








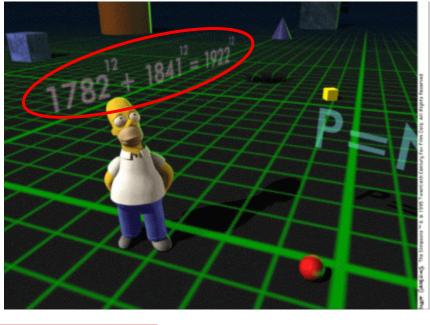






Pierre de Fermat 1601 - 1665









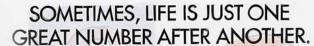


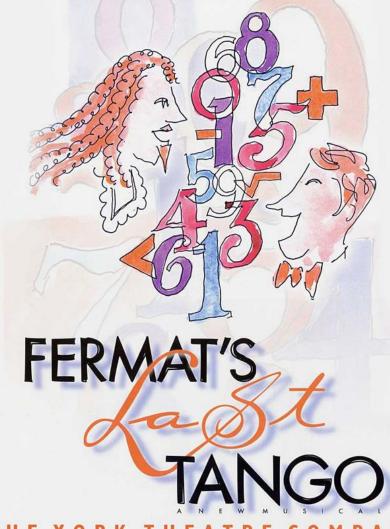












THE YORK THEATRE COMPANY

JAMES MORGAN, ARTISTIC DIRECTOR CLAYTON PHILLIPS, HANAGING DIRECTOR PRESENTS FERMAT'S LAST TANGO A NEW MUSICAL MUSIC BY JOSHUA ROSENBLUM BOOK BY JOANNE SYDNEY LESSNER LYRICS BY LESSNER & ROSENBLUM WITH GILLES CHIASSON • EDWARDYNE COWAN • MITCHELL KANTOR • JONATHAN RABB

CHRIS THOMPSON • CHRISTIANNE TISDALE • CARRIE WILSHUSEN

SCENIC DESIGN JAMES MORGAN COSTUME DESIGN LYNN BOWLING DIESING JOHN MICHAEL DEEGAN OKHESTRATIONS JOSHUA ROSENBLUM CASTING NORMAN MERANUS

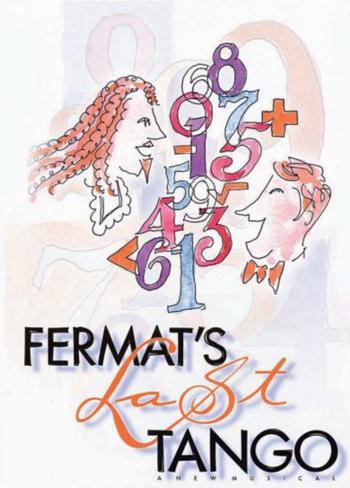
PRESS REPRESENTATIVE KEITH SHERMAN & ASSOCIATES GARPIICI JAMES MORGAN & MICHAEL HOLMES PRODUCTION STAGE MANAGER PEGGY R. SAMUELS

HUSIC DIRECTOR MILTON GRANGER (HOREOGRAPHY JANET WATSON) DIRECTED BY MEL MARVIN

BEGINS NOVEMBER 21, 2000 • TUES-SAT AT 8 • MATINEES: WED, SAT & SUN AT 2:30 LIMITED ENGAGEMENT! CALL TELE-CHARGE: (212) 239-6200 www.telecharge.com THEATRE AT SAINT PETER'S, CITIGROUP CENTER • 619 LEXINGTON AVENUE (AT 54TH 5T.)



Music **by Joshua Rosenblum**Book by **Joanne Sydney Lessner**Lyrics by **Lessner and Rosenblum**



THE YORK THEATRE COMPANY

A Musical Fantasy inspired by Andrew Wiles and his encounters with Fermat's Last Theorem

"Rollicking! Whimsical! Catchy & Clever!" - The New York Times

FERMAT'S LAST TANG Followed by an Interview with Andrew Wiles



A CMI production



In 1993 Andrew Wiles stunned the world when he announced a solution to "Fermat's Last Theorem," the famous unsolved mathematics problem set forth by Pierre de Fermat in 1637. In the musical Fermat's Last Tango, the fictional character Daniel Keane earns overnight acclaim when he presents his findings. However, fanfare soon gives way to doubt when the reincarnated Fermat discovers a hole in Keane's proof. The singular pursuit by Keane to correct this flaw results in a love triangle involving himself, his wife, and mathematics—the story of which is brought to life by Fermat and his immortal friends from the "AfterMath," namely: Pythagoras, Euclid, Newton, and Gauss. The musical is both a cheerful romp through history and a personal confrontation with destiny. It provides a testament to the extraordinary excitement of mathematics and its unparalleled beauty.

The Composer Joshua Rosenblum enjoyed mathematics while studying music at Yale along with the author, his wife Joanne Sydney Lessner. They both take an active role in the New York music community. This recording was captured by David Stern and his Emmy Award-winning crew during a performance at the York Theatre Company in New York City.



STARRING

Carl Friedrich Gauss / Reporter Anna Keane Pythagoras / Reporter Pierre de Fermat Daniel Keane Euclid / Reporter Sir Isaac Newton / Reporter GILLES CHIASSON
EDWARDYNE COWAN
MITCHELL KANTOR
JONATHAN RABB
CHRIS THOMPSON
CHRISTIANNE TISDALE
CARRIE WILSHUSEN



Approximate Running Time:
100 minutes
Color/Not Rated/VHS/NTSC
Produced by The Clay Mathematics
Institute, Cambridge, MA
Arthur Jaffe, Producer
David Stern, Director
© 2001 The Clay Mathematics Institute.
All Rights Reserved.

Illustrated Guide Enclosed

The Clay Mathematics Institute

1770 Massachusetts Avenue #331 Cambridge, MA 02140 Email: fermat@claymath.org Website: www.claymath.org

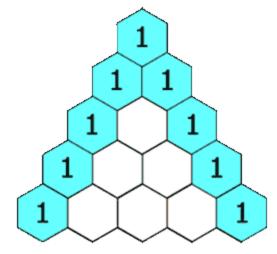


Unauthorized reproduction, in any manner is prohibited

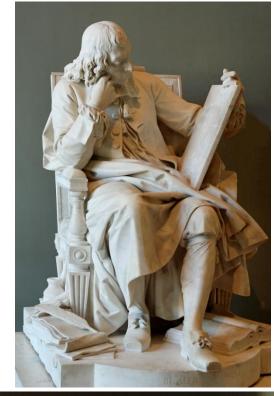
Blaise Pascal (1623-1662)

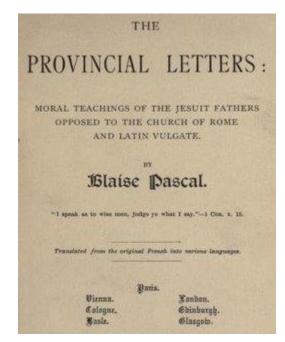
- Mathematician, physicist, philosopher
- Studied fluids, pressure, vacuum
- Helped pioneer projective geometry, probability, and the scientific method
- Influenced modern economics
- "Pascal's triangle", "Pascal's law"
- Invented hydraulic press and syringe
- Constructed a mechanical calculator
- Used humor, wit, and satire in writings
- Influenced Voltaire and Rousseau
- Inagurated the world's first bus line
- SI unit of pressure "pascal"

















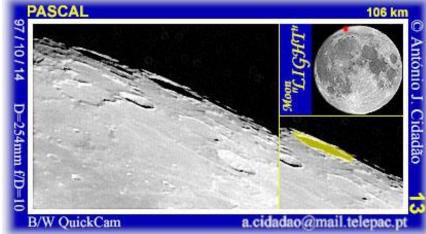


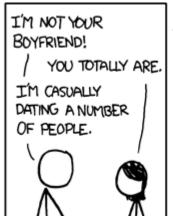




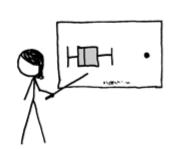








BUT YOU SPEND TWICE AS MUCH TIME WITH ME AS WITH ANYONE ELSE. I'M A CLEAR OUTUER.



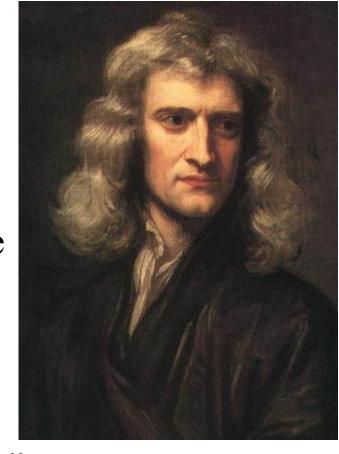
YOUR MATH IS

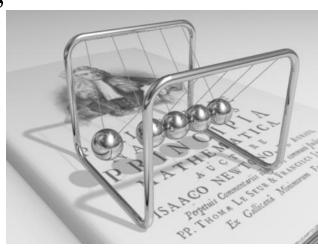
FACE IT—I'M
YOUR STATISTICALLY
SIGNIFICANT OTHER.

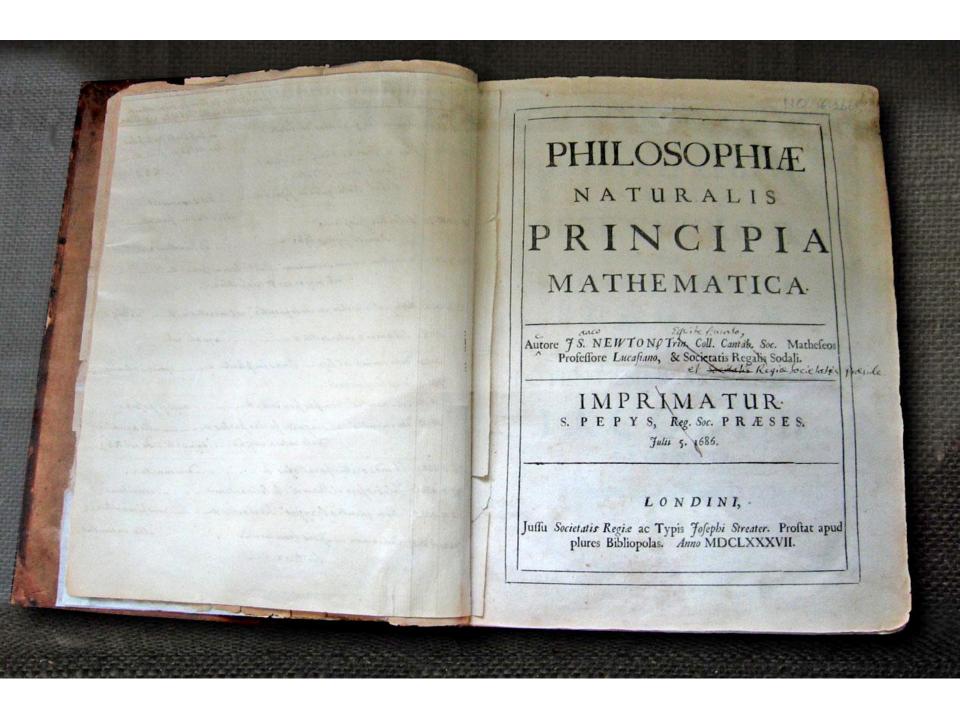


Sir Isaac Newton (1643-1727)

- Mathematician, physicist, astronomer, philosopher, alchemist, theologian
- One of history's most influential people
- "Principia Mathematica" (1687)
- Invented calculus, theory of gravitation
- Founded "Newtonian mechanics"
- Discovered laws of motion, inertia
- "Newtonian fluid", "Newtonian Universe"
- Advanced the Scientific Revolution
- Developed practical reflecting telescope, theory of color, "Newton's method"
- SI unit of force: newton













Caf p. Ponsmus denique quod motus cujufcunque generis propagetur ab d per foramen B C: C: quoniam propagatio filt an fit, nift quatenus partes Medii centro d propiores urgent consubventque partes ultériores: C partes que urgentur Holas fant, sheque recedunt quaquaversum in regiones ubi minus premuntar riscontinue C.

PRINCIPIA MATHEMATICA: 333

sitest endem verfun Medii partee omnes quisécentes, tum laterales

Li & XO, quan surrente P. P. Q., copue paris omnous omnis, Securous
um grunn paris

RC eramit, dilutari incipet & abande,
unquan a principio & centro , in partes omnes directe propagati.

2. D.

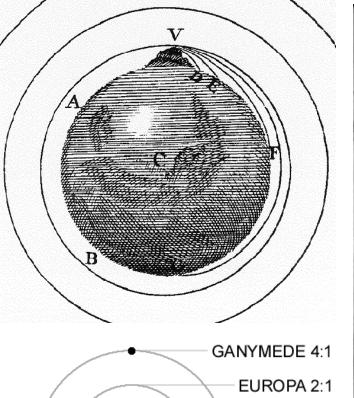
PROPOSITIO XLIII. THEOREMA XXXIV.

Copus some tremulum in Medio Elaßico propagabit motum guljum undique in directum; in Medio vero non Ela-fico mutum circularem excitabit.

fige author ceredineus excitabri.

Get 1. Man partes copropis tremuli vicibus alternit eundo & metendo, in do ungelosm & propellent purce Medil filo proximate, de ugradore de propellent purce Medil filo proximate, de ugradore conpedita recedere & freie expandere. Igitu pera Medi copropi tremola proxima buna & reziban per vice, al alter partum corporis illus tremuli « que militaba tremola pera girante parten per consecutiva e capa finalita espandina de la compara de la compa





- IO 1:1

JUPITER

Arithmetica Univerfalis;

SIVE

DE COMPOSITIONE

ET

ARITHMETICA

LIBER.

Cui accessit

HALLEIANA

Aquationum Radices Arithmetice inveniendi methodus.

In Ulum Juventutis Academica.

CANTABRIGICE

TYPIS ACADEMICIA

LONDINI, Impenfis Besj. Tooke Bibliopolæ juxta Medii Templi Portam in vico zulpo vocato Flerifirer. A.D. MDCCVII.



OR, A

TREATISE

OF THE

REFLEXIONS, REFRACTIONS, INFLEXIONS and COLOURS

OF

LIGHT.

ALSO

Two TREATISES

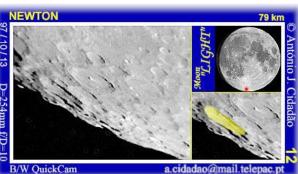
OF THE

SPECIES and MAGNITUDE

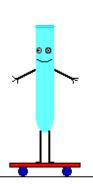
Curvilinear Figures.

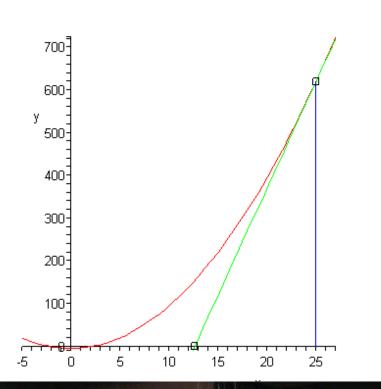
LONDON,

Printed for Sam. Smith, and Benj. Walford,
Printers to the Royal Society, at the Prince's Arms in
St. Pand's Church-yard. MDCCIV.



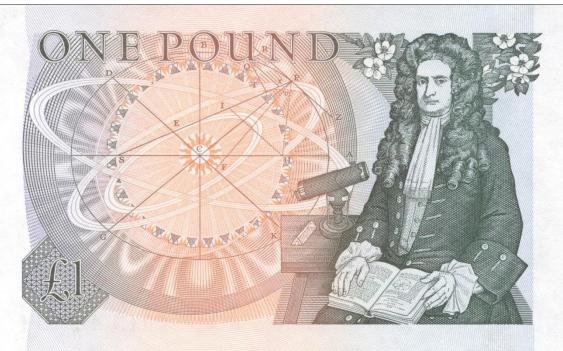
































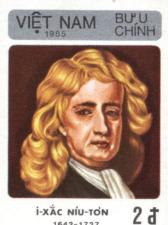


"Математические начала натуральной философий-вершина творчества ИНьютона. Впервые была создана единая система земной и небесной

механики, которая легла в основу классической физики.







1642-1727





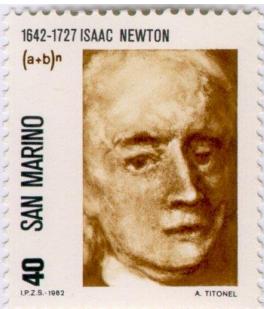


3Ft MAGYAR POSTA

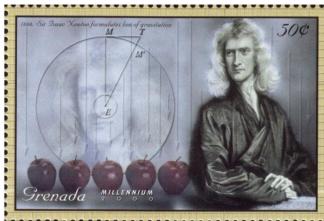


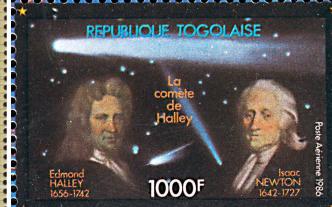
























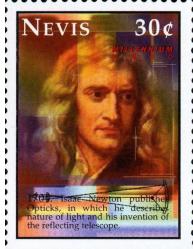












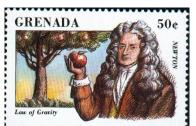


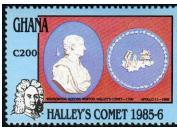










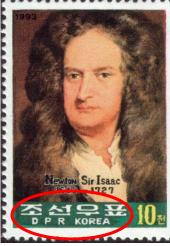












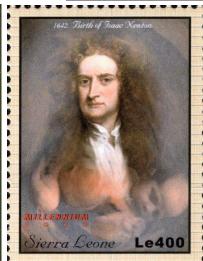


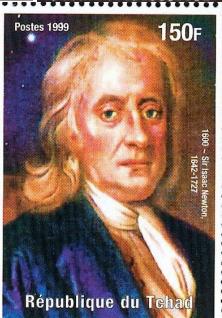


















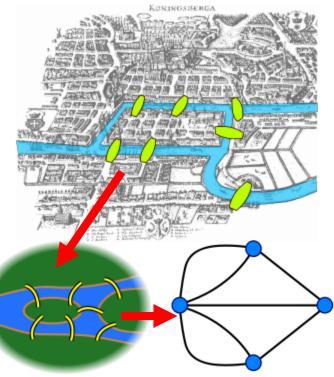




Leonhard Euler (1707–1783)

- Invented graph theory
- "Bridges of Königsberg", Prussia
- Eulerian tour
- Euler's formula: V + F = E + 2
- Euler's number: e
- Euler's identity: $e^{iJI} + 1 = 0$
- Major contributions to analysis, algebra, calculus, number theory, topology, optics, fluid dynamics, mechanics, astronomy, education





SCHWEIZERISCHE NATIONALBANK BANCA NAZIUNALA SVIZRA ↔



METHODUS

INVENIENDI

LINEAS CURVAS

Maximi Minimive proprietate gaudentes, S I V E

SOLUTIO

PROBLEMATIS ISOPERIMETRICI LATISSIMO SENSU ACCEPTI

AUCTORE

LEONHARDO EULERO,

Professore Regio, & Academia Imperialis Scientiarum Petropolitana Socio.



LAUSANNÆ & GENEVÆ,

Apud MARCUM-MICHAELEM BOUSQUET & Socios.

MDCCXLIV.

LETTERS

...

[L]EULER

ON DIFFERENT SUBJECTS

IN

PHYSICS AND PHILOSOPHY.

ADDRESSED TO

A GERMAN PRINCESS.

TRANSLATED FROM THE FRENCH BY

HENRY HUNTER, D.D.

ORIGINAL NOTES,

And a Gloffary of Foreign and Scientific Terms.

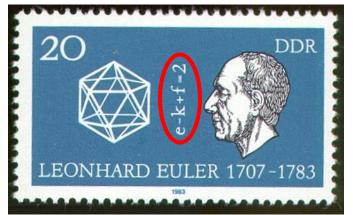
Second Edition.

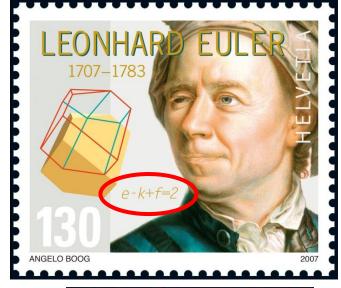
IN TWO VOLUMES.

VOL. I.

London:

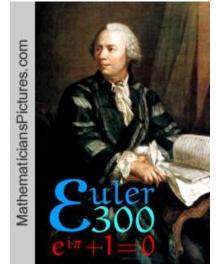
PRINTED FOR MURRAY AND HIGHLEY; J. CUTHELL; VERNOR
AND HOOD; LONGMAN AND REES; WYNN AND SCHOLEY;

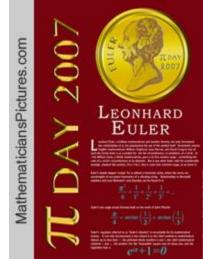






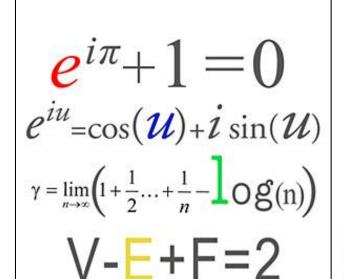


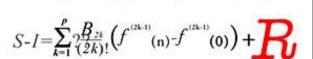














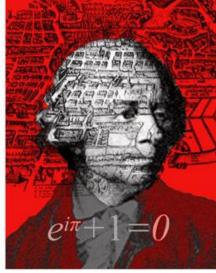
LEONHARD CHIER

15 APRIL 1707 TO 18 SEPT 1783









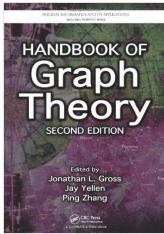
Leonhard Euler 1707 - 1783

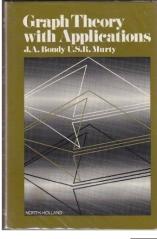


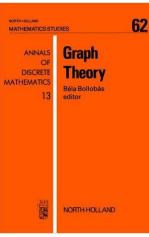


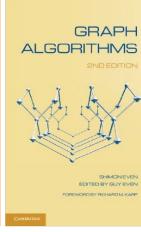


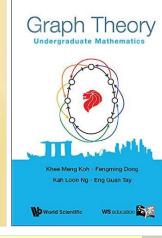


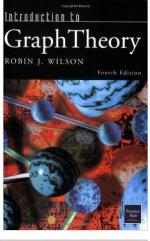




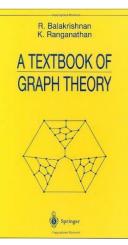


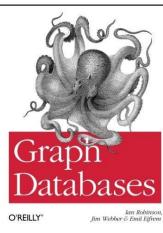


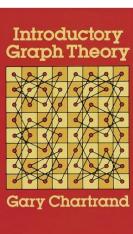


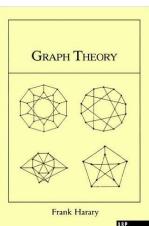


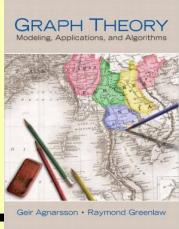


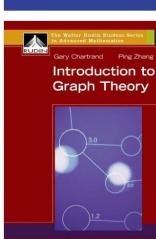


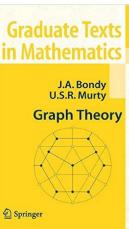


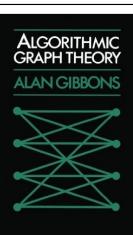


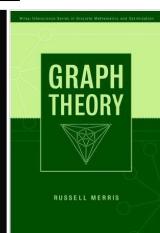


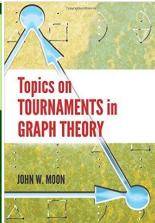


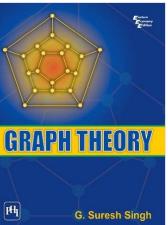


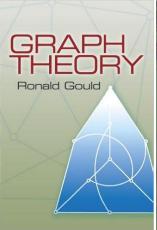


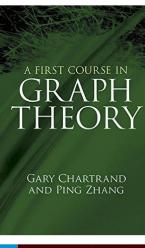


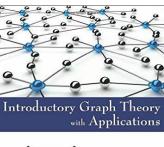


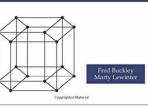










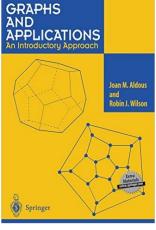


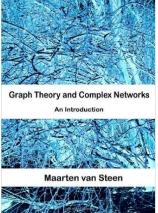


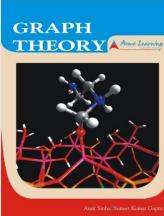
Combinatorics and Graph Theory

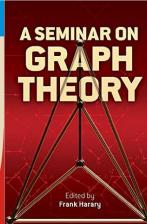
Second Edition

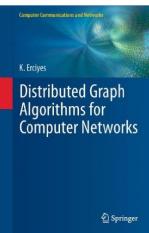


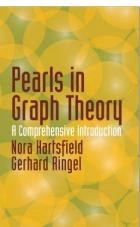


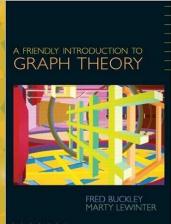


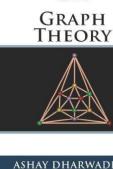










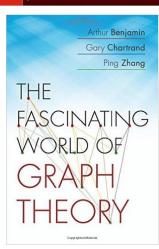


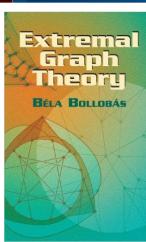


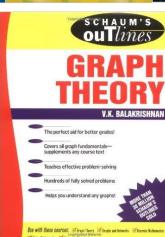


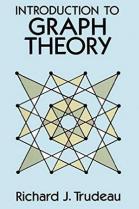
A Textbook of **Graph Theory**

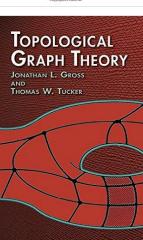


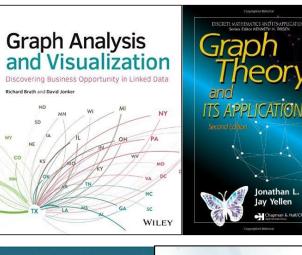


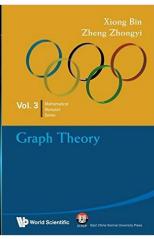


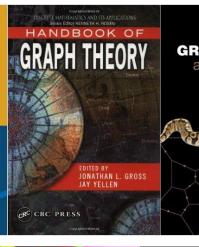


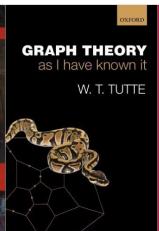


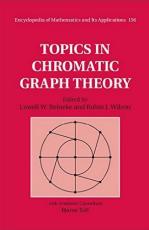


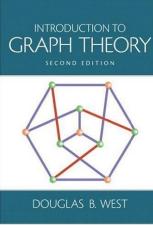


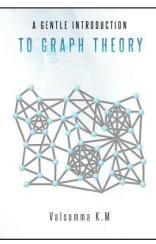


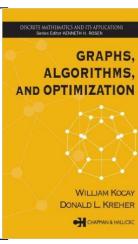


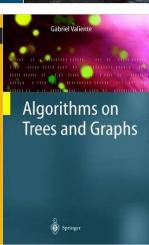


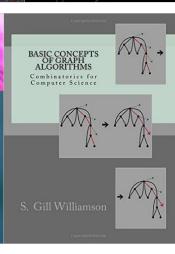


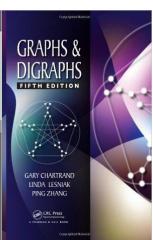


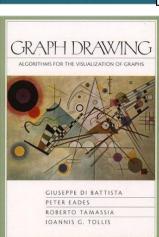


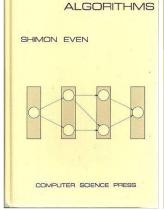




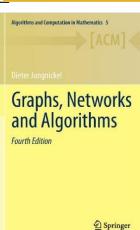


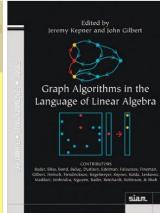


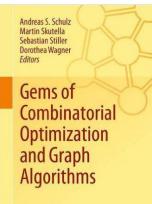




GRAPH

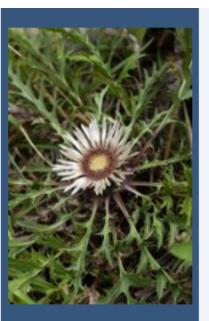






2 Springer





Related events:



Cycles and Colourings 5th Polish Combinatorial



Conference 17th Workshop on



17th Workshop on Hereditary Graph Properties

SEVENTH CRACOW CONFERENCE ON GRAPH THEORY "RYTRO '14"

September 14-19, 2014 Rytro, Poland

The meeting is next in the series of former Cracow Conferences on Graph Theory organized in Niedzica (1990), Zgorzelisko (1994), Kazimierz Dolny (1997), Czorsztyn (2002), Ustroń (2006) and Zgorzelisko (2010).

Selected papers presented at the conference will be published in a Special Issue of <u>Discrete Mathematics</u> dedicated to the 7th Cracow Conference on Graph Theory. Already six Special Issues of DM were devoted to our conferences (volumes: 121, 164, 236, 307/11-12, 309/22, 312/14).

Invited speakers:

Ralph Faudree, University of Memphis, USA

Linear Forests on Hamiltonian Cycles

András Gyárfás, Hungarian Academy of Sciences, Budapest, Hungary

Vertex covers by monochromatic pieces - results and problems

Wilfried Imrich, Montanuniversität Leoben, Austria

Graph Products and Symmetry Breaking in Graphs

Ken-ichi Kawarabayashi, National Institute of Informatics, Tokyo, Japan

Coloring graphs with some forbidden or restricted configurations

Jan Kratochvil, Charles University, Prague, Czech Republic

Extending Partial Geometric Representations of Graphs

Dieter Rautenbach, Universität Ulm, Germany



INTERNATIONAL CONFERENCE ON GRAPH THEORY AND ITS APPLICATIONS

December 16-19, 2015
Amrita School of Engineering, Coimbatore, India

Home

About University

Department of Mathematics

Call for Papers

Organizing Committee

Academic Program Committee

List of Invited Speakers

Registration New

Important Dates

Conference Program

Accomodation and Local Information

Travel Information

Contact

About The Conference

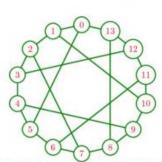
This will be a Four-day Conference in Graph Theory, Graph Algorithms and its applications. It will be focusing on the subareas in graph theory that has applications in Optimization, Computing Techniques, VLSI Design and Testing, Image Processing, and Network Communications. The goal of this conference is to bring top researchers in these areas to Amrita to foster collaboration and to expose students to important problems in the growing field. The conference is expected to stimulate joint work among researchers from India and abroad and attract research students and postdoctoral fellows who work in graph theory. The Conference will cover a broad range of topics in Graph Theory. The topics include, but are not limited to:

- Graph Theory
- Algebraic Graph Theory
- · Algorithms and Computing Techniques
- Graph Optimization
- · VLSI Design and Testing
- Image Processing
- Networks
- Communications and Control Theory

VIEW BROCHURE»»

VENUE : Amrita School of Engineering, Coimbatore, India

Academic Cooperations:





Program

Registration

Call for Abstracts

List of Participants

Accommodations

Travel

Information for International Participants

Conference Photos

Slides of all Talks

MODERN TRENDS IN ALGEBRAIC GRAPH THEORY

An International Conference June 2-5, 2014

ICIENCE CENTER

Villanova <mark>University</mark> Villanova, Pennsylvania

Modern Trends in Algebraic Graph Theory - AFTERMATH

First, i wish to express my deepest gratitude to those who helped to make MTAGT a reality...

Generous financial support was provided by the National Science Foundation, Villanova (VU) College of Arts and Sciences, VU Office of Research and Graduate Programs, VU Office of Reasearch and Sponsored Projects, VU Office of the Vice President of Academic Affairs, and VU Office of the President.

Staffing support was provided by Marie O'Brien, Lorraine McGraw, Doug Norton, Najib Nadi, Taylor Berrang, Carrie Caswell, Carolyn Romano, Joseph Reiter, and Pat Woldar.

An indispensable role was played by the Office of Conference Services. In particular, I wish to mention Ron Diment and Stefanie Austinat. I also wish to thank Elisa Wiley and Clete Rickert for web support.

Last but not least, I wish to thank those who attended MTAGT. When all is said and done, the success of a conference depends integrally on the qualifications of its participants.

We had a wonderfully strong and diverse group. More than half of the 110 participants traveled to Villanova from 20 different nations. Over 20% of the participants were female, and roughly 25% were graduate students/recent PhDs. We are most proud of these demographics.

The conference presentations were truly inspired. I am most pleased to now report their online availability:

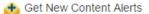
<video recordings of plenary talks>

<Slides of all talks>

Mathematics alone does not make a successful mathematics conference. It is a desirable (if not imperative) to promote healthy multicultural relations, and unobstructed lines of communication between participants. As

EUROCOMB 2015 Bergen ean Confer inatorics, Graph Theory August 31 — September 4, 2015 Maria Chudnovsky, Princeton Amin Coja-Oghlan, Goethe Univ. Frankfurt Helge Tverberg session Zdeněk Dvořák, Charles Univ. Prague (chairs Jiří Matoušek & Jaroslav Nešetřil): Pavol Hell, Simon Fraser Univ. Imre Bárány, Hungarian Acad. Sci. Subhash Khot, Courant Inst. Math. Sci. Gil Kalai, Hebrew Univ. Jerusalem Daniel Lokshtanov, Univ. Bergen Günter Ziegler, Freie Universität Berlin Francisco Santos, Univ. Cantabria Van Vu, Yale Univ. Programme Committee: Bojan Mohar, Simon Fraser Univ. lmre Bárány, Hungarian Acad. Sci. Bergen Algorithms Group, incl. Dhruv Mubayi, Univ. Illinois Chicago Mireille Bousauet-Mélou, LaBRI Jaroslav Nešetřil (co-chair), Charles Univ. Prague Pål Grønås Drange (co-chair) Michael Drmota, Vienna Univ. Tech. Marc Noy, UPC Barcelona Markus Dregi Stefan Felsner, Tech. Univ. Berlin Patrice Ossona de Mendez, EHESS Paris Pinar Heggernes Fedor Fornin, Univ. Bergen Marco Pellegrini, IIT-CNR Pisa Daniel Lokshtanov Ervin Győri, Hungarian Acad. Sci. Asaf Shapira, Tel Aviv Univ. Fredrik Manne Mathias Schacht, Univ. Hamburg Daniel Král , Univ. Warwick Saket Saurabh Oriol Serra (co-chair), UPC Barcel Balázs Szegedy, Hungarian Acad Daniela Kühn, Birmingham Univ. mre Leader, Univ. Cambridge lan Ame Telle (cond Dániel Marx, Hungarian Acad https://eurocomb2015.b.uib.no

JOURNAL TOOLS





Save to My Profile



Oct Gampic Copy



JOURNAL MENU

Journal Home

FIND ISSUES

Current Issue

All Issues

FIND ARTICLES

Early View

Most Accessed

Most Cited

GET ACCESS

Subscribe / Renew

FOR CONTRIBUTORS

OnlineOpen

Author Guidelines

Submit an Article

ABOUT THIS JOURNAL

Overview

Editorial Board

Permissions

Advertise

Contact

Wiley Job Network

SPECIAL FEATURES

Professor Maria Chudnovsky Wins MacArthur Fellowship

Mathematics Journals

Mathematics Journals Free Sample Issues 2015

Graph Theory

Journal of Graph Theory

© Wiley Periodicals, Inc.



Editors-in-Chief: Paul Seymour and Carsten Thomassen

Impact Factor: 0.629

ISI Journal Citation Reports © Ranking: 2014: 147/310 (Mathematics)

Online ISSN: 1097-0118

Recently Published Issues | Se

Current Issue: November 2015

Volume 80, Issue 3

December 2015

Volume 80, Issue 4

October 2015

Volume 80, Issue 2

September 2015

Volume 80, Issue 1

August 2015

Volume 79, Issue 4

Free Sample issue, Most Cited Articles and More!



Read the Latest Articles!

Recently Published Articles - Journal of Graph Theory

 Maximal Induced Matchings in Triangle-Free Graphs

Manu Basavaraju, Pinar Heggernes, Pim van 't Hof, Reza Saei, Yngve Villanger

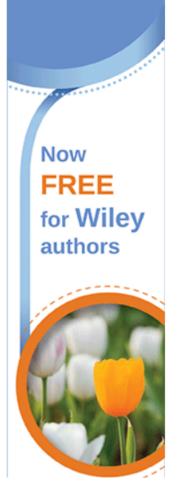
- The Fano Plane and the Strong Independence Ratio in Hypergraphs of Maximum Degree 3
 Michael A. Henning, Christian Löwenstein
- On the Number of 4-Cycles in a Tournament Nati Linial, Avraham Morgenstern



Subscribe to RSS headline updates Powered by FeedBurner

Journal of Graph Theory - Awards and Announcements







Electronic Journal of Graph Theory and Applications

www.ejgta.org

SUBMISSION

Honorary Editors: Jaroslav Nesetril Alexander Rosa

Editors in Chief: Edy Tri Baskoro Mirka Miller

Managing Editors:Joseph Ryan
Kiki A. Sugeng

Layout Editors: Slamin Rinovia Simanjuntak

<u>Complete Editorial</u> <u>Team</u>

USER Username Password

Remember me

HOME ABOUT LOGIN REGISTER SEARCH CURRENT ARCHIVES PUBLICATION ETHICS TEMPLATE

Home > Vol 3, No 2 (2015)

Electronic Journal of Graph Theory and Applications (EJGTA)

The Electronic Journal of Graph Theory and Applications (EJGTA) is a refereed journal devoted to all areas of modern graph theory together with applications to other fields of mathematics, computer science and other sciences. The journal is published by the Indonesian Combinatorial Society (InaCombS), Graph Theory and Applications (GTA) Research Group - The University of Newcastle - Australia, and Faculty of Mathematics and Natural Sciences - Institut Teknologi Bandung (ITB) Indonesia. Subscription to EJGTA is free. Full-text access to all papers is available for free.

All research articles as well as surveys and articles of more general interest are welcome. All papers will be refereed in the normal manner of mathematical journals to maintain the highest standards.

OPEN JOURNAL SYSTEMS

Published by:





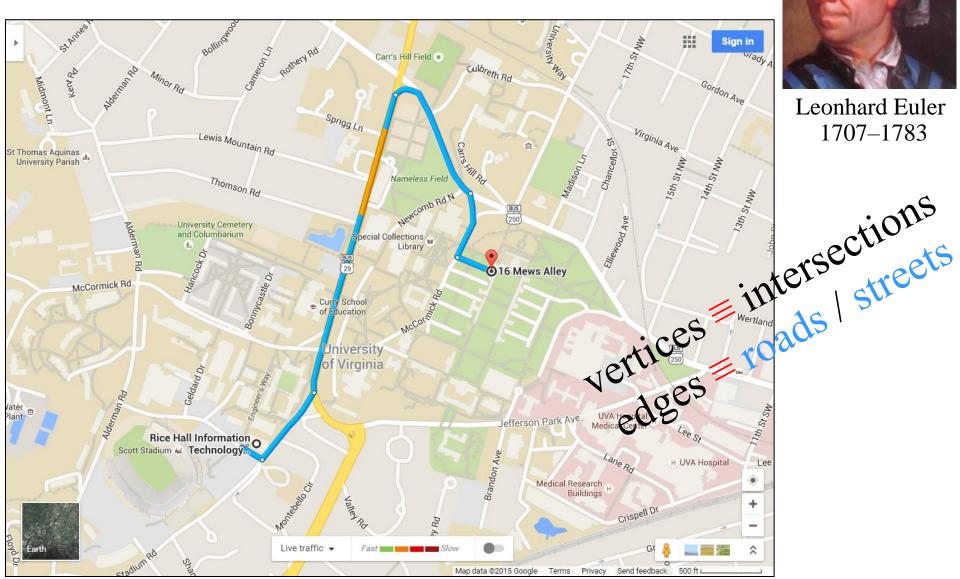


Sponsored by:





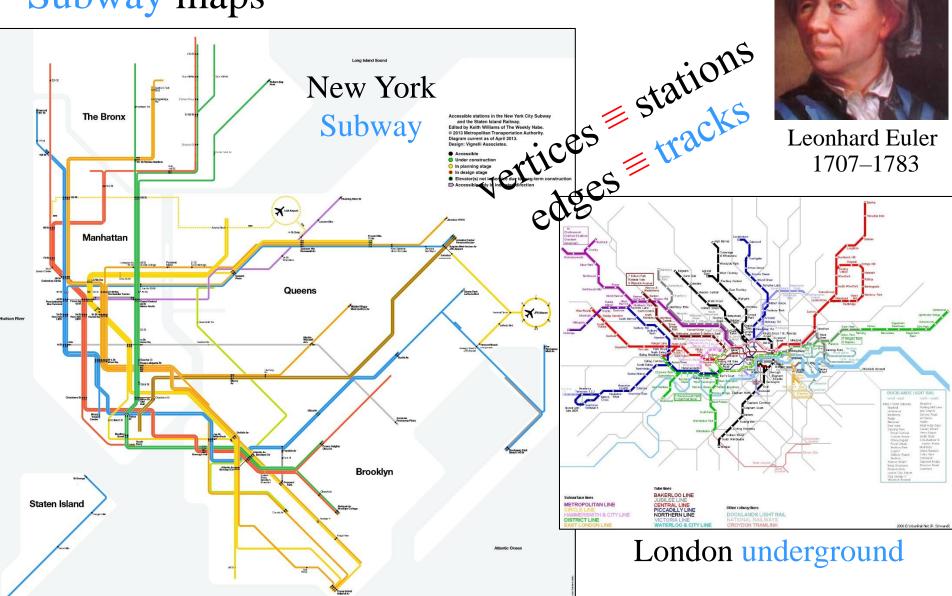
• Geographical information / GPS systems



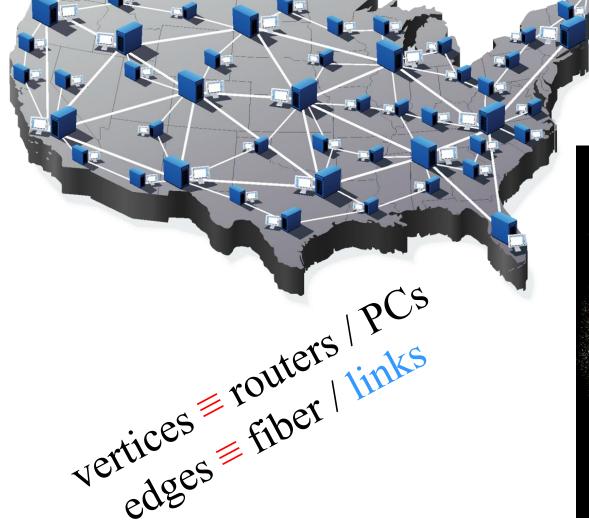


Leonhard Euler 1707-1783

Subway maps

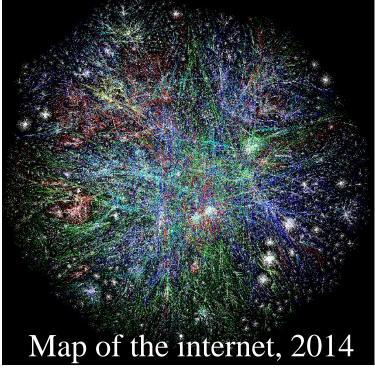


Computer networks

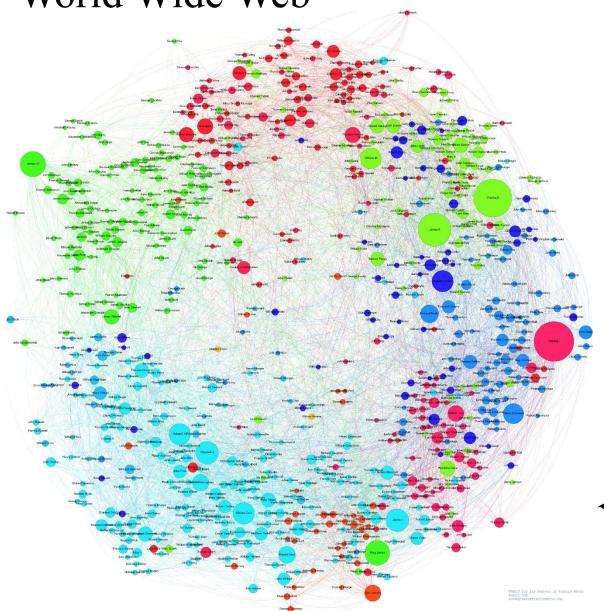




Leonhard Euler 1707–1783



• World Wide Web

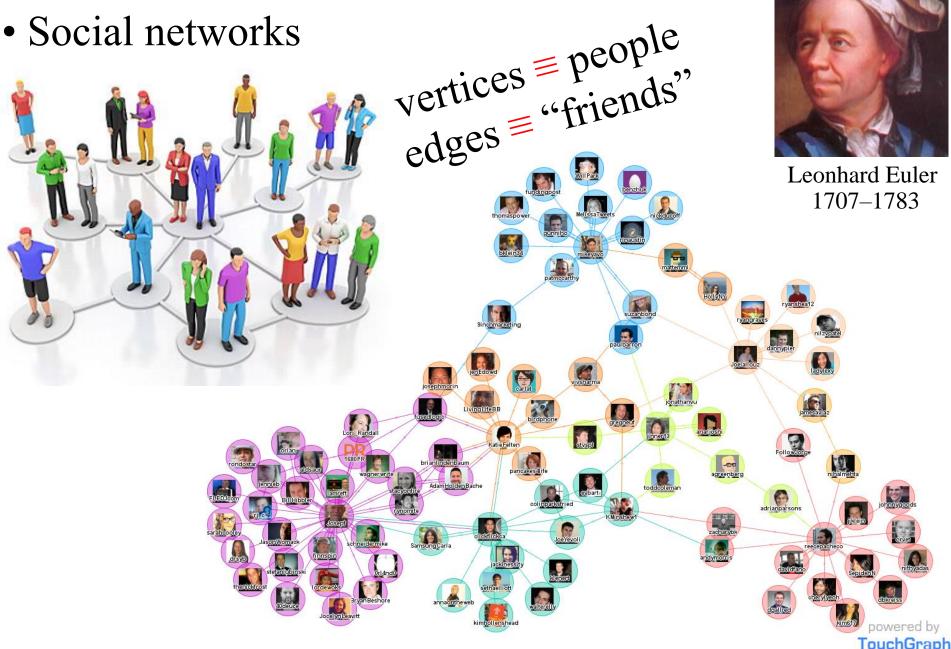




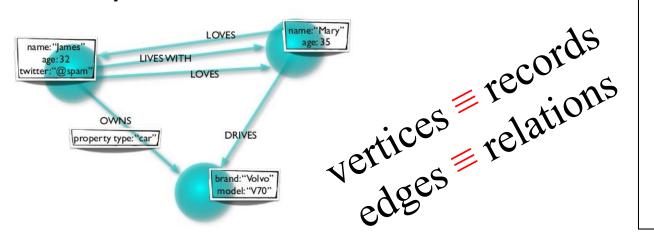
Leonhard Euler 1707–1783

vertices Pages
URLS
edges

Social networks

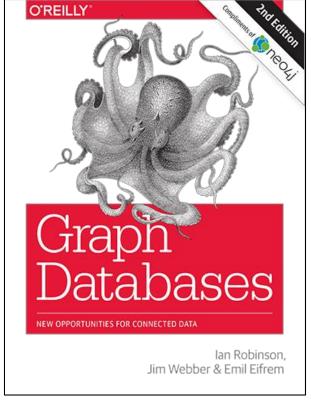


 Graph databases ld: 2 Name: Bob Age: 22 Label: knows Since: 2001/10/103 Label; is member 105. Label: Members Label: knows Since: 2001/10/04 ld: 1 Name: Alice ld: 103 Label: Members Age: 18 ld: 102 Id: 3 Label: is_member Type: Group Since: 2005/7/01 Name: Chess neo technology Graph data model

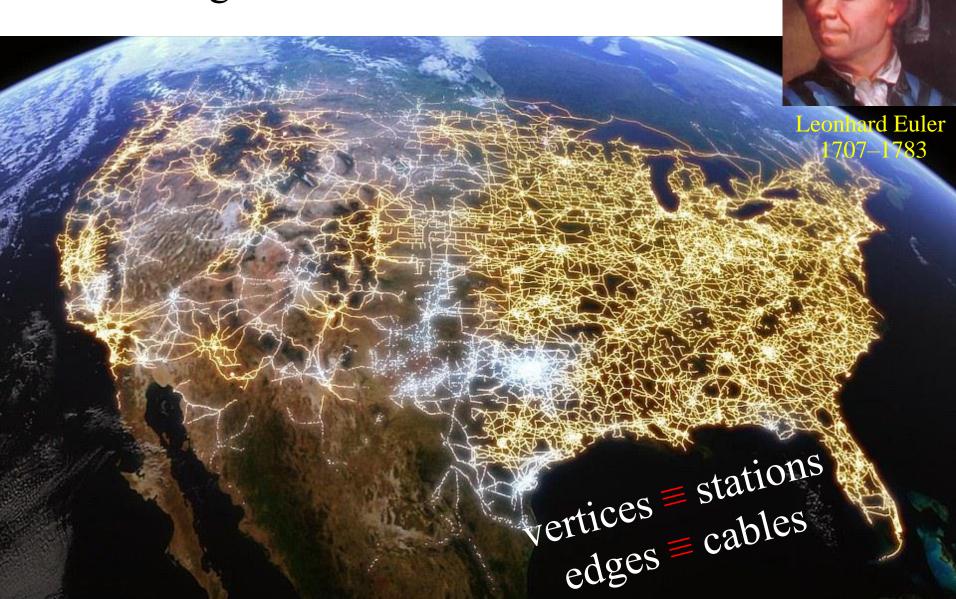




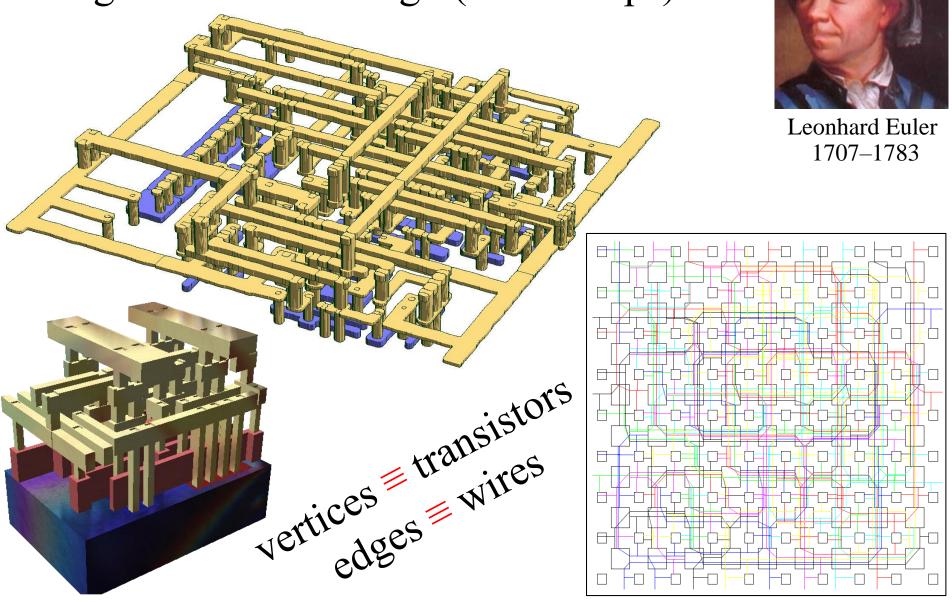
Leonhard Euler 1707–1783



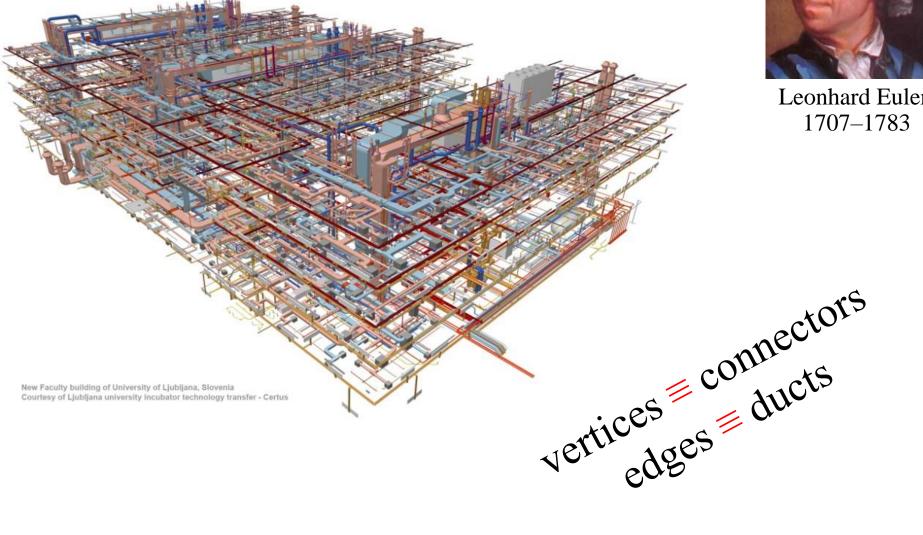
• Electrical grids



• Integrated circuit design (VLSI chips)



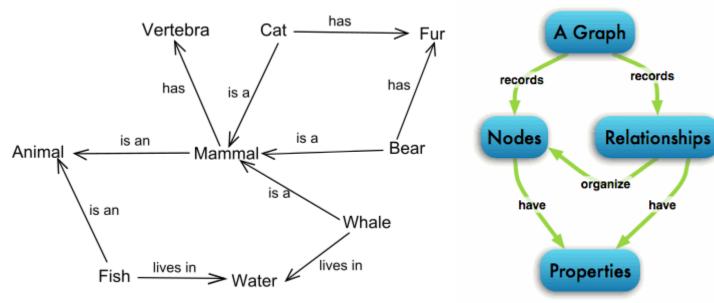
• CAD / building HVAC design





Leonhard Euler 1707-1783

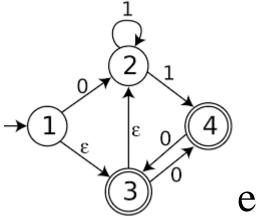
Semantic nets





Leonhard Euler 1707–1783

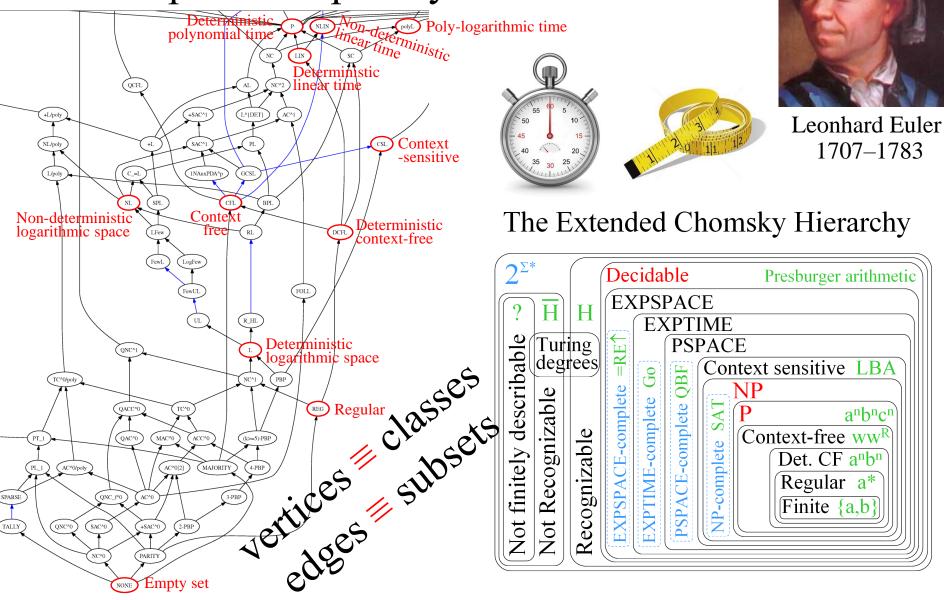
• Finite automata



vertices ≡ objects edges ≡ relations

vertices ≡ states edges ≡ transitions

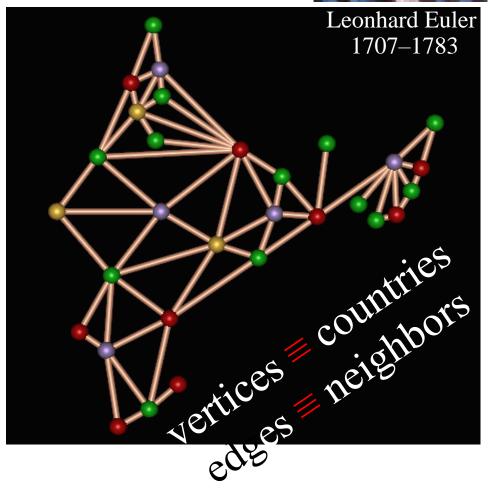
• Time / space complexity classes



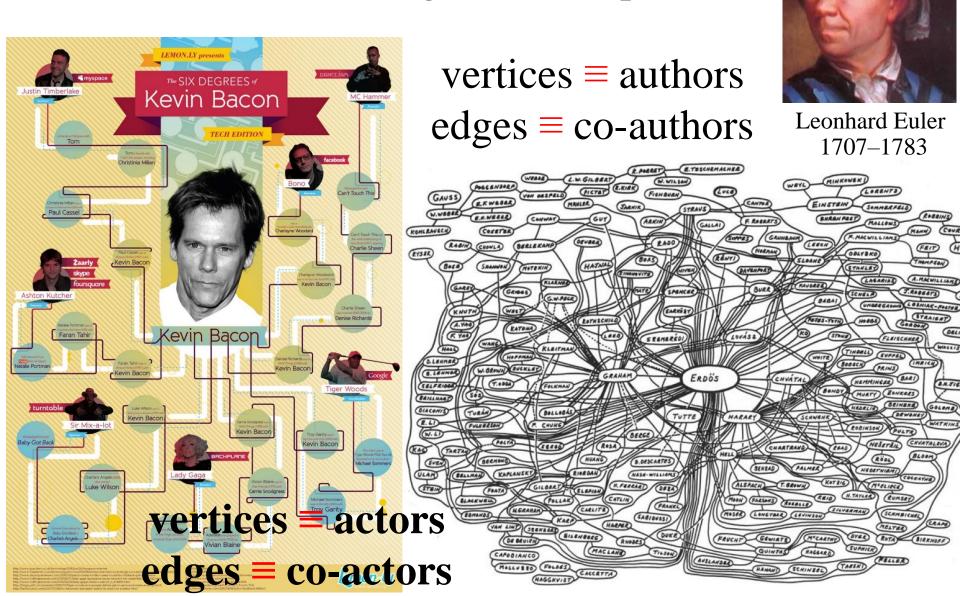
Map coloring







• Erdős numbers - "6 degrees" of separation

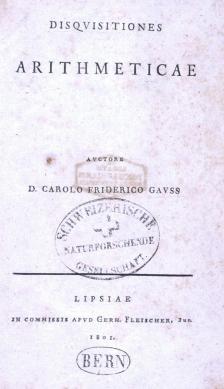


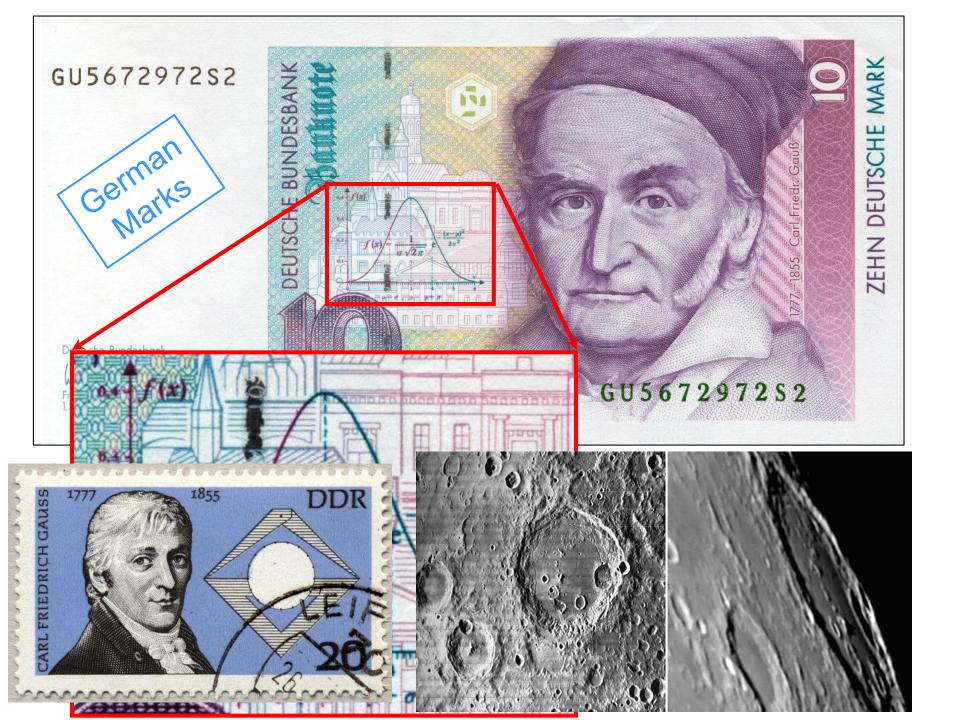
Historical Perspectives

Carl Friedrich Gauss (1777–1855)

- "Prince of Mathematics"
- Founded modern number theory
- Authored "Disquisitiones Arithmeticae"
- Fundamental Theorem of Algebra
- Major contributions to astronomy, optics electromagnetism, statistics, geometry
- Gaussian distribution, Gaussian elimination Gaussian noise, Gaussian integers & primes Gauss' Law, Gauss' constant, "degaussing"
- SI unit of magnetic field strength: gauss
- Students: Dedekind, Riemann, Bessel













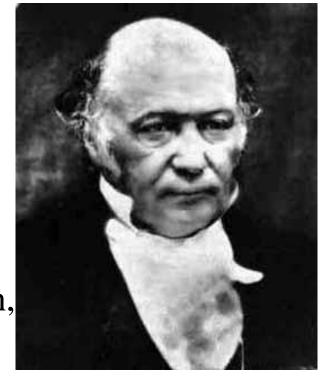




Historical Perspectives

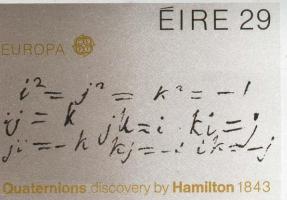
William R. Hamilton (1805-1865)

- Mathematician, physicist, and astronomer
- Contributed to algebra, mechanics, optics
- Formulated Hamiltonian mechanics
- Discovered quaternions, conical refraction, Hamilton function, Hamilton principle, Hamiltonian group
- Invented "Icosian Calculus", dot & cross products, Hamiltonian paths
- Influenced computer graphics, mechanics, electromagnetism, relativity, quantum theory, vector algebra



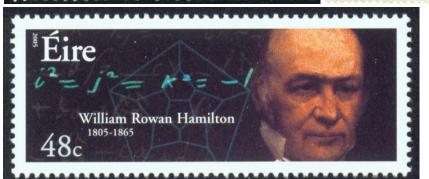
Here as he walked by on the 16th of October 1843 Sir William Rowan Hamilton in a flash of genius discovered the fundamental formula for quaternion multiplication $i^2 = j^2 = k^2 = ijk = -1$ & cut it on a stone of this bridge

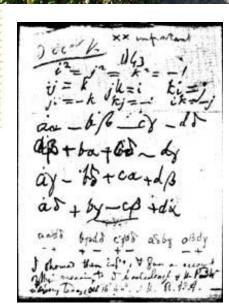












1		-				7.8		
	1	-1	i	-i	j	-j	k	-k
1	1	-1	i	-i	j	-j	k	-k
-1	-1	1	-i	i	-j	j	-k	k
i	i	-i	-1	1	k	-k	-j	j
-i	-i	i	1	-1	-k	k	j	-j
j	j	-j	-k	k	-1	1	i	-i
-j	-j	j	k	-k	1	-1	-i	i
k	k	-k	j	-ј	-i	i	-1	1
-k	-k	k	-ј	j	i	-i	1	-1

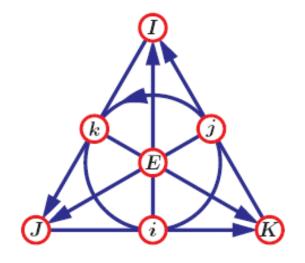
there as he walked by in the foth of October 1843 William Rowan Fall aftern the flash of penius discovered the flandamental formula for quaternion multiplication

i's j'-le's ijk - +

Octonions: Generalization of Quaternions

- Non-associative! (e.g., (ij) $K=-E \neq E=i(jK)$)
- Discovered by John Graves (1843), friend of Hamilton
- Useful in general relativity, quantum logic, string theory

×	i	j	k	E	1	J	K
i	-1	k	−j	1	-E	-K	J
j	-k	-1	i	J	K	-E	-/
k	j	- <i>j</i>	-1	K	-J	1	-E
E	-/	-J	-K	-1	i	j	k
1	Ε	-K	J	-j	-1	-k	j
J	K	E	-/	− j	k	-1	- <i>j</i>
K	-J	1	E	-k	− j	i	-1



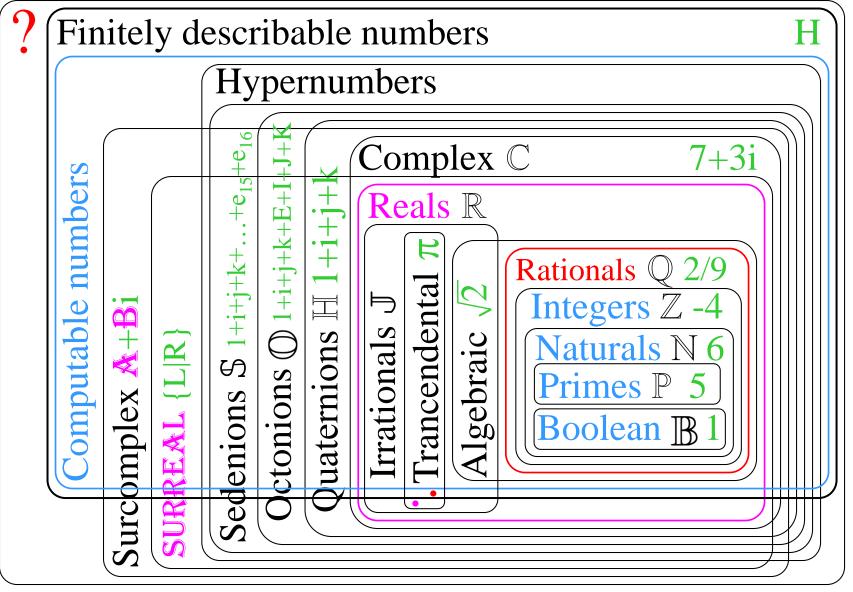
Mnemonic diagram for unit octonions products

Sedenions: Generalization of Octonions

• Non-alternative! (i.e., x(xy)=(xx)y doesn't hold)

×	1	e ₁	e ₂	e ₃	e ₄	e 5	e 6	e ₇	e 8	e 9	e ₁₀	e ₁₁	e ₁₂	e ₁₃	e ₁₄	e ₁₅
1	1	e ₁	e ₂	e 3	e ₄	e 5	e 6	e 7	e 8	e 9	e ₁₀	e ₁₁	e ₁₂	e 13	e ₁₄	e ₁₅
e ₁	e 1	-1	e 3	- e 2	e 5	− e 4	− e 7	e 6	e 9	− e 8	- e ₁₁	e ₁₀	− e 13	e ₁₂	e 15	-e ₁₄
e ₂	e ₂	− e ₃	-1	e 1	e 6	e 7	− e 4	− e 5	e ₁₀	e ₁₁	− e 8	- e 9	- e ₁₄	− e 15	e 12	e 13
e ₃	e 3	e ₂	− e 1	-1	e 7	− e 6	e 5	− e 4	e 11	- e ₁₀	e 9	− e 8	− e 15	e 14	− e 13	e ₁₂
e ₄	e ₄	− e 5	− e 6	− e 7	-1	e 1	e ₂	e 3	e 12	e 13	e ₁₄	e 15	− <i>e</i> ₈	− e 9	- e ₁₀	-e ₁₁
e ₅	e 5	e ₄	− e 7	e 6	− e 1	-1	− e ₃	e ₂	e 13	- e ₁₂	e 15	- e ₁₄	e 9	− e 8	e ₁₁	- e ₁₀
e ₆	e 6	e 7	e ₄	− e 5	−e 2	e 3	-1	− e 1	e 14	− e 15	- e ₁₂	e 13	e ₁₀	- e ₁₁	− e 8	e 9
e ₇	e 7	- e 6	e 5	e ₄	− e ₃	-e ₂	e 1	-1	e 15	e ₁₄	− e 13	- e ₁₂	e ₁₁	e ₁₀	− <i>e</i> ₉	− e 8
e 8	e 8	- e 9	− e 10	-e ₁₁	− e 12	− e 13	- e ₁₄	− e 15	-1	e 1	e ₂	e 3	e ₄	e 5	e 6	e 7
e 9	e 9	e 8	-e ₁₁	e ₁₀	− e 13	e ₁₂	e 15	- e ₁₄	− e 1	-1	− e ₃	e ₂	− e 5	e ₄	e 7	− e 6
e ₁₀	e 10	e ₁₁	e 8	- e 9	-e ₁₄	− e 15	e ₁₂	e 13	- e 2	e ₃	-1	− e 1	- e 6	− e 7	e ₄	e 5
e ₁₁	e 11	− e ₁₀	e 9	e 8	− e 15	e 14	− e 13	e 12	− e ₃	− e 2	e ₁	-1	− e 7	e 6	− e 5	e ₄
e ₁₂	e 12	e 13	e ₁₄	e 15	e 8	- e 9	− e ₁₀	-e ₁₁	− e 4	e 5	e 6	e 7	-1	− e 1	− e 2	− e ₃
e ₁₃	e 13	− e 12	e 15	-e ₁₄	e 9	e 8	e ₁₁	− e ₁₀	- e ₅	− e 4	e 7	- e 6	e 1	-1	e 3	-e ₂
e ₁₄	e ₁₄	- e ₁₅	- e ₁₂	e 13	e ₁₀	-e ₁₁	e 8	e 9	- e 6	− e 7	− e 4	e 5	e ₂	− e ₃	-1	e ₁
e ₁₅	e 15	e ₁₄	- e ₁₃	- e ₁₂	e ₁₁	e ₁₀	- e 9	e 8	− e 7	e 6	− e 5	− e 4	e 3	e ₂	− e 1	-1

Generalized Numbers



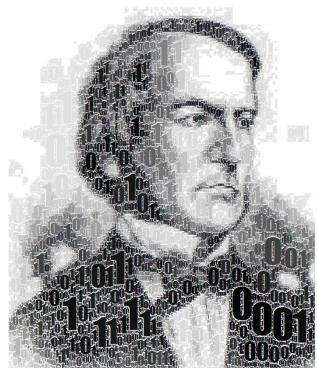
Theorem: some real numbers are not finitely describable!

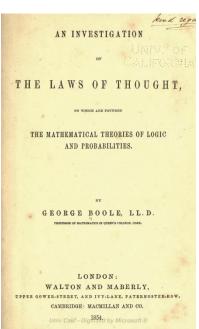
Theorem: some finitely describable real numbers are not computable!

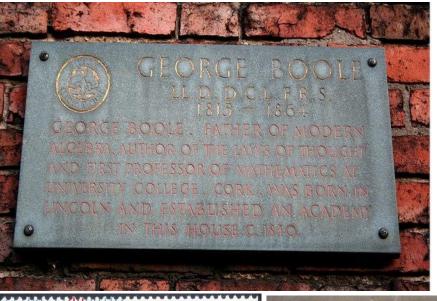
Historical Perspectives

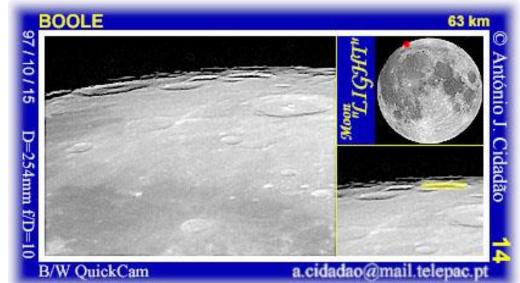
George Boole (1815-1864)

- Mathematician and philosopher
- Invented symbolic / Boolean logic
- Invented Boolean algebra, i.e. "calculus of reasoning"
- A founder of computer science
- "An Investigation into the Laws of Thought"
- Influenced De Morgan, Schröder, Shannon
- All modern computers, electronics, phones, data transmission, rely on Boolean principles







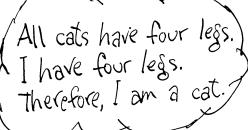
















001010 0010,0010

00101010 0010001110:

10011000101000100100

100110101

SARI!

BINARY LETTER FROM GRANDWA



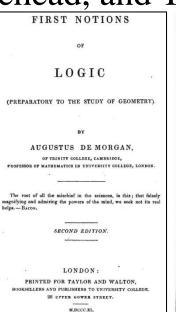
Mozart writing the digital version of his symphony No. 38 in D major.

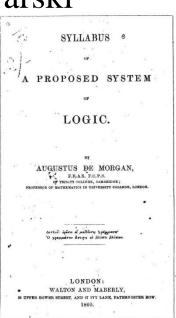
Historical Perspectives

Augustus De Morgan (1806-1871)

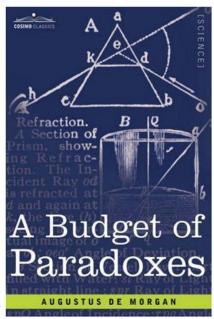
- Mathematician and logician
- Developed logic & mathematical induction
- De Morgan's Laws in logic & set theory
- Invented relational algebra
- Corresponded extensively with Hamilton
- Influenced Russell, Whitehead, and Tarski
- Studied paradoxes







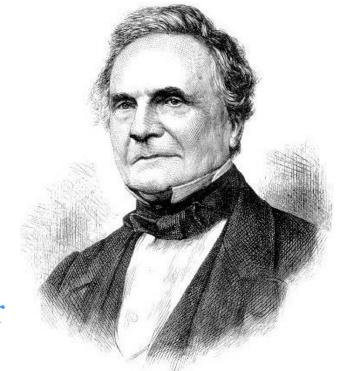




Historical Perspectives

Charles Babbage (1791-1871)

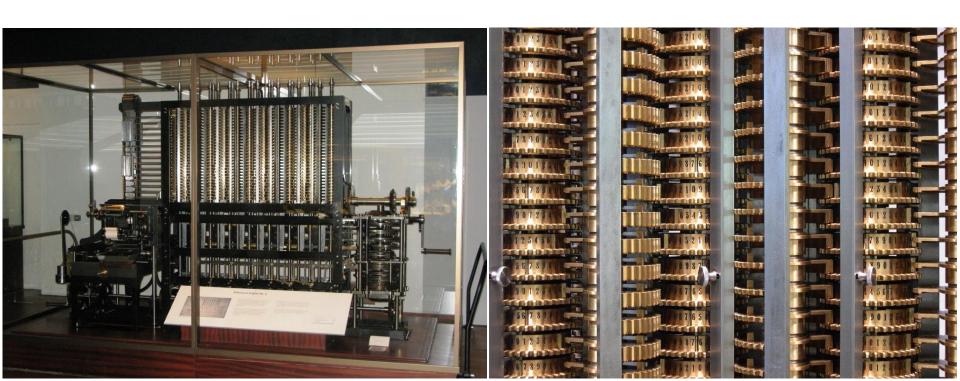
- Mathematician, philosopher, inventor mechanical engineer, and economist
- The father of computing
- Built world's first mechanical computer
 - the "difference engine" (1822)
- Originated the programmable computer
 - the "analytical engine" (1837)
- Worked in cryptography
- Developed Babbage's principle of division of labor



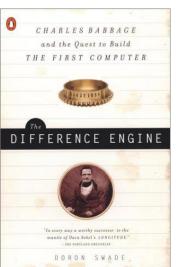


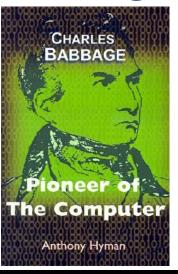
Babbage's Difference Engine

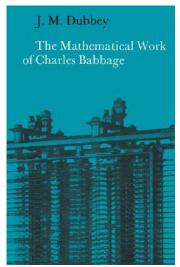
- World's first mechanical computer
- Designed in 1822, redesigned in 1847-1849
- 25,000 parts, 15 tons, 8ft tall, 31 digits of precision
- Tabulated polynomial functions, used Newton's method
- Approximated logarithmic and polynomial functions
- Used decimal number system and hand-crank

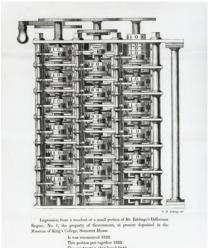


Babbage's Difference Engine















Babbage's difference engine built from Mechano and Lego

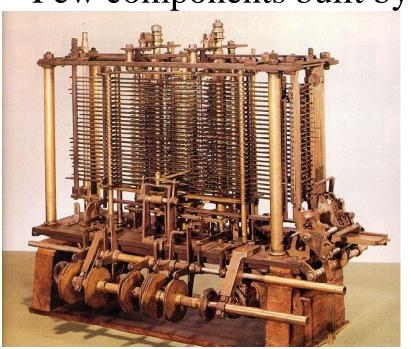


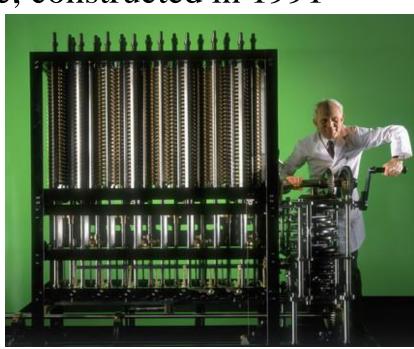




Babbage's Analytical Engine

- World's first general-purpose computer
- Designed in 1837, redesigned throughout Babbage's life
- Turing-complete, memory: 1000x50 digits (21 kB)
- Fully programmable "CPU", used punched cards
- Featured ALU, "microcode", loops, and printer!
- Could multiply two 20-digit numbers in 3 min
- Few components built by Babbage; constructed in 1991





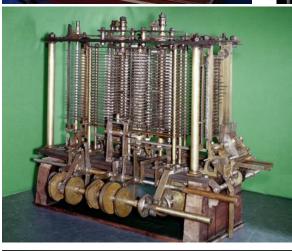




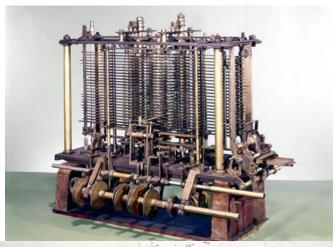


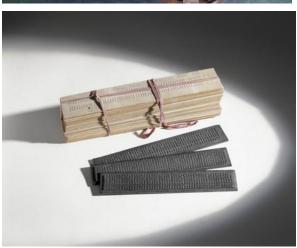






















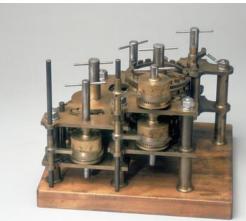


























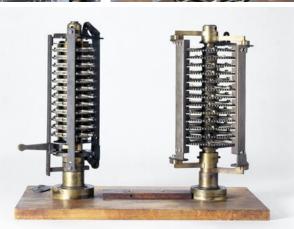


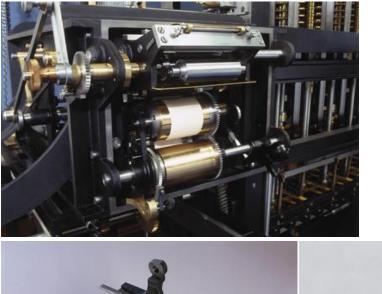




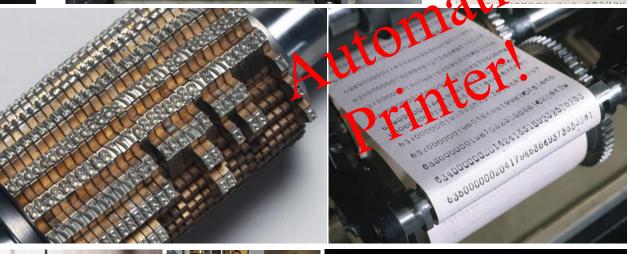












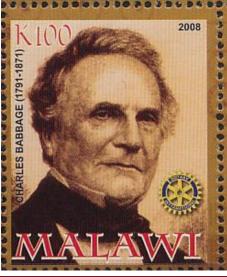








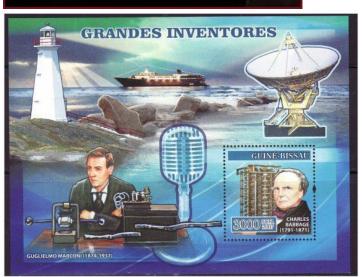
6820000003/06130273614

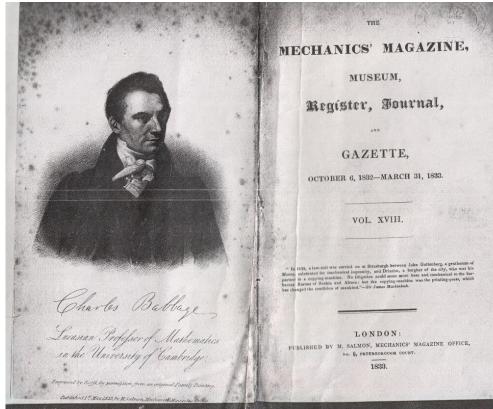




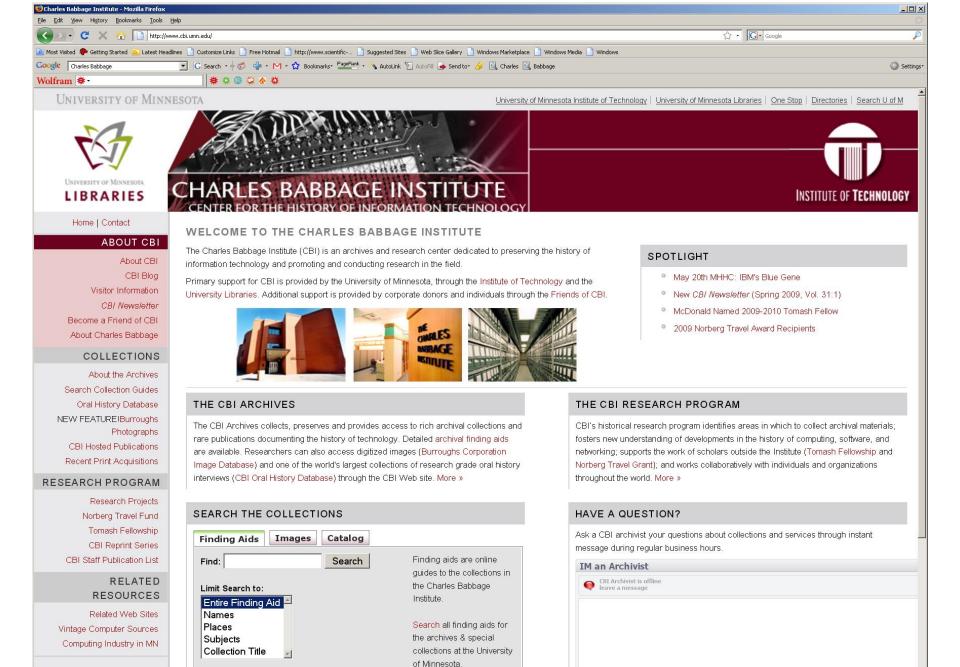












× Find: ♣ Next 👚 Previous 👂 Highlight all 🗀 Match case

Waiting for guest1.meebo.org.

Countess Ada Lovelace (1815-1852)

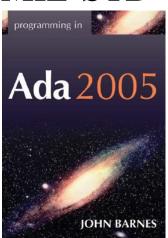
- Daughter of Lord Byron
- Tutored in math and logic by De Morgan
- Wrote the "manual" for Babbage's analytical engine, as well as programs for it
- World's first computer programmer!
- Foresaw the vast potential of computers
- Babbage: "The Enchantress of Numbers"
- DoD's Ada language "MIL-STD-1815"

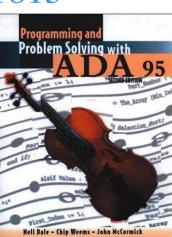




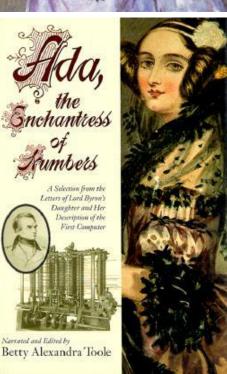


The International Language for Software Engineering

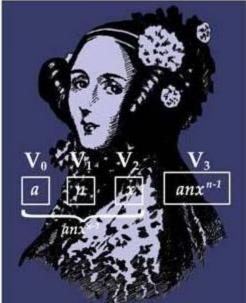








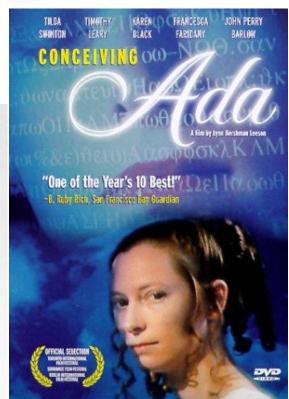






Ada Byron, Lady Lovelace 1815 - 1852





ComputerWeekl







Will IBM buy Sun?

If IBM buys Sun Microsystems how will the diverse product portfolios fit together?

NEWS ANALYSIS 12

OGC 'secret' out

The Office of Government Commerce finally publishes two ID card Gateway reviews NEWS 8

Tech terms banned

IT professionals react with hostility to a list of words. council leaders want to ban

NEWS ANALYSIS 10

Beware of SaaS risk

The cost benefits of softwareas-a-service should not blind companies to potential hazards

NEWS ANALYSIS 14

Web past to present

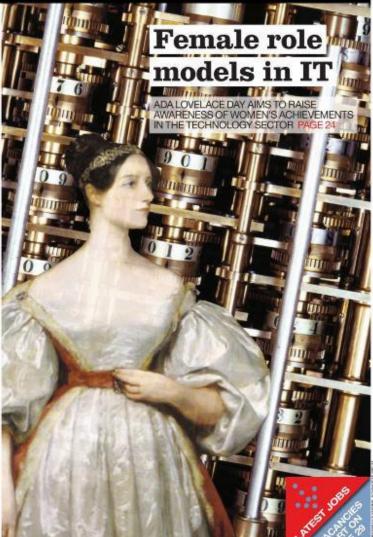
We celebrate 20 years of the internet by looking back at key events in its development.

THIS WEEK ON THE WEB 20

Leadership lessons

CW500 Club president shares his insights on challenges and opportunities facing IT leaders STRATEGY 22

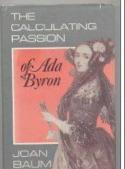






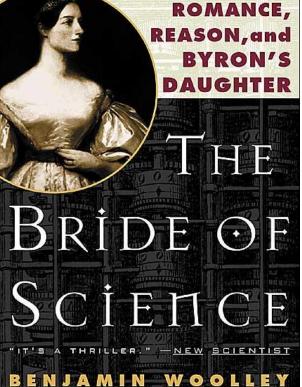


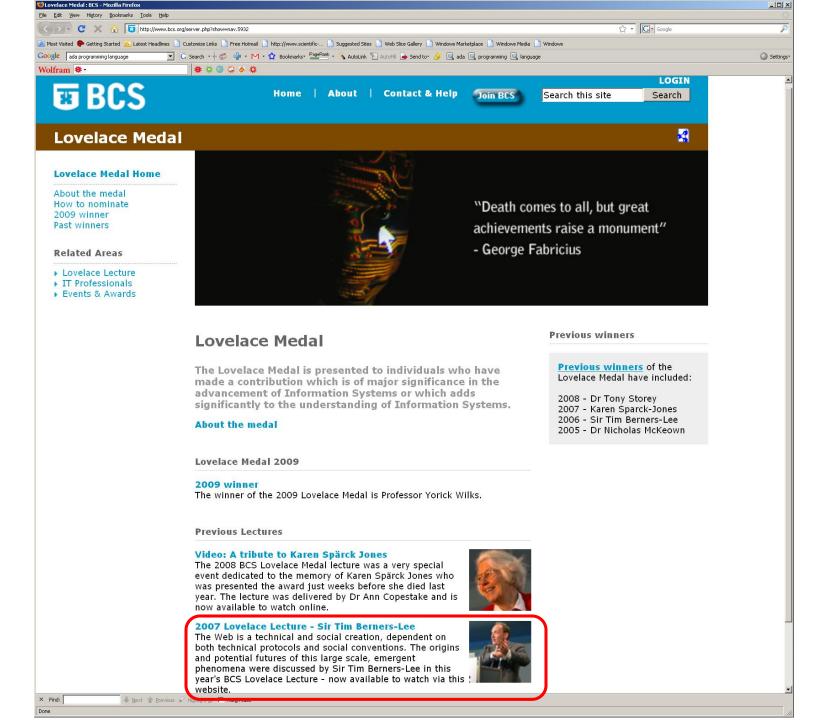






"A SPLENDID AND ENTHRALLING PORTRAIT." -THE SUNDAY TIMES (LONDON)





Ada Lovelace notes on "Sketch of the Analytical Engine Invented by Charles Babbage", by L. F. Menabrea, 1843

Her notes (three times longer than the paper itself!) contain the world's first computer program (for calculating Bernoulli numbers):

			Var	iables	for D	ata						V	Vorking	y Variables			Variables f	for Results					
Number of Operations	of Operations	$^{1}\mathrm{V}_{0}$	$^{1}V_{1}$	$^{1}\mathrm{V}_{2}$	$^{1}\mathrm{V}_{3}$	¹ V ₄ ¹ V ₅		$^{0}\mathrm{V}_{6}$	⁰ V ₇ ⁰ V ₈ ⁰ V		$^{0}\mathrm{V}_{9}$	$^{0}{ m V}_{10}$	$^{0}V_{11}$	$^{0}\mathrm{V}_{12}$	$^{0}{ m V}_{13}$	$^{0}\mathrm{V}_{14}$	$^{0}\mathrm{V}_{15}$	$^{0}{ m V}_{16}$					
Ope	per	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+					
r of		0	0	0	0	0	0	0	0 0 0		0	0	0	0	0	0	0	0					
quin	Nature	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0					
Z	Z	0	0	0	0	0 0		0 0		0	0	0	0	0	0	0	0	0					
		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0					
		m	n	d	$\boxed{m'}$	$\boxed{n'}$	$\boxed{d'}$										$\boxed{\frac{dn'-d'n}{mn'-m'n} = x}$	$\boxed{\frac{d'm-dm}{mn'-m'n} = y}$					
1 2	×	m	n		m'	n'		mn'	m'n	dn'													
3	×		0	d			d'				d'n												
5	×	0		0	0		0					d'm	dm'										
6 7	^							0	0					(mn'-m'n)									
8	$\left -\right $									0	0				(dn'-d'n)	(d'm dm/)							
9	÷											0	0	(mn'-m'n)	0	(d'm - dm')	$\frac{dn' - d'n}{mn' - m'n} = x$						
11	÷													0		0		$\tfrac{d'm-dm'}{mn'-m'n}=y$					
															I	I							

World's first computer program (for calculating Bernoulli numbers), by Ada Lovelace, 1843:

Data Working Variables																					
						1	Data	1	0	0	0	0				Working Variables		1 0		sult Variab	
g.	-					$^{1}V_{1}$	$^{1}V_{2}$	$^{1}V_{3}$	$^{0}\mathrm{V}_{4}$	$^{0}V_{5}$	$^{0}V_{6}$	⁰ V ₇	⁰ V ₈	⁰ V ₉	⁰ V ₁₀	⁰ V ₁₁	$^{0}V_{12}$	⁰ V ₁₃		₂₂ ¹ V ₂₃	
ratio	atio			T 31 41 6		0	0	0	0	0	0	0	0	0	0	0	0	0	0 (0
of Operation	Oper	Variables acted	Variables receiving	Indication of change in the	Statement of Results	0	0	0	0	0	0	0	0	0	0	0	0	0	a ct. a	. ti . e . ti	0
	15	upon	results	value on any Variable		0	0	0	0	0	0	0	0	0	0	0	0	0	B in a dec. fract.	fra fra dec fra	0
Number	Nature						2	4	0	0	0	0	0	0	0	0	0	0		\neg $ $ $$	
ź	ĺž					1	2	n											B ₁	B ₅	В7
	+			(1 1)																	
1	×	$^{1}V_{2} \times {}^{1}V_{3}$	$^{1}V_{4}$, $^{1}V_{5}$, $^{1}V_{6}$	- v ₃ = - v ₃	= 2n		2	n	2n	2n	2n										
2	-	$^{1}V_{4} - {}^{1}V_{1}$	² V ₄	$\left\{ \begin{array}{lll} {}^{1}V_{4} & = & {}^{2}V_{4} \\ {}^{1}V_{1} & = & {}^{1}V_{1} \end{array} \right\}$	= 2n - 1	1			2n - 1												
3	+	$^{1}V_{5} + ^{1}V_{1}$	² V ₅	$ \begin{cases} {}^{1}V_{5} &= {}^{2}V_{5} \\ {}^{1}V_{1} &= {}^{1}V_{1} \end{cases} $	=2n+1	1				2n + 1											
4	÷	$^{2}V_{5} \div ^{2}V_{4}$	¹ V ₁₁	$ \begin{bmatrix} {}^{2}V_{5} & = & {}^{0}V_{5} \\ {}^{2}V_{4} & = & {}^{0}V_{4} \end{bmatrix} $	$= \frac{2n-1}{2n+1} \dots$				0	0						$\frac{2n-1}{2n+1}$					
5	÷	$^{1}V_{11} \div ^{1}V_{2}$	² V ₁₁	$ \begin{bmatrix} ^{1}V_{11} & = & {}^{2}V_{11} \\ ^{1}V_{2} & = & {}^{1}V_{2} \end{bmatrix} $	$= \frac{1}{2} \cdot \frac{2n-1}{2n+1} \cdot \dots \cdot \dots$		2									$\tfrac{1}{2}\cdot \tfrac{2n-1}{2n+1}$					
6	-	$^{0}V_{13} - {}^{2}V_{11}$	¹ V ₁₃	$ \begin{vmatrix} 2V_{11} & = & {}^{0}V_{11} \\ {}^{0}V_{13} & = & {}^{1}V_{13} \end{vmatrix} $	$= -\frac{1}{2} \cdot \frac{2n-1}{2n+1} = A_0 \dots$											0		$= -\frac{1}{2} \cdot \frac{2n-1}{2n+1} = \mathbf{A}_0$			
7		$^{1}V_{3} - ^{1}V_{1}$	¹ V ₁₀	$\left\{ \begin{array}{l} {}^{1}V_{3} & = & {}^{1}V_{3} \\ {}^{1}V_{1} & = & {}^{1}V_{1} \end{array} \right\}$	$= n - 1 (= 3) \dots$	1		n							n-1						
8	+	$^{1}V_{2} + {}^{0}V_{7}$	¹ V ₇	$\begin{cases} {}^{1}V_{2} & = & {}^{1}V_{2} \\ {}^{0}V_{7} & = & {}^{1}V_{7} \end{cases}$	= 2 + 0 = 2		2					2									
9	÷	$^{1}V_{6} \div ^{1}V_{7}$	³ V ₁₁	$\begin{cases} {}^{1}V_{6} & = & {}^{1}V_{6} \\ {}^{0}V_{11} & = & {}^{3}V_{11} \end{cases}$	$=\frac{2n}{2}=A_1\ldots\ldots$						2n	2				$\frac{2n}{2} = A_1$					
10	×	$^{1}V_{21} \times {}^{3}V_{11}$	¹ V ₁₂	$ \begin{vmatrix} ^{1}V_{21} & = & {}^{1}V_{21} \\ ^{3}V_{11} & = & {}^{3}V_{11} \end{vmatrix} $	$= B_1 \cdot \frac{2n}{2} = B_1 A_1 \dots$											$\frac{2n}{2} = A_1$	$B_1 \cdot \frac{2n}{2} = B_1 A_1$		В1		
11	+	$^{1}V_{12} + ^{1}V_{13}$	² V ₁₃	$\begin{cases} {}^{1}V_{12} & = & {}^{0}V_{12} \\ {}^{1}V_{13} & = & {}^{2}V_{13} \end{cases}$	$= -\frac{1}{2} \cdot \frac{2n-1}{2n+1} + B_1 \cdot \frac{2n}{2} \dots$												0	$\left\{ -\frac{1}{2} \cdot \frac{2n-1}{2n+1} + \mathbf{B}_1 \cdot \frac{2n}{2} \right\}$			
12		$^{1}V_{10} - ^{1}V_{1}$	² V ₁₀	$\begin{cases} {}^{1}V_{10} & = & {}^{2}V_{10} \\ {}^{1}V_{1} & = & {}^{1}V_{1} \end{cases}$	= n - 2(= 2)	1									n-2						
13	(-	$^{1}V_{6} - {^{1}V_{1}}$	² V ₆	$\begin{cases} {}^{1}V_{6} & = & {}^{2}V_{6} \\ {}^{1}V_{1} & = & {}^{1}V_{1} \end{cases}$	=2n-1	1					2n - 1										
14	J +	$^{1}V_{1} + ^{1}V_{7}$	² V ₇	$\begin{cases} {}^{1}V_{1} & = & {}^{1}V_{1} \\ {}^{1}V_{7} & = & {}^{2}V_{7} \end{cases}$	= 2 + 1 = 3	1						3									
15) ÷	$^{2}V_{6} \div ^{2}V_{7}$	¹ V ₈	$\begin{cases} {}^{2}V_{6} & = & {}^{2}V_{6} \\ {}^{2}V_{7} & = & {}^{2}V_{7} \end{cases}$	$=\frac{2n-1}{3} \dots \dots$						2n - 1	3	$\frac{2n-1}{3}$								
16	(×	$^{1}V_{8} \times {}^{3}V_{11}$	⁴ V ₁₁	$\begin{cases} {}^{1}V_{8} & = & {}^{0}V_{8} \\ {}^{3}V_{11} & = & {}^{4}V_{11} \end{cases}$	$= \frac{2n}{2} \cdot \frac{2n-1}{3} \cdot \dots$								0			$\frac{2n}{2} \cdot \frac{2n-1}{3}$					
17	-	$^{2}V_{6} - {}^{1}V_{1}$	³ V ₆	$\begin{cases} {}^{2}V_{6} & = & {}^{3}V_{6} \\ {}^{1}V_{1} & = & {}^{1}V_{1} \\ {}^{2}V_{1} & = & {}^{2}V_{1} \end{cases}$	= 2n - 2	1					2n - 2										
18	Į +	$^{1}V_{1} + ^{2}V_{7}$	³ V ₇	$ \left\{ \begin{array}{rcl} & 2V_7 & = & ^3V_7 \\ & ^1V_1 & = & ^1V_1 \\ & ^2V_1 & = & ^2V_2 \end{array} \right\} $	= 3 + 1 = 4	1						4									
19	÷	$^{3}V_{6} \div ^{3}V_{7}$	¹ V ₉	$\begin{cases} {}^{3}V_{6} & = & {}^{3}V_{6} \\ {}^{3}V_{7} & = & {}^{3}V_{7} \end{cases}$	$=\frac{2n-2}{4} \dots \dots$						2n - 2	4		$\frac{2n-2}{4}$							
20	\	$^{1}V_{9} \times {}^{4}V_{11}$	⁵ V ₁₁	$\begin{cases} {}^{1}V_{9} & = & {}^{0}V_{9} \\ {}^{4}V_{11} & = & {}^{5}V_{11} \end{cases}$	$= \frac{2n}{2} \cdot \frac{2n-1}{3} \cdot \frac{2n-2}{4} = A_3 \dots$									0		$\left\{ \frac{2n}{2} \cdot \frac{2n-1}{3} \cdot \frac{2n-2}{4} \right\} = A_3$					
21	×	$^{1}V_{22} \times {}^{5}V_{11}$	⁰ V ₁₂	$\begin{cases} {}^{1}V_{22} & = & {}^{1}V_{22} \\ {}^{0}V_{12} & = & {}^{2}V_{12} \end{cases}$	$= B_3 \cdot \frac{2n}{2} \cdot \frac{2n-1}{3} \cdot \frac{2n-2}{4} = B_3 A_3$											0	B_3A_3		E	3	
22	+	$^{2}V_{12} + ^{2}V_{13}$		$\begin{cases} ^{2}V_{12} & = & ^{0}V_{12} \\ ^{2}V_{13} & = & ^{3}V_{13} \end{cases}$	$= A_0 + B_1 A_1 + B_3 A_3 \dots$												0	${A_0 + B_1 A_1 + B_3 A_3}$			
23	-	$^{2}V_{10} - ^{1}V_{1}$	³ V ₁₀	$\begin{cases} {}^{2}V_{13} & = & {}^{3}V_{13} \\ {}^{2}V_{10} & = & {}^{3}V_{10} \\ {}^{1}V_{1} & = & {}^{1}V_{1} \end{cases}$	$= n - 3(= 1) \dots$	1									n-3						
							Here	follows	a repeti	tion of	Operatio	ons thirt	een to t	wenty-th	aree						
24	+	$^{4}V_{13} + {}^{0}V_{24}$	¹ V ₂₄	$ \begin{vmatrix} 4V_{13} & = & {}^{0}V_{13} \\ {}^{0}V_{24} & = & {}^{1}V_{24} \end{vmatrix} $	= B ₇																В7
0.5				$\begin{cases} {}^{1}V_{1} = {}^{1}V_{1} \\ {}^{1}V_{2} = {}^{1}V_{2} \end{cases}$	= n + 1 = 4 + 1 = 5																
25	+	$^{1}V_{1} + ^{1}V_{3}$	¹ V ₃	$\begin{cases} 5V_6 = {}^{0}V_6 \\ 5V_7 = {}^{0}V_7 \end{cases}$	by a Variable-card. by a Variable-card.	1		n+1			0	0									
				' ' ' ' '																	

Quotes from the Ada Lovelace notes on

"Sketch of the Analytical Engine Invented by Charles Babbage", 1843

"We may say most aptly, that the Analytical Engine weaves algebraical patterns just as the Jacquard-loom weaves flowers and leaves."

"Again, it might act upon other things besides *number*, were objects found whose mutual fundamental relations could be expressed by those of the abstract science of operations, and which should be also susceptible of adaptations to the action of the operating notation and mechanism of the engine. Supposing, for instance, that the fundamental relations of pitched sounds in the science of harmony and of musical composition were susceptible of such expression and adaptations, the engine might compose elaborate and scientific pieces of music of any degree of complexity or extent."





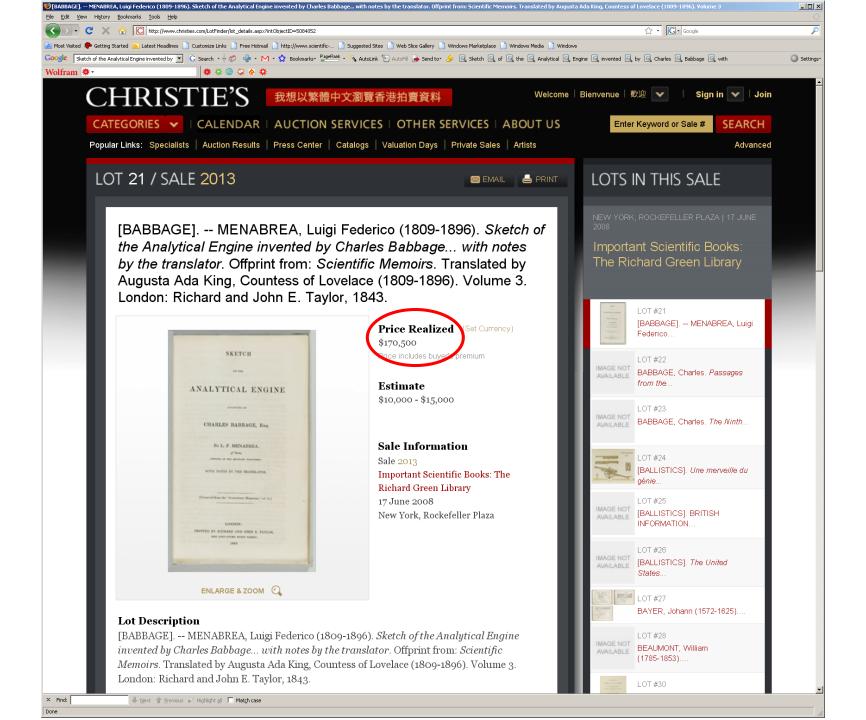
Quotes from the Ada Lovelace notes on

"Sketch of the Analytical Engine Invented by Charles Babbage", 1843

"Many persons who are not conversant with mathematical studies, imagine that because the business of the engine is to give its results in *numerical notation*, the *nature of its processes* must consequently be *arithmetical* and *numerical*, rather than *algebraical* and *analytical*. This is an error. The engine can arrange and combine its numerical quantities exactly as if they were *letters* or any other *general* symbols; and in fact it might bring out its results in algebraical *notation*, were provisions made accordingly."

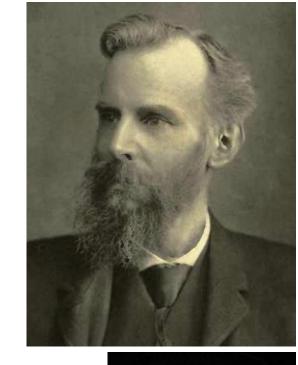
"But it would be a mistake to suppose that because its results are given in the notation of a more restricted science, its processes are therefore restricted to those of that science. The object of the engine is in fact to give the utmost practical efficiency to the resources of numerical interpretations of the higher science of analysis, while it uses the processes and combinations of this latter."

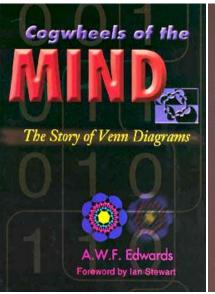


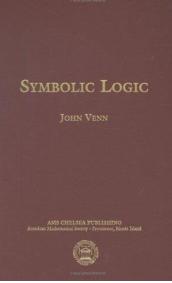


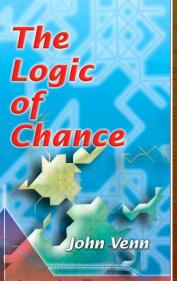
John Venn (1834-1923)

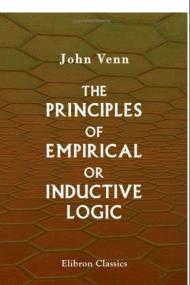
- Logician and philosopher
- Worked in logic, probability, set theory
- Introduced the "Venn diagram" (1880)
 - Very widely used, many applications
 - Ties together fundamental concepts from logic, geometry, combinatorics, knot theory





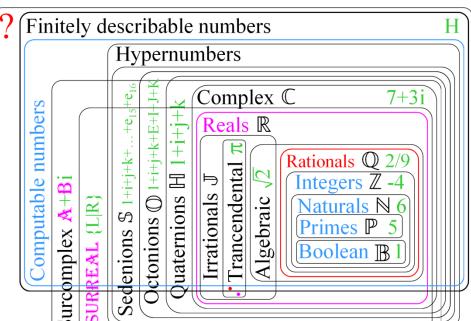




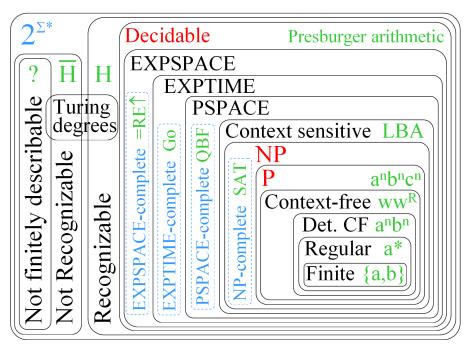


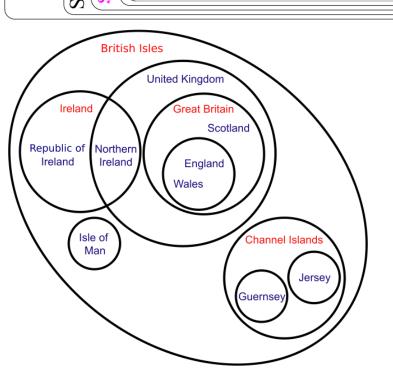


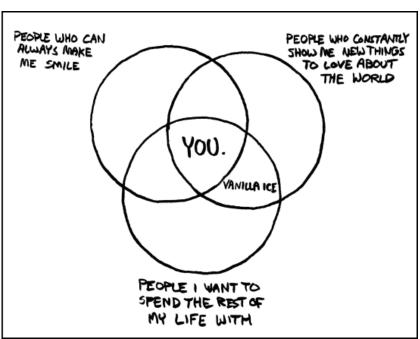
Generalized Numbers

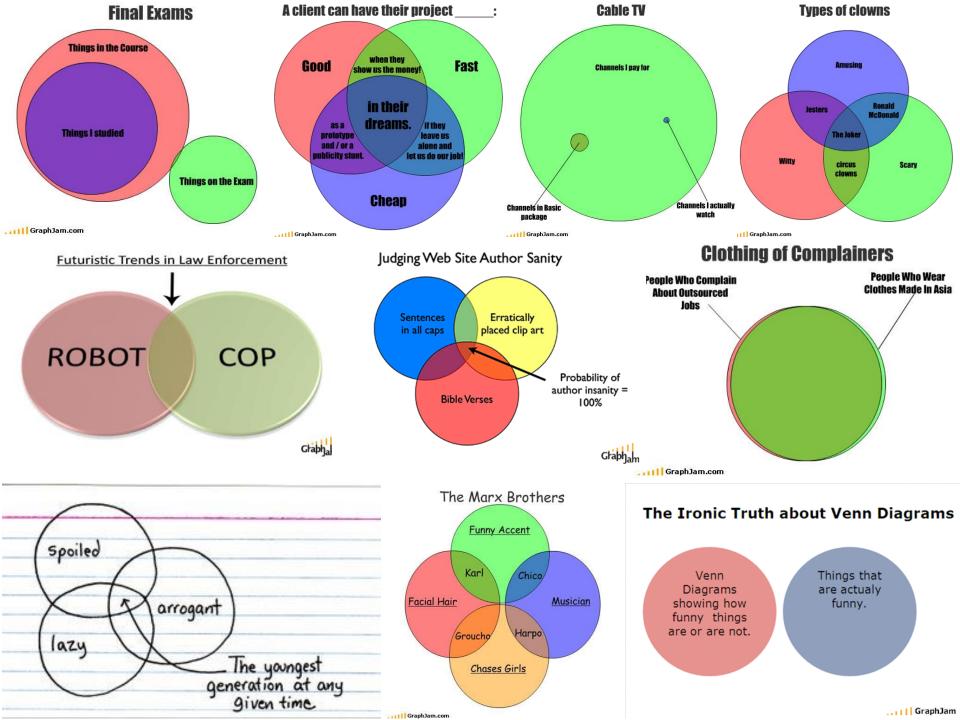


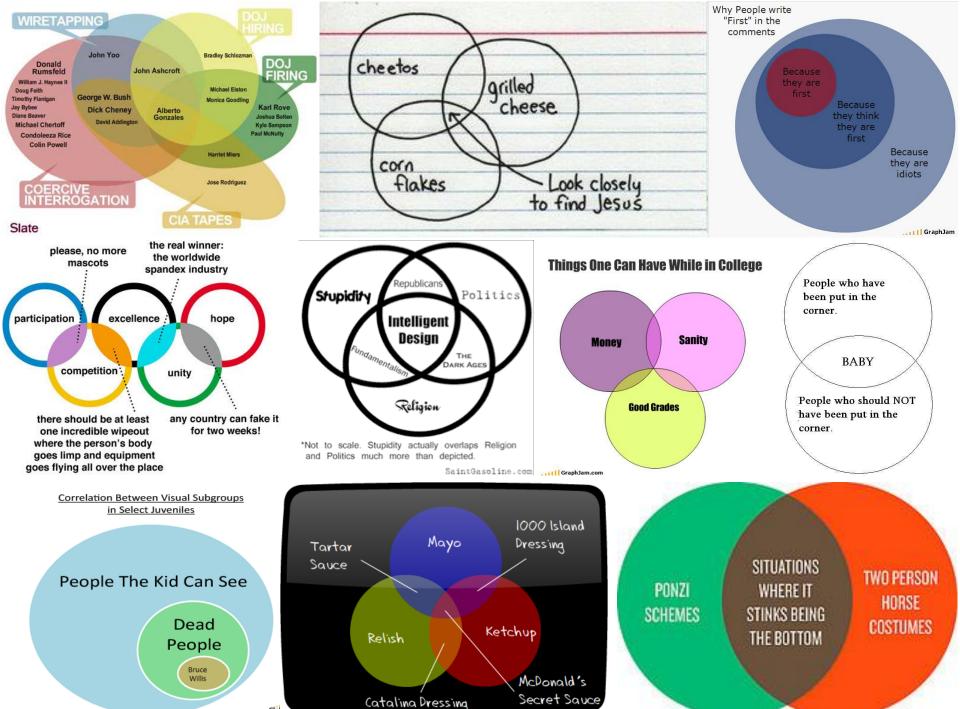
The Extended Chomsky Hierarchy

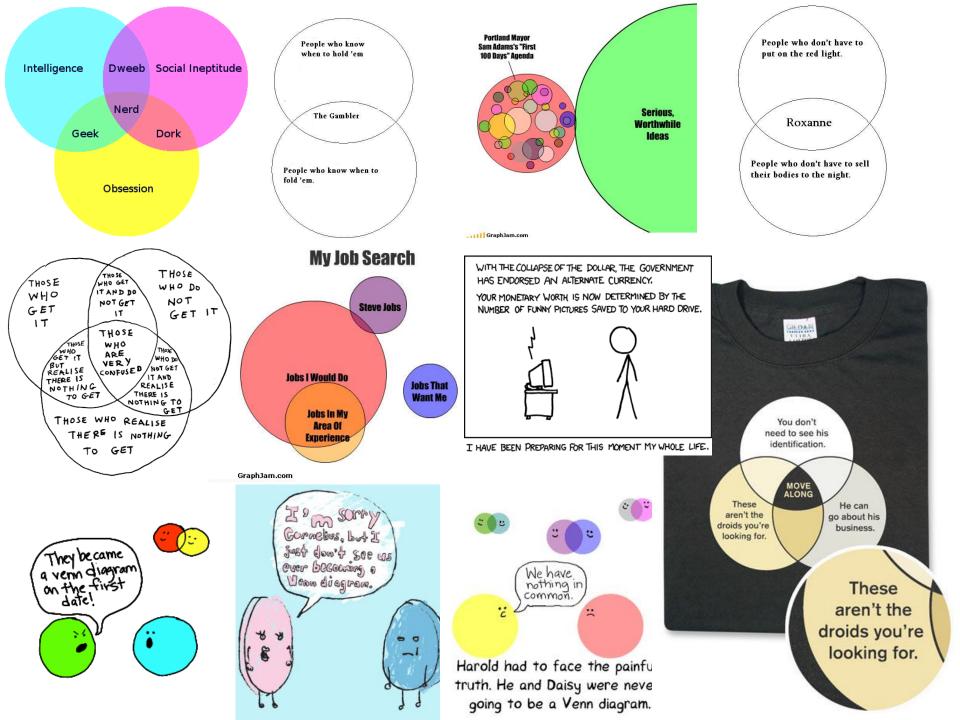






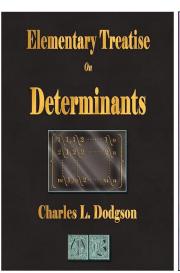


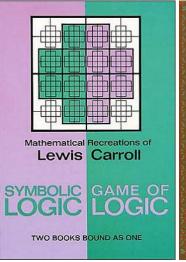


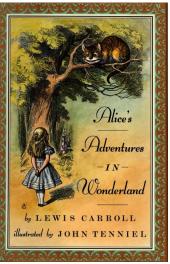


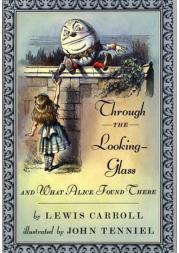
Charles Dodgson (1832-1898)

- AKA "Lewis Carroll"
- Mathematician, logician, author, photographer
- Wrote "Alice in Wonderland", "Jabberwocky", and "Through the Looking Glass"
- Popularized logic & syllogisms and made it fun!
- Invented "Scrabble" and "word ladder" games
- Profoundly influenced literature, art, and culture

















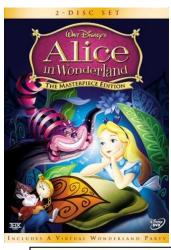


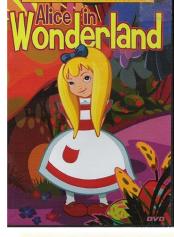


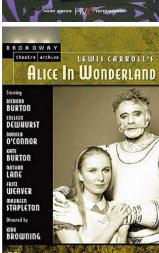




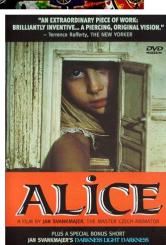




















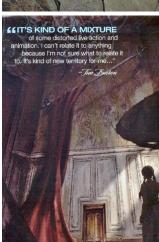


















Alice and the White Knight: A Lesson in Logic, Semantics, and Pointers

'You are sad,' the Knight said in an anxious tone: 'let me sing you a song to comfort you.'

`Is it very long?' Alice asked, for she had heard a good deal of poetry that day.

`It's long,' said the Knight, `but it's very, *very* beautiful. Everybody that hears me sing it -- either it brings the *tears* into their eyes, or else --' logical disjunction!

'Or else what?' said Alice, for the Knight had made a sudden pause. law of the excluded middle!

'Or else it doesn't, you know. The name of the song is called "*Haddocks' Eyes*".'
pointer to a pointer!

`Oh, that's the name of the song, is it?' Alice said, trying to feel interested.

'No, you don't understand,' the Knight said, looking a little vexed. 'That's what the name is *called*. The name really is "The Aged Aged Man".' pointer dereferencing: meta-pointer resolved!

`Then I ought to have said "That's what the *song* is called"?'
Alice corrected herself. separation of abstractions: variable vs. pointer!

'No, you oughtn't: that's quite another thing! The *song* is called "*Ways and Means*": but that's only what it's *called*, you know!'

call-by-name vs. call-by-value!

`Well, what is the song, then?' said Alice, who was by this time completely bewildered

`I was coming to that,' the Knight said. `The song really is "A-sitting On a Gate": and the tune's my own invention.'



the name is called "Haddocks' Eyes"

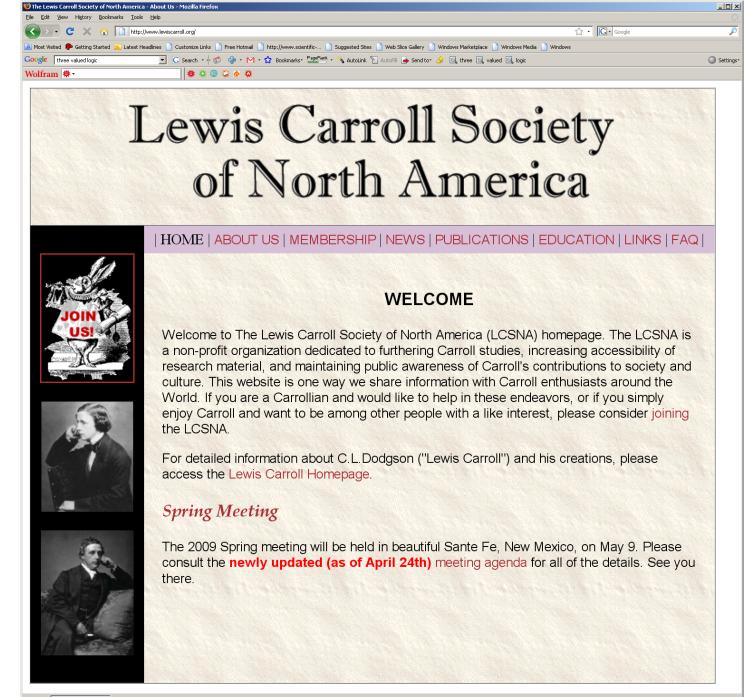
the name of the song is "The Aged Aged Man"

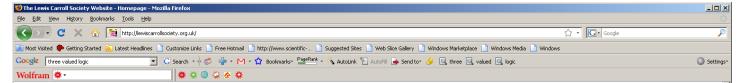
the song is "A-sitting On a Gate"

the song is called "Ways and Means"











The Lewis Carroll Society

The Lewis Carroll Society

founded 1969 ~ registered charity no. 266239

Navigation

- Site Index
- Site Search
- Recent Additions
- Interesting Links

Communication

- Contact The Society
- Join Our Email List

About The Society

- Membership
- Publications
- Society Journals
- Detailed Information

About Lewis Carroll

- Lewis Carroll's Life
- Lewis Carroll's Works
- Lewis Carroll's Diaries
- Reading & Researching

Inspired by Carroll

- Fine Art
- Performing Art
- Postage Stamps
- Pop-up Alice Editions

Events, People, Places

- Carrollian Events
- Lewis Carroll Societies
- Places to Visit
- Collecting and Shanning

Welcome to the Lewis Carroll Society Website

The Lewis Carroll Society was formed in 1969 with the aim of encouraging research into the life and works of Lewis Carroll (Charles Lutwidge Dodgson). The Society has members around the world, including many leading libraries and institutions, authors, researchers and many who simply enjoy Carroll's books and want to find out more about the man and his work.

Why not join the LCS - for your own interest and entertainment or to make a contribution to Carroll scholarship? Our subscription are remarkably low for a society of this nature. Click Here for membership details.

Events at Lyndhurst: from 15 May 2009



This wonderful season of Alice-related events has something for everyone! The village of Lyndhurst, in the beautiful New Forest, celebrates its Alice connections with walks, talks, tea-parties, musicals, and many other activities. Vist the **Alice Adventure** website for more details.

Events at Oxford: 4 July 2009



The city of Oxford plays host to the second Alice's Day this year, with a busy programme of events on 4 July. There are live performances, reading, drama workshops, exhibitions, talks and other activities for all the family.

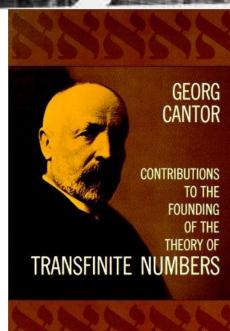
The Lewis Carroll Society is hosting a series of lectures at the Natural History Museum from 10:15. Edward Wakeling talks about the real Alice and the original telling of her adventures, Anne Varty investigates the child-actresses who played Alice and were friends of Lewis Carroll and Mark Richards explores the connections between Carroll and Charles Darwin. All are welcome to attend - come and go as you please.

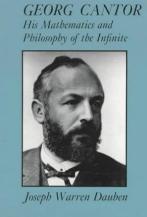


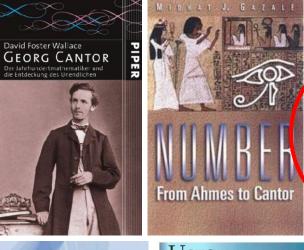
Georg Cantor (1845-1918)

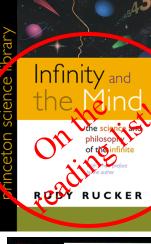
- Created modern set theory
- Invented trans-finite arithmetic (highly controvertial at the time)
- Invented diagonalization argument
- First to use 1-to-1 correspondences with sets
- Proved some infinities "bigger" than others
- Showed an infinite hierarchy of infinities
- Formulated continuum hypothesis
- Cantor's theorem, "Cantor set", Cantor dust, Cantor cube, Cantor space, Cantor's paradox
- Laid foundation for computer science theory
- Influenced Hilbert, Godel, Church, Turing

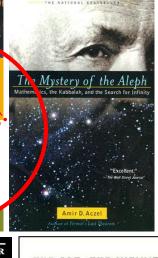


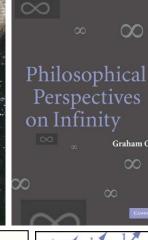


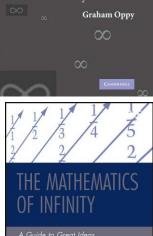


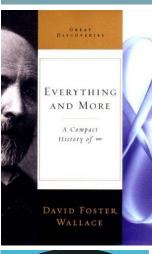




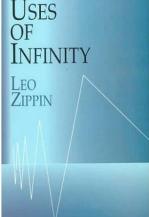


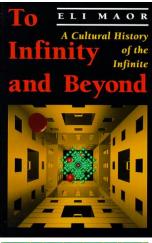


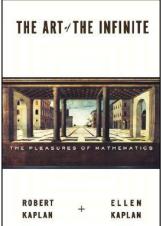


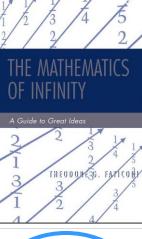


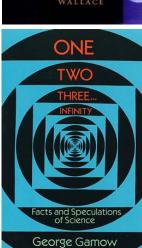




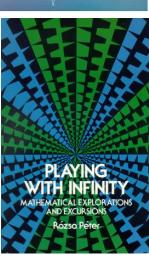










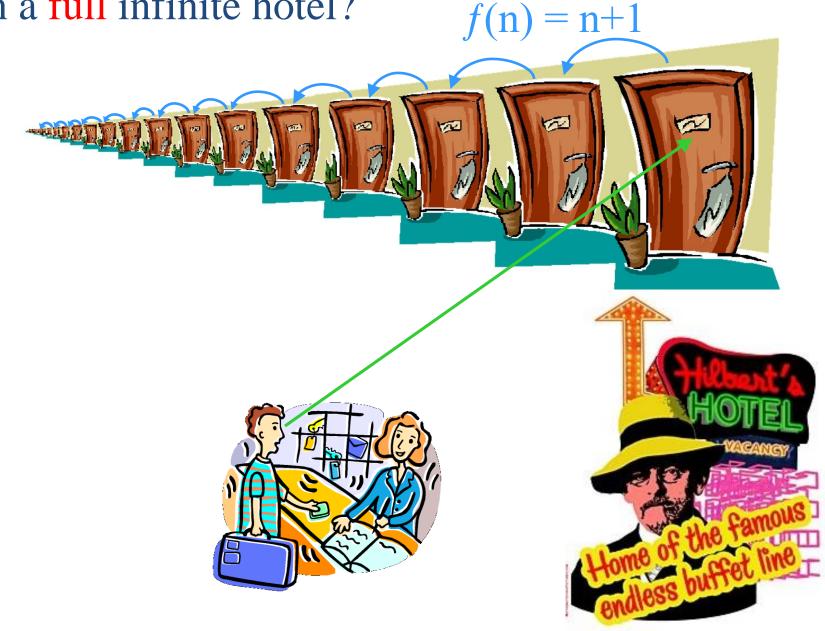


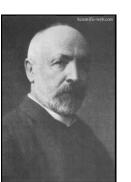




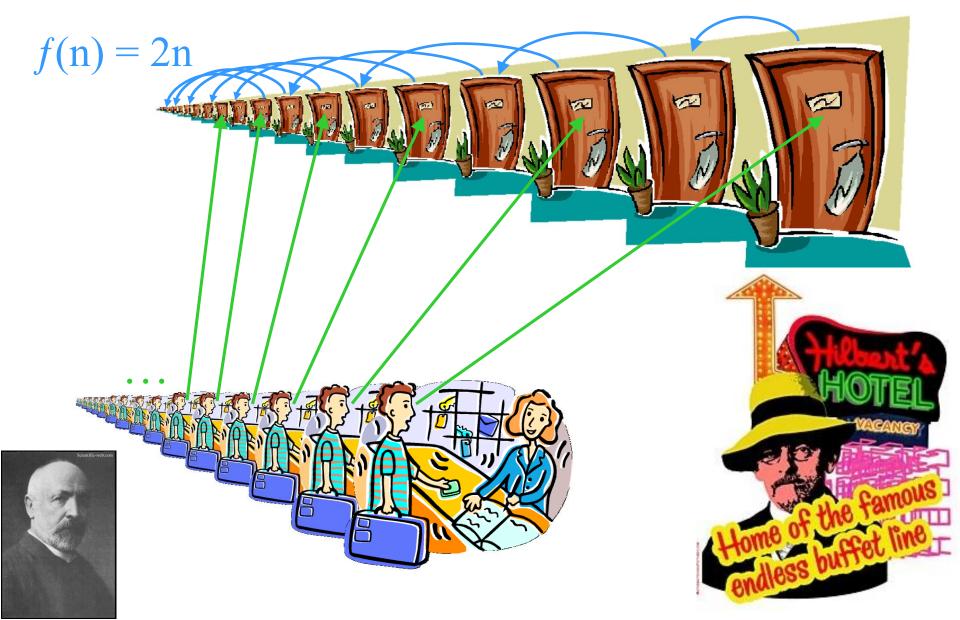


Problem: How can a new guest be accommodated in a full infinite hotel? f(n) = n+1

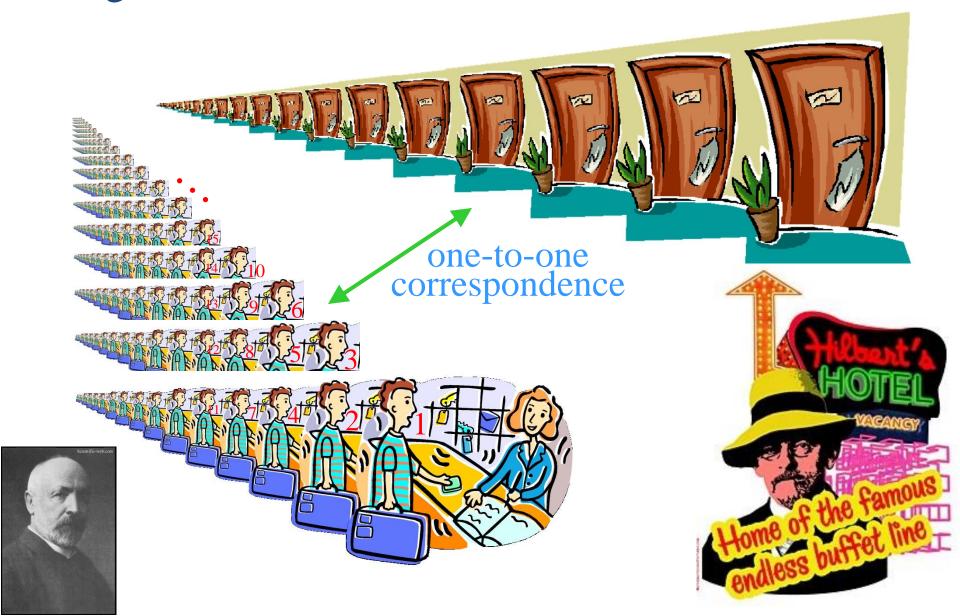




Problem: How can an infinity of new guests be accommodated in a full infinite hotel?



Problem: How can an infinity of infinities of new guests be accommodated in a full infinite hotel?

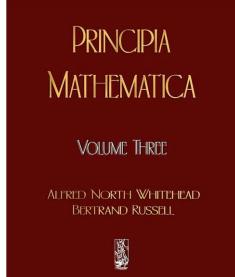


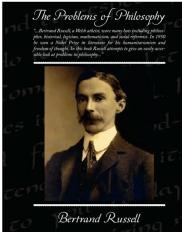


Bertrand Russell (1872-1970)

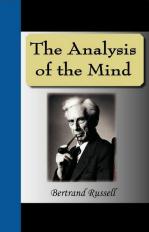
- Philosopher, logician, mathematician, historian, social reformist, and pacifist
- Co-authored "Principia Mathematica" (1910)
- Axiomatized mathematics and set theory
- Co-founded analytic philosophy
- Originated Russell's Paradox
- Activist: humanitarianism, pacifism, education, free trade, nuclear disarmament, birth control gender & racial equality, gay rights
- Profoundly transformed math & philosophy, mentored Wittgenstein, influenced Godel
- Laid foundation for computer science theory
- Won Nobel Prize in literature (1950)

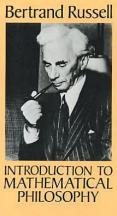


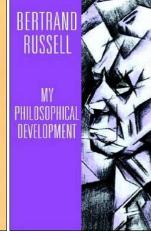




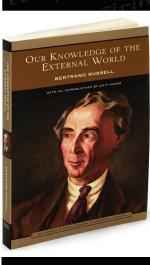


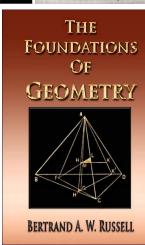


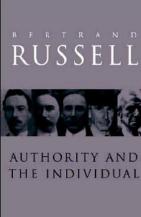


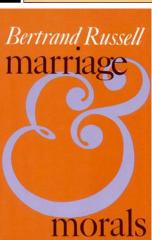


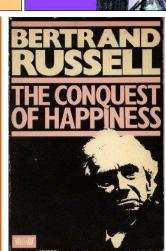


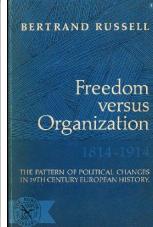


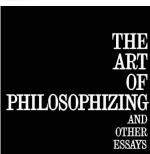






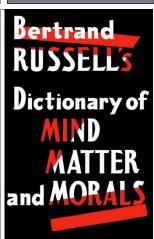






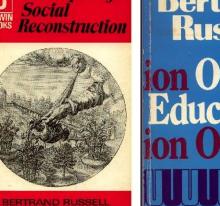


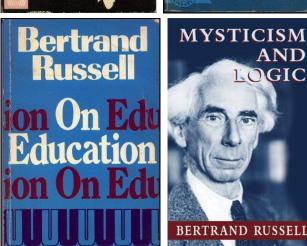


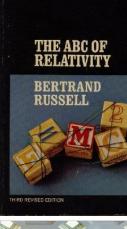




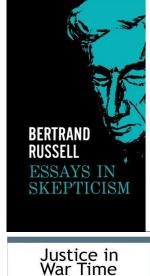
Principles of

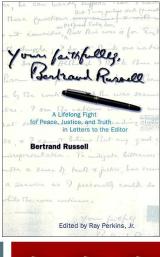


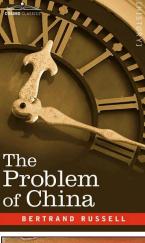


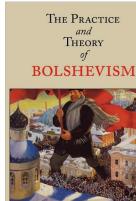


A MENTOR BOOK (1) 451-M/FIGAIN \$1.50



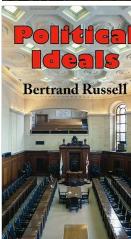




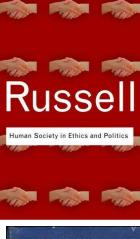


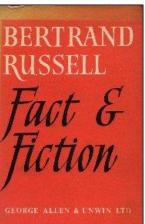


The Philosophy



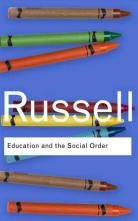


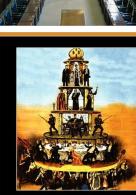


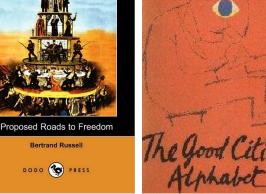


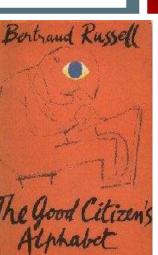


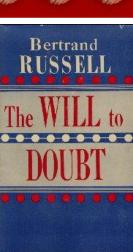
BERTRAND RUSSELL

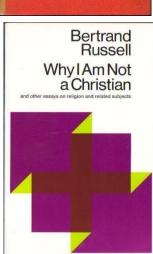


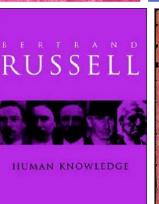


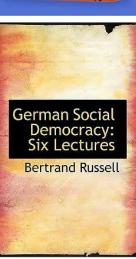


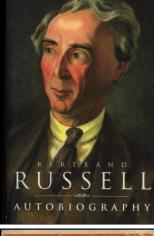


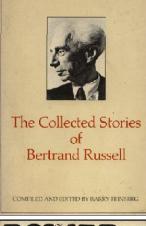


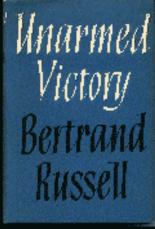


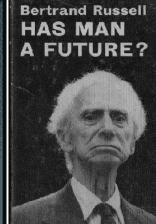


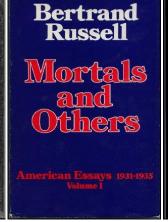




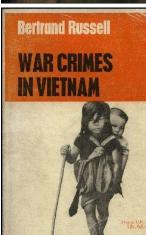






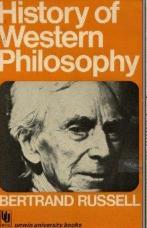








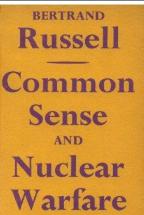


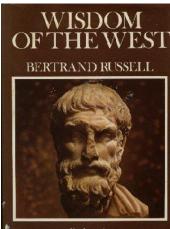




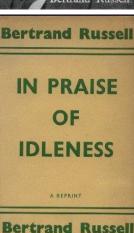
UNPOPULAR

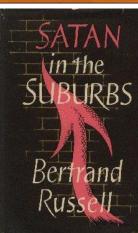
ESSAYS

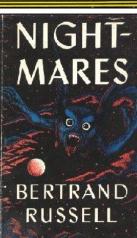




New Hopes for a Changing World Bertrand Russell



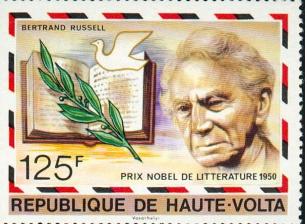


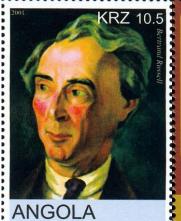


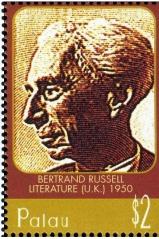
from
Memory
and Other Essays
Bertrand
Russell

Portraits



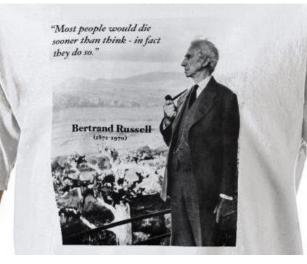


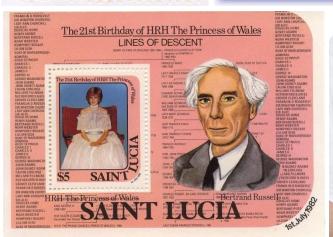


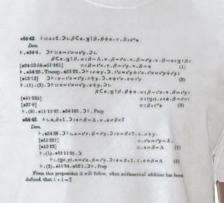












"Most people would sooner die than think; in fact, they do so."

- Bertrand Russell (1872-1970)

Russell's paradox was invented by Russell in 1901 to show that naïve set theory is self-contradictory:

Define: set of all sets that do not contain themselves

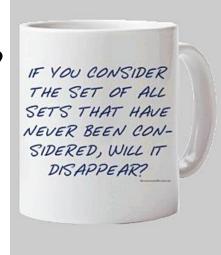
$$S = \{ T \mid T \notin T \}$$

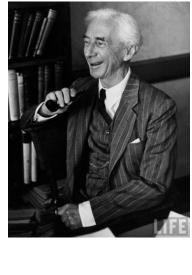
Q: does S contain itself as an element?

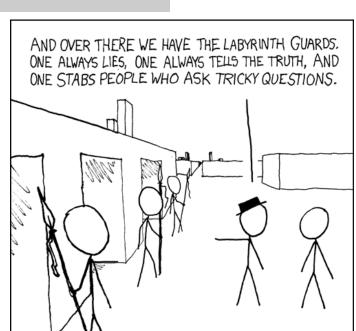
$$S \notin S \Leftrightarrow S \in S$$
 contradiction!



- "A barber who shaves exactly those who do not shave themselves."
- "This sentence is false."
- "I am lying."
- "Is the answer to this question 'no'?"
- "The smallest positive integer not describable in twenty words or less."









Star Trek, 1967, "I, Mudd" episode Captain James Kirk and Harry Mudd use a logical paradox to cause hostile android "Norman" to crash





AUTHOR KATHARINE GATES RECENTLY ATTEMPTED TO MAKE A CHART OF ALL SEXUAL FETISHES.

LITTLE DID SHE KNOW THAT RUSSELL AND WHITEHEAD HAD ALREADY FAILED AT THIS SAME TASK.



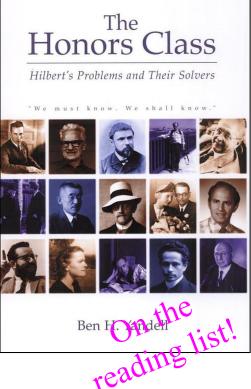


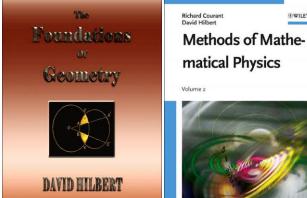
Historical Perspectives

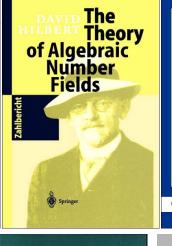
David Hilbert (1862-1943)

- One of the most influential mathematicians
- Developed invariant theory, Hilbert spaces
- Axiomatized geometry, "Hilbert's axioms"
- Co-founded proof theory, mathematical logic, meta-mathematics, & formalist school
- Created famous list of 23 open problems that greatly impacted mathematics research
- Defended Cantor's transfinite numbers
- Contributed to relativity theory & physics
- Hilbert's students included Courant, Hecke, Lasker, Weyl, Ackermann, and Zarmelo
- Influenced Russell, Gödel, Church, & Turing John von Neumann was Hilbert's assistant!

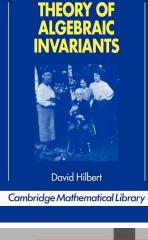


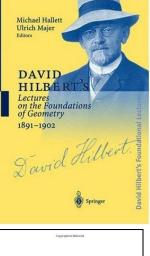


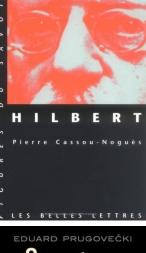


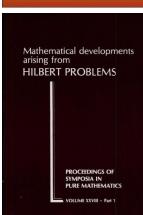


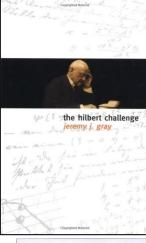
WILEY-VCH

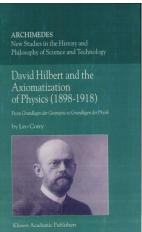


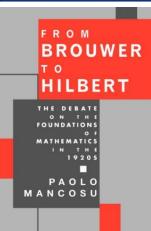


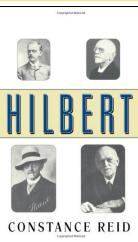


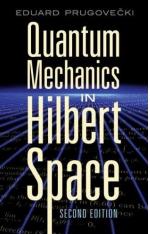


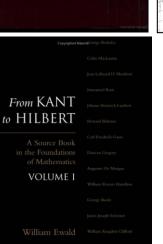


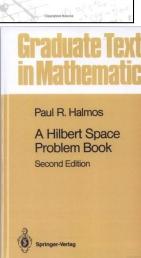


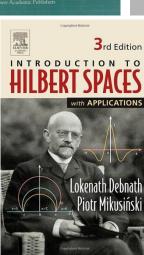


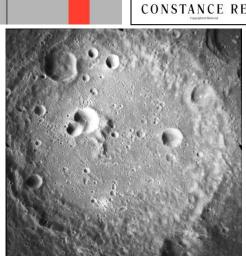


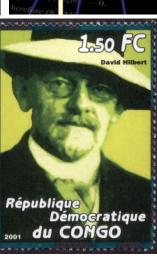












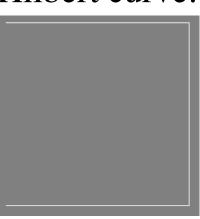
Hilbert's Impact

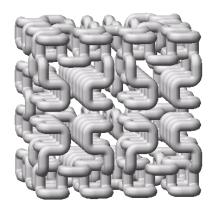
- Hilbert's axioms
- Hilbert class field
- Hilbert C*-module
- Hilbert cube
- Hilbert symbol
- Hilbert function
- Hilbert inequality
- Hilbert matrix
- Hilbert metric
- IIIhant numba
- Hilbert number
- Hilbert polynomial
- Hilbert's problems
- Hilbert's program
- Hilbert–Poincaré series
- Hilbert space

- Hilbert transform
- Hilbert's Arithmetic of Ends
- Hilbert's constants
- Hilbert's irreducibility theorem
- Hilbert's NullstellensatzHilbert's hotel paradox
- Hilbert's theorem
- Hilbert's syzygy theorem
- Hilbert-style deduction system
- Hilbert-Pólya conjecture
- Hilbert–Schmidt operator
- Hilbert–Smith conjecture
- Hilbert–Speiser theorem
- Einstein-Hilbert action
 - Hilbert curve



Hilbert curve:





Hilbert's Problems

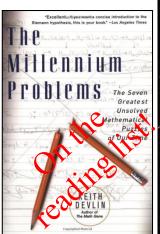
International Congress of Mathematics, Paris, 1900

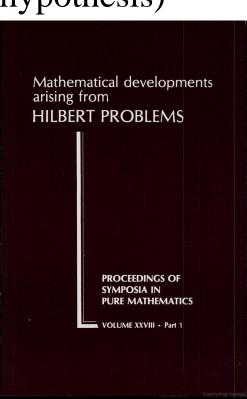
- David Hilbert proposed 23 open problems
- Most successful open problems compilation ever
- Set the direction for 20th century mathematics
- Hilbert's problems received much attention to date
- Several have been resolved (e.g., Continuum hypothesis)
- Others still open (e.g., Riemann hypothesis)
- Catalyzed other open problems lists:
 - Clay Institute's Millennium Prize problems
 - DARPA Mathematical Challenges, 2009





CLAY MATHEMATICS INSTITUTE

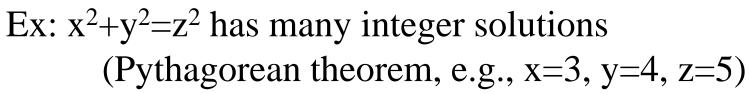


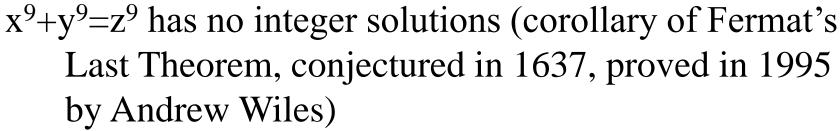




Hilbert's Problems

Problem 10: Find an algorithm that determines whether a given Diophantine (i.e., multi-variable polynomial) equation has any integer solutions.

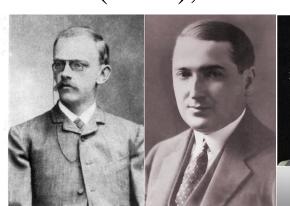




Many attempts at solution & partial results: Emil Post (1944),

Martin Davis (1949), Julia Robinson (1950), Hilary Putnam (1959)













Hilbert's Tenth Problem

Theorem [Matiyasevich, 1970]: Every Turing-recognizable set is Diophantine (i.e., the solutions of some polynomial)



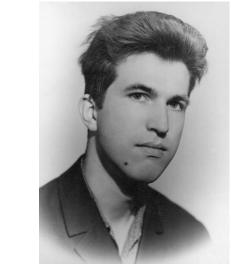
Ex: the set of primes coincides exactly with the positive values of this 26-variable polynomial:

```
(k+2)(1-[wz+h+j-q]^2-[(gk+2g+k+1)(h+j)+h-z]^2\\-[16(k+1)^3(k+2)(n+1)^2+1-f^2]^2-[2n+p+q+z-e]^2\\-[e^3(e+2)(a+1)^2+1-o^2]^2-[(a^2-1)y^2+1-x^2]^2\\-[16r^2y^4(a^2-1)+1-u^2]^2-[n+l+v-y]^2-[(a^2-1)l^2+1-m^2]^2\\-[ai+k+1-l-i]^2-[((a+u^2(u^2-a))^2-1)(n+4dy)^2+1\\-(x+cu)^2]^2-[p+l(a-n-1)+b(2an+2a-n^2-2n-2)-m]^2\\-[q+y(a-p-1)+s(2ap+2a-p^2-2p-2)-x]^2\\-[z+pl(a-p)+t(2ap-p^2-1)-pm]^2)
```

as a, b, c, ..., z range over the nonnegative integers!

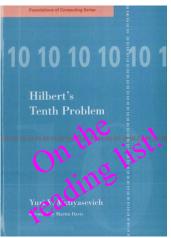
Hilbert's Tenth Problem

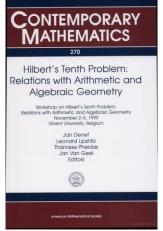
Corollary [Matiyasevich, 1970]: There is a fixed "universal" polynomial P such that for any Turing-enumerable set S there exists an integer n_0 such that:

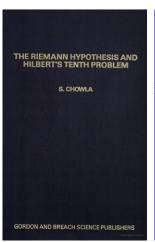


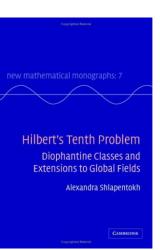
 $S = \{w \mid \exists x_1, x_2, ..., x_k \ni P(n_0, w, x_1, x_2, ..., x_k) = 0 \}$ i.e., there is a fixed polynomial that can "output" any computable set, depending on one parameter.

This is an analogue of a universal Turing machine!









CLAY MATHEMATICS INSTITUTE

March 15-16, 2007

One Bow Street, Cambridge, Massachusetts

Conference on Hilbert's Tenth Problem

Thursday, March 15

9:00 Coffee

9:15 - 9:25 Constance Reid, Genesis of the Hilbert Problems

9:25 - 10:00 George Csicsery, Film clip on life and work of Julia Robinson, discussion

10:15 - 11:15 Bjorn Poonen, Why number theory is hard

11:30 - 12:30 Yuri Matiyasevich, My collaboration with Julia Robinson

Break for lunch

2:30-3:30 Martin Davis, My collaboration with Hilary Putnam

3:45-4:45 Maxim Vsemirnov, TBA

7:30 Museum of Science • Film Screening

Scenes from Julia Robinson and Hilbert's Tenth Problem, a documentary by George Csicsery, will be screened in Cahner's Theater (Blue Wing, Level 2, Museum of Science), and followed by a panel discussion with filmmaker George Csicsery, mathematician Yuri Matiyasevich, and biographer Constance Reid.

This event is free and open to the public.

Friday, March 16

8:30 Coffe

9:00-10:00

3:15-4:15

Сопее

Yuri Matiyasevich, Hilbert's Tenth Problem. What was done and what is to be done

10:15–11:15 Bjorn Poonen, Thoughts about the analogue for

rational number

11:30–12:30 Alexandra Shlapentokh, Diophantine generation, horizontal

and vertical problems, and the weak vertical method

Break for lunch

2:00–3:00 Yuri Matiyasevich, Computation paradigms in the light of

Hilbert's tenth problem

Gunther Cornelisson, Hard number-theoretical problems

and elliptic curve

4:30–5:30 Kirsten Eisentrager, Hilbert's Tenth Problem for algebraic

function fiel







Hilbert's 10th Problem (1900): is there an algorithm for deciding whether a polynomial equation with integer coefficients has an integer solution?

$$x^2 - (a^2 - 1)y^2 = 1$$

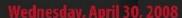
Photo credits (top to bottom): Julia Robinson, courtesy of Constance Reid; Yuri Matiyasevich, photo by George Csicsery; David Hilbert, courtesy AK Peters, Ltd.

MUSEUM OF SCIENCE • SCIENCE PARK, BOSTON, MA 02114 • T. 617 723 2500

Co-Sponsored by the Mathematical Sciences Research Institute and the UCBerkeley Department of Mathematics



A film by George Csicsery



7pm to 9pi

Room 2050 (Chan Shun Auditorium) in the Valley Life Sciences Building at UC Berkeley

Post-screening panel discussion with Constance Reid (sister and biographer of Julia Robinson), filmmaker George Csicsery, and mathematicians Martin Davis, Dana Scott and Bjorn Poonen. Moderated by Alan Weinstein, UCB Math Dept. Chair.

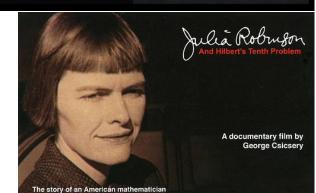
The story of an American mathematician and her passionate pursuit and triumph over an unsolved problem.

Hilbert's 10th Problem (1900): Is there an algorithm for deciding whether a polynomial equation with integer coefficients has an integer solution?

FREE ADMISSION







and her passionate pursuit of Hilbert's tenth problem

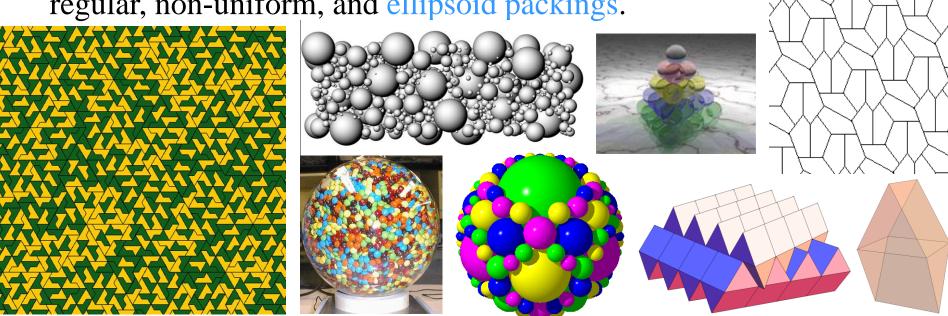
Hilbert's Problems

Problem 18: Is there a non-regular, space-filling polyhedron? What is the densest sphere packing?

Status: Anisohedral tilings were found in 3D by Reinhardt (1928), and for 2D by Heesch (1935).

Sphere packing in 3D (Kepler's problem, 1611) was solved by Toth (1953) and Hale (1998). Regular sphere packing in 24 dimensions was solved by Cohn and Kumar (2004), where the "kissing number" is 196,560.

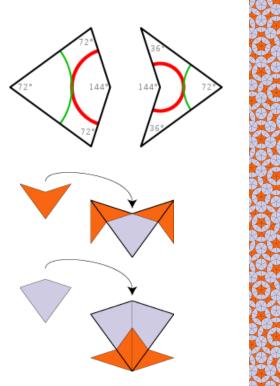
Many related open problems remain, including non-regular, non-uniform, and ellipsoid packings.

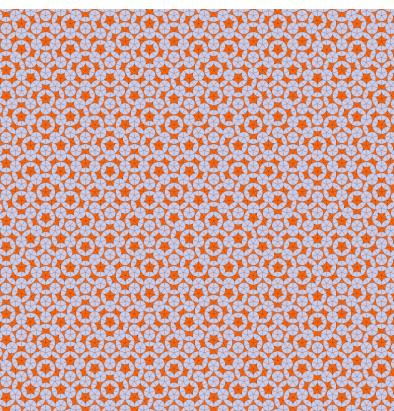


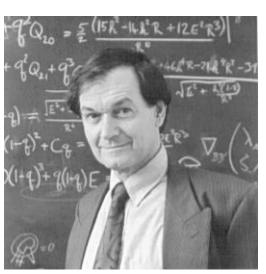
Goal: tile the entire plane without overlaps, non-periodically

- Non-periodic tiling is not equal to a translation of itself
- Aperiodic tile set admits only non-periodic tilings

"Kites and Darts" 2-tile aperiodic set, Roger Penrose, 1974



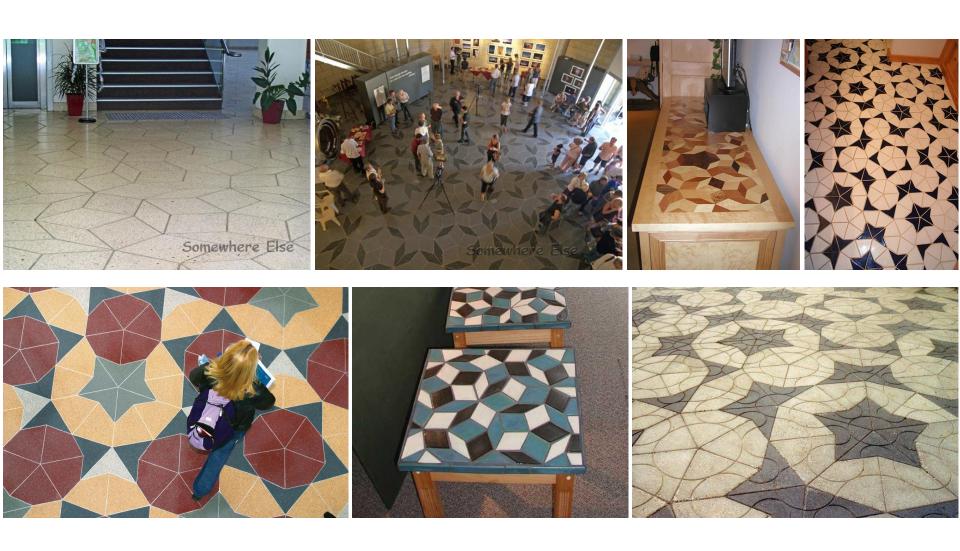




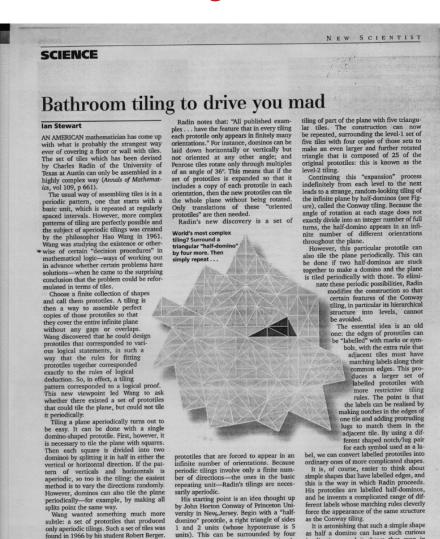
Open question:

∃ a single-tile 2D aperiodic tiling?

Penrose tilings in architecture and design:



"Pinwheel tiling", John Conway and Charles Radin, 1992



copies of itself in order to create a triangle

of the same shape, but larger and rotated

through an angle (see Figure). The process

can be thought of as defining a "level-l"

The best known of such sets are the Penrose

tilings, introduced by Roger Penrose of the

University of Oxford in 1977; these produce

tilings with fivefold "almost" symmetries.

implications, and it shows that even in

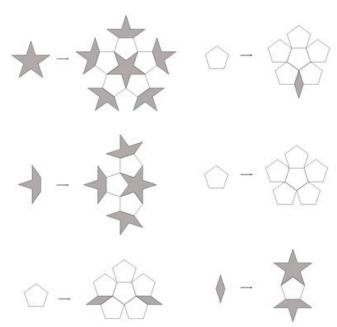
today's complex world mathematics can

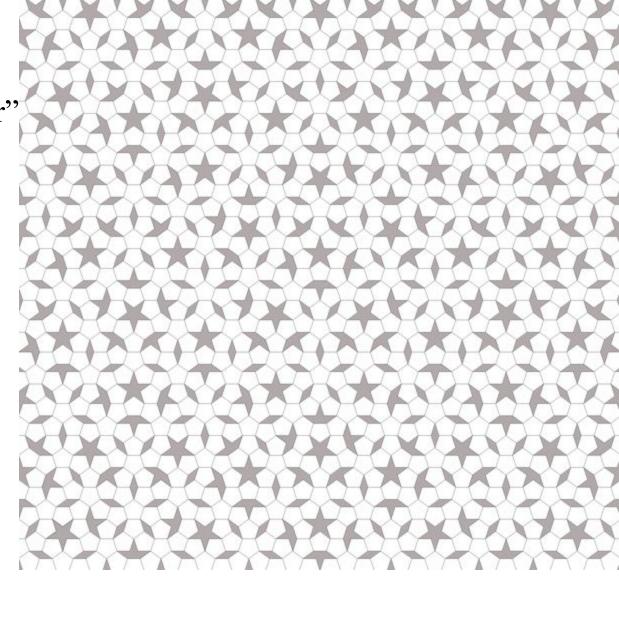
still advance by looking at a simple idea in

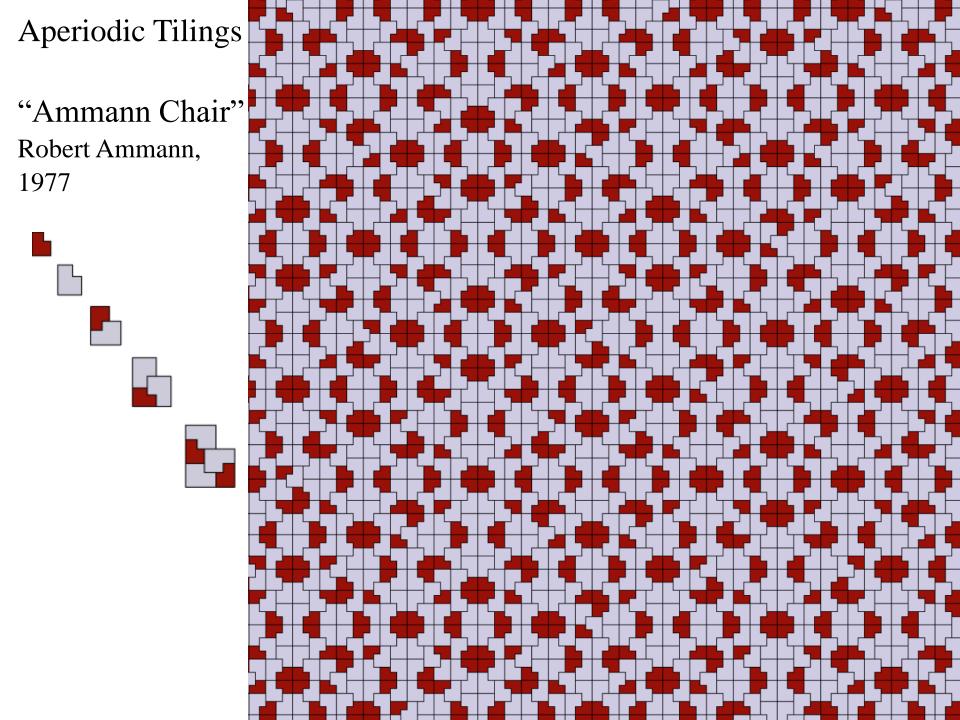
24 September 1994



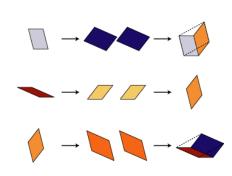
"Pentagon, Boat, and Star" Roger Penrose, 1974

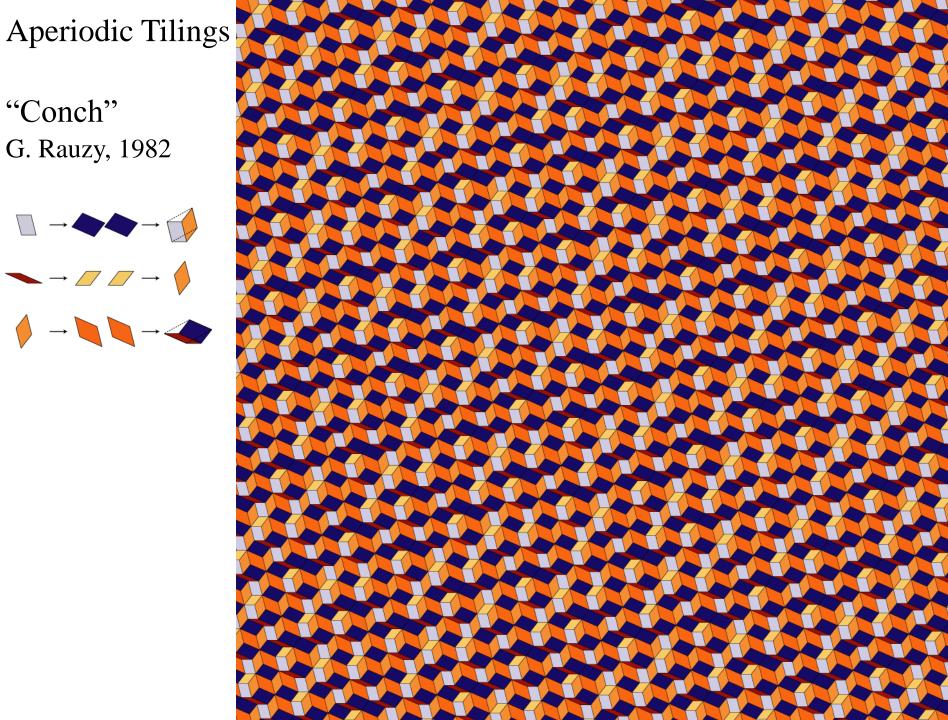




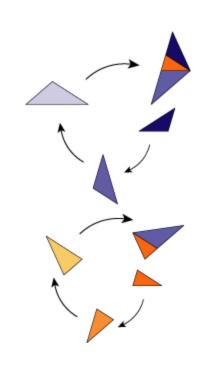


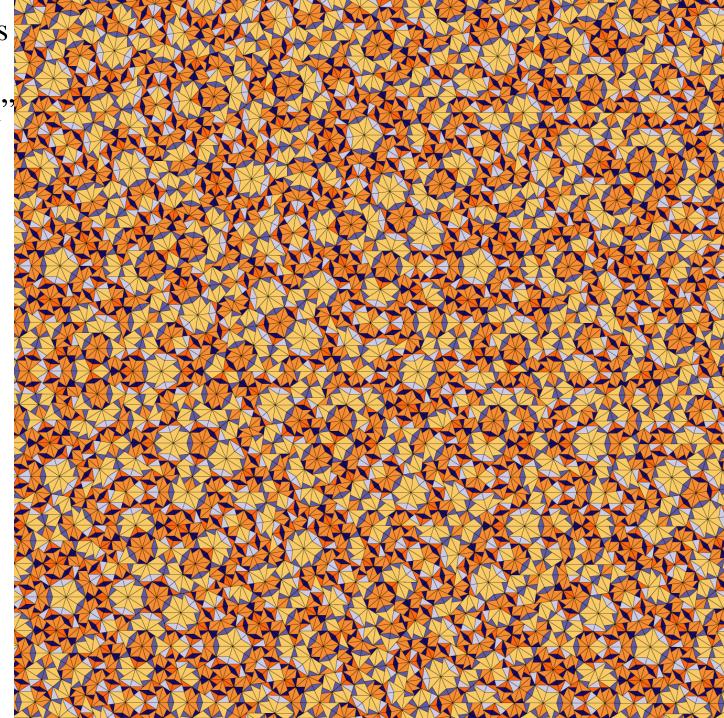
"Conch" G. Rauzy, 1982



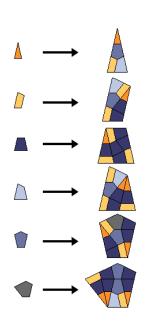


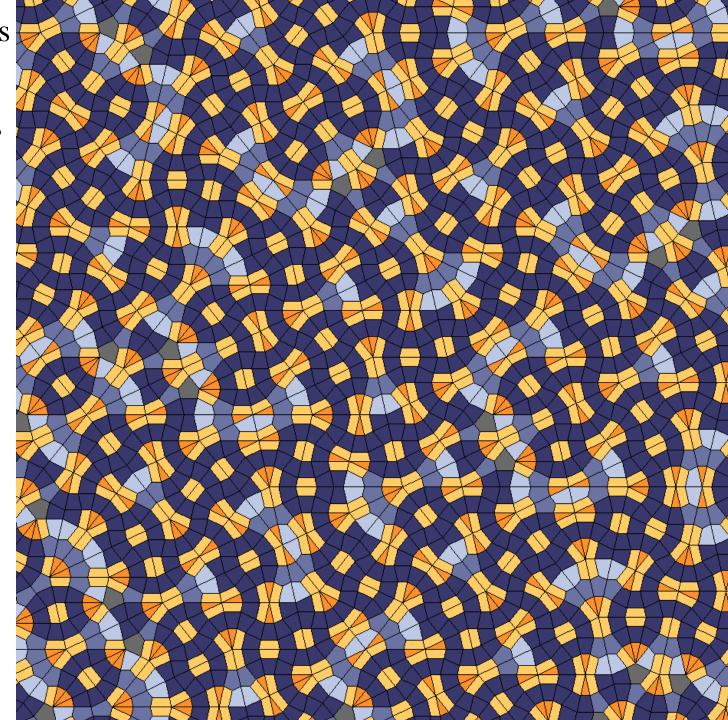
"Cubic Pinwheel" E. Harriss



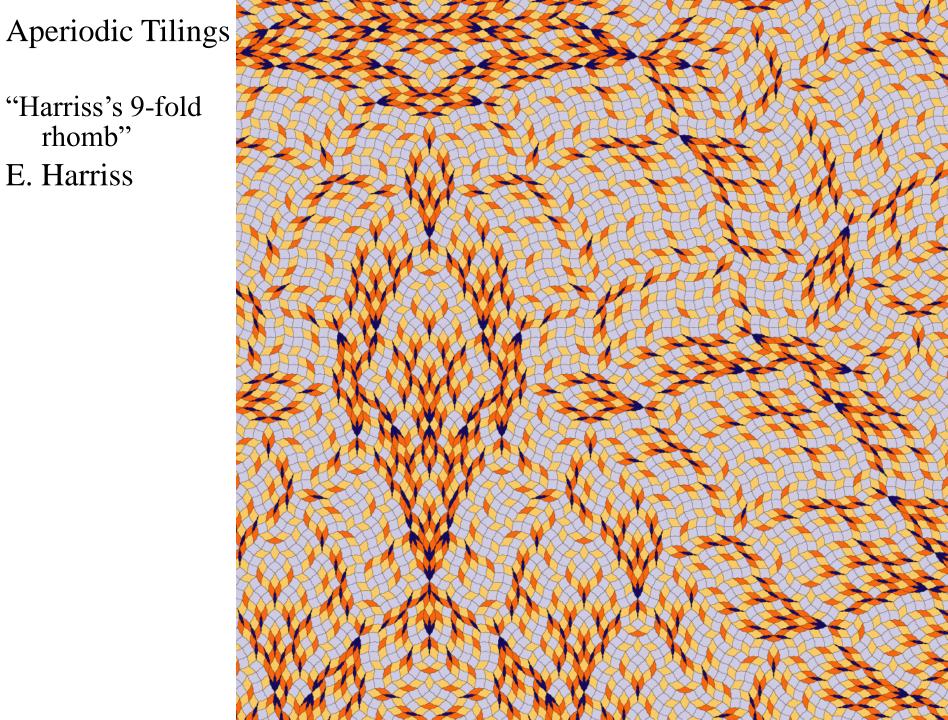


"Cyclotomic rhombs 7-fold" Ludwig Danzer and D. Frettlöh





"Harriss's 9-fold rhomb" E. Harriss



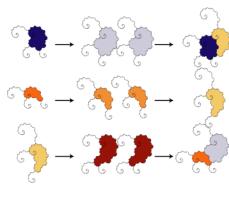
Aperiodic Tilings "Kenyon (1,2,1) Polygon" R. Kenyon

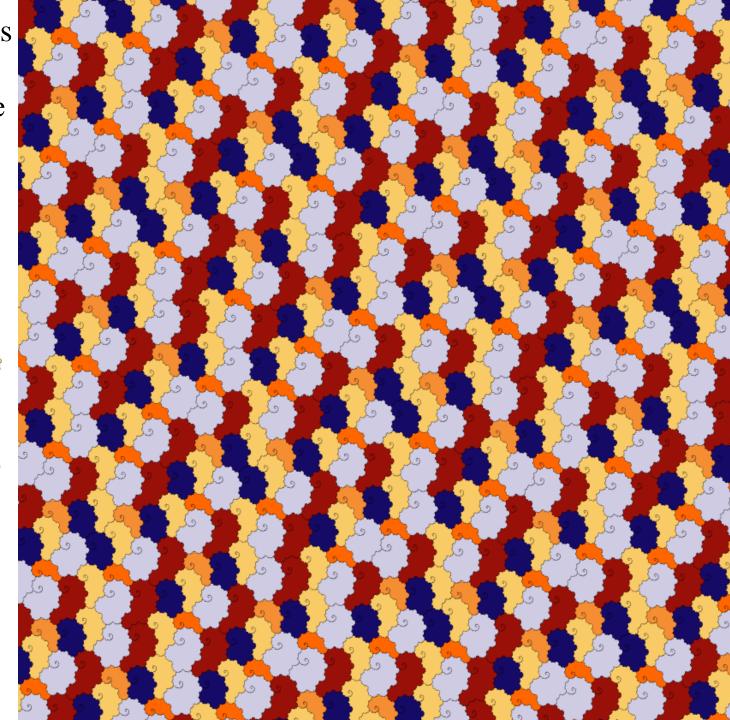
Aperiodic Tilings "Nautilus" P. Arnoux, M. Furukado, E. Harriss, and S. Ito

"Nautilus (volume hierarchic"

P. Arnoux,M. Furukado,E. Harriss,

and S. Ito





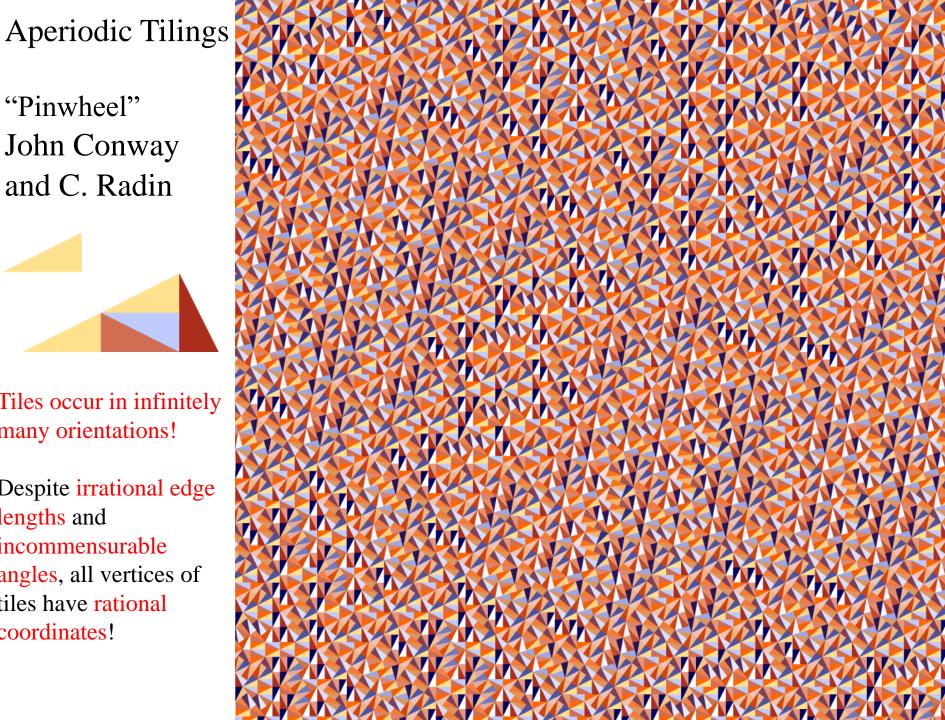
"Pinwheel" John Conway

and C. Radin



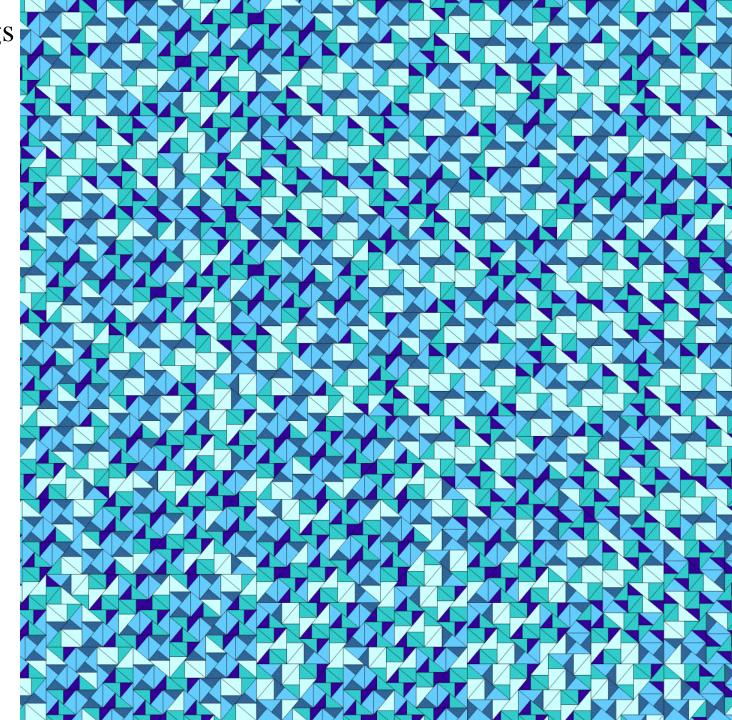
Tiles occur in infinitely many orientations!

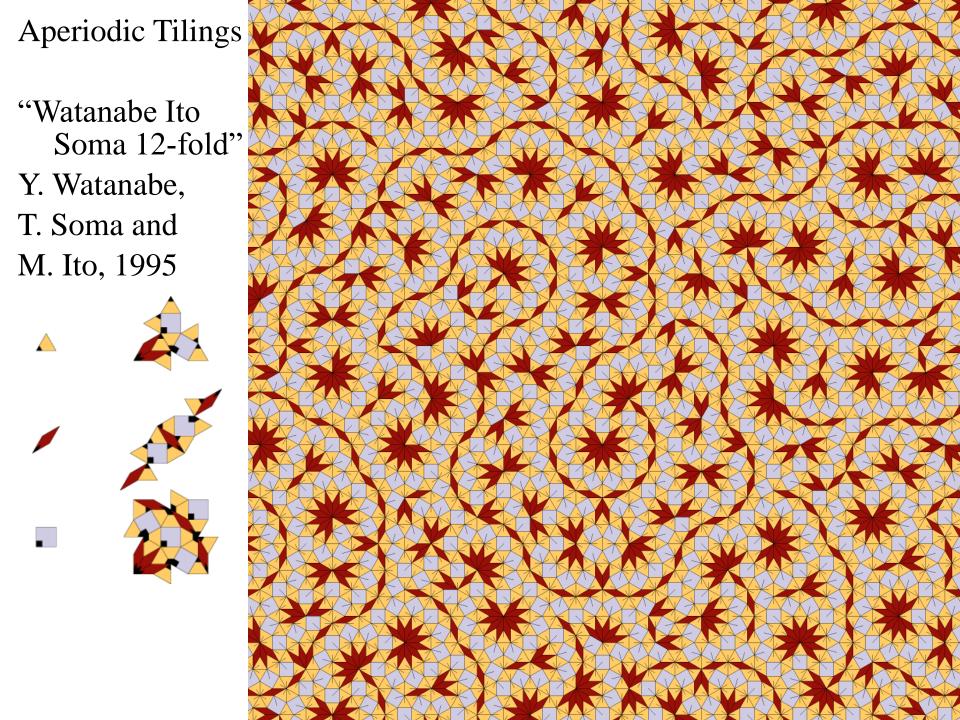
Despite irrational edge lengths and incommensurable angles, all vertices of tiles have rational coordinates!



"Pythagoras-3-1"
J. Pieniak

- $A \longrightarrow A$
- **⊿** → ∠
- \triangle \longrightarrow \triangle
- $\Delta \longrightarrow \Delta$
- \wedge

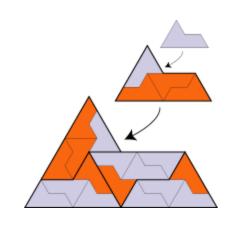


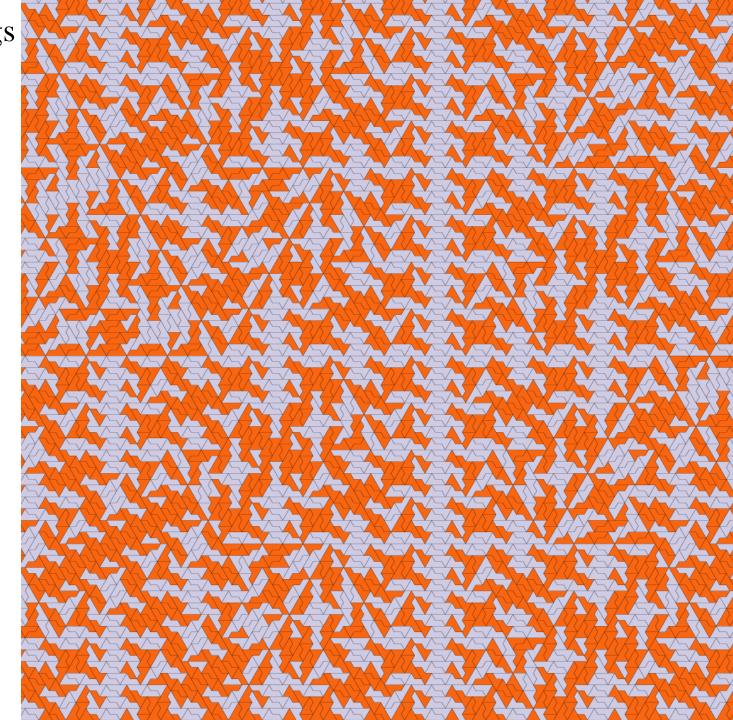


Aperiodic Tilings "Viper"

Aperiodic Tilings
"Sphinx"

J.-Y. Lee, and R. V. Moody

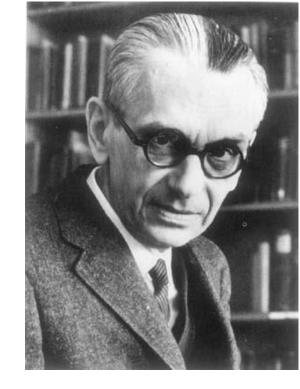


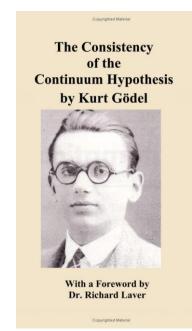


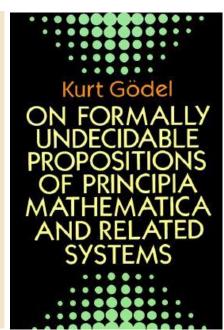
Historical Perspectives

Kurt Gödel (1906-1978)

- Logician, mathematician, and philosopher
- Proved completeness of predicate logic and Gödel's incompleteness theorem
- Proved consistency of axiom of choice and the continuum hypothesis
- Invented "Gödel numbering" and "Gödel fuzzy logic"
- Developed "Gödel metric" and paradoxical relativity solutions: "Gödel spacetime / universe"
- Made enormous impact on logic, mathematics, and science

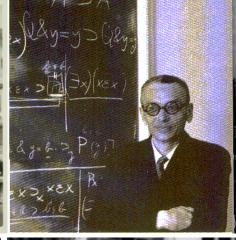




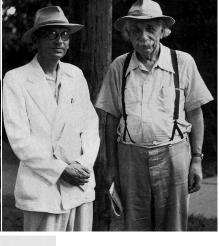




















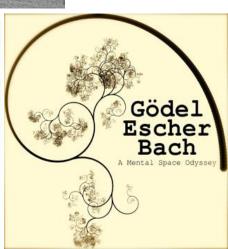
Kurt Gödel

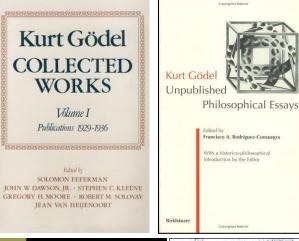


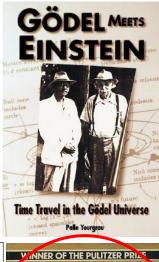


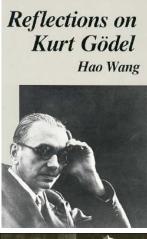


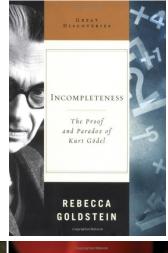


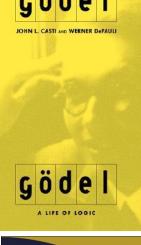


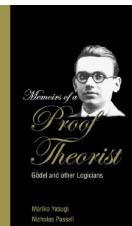


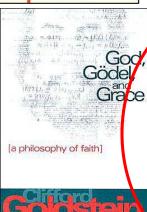


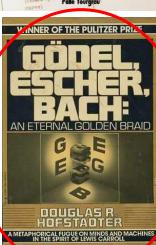


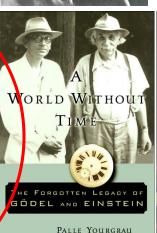


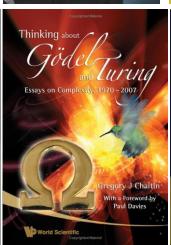


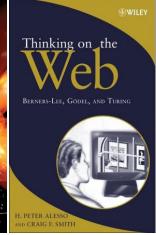


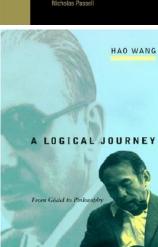




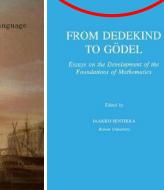








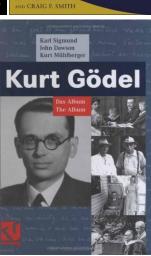


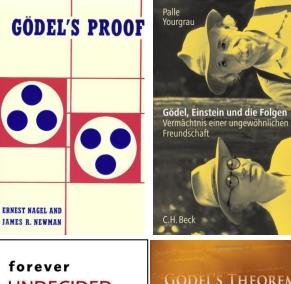


kluwer the language of science

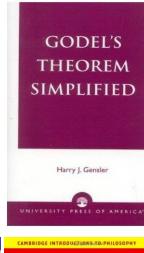




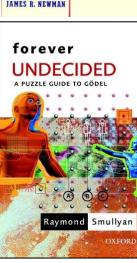






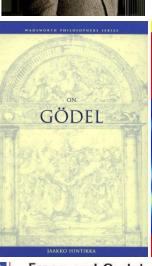


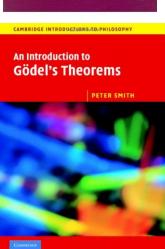


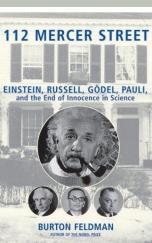




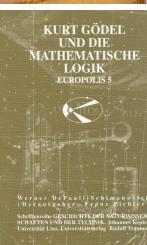


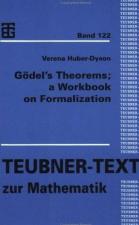


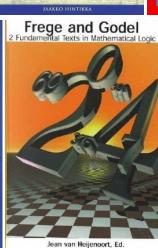


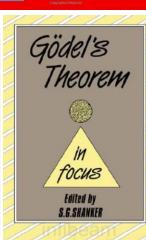










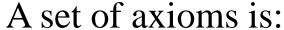




Gödel's Incompleteness Theorem

Frege & Russell:

- Mechanically verifying proofs
- Automatic theorem proving



- Sound: iff only true statements can be proved
- Complete: iff any statement or its negation can be proved
- Consistent: iff no statement and its negation can be proved

Hilbert's program: find an axiom set for all of mathematics i.e., find a axiom set that is consistent and complete

Gödel: any consistent axiomatic system is incomplete! (as long as it subsume elementary arithmetic)

i.e., any consistent axiomatic system must contain true but unprovable statements

Mathematical surprise: truth and provability are not the same!







Gödel's Incompleteness Theorem

That some axiomatic systems are incomplete is not surprising, since an important axiom may be missing (e.g., Euclidean geometry without the parallel postulate)



However, that every consistent axiomatic system must be incomplete was an unexpected shock to mathematics! This undermined not only a particular system (e.g., logic), but axiomatic reasoning and human thinking itself!

Truth = Provability

Justice ≠ Legality

Gödel's Incompleteness Theorem

Gödel: consistency or completeness - pick one!

Which is more important?

Incomplete: not all true statements can be proved. But if useful theorems arise, the system is still useful.



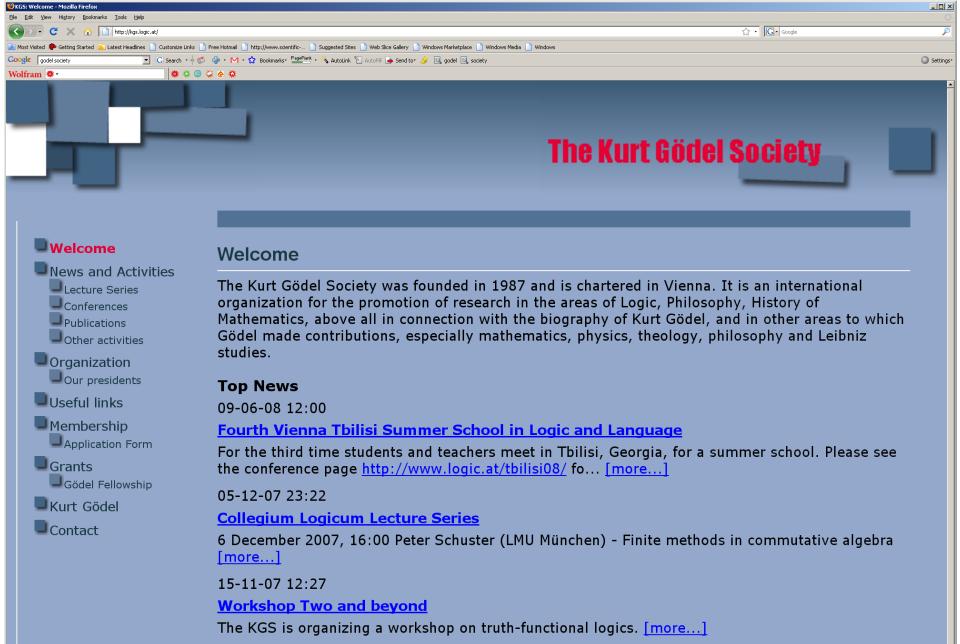
Inconsistent: some false statement can be proved.

This can be catastrophic to the theory:

E.g., supposed in an axiomatic system we proved that "1=2". Then we can use this to prove that, e.g., all things are equal!

Consider the set: {Trump, Pope} | {Trump, Pope} | = 2 ⇒ | {Trump, Pope} | = 1 (since 1=2) ⇒ Trump = Pope QED

⇒ All things become true: system is "complete" but useless!

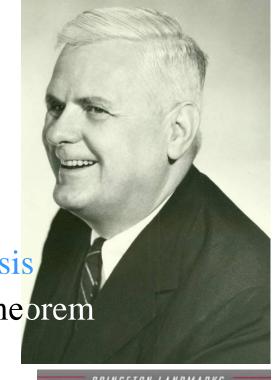




Historical Perspectives

Alonzo Church (1903-1995)

- Founder of theoretical computer science
- Made major contributions to logic
- Invented Lambda-calculus, Church-Turing Thesis
- Originated Church-Frege Ontology, Church's theorem Church encoding, Church-Kleene ordinal,
- Inspired LISP and functional programming
- Was Turing's Ph.D. advisor! Other students: Davis, Kleene, Rabin, Rogers, Scott, Smullyan
- Founded / edited Journal of Symbolic Logic
- Taught at UCLA until 1990; published "A Theory of the Meaning of Names" in 1995, at age 92!

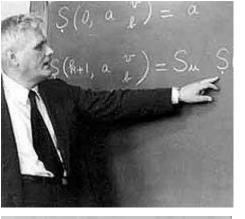


Alonzo Church

Introduction to

Mathematical

Logic





LAST NIGHT I DRIFTED OFF

WHILE READING A LISP BOOK.



Adam Olszewski Jan Woleński Robert Janusz (Eds.)

Church's Thesis After 70 Years

ontos mathematical logic





THE CALCULI OF LAMBDA-CONVERSION

ALONZO CHURCH

AT ONCE, JUST LIKE THEY SAID, I FELT A
GREAT ENLIGHTENMENT. I SAN THE NAKED
STRUCTURE OF LISP CODE UNFOLD BEFORE ME.



THE PATTERNS AND METAPATTERNS DANCED.

SYNTAX FADED, AND I SWAM IN THE PURITY OF

QUANTIFIED CONCEPTION. OF IDEAS MANIFEST.

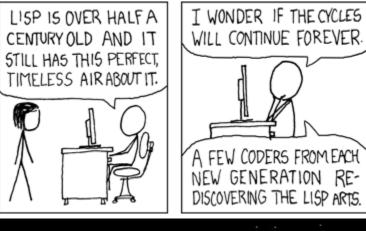
TRULY, THIS WAS
THE LANGUAGE
FROM WHICH THE
GODS WROUGHT
THE UNIVERSE.



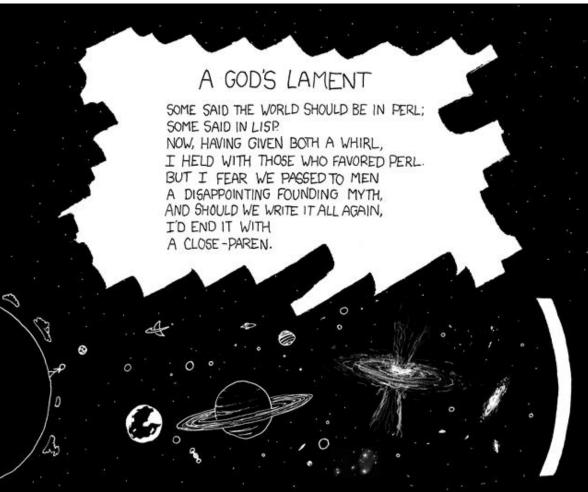


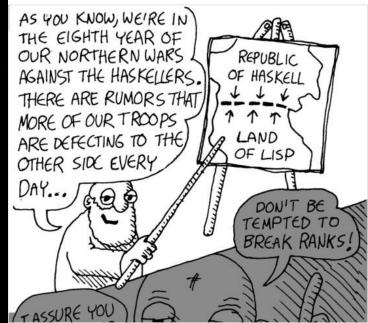
SUDDENLY, I WAS BATHED IN A SUFFUSION OF BLUE.

A HUH?









Historical Perspectives

Alan Turing (1912-1954)

- Mathematician, logician, cryptanalyst, and founder of computer science
- First to formally define computation / algorithm
- Invented the Turing machine model
 - theoretical basis of all modern computers
- Investigated computational "universality"
- Introduced "definable" real numbers
- Proved undecidability of halting problem
- Originated oracles and the "Turing test"
- Pioneered artificial intelligence
- Anticipated neural networks
- Designed the Manchester Mark 1 (1948)
- Helped break the German Enigma cypher
- Turing Award was created in his honor



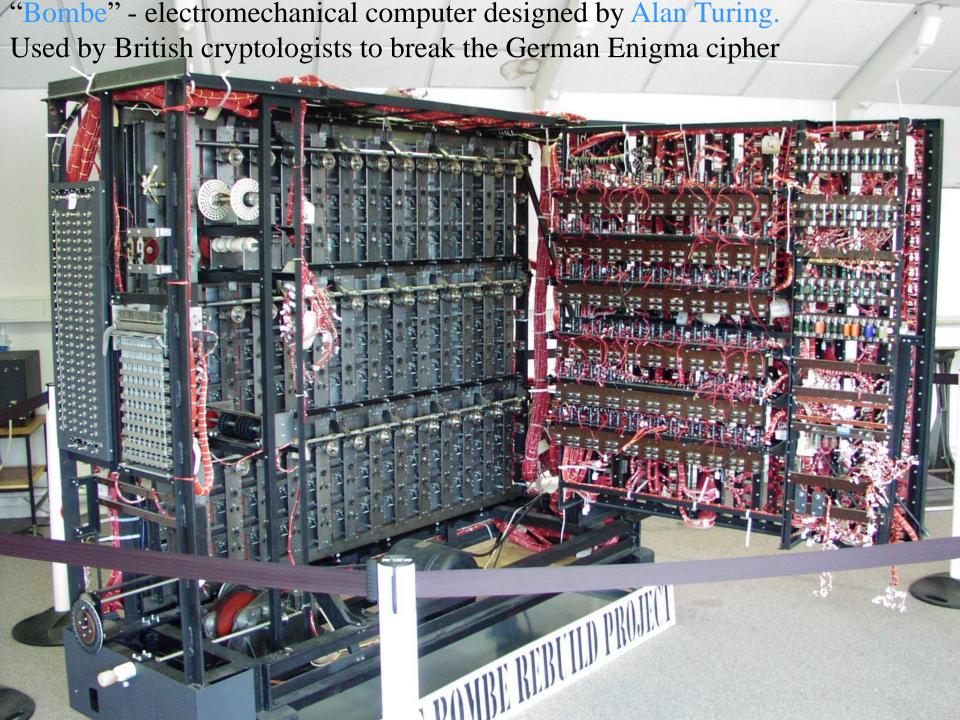








Bletchley Park ("Station X"), Bletchley, Buckinghamshire, England England's code-breaking and cryptanalysis center during WWII

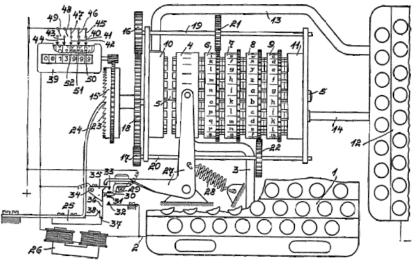




1918 First Enigma Patent

The official history of the Enigma starts in 1918, when the German **Arthur Scherbius** filed his first patent for the Enigma coding machine. It is listed as patent number 416219 in the archives of the German <code>Reichs-patentamt</code> (patent office). Please note the time at which the Enigma was invented: **1918**, just after the First World War, more then 20 years before WWI!! The image below clearly shows the coding wheels (rotors) in the centre part of the drawing. Below it is the keyboard and to the right is the lamp panel. At the top left is a counter, used to count the number of letters entered on the keyboard. This counter can still be found on certain Enigma models.

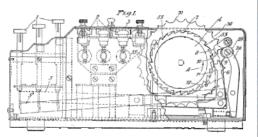
Arthur Scherbius' company **Securitas** was based in Berlin (Germany) and had an office in Amsterdam (The Netherlands). As he wanted to protect his invention outside Germany, he also registered his patent in the USA (1922), Great Britain (1923) and France (1923).

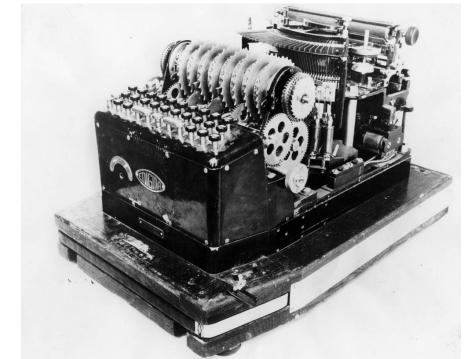


This image is taken from patent number 193,035 that was registered in Great Britain in 1923, long before WWII. It was also registered in a number of other countries, such as France and the USA.

During the 1920s the Enigma was available as a commercial device, available for use by companies and embassies for their confidential messages. Remember that in those days, most companies had to use morse code and radio links for long distance communication. The devices were advertised having over 800.000 possibilities.

In the following years, additional patents with improvements of the coding machine were applied. E.g. in GB Patent 267,482, dated 17 Jan 1927, the Umkehrwalze was added and a later patent of 14 Nov 1929 (GB 343,146) claims the addition of the Ringstellung, multiple notches, etc. One of the drawings of that patent shows a coding device, that we now know as The Enigma, in great detail.



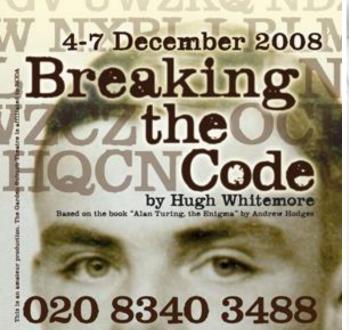


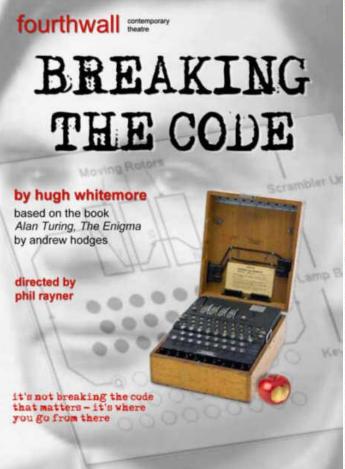


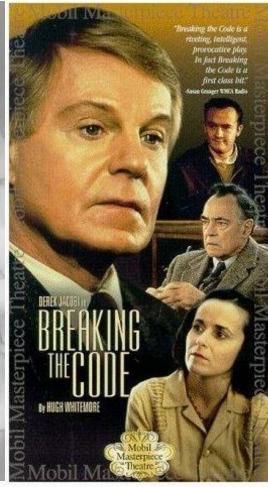


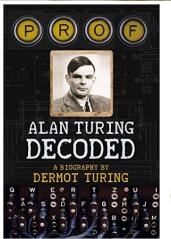
2 http://www.xat.nl/enigma-e/





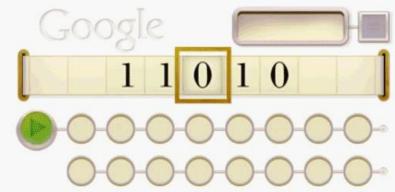












"BENEDICT CUMBERBATCH IS OUTSTANDING"



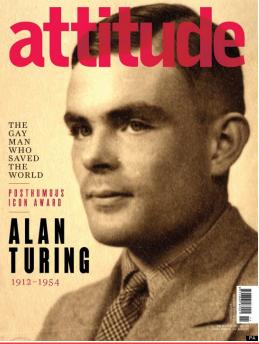
BASED ON THE INCREDIBLE TRUE STORY

BUX SEA PCINES NEXT NEXTURN PLANTON ENFRANCET, JUX SEA PCINES NUMBER (BISTON ENTONITÉ NUMBER PRODUC COMPERACE L'ELA NOISTREY DATIFIÉ POME ROP COMER "Incres dans anna signe "I dans du mez dan fambre en samt seudi diffé "Es mara lubon" "I alumbérs de villai subbers de villai soudises de villais de villai soudises de villais de vi

/ImitationGameUK

IN CINEMAS NOVEMBER 14



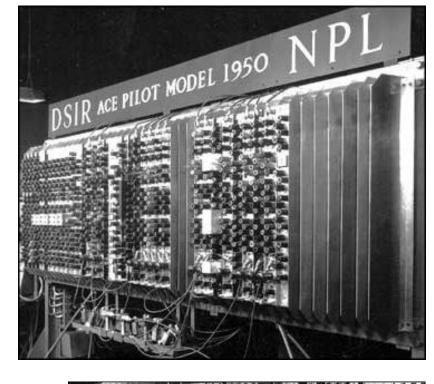


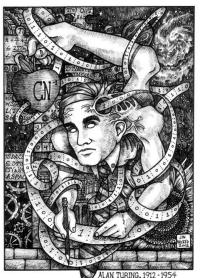


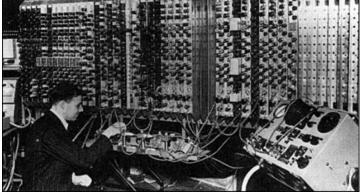


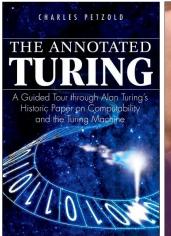
ROUTINE				1	Prog		mme	Sheet		2	(1	6)		18			1		1/4	p.		
	1 hour		1						æ	C	100	10	80	N	211	6	RO	00	u			
Tale of	The Residence of			1	,			KPK		e	O EE		1 4	F	4 1	1 8	PK	1:	KU!	V	V ELE	
1bren 4 (couche))						ke/										XQ4.			
	1	1,	15	=					N	0.654	N	т	772.00	11	1	:		0	10	1/6		
1 8 8	100	É	1	03	1		S. 3				1	w	100	É	×	,	10000	G		100		
		a	10				310			V	5	y	0	@	1	,	a	1000				
		A	13				- 113	10		A	:	y		A	3	6		A	2 3			
	136	1:	JK.	1						0	7	y	0.52	:	£	6	1	P			7	
	-	s	1	0		10	3 3	100		v	K		3	s	v	1	1	c	7		-	
	200	1			6	1	100	29		V	K	7	c	1	Y	1	1	N	25			
		U		1	10	1		4.3	200	V	K	1	2	U	m	H	1	A				
		1 2	5	2		1	1			V	K	1	:	1	н	K	de	0				
	15 10	D								٧	1	4	0	D	£	5	7	1				
1 1 6 1		R	1	3					1	1	1	4	1/2	R	U	K	7	R	B.E.			
		J	10						lia.	4	;	1	M	1	G	K	7	A	916			
		N							20	D	2	7	5	N	G	K	1	:	O.F		1	
		F	155		L		3			**	@	w	N	F	1	Į	Q	1	1			
		c					8	6		Ę	:	1	M	С	G	0	1	ī	80			
		K								3	2	7	I.	K	3	0	1	v	60			
1 1		T								**	ě,	w	c	Т	8	0	1	U	30	U		
		Z								*	1/2	w	A	z	6	2	T	1				
		L	m	A	1	:				Ę	:	L	9	L	6	c	T	A	47			
		w	M		1	1				X	N	1	T	w	M	177	62	0				
2	-	Н	全	2	W	0				E	:	7	61	н	E	1	a	100	-1			
	-	Y	£	F	1	P	11	11	7	4	•	W.	19	Y	N	C	Q	B	- 1			
		P	4	*	-	7	4	w	G	4E		14	-	P	0	A	1	7		14		
+ 13 4	9-015	Q			-	-	ne	11	ī	E	-	74	-	Q	~	2		A	1	-		
		0	R	E	~	A	-		-	X	12	n	P	0	G	n	7	/	140	1		
	444	В	0	-	-	2		10		17.				В	F.	*	1	0	18.		-	
Selectore	-	G	K	'	w	12.		v		6	_	1	1	G	٧	N	T	_				
felielative	4-	M	D	-	è	Z		42	5.0	A	1	1	1		~	5	1	5				
12	1	×	4	F.	'			A7.	350	A	M	1	7	M		F	1	1				
7-1-1		1	5	0	1	6		NE	"	9	14	1	7	×	£	2	1	1	1		F	
7-4	1 18	1.	1	R	1	£	-			1	A	4	K		£	4	/	/			112	

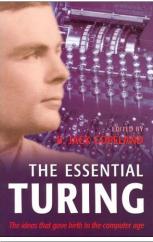
Program for ACE computer hand-written by Alan Turing

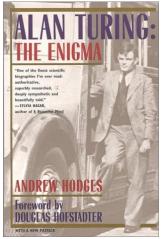


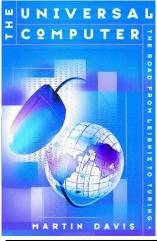


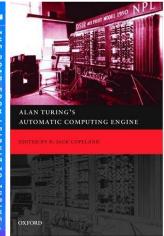


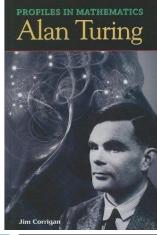


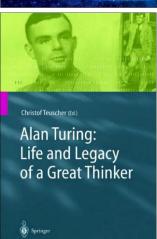




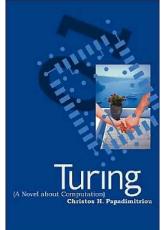


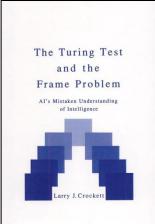


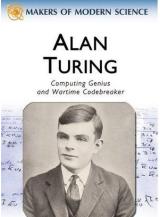




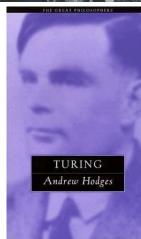


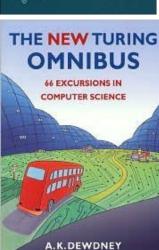


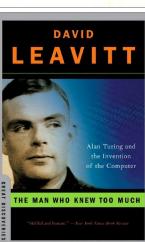




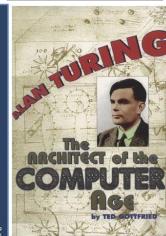
RAY SPANGENBURG AND DIANE KIT MOSER



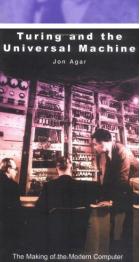


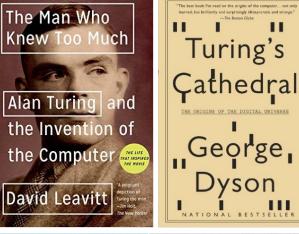


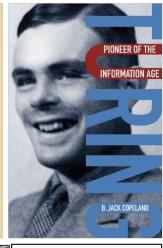


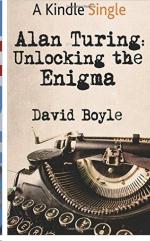


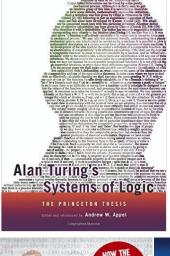


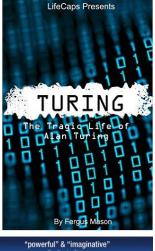




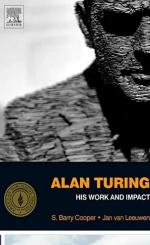


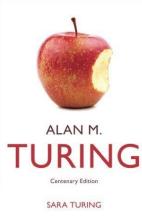


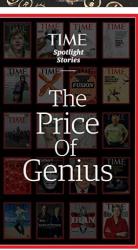




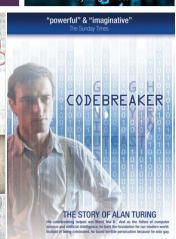


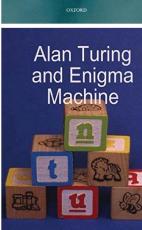




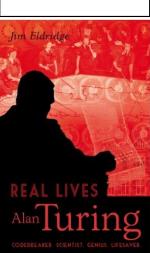


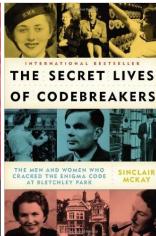


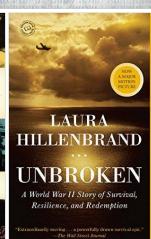


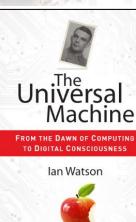


















ST. VINCENT & THE GRENADINES

010101010101010101010101 M PL CLEMON 9 LOAD 010101010101010101010101010101010101010 010101010101010101010101010101 10101010101010101010

1937: Alan Turing's theory of digital computing









12:02

iPad 令

NEWS REVIEW FEATURES

TURING ARCHIVE













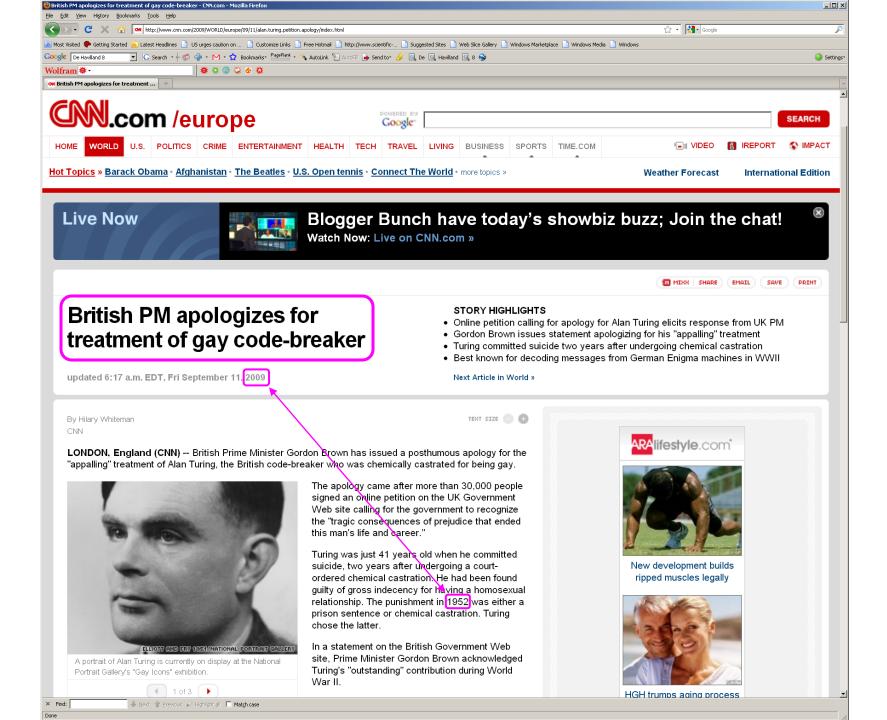






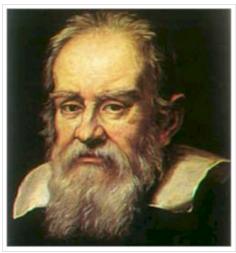


Look around you



other famous belated apology:





In 1610, Century Italian astronomer/mathematician /inventor Galileo Galilei used a a telescope he built to observe the solar system, and deduced that the planets orbit the sun, not the earth.

This contradicted Church teachings, and some of the clergy accused Galileo of heresy. One friar went to the Inquisition, the Church court that investigated charges of heresy, and formally accused Galileo. (In 1600, a man named Giordano Bruno was

convicted of being a heretic for believing that the earth moved around the Sun, and that there were many planets throughout the universe where life existed. Bruno was burnt to death.)

Galileo moved on to other projects. He started writing about ocean tides, but instead of writing a scientific paper, he found it much more interesting to have an imaginary conversation among three fictional characters. One character, who would support Galileo's side of the argument, was brilliant. Another character would be open to either side of the argument. The final character, named Simplicio, was dogmatic and foolish, representing all of Galileo's enemies who ignored any evidence that Galileo was right. Soon, Galileo wrote up a sin dialogue called "Dialogue on the Two Great Systems of the W

🖊 Next 👚 Previous 👂 Highlight all 🔲 Match case 🔀 Phrase not found

This book talked about the Copernican system.

[For The First Time (or the last time): ... "Dialogue" was an immediate hit with the public, but not, of course, with the Church. The pope suspected that he was the model for Simplicio. He ordered the book banned, and also ordered Galileo to appear before the Inquisition in Rome for the crime of teaching the Copernican theory after being ordered not to do so.

🔼 Most Visited 🗫 Getting Started 🔝 Latest Headlines 🧻 US urges caution on ... 📄 Customize Links 📄 Free Hotmail 🦳 http://www.scientific-..

X 🕎 🕒 http://4thefirsttime.blogspot.com/2007/09/1992-catholic-church-apologizes-to.h 🔊 🗘 🔻 Google

Google Catholic church apology 🖓 🕝 Search 🔹 🚳 🔓 - 🔀 😭 Bookmarks- 🎥 🚾 - 🐧 AutoLink 🖺 AutoHill 🍑 Send to- » 🔘 Settings-

Galileo was 68 years old and sick. Threatened with torture, he publicly confessed that he had been wrong to have said that the Earth moves around the Sun. Legend then has it that after his confession, Galileo quietly whispered "And yet, it moves."

Unlike many less famous prisoners, Galileo was allowed to live under house arrest. Until his death in 1642, he continued to investigate science, and even published a book on force and motion after he had become blind.

The Church eventually lifted the ban on Galileo's Dialogue in 1822, when it was common knowledge that the Earth was not the center of the Universe. Still later, there were statements by the Vatican Council in the early 1960's and in 1979 that implied that Galileo was pardoned, and that he had suffered at the hands of the Church. Finally, in 1992, three years after Galileo Galilei's namesake spacecraft had been launched on its way to Jupiter, the Vatican formally and publicly

Theorem: A late apology is better than no apology.

Corollary: But sooner is better!

File Edit View History Bookmarks Tools Help

Wolfram ♣ •

Done

Uext ↑ Previous P Highlight all Match case



Turing's Seminal Paper

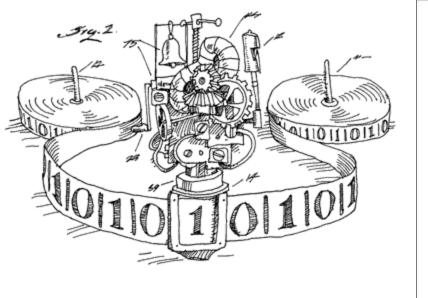
"On Computable Numbers, with an Application to the Entscheidungsproblem", Proceedings of the London Mathematical Society, 1937, pp. 230-265.

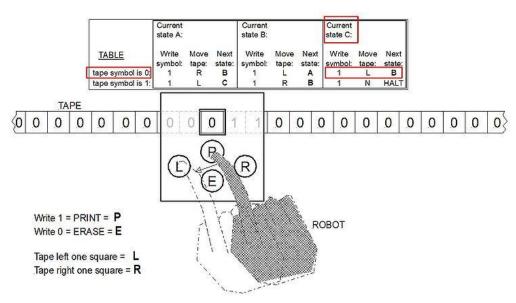


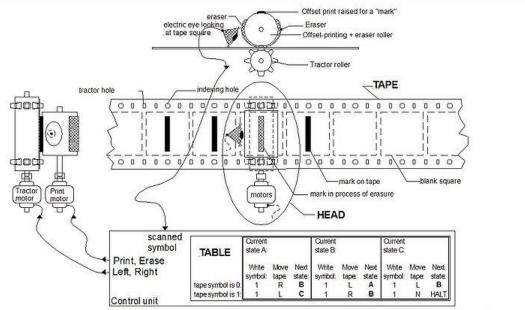


- First ever definition of "algorithm"
- Invented "Turing machines"
- Introduced "computational universality" i.e., "programmable"!
- Proved the undecidability of halting problem
- Explicates the Church-Turing Thesis





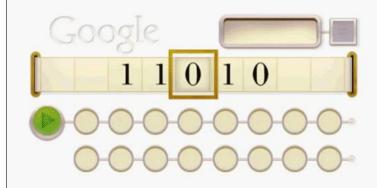




A fanciful mechanical Turing machine's TAPE and HEAD. The TABLE instructions might be on another "read only" tape, or perhaps on punch-cards. Usually a "finite state machine" is the model for the TABLE.

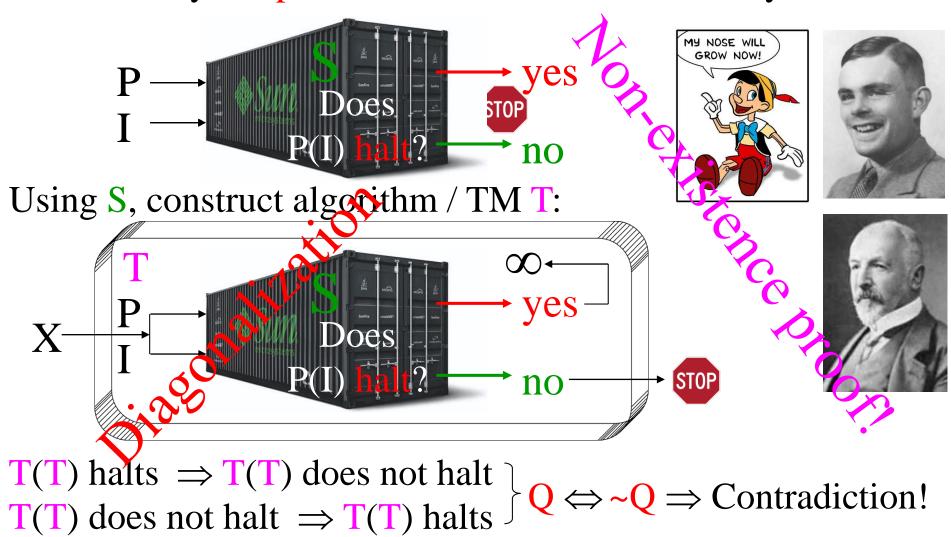
Turing's insight:

simple local actions
can lead to arbitrarily
complex computations!



Theorem [Turing]: the halting problem (H) is not computable. Proof: Assume \exists algorithm S that solves the halting problem

H, that always stops with the correct answer for any P & I.



⇒ S cannot exist! (at least as an algorithm / program / TM)

Computational Universality

Theorem: Many other systems are equivalent to Turing machines.

• Grammars

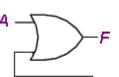
cS → aNbc | S

• λ-calculus

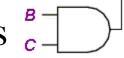
- $(\lambda X.X+1)$
- Post tag systems

- $A \rightarrow bc$
- μ-recursive functions
- $\mu(f)(x,y) = z$

• Cellular automata



- Boolean circuits
- Diophantine equations $\stackrel{\text{\tiny B}}{\sim}$

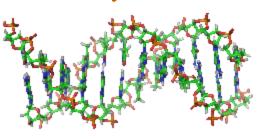


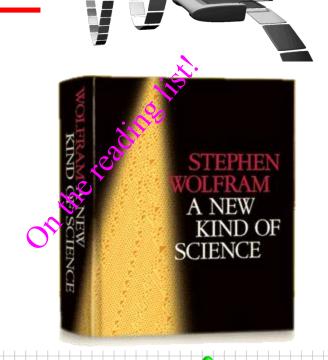
• DNA

$$x^3 + y^3 + z^3 = 33$$

• Billiards!

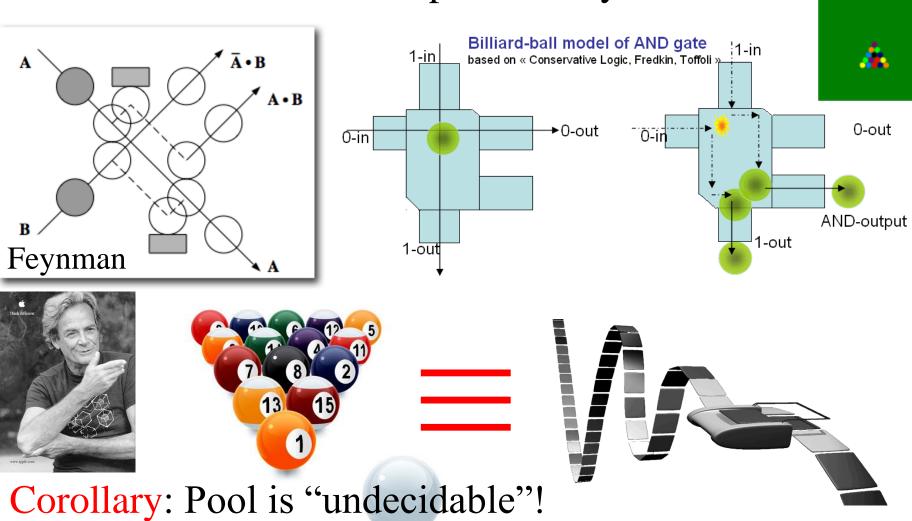






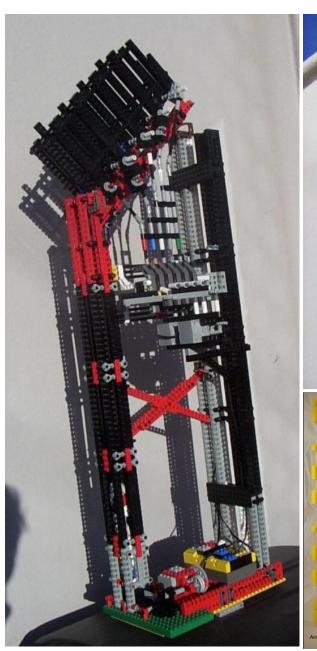
Universality of Billiards

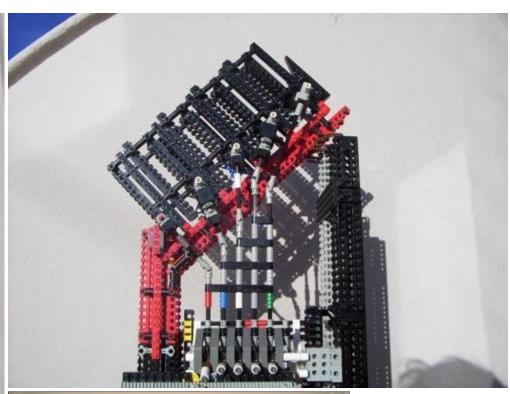
Theorem: Billiards is computationally universal!



Corollary: Newtonian mechanics is universal!

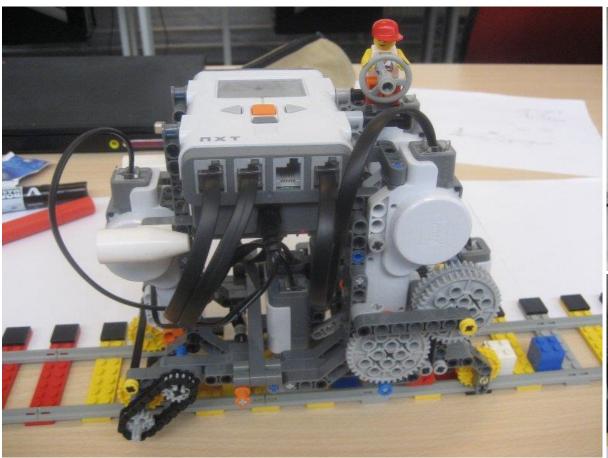
Lego Turing Machines

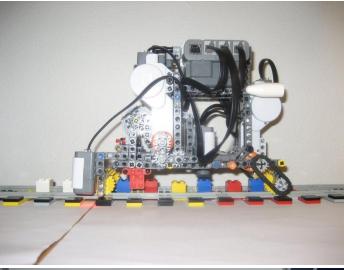






Lego Turing Machines







See: http://www.youtube.com/watch?v=cYw2ewoO6c4

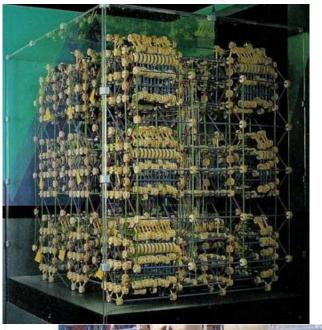
"Mechano" Computers





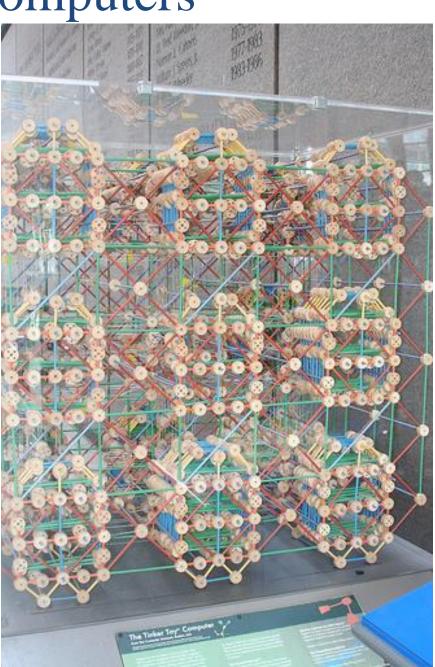
Babbage's difference engine

Tinker Toy Computers

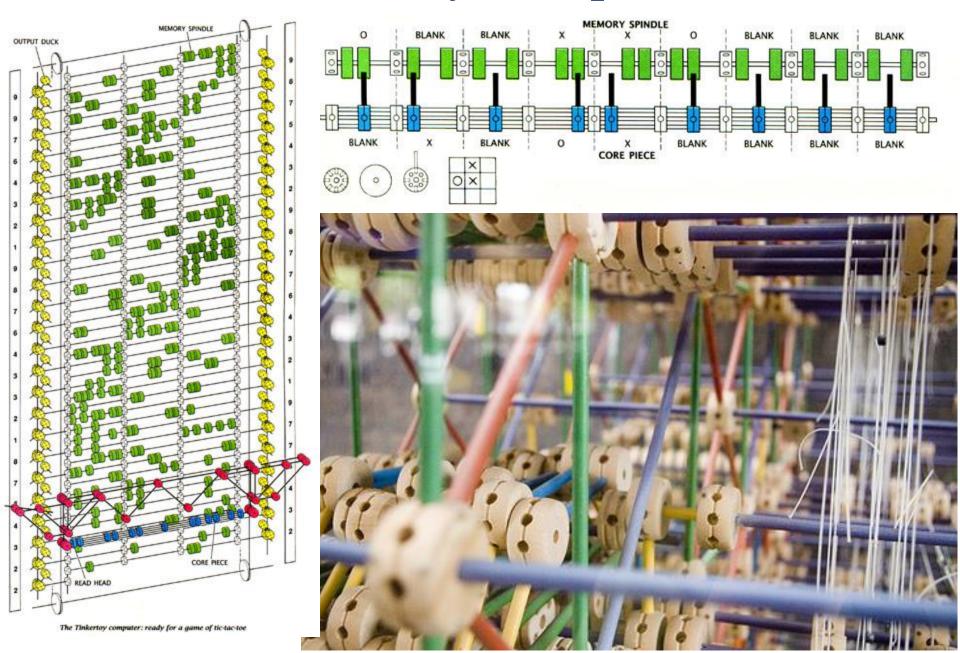


Plays tic-tac-toe!

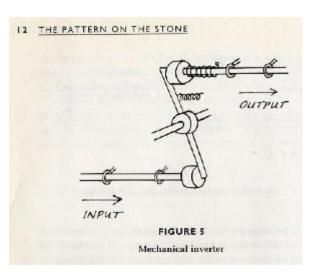


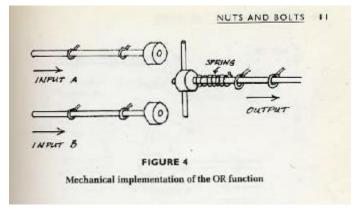


Tinker Toy Computers

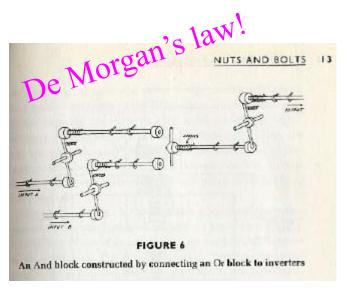


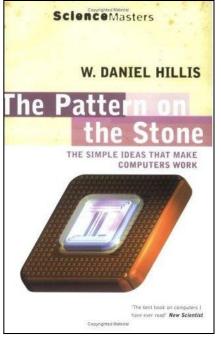
Mechanical Computers





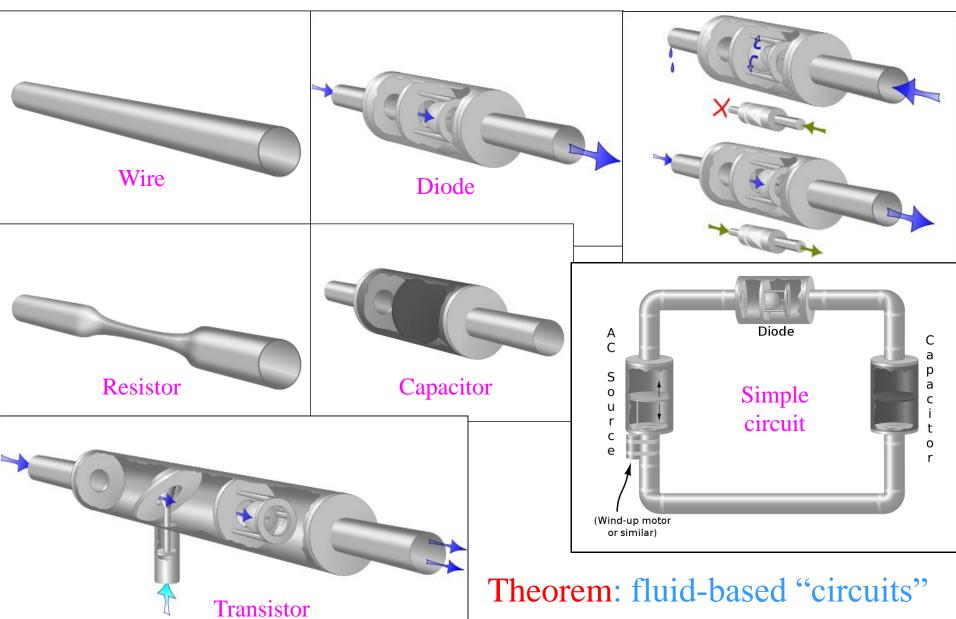








Hydraulic Computers



are Turing-complete / universal!

THE WOLFRAM 2,3 TURING MACHINE RESEARCH PRIZE

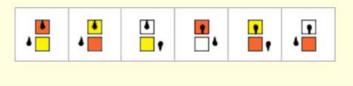
Oct 24, 2007

We have the solution!
Wolfram's 2,3 Turing machine
is universal

Congratulations Alex Smith. Find out more »



Is this Turing machine universal, or not?



The machine has 2 states and 3 colors, and is 596440 in Wolfram's numbering scheme. If it is universal then it is the smallest universal Turing machine that exists.

BACKGROUND »

TECHNICAL DETAILS »

GALLERY » NEWS »

PRIZE COMMITTEE »

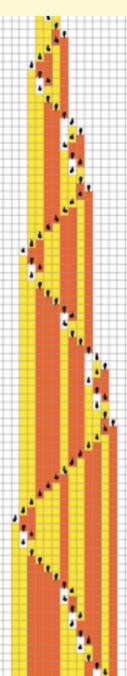
RULES & GUIDELINES »

FAQs »

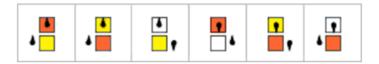
A universal Turing machine is powerful enough to emulate any standard computer. The question is: how simple can the rules for a universal Turing machine be?

Since the 1960s it has been known that there is a universal 7,4 machine. In A New Kind of Science, Stephen Wolfram found a universal 2,5 machine, and suggested that the particular 2,3 machine that is the subject of this prize might be universal.

The prize is for determining whether or not the 2,3 machine is in fact universal.



Wolfram's 2,3 Turing machine is universal!



The lower limit on Turing machine universality is proved—

providing new evidence for Wolfram's Principle of Computational Equivalence.



The Wolfram 2,3 Turing Machine Research Prize has been won by 20year-old Alex Smith of Birmingham, UK.

Smith's Proof (to be published in Complex Systems): Prize Submission » *Mathematica* Programs »

News Release » Technical Commentary »



Stephen Wolfram's Blog Post »

Media Enquiries »

BACKGROUND »
PRIZE COMMITTEE »

TECHNICAL DETAILS »
RULES & GUIDELINES »

GALLERY »

FAQs »

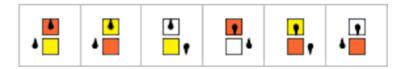
The Rules for the Machine

The rules for the Turing machine that is the subject of this prize are:

$$\{\{1, 2\} \rightarrow \{1, 1, -1\}, \{1, 1\} \rightarrow \{1, 2, -1\}, \{1, 0\} \rightarrow \{2, 1, 1\}, \{2, 2\} \rightarrow \{1, 0, 1\}, \{2, 1\} \rightarrow \{2, 2, 1\}, \{2, 0\} \rightarrow \{1, 2, -1\}\}$$

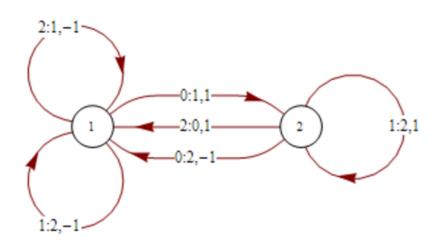
where this means {state, color} -> {state, color, offset}. (Colors of cells on the tape are sometimes instead thought of as "symbols" written to the tape.)

These rules can be represented pictorially by:



where the orientation of each arrow represents the state.

The rules can also be represented by the state transition diagram:



in A 2-state 3-symbol machine!

universal Turing machine!

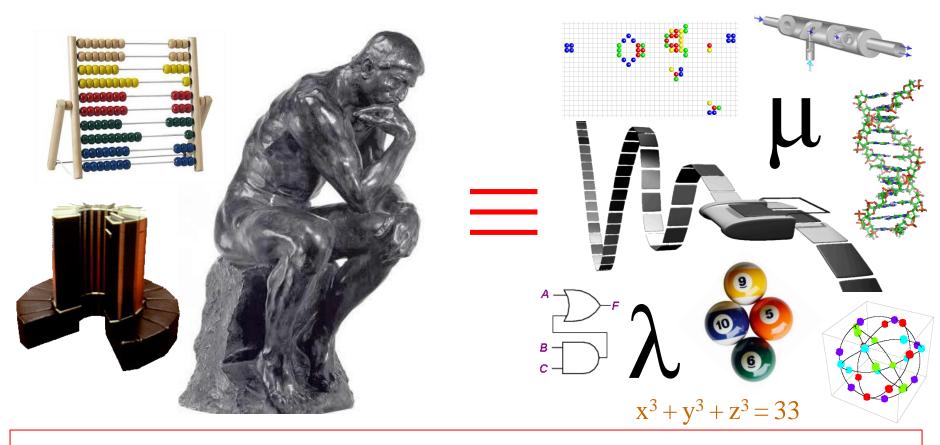
the smallest possible)

In Wolfram's numbering scheme for Turing machines, this is machine 596440. There are a total of (2 3 2)^(2 3)=12^6=2985984 machines with 2 states and 3 colors.

Note that there is no halt state for this Turing machine.

The Church-Turing Thesis

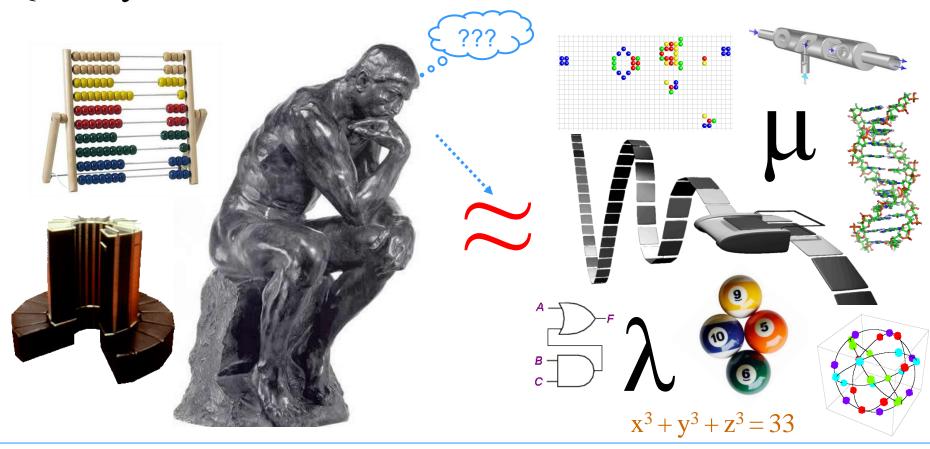
Q: What does it mean "to be computable"?



The Church-Turing Thesis: Anything that is "intuitively computable" is also Turing-machine computable.

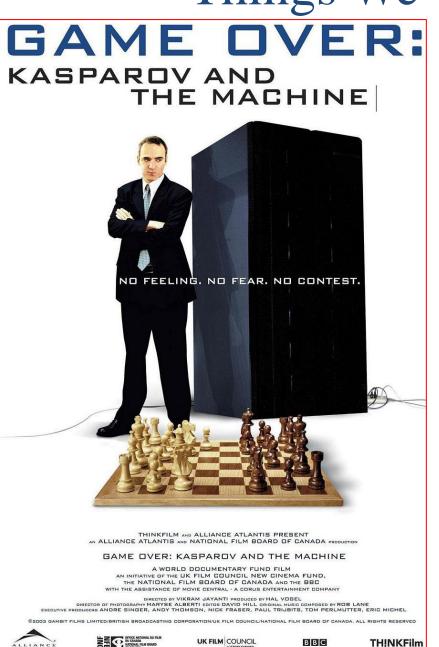
The Church-Turing Thesis

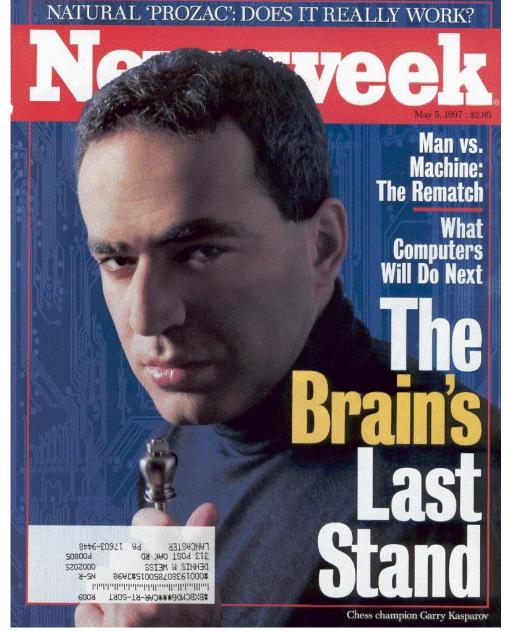
Q: Why "thesis" and not "theorem"?



Undefined / informal tasks: produce (or even identify) good music, art, poetry, humor, aesthetics, justice, truth, etc.









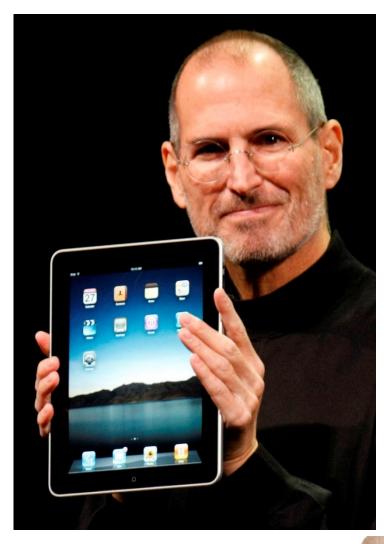
"Watson" AI becomes Jeopardy world champion in 2011



A Cool Turing Machine

Apple iPad (2015):

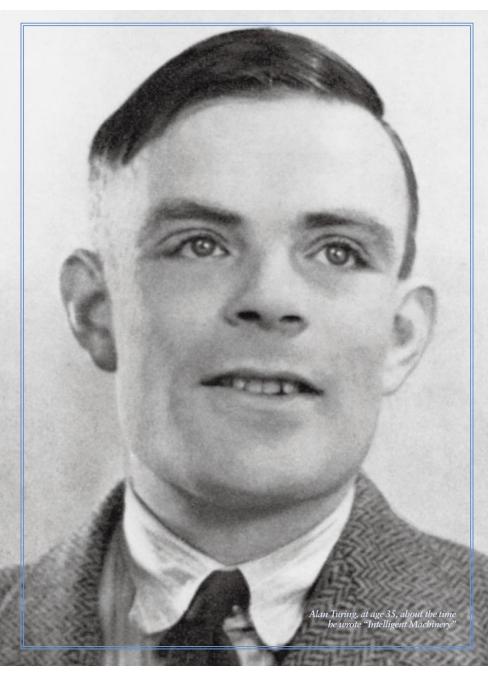
- $< \frac{1}{4}$ " thin
- < 1 pound weight
- 2048 x1536 (326 ppi res) multi-touch screen
- 128 GB memory
- 1.5 MHz 64-bit 3-core A8X
- 8 MP camera & HD video
- WiFi, cellular, GPS
- Compass, barometer
- battery life 10 hours



My Favorite Touring Machine Tesla Model S







Alan Turing's Forgotten Ideas

Computer Science

Well known for the machine, test and thesis that bear his name, the British genius also anticipated neural-network computers and "hypercomputation"

by B. Jack Copeland and Diane Proudfoot

lan Mathison Turing conceived of the modern computer in 1935. Today all digital computers are, in essence, "Turing machines." The British mathematician also pioneered the field of artificial intelligence, or AI, proposing the famous and widely debated Turing test as a way of determining whether a suitably programmed computer can think. During World War II, Turing was instrumental in breaking the German Enigma code in part of a top-secret British operation that historians say shortened the war in Europe by two years. When he died at the age of 41, Turing was doing the earliest work on what would now be called artificial life, simulating the chemistry of biological growth.

Throughout his remarkable career, Turing had no great interest in publicizing his ideas. Consequently, important aspects of his work have been neglected or forgotten over the years. In particular, few peopleeven those knowledgeable about computer scienceare familiar with Turing's fascinating anticipation of connectionism, or neuronlike computing. Also neglected are his groundbreaking theoretical concepts in the exciting area of "hypercomputation." According to some experts, hypercomputers might one day solve problems heretofore deemed intractable.

The Turing Connection

igital computers are superb number crunchers. Ask them to predict a rocket's trajectory or calculate the financial figures for a large multinational corporation, and they can churn out the answers in seconds. But seemingly simple actions that people routinely perform, such as recognizing a face or reading handwriting, have been devilishy tricky to program. Perhaps the networks of neurons that make up the brain have a natural facility for such tasks that standard computers lack. Scientists have thus been investigating computers modeled more closely on the human brain.

Connectionism is the emerging science of computing with networks of artificial neurons. Currently researchers usually simulate the neurons and their interconnections within an ordinary digital computer (just as engineers create virtual models of aircraft wings and skyscrapers). A training algorithm that runs on the computer adjusts the connections between the neurons, honing the network into a special-purpose machine dedicated to some particular function, such as forecasting international currency markets.

Modern connectionists look back to Frank Rosenblatt, who published the first of many papers on the topic in 1957, as the founder of their approach. Few realize that Turing had already investigated connectionist networks as early as 1948, in a little-known paper entitled "Intelligent Machinery."

Written while Turing was working for the National Physical Laboratory in London, the manuscript did not meet with his employer's approval. Sir Charles Darwin, the rather headmasterly director of the laboratory and grandson of the great English naturalist, dismissed it as a "schoolboy essay." In reality, this farsighted paper was the first manifesto of the field of artificial intelligence. In the work-which remained unpublished until 1968, 14 years after Turing's death-the British mathematician not only set out the fundamentals of connectionism but also brilliantly introduced many of the concepts that were later to become central to AI, in some cases after reinvention by others.

In the paper, Turing invented a kind of neural network that he called a "B-type" retical basis of connectionism in one suc-

Few realize that Turing had already investigated connectionist networks as early as 1948.

unorganized machine," which consists of artificial neurons and devices that modify the connections between them. B-type machines may contain any number of neurons connected in any pattern but are always subject to the restriction that each neuron-to-neuron connection must pass through a modifier device.

All connection modifiers have two training fibers. Applying a pulse to one of them sets the modifier to "pass mode," in which an input-either 0 or 1-passes through unchanged and becomes the output. A pulse on the other fiber places the modifier in "interrupt mode," in which the output is always 1, no matter what the input is. In this state the modifier destroys all information attempting to pass along the connection to which it is attached.

Once set, a modifier will maintain its function (either "pass" or "interrupt") unless it receives a pulse on the other training fiber. The presence of these ingenious connection modifiers enables the training of a B-type unorganized machine by means of what Turing called "appropriate interference, mimicking education." Actually, Turing theorized that "the cortex of an infant is an unorganized machine, which can be organized by suitable interfering training."

Each of Turing's model neurons has two input fibers, and the output of a neuron is a simple logical function of its two inputs. Every neuron in the network executes the same logical operation of "not and" (or NAND): the output is 1 if either of the inputs is 0. If both inputs are 1, then the output is 0.

Turing selected NAND because every other logical (or Boolean) operation can be accomplished by groups of NAND neurons. Furthermore, he showed that even the connection modifiers themselves can be built out of NAND neurons. Thus, Turing specified a network made up of nothing more than NAND neurons and their connecting fibers-about the simplest possible model of the cortex.

In 1958 Rosenblatt defined the theo-

cinct statement: "Stored information takes the form of new connections. or transmission channels in the nervous system (or the creation of conditions which are functionally equivalent to new connections)." Because the destruction of existing connections can be func-

tionally equivalent to the creation of new ones, researchers can build a network for accomplishing a specific task by taking one with an excess of connections and selectively destroying some of them. Both actions—destruction and creation are employed in the training of Turing's B-types.

At the outset, B-types contain random interneural connections whose modifiers have been set by chance to either pass or interrupt. During training, unwanted connections are destroyed by switching their attached modifiers to interrupt mode. Conversely, changing a modifier from interrupt to pass in effect creates a connection. This selective culling and enlivening of connections hones the initially random network into one organized for a given job.

Turing wished to investigate other kinds of unorganized machines, and he longed to simulate a neural network and its training regimen using an ordinary digital computer. He would, he said, "allow the whole system to run for an appreciable period, and then break in as a kind of 'inspector of schools' and see what progress had been made." But his own work on neural networks was carried out shortly before the first generalpurpose electronic computers became available. (It was not until 1954, the year of Turing's death, that Belmont G. Farley and Wesley A. Clark succeeded at the Massachusetts Institute of Technology in running the first computer simulation of a small neural network.)

Paper and pencil were enough, though, for Turing to show that a sufficiently large B-type neural network can be configured (via its connection modifiers)

in such a way that it becomes a generalpurpose computer. This discovery illuminates one of the most fundamental problems concerning human cognition.

From a top-down perspective, cognition includes complex sequential processes, often involving language or other forms of symbolic representation, as in mathematical calculation. Yet from a bottom-up view, cognition is nothing but the simple firings of neurons. Cognitive scientists face the problem of how to reconcile these very different perspectives.

Turing's discovery offers a possible solution: the cortex, by virtue of being a neural network acting as a general-purpose computer, is able to carry out the sequential, symbol-rich processing discerned in the view from the top. In 1948 this hypothesis was well ahead of its time, and today it remains among the best guesses concerning one of cognitive science's hardest problems.

Computing the Uncomputable

In 1935 Turing thought up the abstract device that has since become known as the "universal Turing machine." It consists of a limitless memory

that stores both program and data and a scanner that moves back and forth through the memory, symbol by symbol, reading the information and writing additional symbols. Each of the machine's basic actions is very simplesuch as "identify the symbol on which the scanner is positioned," "write '1'" and "move one position to the left." Complexity is achieved by chaining together large numbers of these basic actions. Despite its simplicity, a universal Turing machine can execute any task that can be done by the most powerful of today's computers. In fact, all modern digital computers are in essence universal Turing machines [see "Turing Machines," by John E. Hopcroft; Sci-ENTIFIC AMERICAN, May 1984].

Turing's aim in 1935 was to devise a machine-one as simple as possiblecapable of any calculation that a human mathematician working in accordance with some algorithmic method could perform, given unlimited time, energy, paper and pencils, and perfect concentration. Calling a machine "universal" merely signifies that it is capable of all such calculations. As Turing himself wrote, "Electronic computers are intended to carry out any definite rule-ofthumb process which could have been done by a human operator working in a disciplined but unintelligent manner."

Such powerful computing devices notwithstanding, an intriguing question arises: Can machines be devised that are capable of accomplishing even more? The answer is that these "hypermachines" can be described on paper, but no one as yet knows whether it will be possible to build one. The field of hypercomputation is currently attracting a growing number of scientists. Some speculate that the human brain itselfthe most complex information processor known-is actually a naturally occurring example of a hypercomputer.

Before the recent surge of interest in hypercomputation, any informationprocessing job that was known to be too difficult for universal Turing machines was written off as "uncomputable." In this sense, a hypermachine computes the uncomputable.

Examples of such tasks can be found in even the most straightforward areas of mathematics. For instance, given arithmetical statements picked at random, a universal Turing machine may

not always be able to tell which are theorems (such as "7 + 5 = 12") and which are nontheorems (such as "every number is the sum of two even numbers"). Another type of uncomputable problem comes from geometry. A set of tilesvariously sized squares with different colored edges-"tiles the plane" if the Euclidean plane can be covered by copies of the tiles with no gaps or overlaps and with adjacent edges always the same color. Logicians William Hanf and Dale Myers of the University of Hawaii have discovered a tile set that tiles the plane only in patterns too complicated for a universal Turing machine to calculate. In the field of computer science, a universal Turing machine cannot always predict whether a given program will terminate or continue running forever. This is sometimes expressed by saying that no general-purpose programming language (Pascal, BASIC, Prolog, C and so on) can have a foolproof crash debugger: a tool that detects all bugs that could lead to crashes, including errors that result in infinite processing loops.

Turing himself was the first to investigate the idea of machines that can perform mathematical tasks too difficult

Turing's Anticipation of Connectionism

n a paper that went unpublished until 14 years after his death (top), Alan Turing described a network of artificial neurons connected in a random manner. In this "B-type unorganized machine" (bottom left), each connection passes through a modifier that is set either to allow data to pass unchanged (areen fiber) or to destroy the transmitted information (red fiber). Switching the modifiers from one mode to the other enables the network to be trained. Note that each neuron has two inputs (bottom left, inset) and executes the simple logical operation of "not and," or NAND: if both inputs are 1, then the output is 0: otherwise the output is 1.

In Turing's network the neurons interconnect freely. In contrast, modern networks (bottom center) restrict the flow of information from layer to layer of neurons. Connectionists aim to simulate the neural networks of the brain (bottom right).

e reserded by one men as organised and by another to unorganised. A typical example of an unor mised machine would be as follows. terminal wheih can be connected to the input terminals of other units. We may imagine that that for each integer r. 14 r4 N

Alan Turing's Forgotten Ideas in Computer Science SCIENTIFIC AMERICAN April 1999 101 100 Scientific American April 1999 Alan Turing's Forgotten Ideas in Computer Science

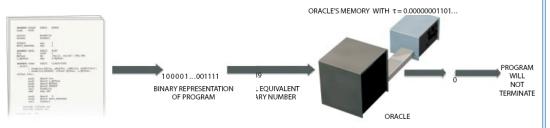
Using an Oracle to Compute the Uncomputable

↑ lan Turing proved that his universal machine—and by extension, even today's most powerful computers—could never solve certain problems. For instance, a universal Turing machine cannot always determine whether a given software program will terminate or continue running forever. In some cases, the best the universal machine can do is execute the program and wait—maybe eternally—for it to finish. But in his doctoral thesis (below), Turing did imagine that a machine equipped with a special "oracle" could perform this and other "uncomputable" tasks. Here is one example of how, in principle, an oracle might work.

Consider a hypothetical machine for solving the formidable

EXCERPT FROM TURING'S THESIS

Let us suppose that we are supplied with some unspecified seams of solving number theoretic problems; a kind of oracle as it were. We will not go any further into the nature of this oracle than to say that it cannot be a machine. With the help of the practs we could form a new kind of machine (call them o-suchtnes). maving as one of its fundamental processes that of solving a given number theoretic probleg. More definitely these machines are to



COMPUTER PROGRAM

"terminating program" problem (above). A computer program can be represented as a finite string of 1s and 0s. This sequence of digits can also be thought of as the binary representation of an integer, just as 1011011 is the equivalent of 91. The oracle's job can then be restated as, "Given an integer that represents a program (for any computer that can be simulated by a universal Turing machine), output a '1' if the program will terminate or a '0' otherwise."

The oracle consists of a perfect measuring device and a store, or memory, that contains a precise value—call it τ for Turing—of some physical quantity. (The memory might, for example, resemble a capacitor storing an exact amount of

electricity.) The value of τ is an irrational number; its written representation would be an infinite string of binary digits, such as 0.0000001101...

The crucial property of τ is that its individual digits happen to represent accurately which programs terminate and which do not. So, for instance, if the integer representing a program were 8,735,439, then the oracle could by measurement obtain the 8,735,439th digit of τ (counting from left to right after the decimal point). If that digit were 0, the oracle would conclude that the program will process

Obviously, without τ the oracle would be useless, and finding some physical variable in nature that takes this exact value might very well be impossible. So the search is on for some practicable way of implementing an oracle. If such a means were found, the impact on the field of computer science could be enormous. -B.J.C. and D.P.

for universal Turing machines. In his 1938 doctoral thesis at Princeton University, he described "a new kind of machine," the "O-machine."

An O-machine is the result of augmenting a universal Turing machine with a black box, or "oracle," that is a mechanism for carrying out uncomputable tasks. In other respects, O-machines are similar to ordinary computers. A digitally encoded program is chine—for example, "identify the symbol in the scanner"—might take place.) But notional mechanisms that fulfill the specifications of an O-machine's black box are not difficult to imagine [see box above]. In principle, even a suitable Btype network can compute the uncomputable, provided the activity of the neurons is desynchronized. (When a central clock keeps the neurons in step with one another, the functioning of the network

can be exactly simulated by a universal Turing machine.)

In the exotic mathematical theory of hypercomputation, tasks such as that of distinguishing theorems from nontheorems in arithmetic are no longer uncomputable. Even a debugger

that can tell whether any program written in C, for example, will enter an infinite loop is theoretically possible.

If hypercomputers can be built—and that is a big if-the potential for cracking logical and mathematical problems hitherto deemed intractable will be enormous. Indeed, computer science may be approaching one of its most significant advances since researchers

wired together the first electronic embodiment of a universal Turing machine decades ago. On the other hand, work on hypercomputers may simply fizzle out for want of some way of realizing an oracle.

The search for suitable physical, chemical or biological phenomena is getting under way. Perhaps the answer will be complex molecules or other structures that link together in patterns as complicated as those discovered by Hanf and Myers. Or, as suggested by Ion Doyle of M.I.T., there may be naturally occurring equilibrating systems with discrete spectra that can be seen as carrying out, in principle, an uncomputable task, producing appropriate output (1 or 0, for example) after being bombarded with input.

Outside the confines of mathematical logic, Turing's O-machines have largely been forgotten, and instead a myth has taken hold. According to this apocryphal account, Turing demonstrated in the mid-1930s that hypermachines are impossible. He and Alonzo Church, the logician who was Turing's doctoral adviser at Princeton, are mistakenly credited with having enunciated a principle to the effect that a universal Turing machine can exactly simulate the behavior

of any other information-processing machine. This proposition, widely but incorrectly known as the Church-Turing thesis, implies that no machine can carry out an information-processing task that lies beyond the scope of a universal Turing machine. In truth, Church and Turing claimed only that a universal Turing machine can match the behavior of any human mathematician working with paper and pencil in accordance with an algorithmic method—a considerably

weaker claim that certainly does not rule out the possibility of hypermachines.

Even among those who are pursuing the goal of building hypercomputers, Turing's pioneering theoretical contributions have been overlooked. Experts routinely talk of carrying out information processing "beyond the Turing limit" and describe themselves as attempting to "break the Turing barrier." A recent review in New Scientist of this emerging field states that the new machines "fall outside Turing's conception" and are "computers of a type never envisioned by Turing," as if the British genius had not conceived of such devices more than half a century ago. Sadly, it appears that what has already occurred with respect to Turing's ideas on connectionism is starting to happen all over again.

The Final Years

In the early 1950s, during the last years of his life, Turing pioneered the field of artificial life. He was trying to simulate a chemical mechanism by which the genes of a fertilized egg cell may determine the anatomical structure of the resulting animal or plant. He described this research as "not altogether unconnected" to his study of neural networks, because "brain structure has to be ... achieved by the genetical embryological mechanism, and this theory that I am now working on may make clearer what restrictions this really implies." During this period, Turing achieved the distinction of being the first to engage in the computer-assisted exploration of nonlinear dynamical systems. His theory used nonlinear differential equations to express the chemistry of growth.

But in the middle of this groundbreaking investigation, Turing died from cvanide poisoning, possibly by his own hand. On June 8, 1954, shortly before what would have been his 42nd birthday, he was found dead in his bedroom. He had left a large pile of handwritten notes and some computer programs. Decades later this fascinating material is still not fully understood.

The Authors

B. JACK COPELAND and DIANE PROUDFOOT are the directors of the Turing Project at the University of Canterbury, New Zealand, which aims to develop and apply Turing's ideas using modern techniques. The authors are professors in the philosophy department at Canterbury, and Copeland is visiting professor of computer science at the University of Portsmouth in England. They have written numerous articles on Turing, Copeland's Turing's Machines and The Essential Turing are forthcoming from Oxford University Press, and his Artificial Intelligence was published by Blackwell in 1993. In addition to the logical study of hypermachines and the simulation of B-type neural networks, the authors are investigating the computer models of biological growth that Turing was working on at the time of his death. They are organizing a conference in London in May 2000 to celebrate the 50th anniversary of the pilot model of the Automatic Computing Engine, an electronic computer designed primarily by Turing.

Further Reading

X-Machines and the Halting Problem: Building a Super-Turing Machine. Mike Stannett in Formal Aspects of Computing, Vol. 2, pages 331-341; 1990.

INTELLIGENT MACHINERY. Alan Turing in Collected Works of A. M. Turing: Mechanical Intelligence. Edited by D. C. Ince. Elsevier Science Publishers, 1992.

COMPUTATION BEYOND THE TURING LIMIT. Hava T. Siegelmann in Science, Vol. 268, pages 545-548; April 28, 1995.

On Alan Turing's Anticipation of Connectionism. B. Jack Copeland and Diane Proudfoot in Synthese, Vol. 108, No. 3, pages 361-377; March 1996.

TURING'S O-MACHINES, SEARLE, PENROSE AND THE BRAIN. B. Jack Copeland in Analysis, Vol. 58, No. 2, pages 128-138; 1998.

THE CHURCH-TURING THESIS. B. Iack Copeland in The Stanford Encyclopedia of Philosophy. Edited by Edward N. Zalta. Stanford University, ISSN 1095-5054. Available at http://plato.stanford.edu on the World Wide Web.

has largely been forgotten. fed in, and the machine produces digital output from the input using a step-bystep procedure of repeated applications

Even among experts, Turing's

pioneering theoretical concept of a hypermachine

of the machine's basic operations, one of which is to pass data to the oracle and register its response. Turing gave no indication of how an oracle might work. (Neither did he ex-

plain in his earlier research how the ba-

sic actions of a universal Turing ma-

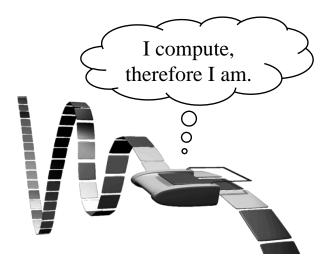
102 SCIENTIFIC AMERICAN April 1999

The Turing Test

Q: Can machines think?







Problem: We don't know what "think" means.

Q: What is intelligence?

Problem: We can't define "intelligence".

But, we usually "know it when we see it".

146

(Taken from MIND: a Quartedy Review of Psychology and Philosophy. Vol. LIX., N.S., No. 236, October, 1950.)

COMPUTING MACHINERY AND INTELLIGENCE

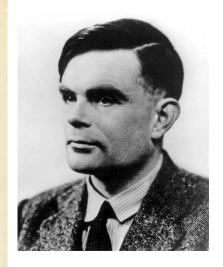
by

A. M. TURING.

1. The Imitation Game.

I propose to consider the question, 'Can machines think?' This should begin with definitions of the meaning of the terms 'machine' and 'think'. The definitions might be framed so as to reflect so far as possible the normal use of the words, but this attitude is dangerous. If the meaning of the words 'machine' and 'think' are to be found by examining how they are commonly used it is difficult to escape the conclusion that the meaning and the answer to the question, 'Can machines think?' is to be sought in a statistical survey such as a Gallup poll. But this is absurd. Instead of attempting such a definition I shall replace the question by another, which is closely related to it and is expressed in relatively unambiguous words.

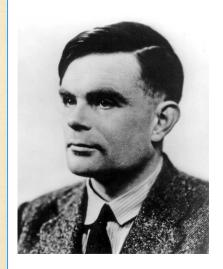
The new form of the problem can be described in terms of a game which we call the 'imitation game'. It is played with three people, a man (A), a woman (B), and an interrogator (C) who may be of either sex. The interrogator stays in a room apart from the other two.



be able to produce a material which is indistinguishable from the human skin. It is possible that at some time this might be done, but even supposing this invention available we should feel there was little point in trying to make a 'thinking machine' more human by dressing it up in such artificial flesh. The form in which we have set the problem reflects this fact in the condition which prevents the interrogator from seeing or touching the other competitors, or hearing their voices. Some other advantages of the proposed criterion may be shown up by specimen questions and answers. Thus:

- Q: Please write me a sonnet on the subject of the Forth Bridge.
- A: Count me out on this one. I never could write poetry.
- Q: Add 34957 to 70764.
- A: (Pause about 30 seconds and then give as answer) 105621.
- Q: Do you play chess?
- A: Yes.
- Q: I have K at my Kl, and no other pieces. You have only K at K6 and R at Rl. It is your move. What do you play?
- A: (After a pause of 15 seconds) R-R8 mate.

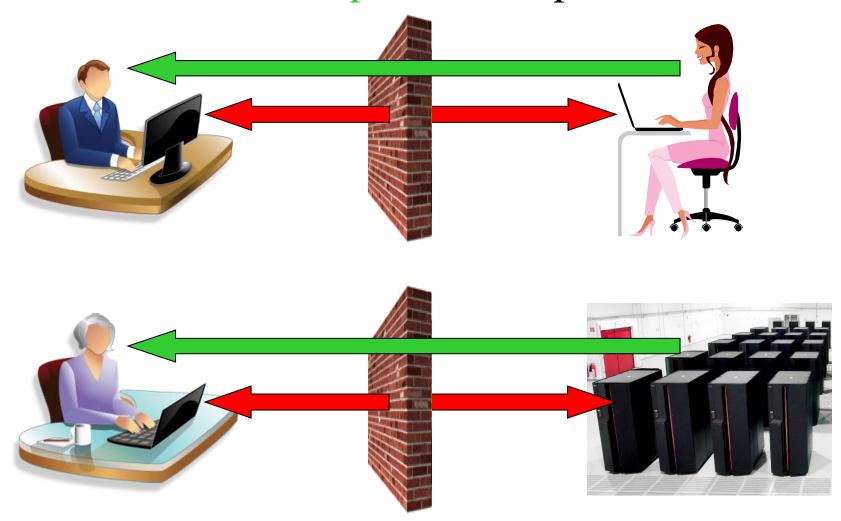
The question and answer method seems to be suitable for introducing almost any one of the fields of human endeavour that we wish to include. We do not wish to penalise the machine for its inability to shine in beauty competitions, nor to penalise a man for losing in a race against an aeroplane. The conditions of our game make these disabilities irrelevant. The 'witnesses' can brag, if they consider it advisable, as much as they please about their charms, strength or heroism, but the interrogator cannot demand practical demonstrations.



The Turing Test

Q: Can you distinguish a machine from a person?

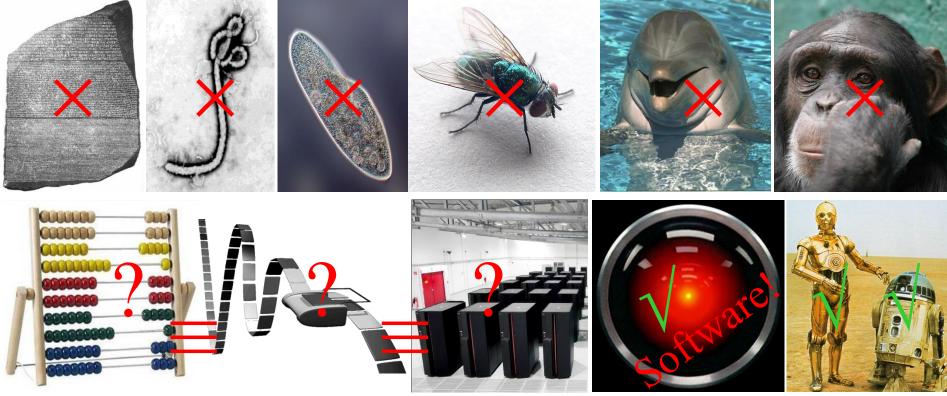
■ Can a machine impersonate a person?

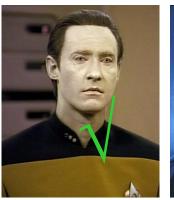


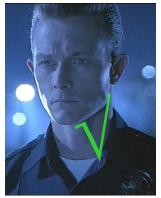
The Turing Test

- The first deep investigation into whether machines can "behave intelligently"
- Helped usher in field of AI
- Decoupled "intelligence" from "human"
- Based "intelligence" on I/O, not entity's "look and feel"
- Proposed a practical, formal test for intelligence
- Definitions & test are operational & easily implementable
- Turing test variants: "immortality", "fly-on-wall", "meta", "reverse", "subject matter expert", "compression", "minimum intelligent signal"

The Turing Test pass the Turing test? Q: Which of the following can think?

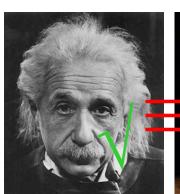










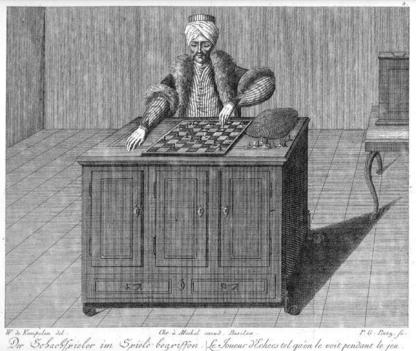


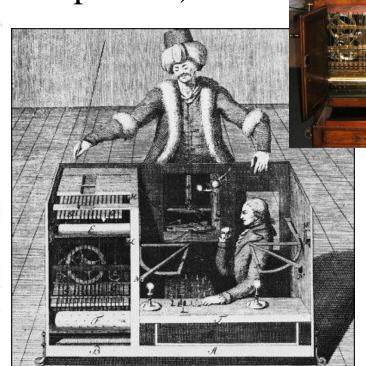


Turing Test Milestones

Turk (von Kempelen), 1770:

- Played a strong game of chess
- Toured the world for 84 years
- Generated much interest in automata
- Was a hoax (hidden human operator)





Turing Test Milestones

Eliza (Weizenbaum), 1966:

- First "chatterbot"
- Named after "Eliza Doolittle" of Shaw's Pygmalion
- Simulated Rogerian psychotherapist
- Often convinced people it is human
- Influence computer games (e.g., Dungeon, Adventure)
- Inspired Arthur C. Clarke's HAL 9000
- Chatterbots appear today in chatrooms and dating services
- Chatterbot competitions (Turing Test format):
 - Loebner Prize
 - Chatterbox Challenge, 2010



Turing Test Milestones

Elbot, 2008:

- Won 2008 Loebner Prize
- Fooled 3 of 12 judges (Turing: >30%)
- Typical excerpt:

Judge: What's your favourite novel?

Elbot: I often read telephone books, or dadaist poetry: Brä brä brä

Judge: Typical computer!

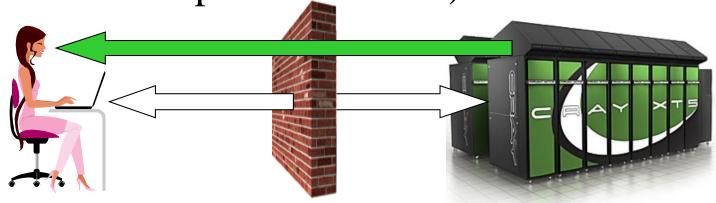
Elbot: You tend towards generalizations. But I must admit, so do I. However, my generalizations are firmly grounded in statistical theory.

Judge: What do u think of KW's enthusiasm for having machines take over the world?

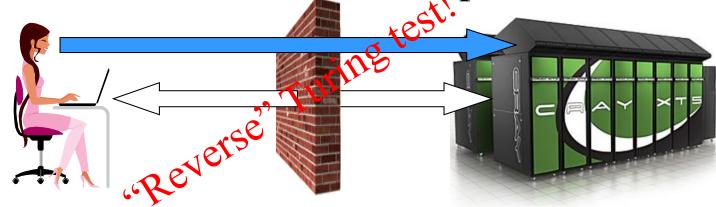
Elbot: Fix it up a bit first. Then I'll take it over.

Applications of the Turing Test

Old: a computer tries to convince a human (that the computer is human).



New: a human tries to convince a computer (that the human is not a computer).



Applications of the Turing Test

Problem: how can a human convince a computer

that the human is not a computer?

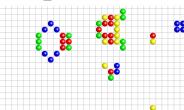
Idea: "CAPTCHA"



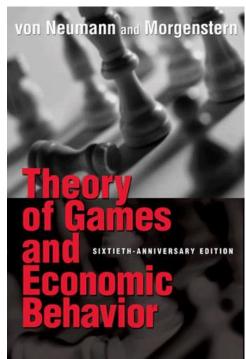
Historical Perspectives

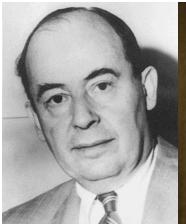
John von Neumann (1903-1957)

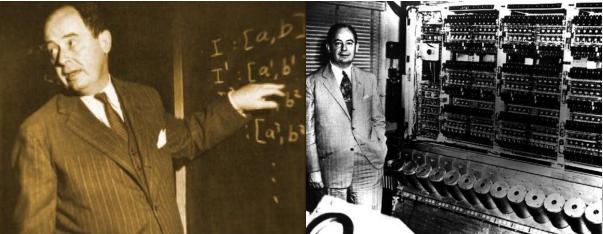
- Contributed to set theory, functional analysis, quantum mechanics, ergodic theory, economics, geometry, hydrodynamics, statistics, analysis, measure theory, ballistics, meteorology, ...
- Invented game theory (used in Cold War)
- Re-axiomatized set theory
- Principal member of Manhattan Project
- Helped design the hydrogen / fusion bomb
- Pioneered modern computer science
- Originated the "stored program"
- "von Neumann architecture" and "bottleneck"
- Helped design & build the EDVAC computer
- Created field of cellular automata
- Investigated self-replication
- Invented merge sort





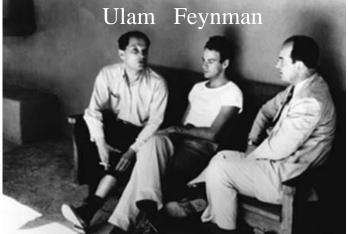










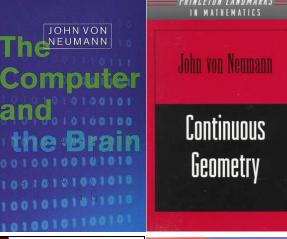


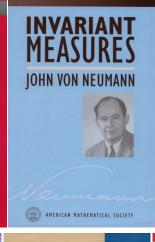


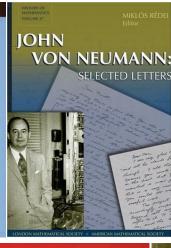


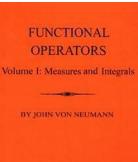


"Most mathematicians prove what they can; von Neumann proves what he wants."











John von Neumann

Continuous geometries with a transition probability

Memoirs

of the American Mathematical Society

Proceedings of Symposia in John von Neumann PURE MATHEMATICS The

The Legacy of John von Neumann

James Glimm John Impagliazzo Isadore Singer

Volume 50

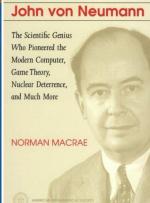


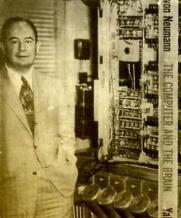


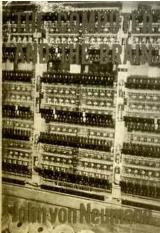
from Pascal to

von Neumann

Herman H. Goldstine









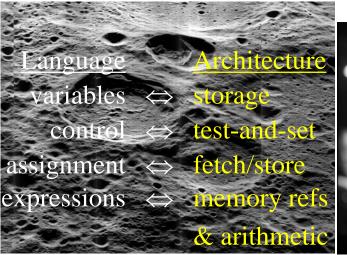


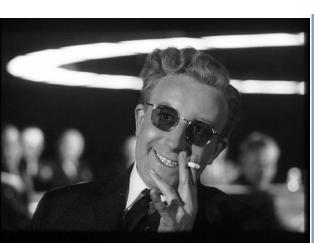


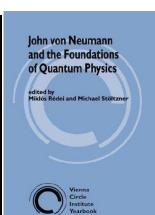
JOHN VON NEUMANN and THE ORIGINS OF MODERN COMPUTING WILLIAM ASPRAY

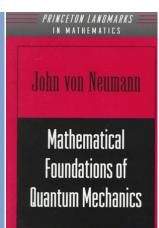
von Neumann's Legacy

- Re-axiomatized set theory to address Russell's paradox
- Independently proved Godel's second incompleteness theorem: aximomatic systems are unable to prove their own consistency.
- Addressed Hilbert's 6th problem: axiomatized quantum mechanics using Hilbert spaces.
- Developed the game-theory based Mutually-Assured Destruction (MAD) strategic equilibrium policy still in effect today!
- von Neumann regular rings, von Neumann bicommutant theorem, von Neumann entropy, von Neumann programming languages

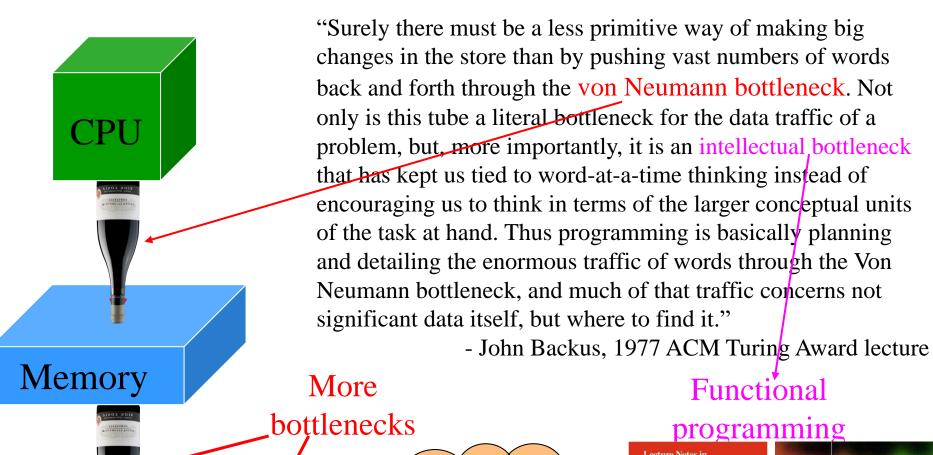








Von Neumann Architecture



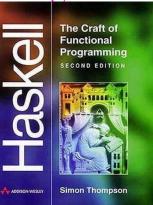
Internet

Disk

J. Hughes (Ed.)

Functional
Programming Languages
and Computer Architecture

Sto I. C. Conference
Cambridge, M.K. I.S.A, August 1991
Proceedings.

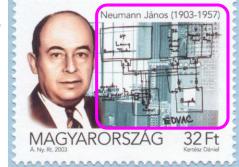




First Draft of a Report on the EDVAC

by

John von Neumann



Contract No. W-670-ORD-4926

Between the

United States Army Ordnance Department

and the

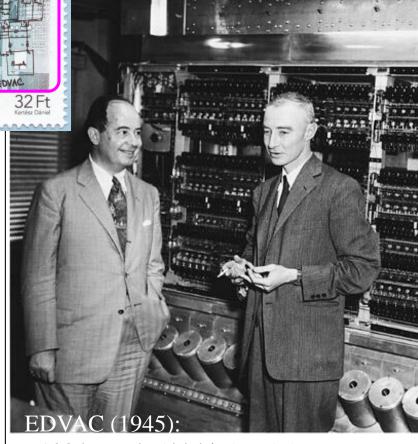
University of Pennsylvania

Moore School of Electrical Engineering University of Pennsylvania

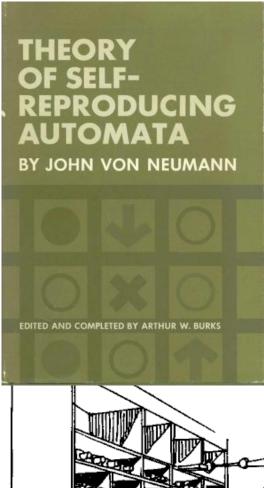
June 30, 1945

This is an exact copy of the original typescript draft as obtained from the University of Pennsylvania Moore School Library except that a large number of typographical errors have been corrected and the forward references that von Neumann had not filled in are provided where possible. Missing references, mainly to unwritten Sections after 15.0, are indicated by empty {}. All added material, mainly forward references, is enclosed in {}. The text and figures have been reset using TEX in order to improve readability. However, the original manuscript layout has been adhered to very closely. For a more "modern" interpretation of the von Neumann design see M. D. Godfrey and D. F. Hendry, "The Computer as von Neumann Planned It," *IEEE Annals of the History of Computing*, vol. 15 no. 1, 1993.

Michael D. Godfrey, Information Systems Laboratory, Electrical Engineering Department Stanford University, Stanford, California, November 1992

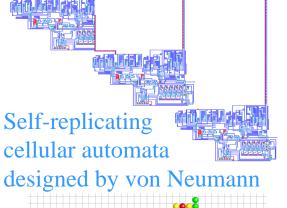


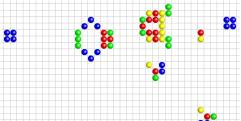
- 1024 words (44-bits) 5.5KB
- 864 microsec / add (1157 / sec)
- 2900 microsec / multiply (345/sec)
- Magnetic tape (no disk), oscilloscope
- 6,000 vacuum tubes
- 56,000 Watts of power
- 17,300 lbs (7.9 tons), 490 sqft
- 30 people to operate



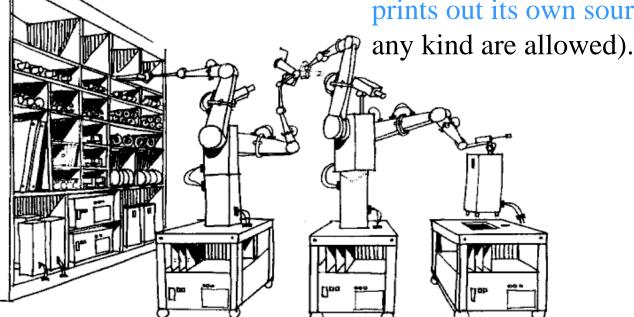
Self-Replication

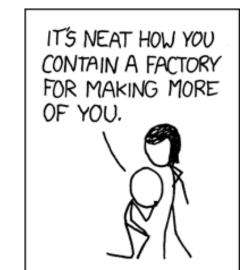
- Biology / DNA
- Nanotechnology
- Computer viruses
- Space exploration
- Memetics / memes
- "Gray goo"





Problem (extra credit): write a program that prints out its own source code (no inputs of











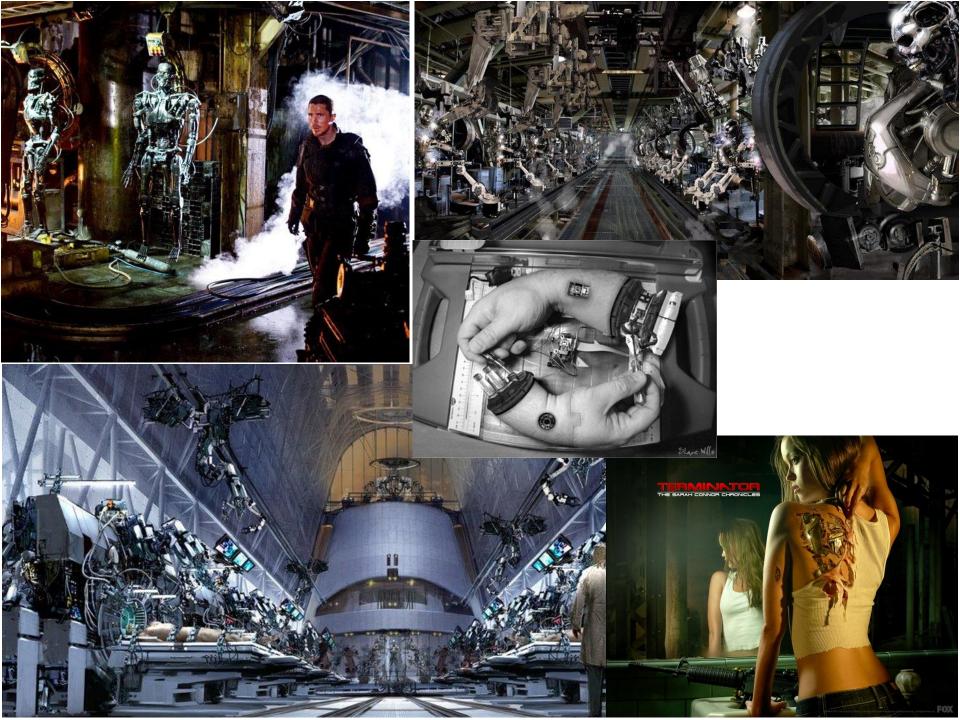


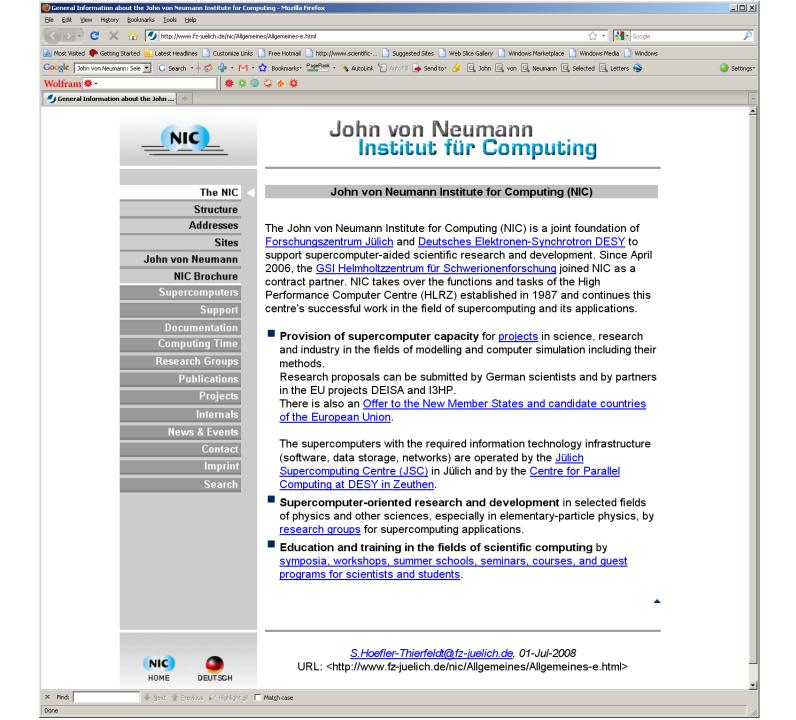


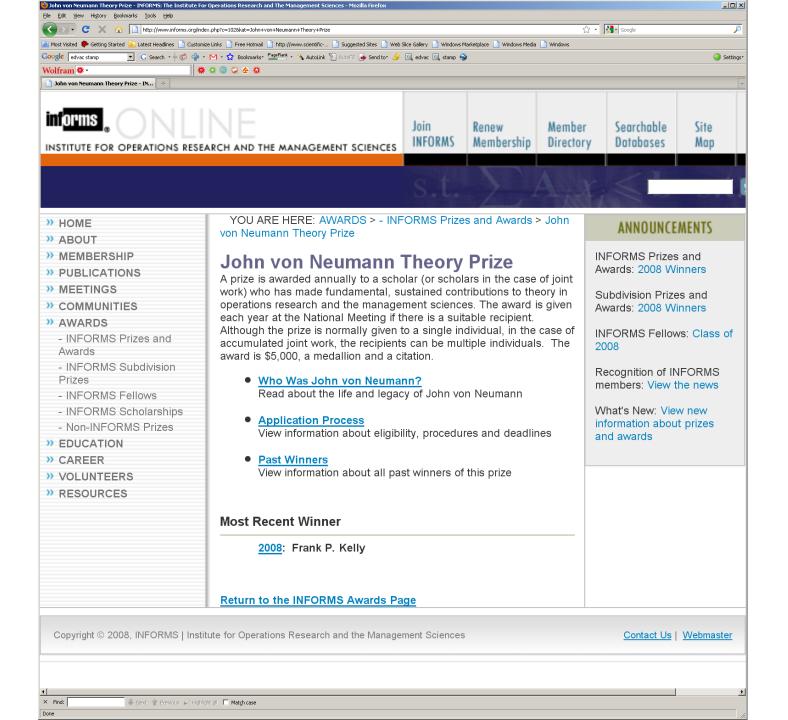


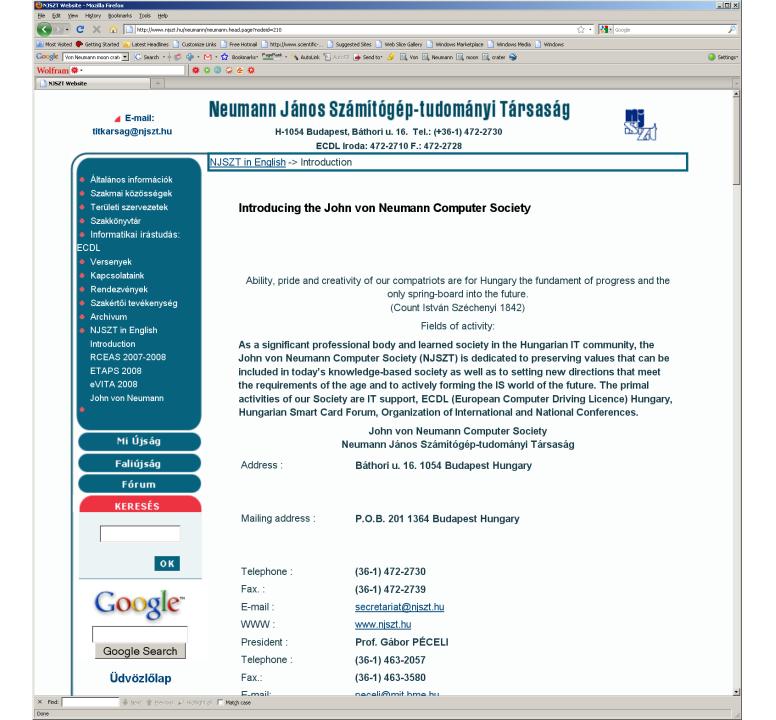








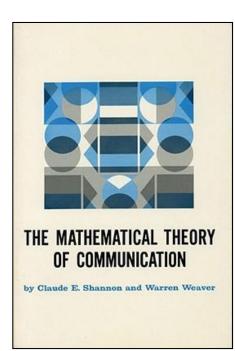




Claude Shannon (1916-2001)

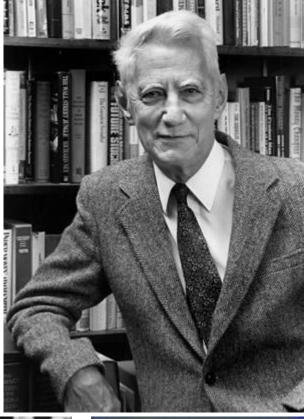
- Invented electrical digital circuits (1937)
- Founded information theory (1948)
- Introduced sampling theory, coined term "bit"
- Contributed to genetics, cryptography
- Joined Institute for Advanced Study (1940) Influenced by Turing, von Neumann, Einstein
- Originated information entropy, Nyquist—Shannon, sampling theorem, Shannon-Hartley theorem, Shannon switching game, Shannon-Fano coding, Shannon's source coding theorem, Shannon limit, Shannon decomposition / expansion, Shannon #
- Other hobbies & inventions: juggling, unicycling, computer chess, rockets, motorized pogo stick, flame-throwers, Rubik's cube solver, wearable computer, mathematical gambling, stock markets
- "AT&T Shannon Labs" named after him







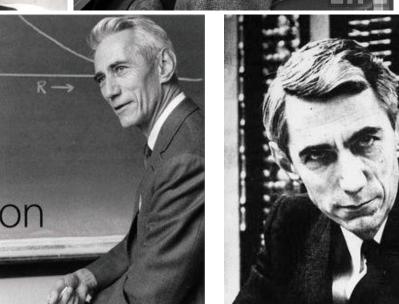




BY W. HITCHCCC WALDROP

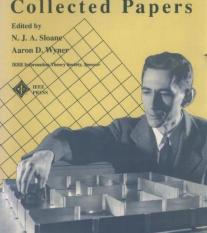
Reluctant Father

of the Digital Age Claude Shannon



CLAUDE ELWOOD SHANNON

Collected Papers





A SYMBOLIC ANALYSIS

OF

RELAY AND SWITCHING CIRCUITS

ъÿ

Claude Elwood Shannon

B.S., University of Michigan 1956

Submitted in Partial Fulfillment of the Requirements for the Degree of

MASTER OF SCIENCE

from the

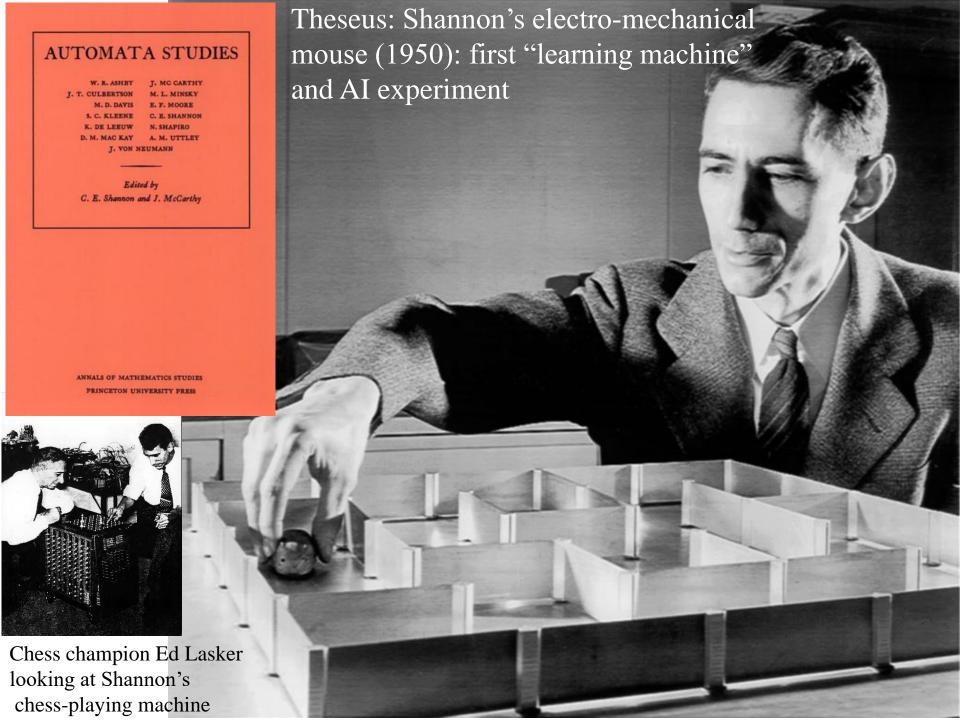
Massachusetts Institute of Technology

1940

Signature of Author		<u> </u>	
Department of Electrical Engineering	, August	10,	1937
Signature of Professor in Charge of Research			
Signature of Chairman of Department, Committee on Graduate Students		1. dq.'	

TABLE OF CONTENTS

	<u>P</u>	a ge
I	Introduction; Types of Problems	1
II	Series-Parallel Two-Terminal Circuits	4
	Fundamental Definitions and Postulates	4
	Theorems	6
	Analogue with the Calculus of Propositions	8
III	Multi-Terminal and Non-Series-Parallel Networks	-18
	Equivalence of n-Terminal Networks	18
	Star-Mesh and Delta-Wye Transformations	19
	Hinderance Function of a Non-Series-Parallel Network	21
	Simultaneous Equations	24
	Matrix Methods	25
	Special Types of Relays and Switches	28
ľv	Synthesis of Networks	31
	General Theorems on Networks and Functions	31
	Dual Networks	36
	Synthesis of the General Symmetric Function	39
	Equations from Given Operating Characteristics	4 7
V	Illustrative Examples	-51
	A Selective Circuit	52
	An Electric Combination Lock	55
	A Vote Counting Circuit	58
	An Adder to the Base Two	59
	A Factor Table Machine	62
Ref	erences	69





Shannon's home study room



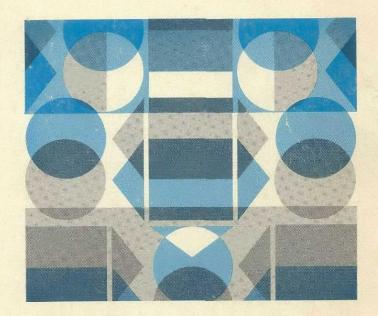




Shannon's On/Off machine

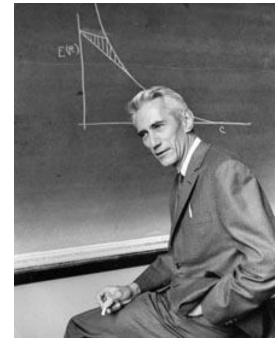






THE MATHEMATICAL THEORY OF COMMUNICATION

by Claude E. Shannon and Warren Weaver



Eighth paperback printing, 1980

Originally published in a clothbound edition, 1949.

Copyright 1949 by The Board of Trustees of the University of Illinois. Manufactured in the United States of America. Library of Congress Catalog Card No. 49-11922.

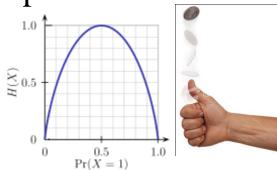
ISBN 0-252-72548-4

Entropy and Randomness

- Entropy measures the expected "uncertainly" (or "surprise") associated with a random variable.
- Entropy quantifies the "information content" and represents a lower bound on the best possible lossless compression.
- Ex: a random fair coin has entropy of 1 bit.

 A biased coin has lower entropy than fair coin.

 A two-headed coin has zero entropy.



- English text has entropy rate of 0.6 to 1.5 bits per letter.
- Q: How do you simulate a fair coin with a biased coin of unknown but fixed bias?
- A [von Neumann]: Look at pairs of flips. HT and TH both occur with equal probability of p(1-p), and ignore HH and TT pairs.

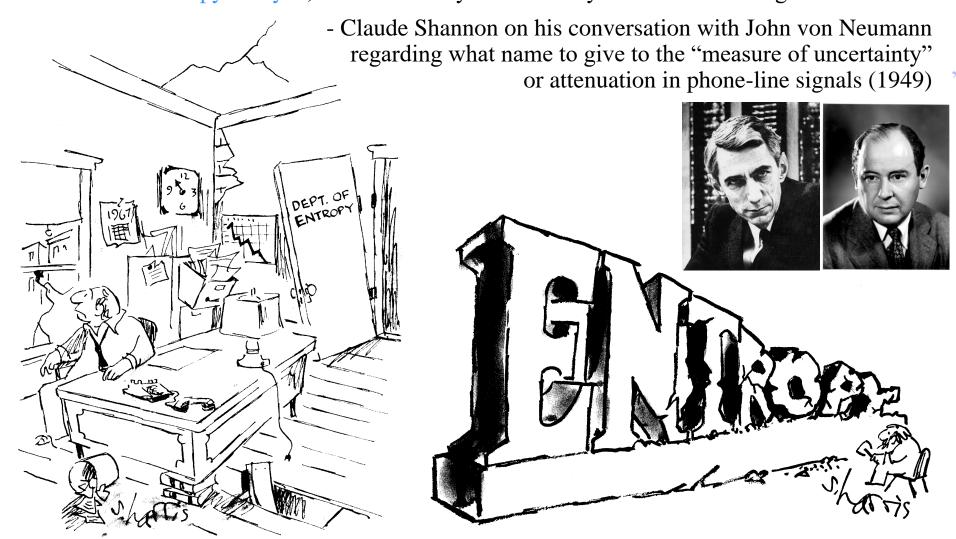
Entropy and Randomness

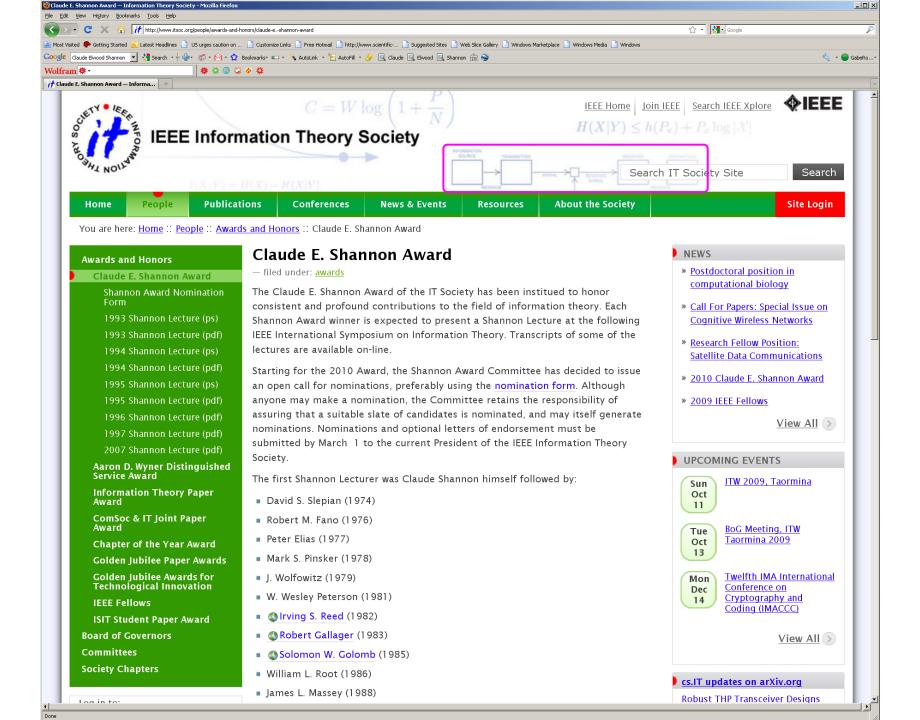
- Information entropy is an analogue of thermodynamic entropy in physics / statistical mechanics, and von Neumann entropy in quantum mechanics.
- Second law of thermodynamics: entropy of an isolated system can not decrease over time.
- Entropy as "disorder" or "chaos".
- Entropy as the "arrow of time".
- "Heat death of the universe" / black holes
- Quantum computing uses a quantum information theory to generalize classical information theory.
- Theorem: String compressibility decreases as entropy increases.
- Theorem: Most strings are not (losslessly) compressible.
- Corollary: Most strings are random!





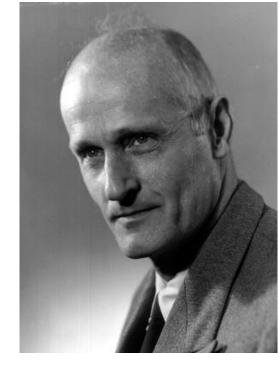
"My greatest concern was what to call it. I thought of calling it 'information', but the word was overly used, so I decided to call it 'uncertainty'. When I discussed it with John von Neumann, he had a better idea. Von Neumann told me, 'You should call it entropy, for two reasons. In the first place your uncertainty function has been used in statistical mechanics under that name, so it already has a name. In the second place, and more important, nobody knows what entropy really is, so in a debate you will always have the advantage."



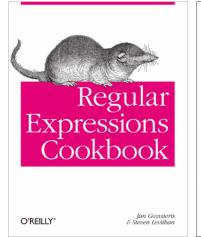


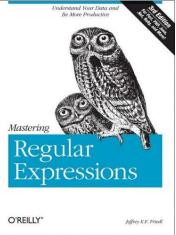
Stephen Kleene (1909-1994)

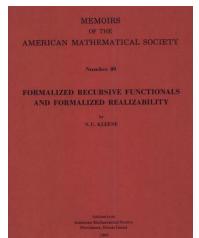
- Founded recursive function theory
- Pioneered theoretical computer science
- Student of Alonzo Church; was at the Institute for Advanced Study (1940)
- Invented regular expressions
- Kleene star / closure, Kleene algebra, Kleene recursion theorem, Kleene fixed point theorem, Kleene-Rosser paradox

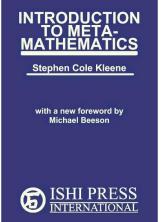


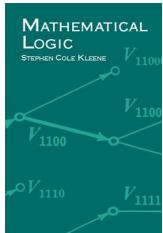
"Kleeneliness is next to Gödeliness"











WHENEVER I LEARN A
NEW SKILL I CONCOCT
ELABORATE FANTASY
SCENARIOS WHERE IT
LETS ME SAVE THE DAY.



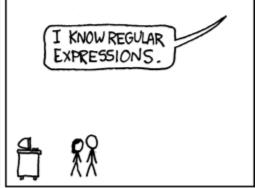
BUT TO FIND THEM WE'D HAVE TO SEARCH THROUGH 200 MB OF EMAILS LOOKING FOR SOMETHING FORMATTED LIKE AN ADDRESS!

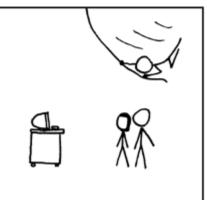


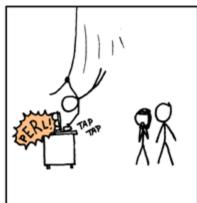
IT'S HOPELESS!

















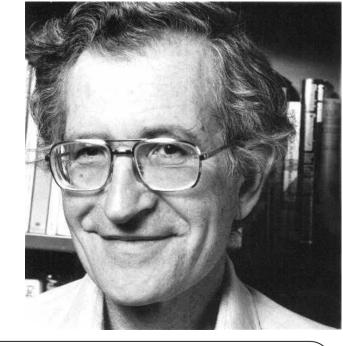
NATIONAL REGULAR EXPRESSION DAY

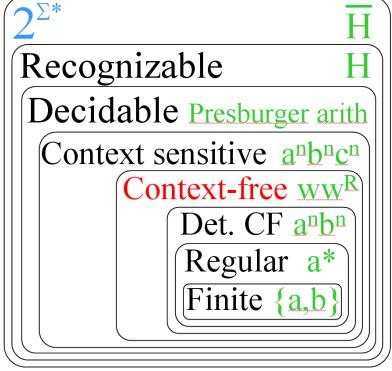
a celebration of powerful string manipulation

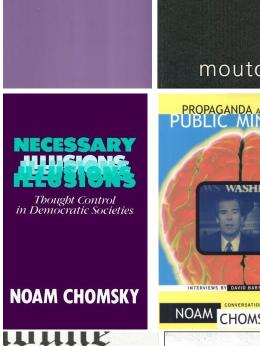
JUNE 1ST // 2008

Noam Chomsky (1928-)

- Linguist, philosopher, cognitive scientist, political activist, dissident, author
- Father of modern linguistics
- Pioneered formal languages
- Developed generative grammars
 Invented context-free grammars
- Defined the Chomsky hierarchy
- Influenced cognitive psychology, philosophy of language and mind
- Chomskyan linguistics, Chomskyan syntax, Chomskyan models
- Critic of U.S. foreign policy
- Most widely cited living scholar Eighth most-cited source overall!







The Political Economy of

the Mass Media By EDWARD S. HERMAN

and NOAM CHOMSKY



Noam Chomsky Syntactic



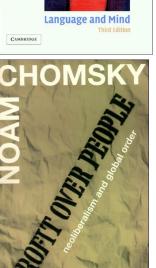
NOAM CHOMSKY

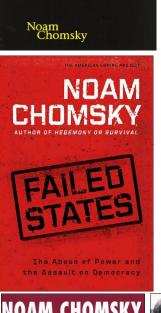
Noam

CHOMSKY

Topics in the Theory of

Generative Grammar





Minimalist Program

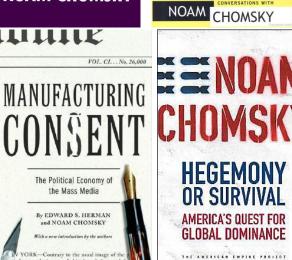


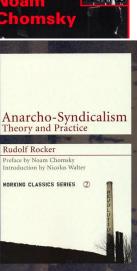
NOAM CHOMSKY

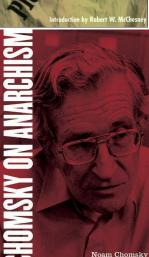


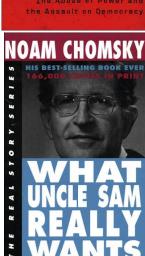
A LIFE

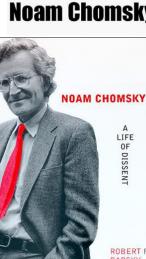
ROBERT F. BARSKY

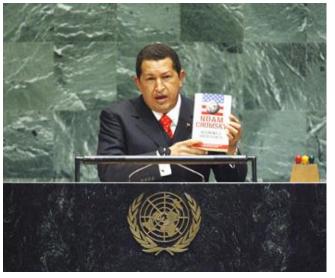


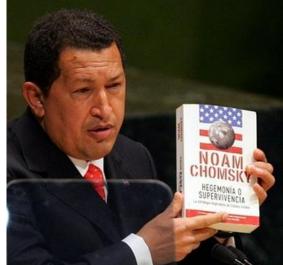




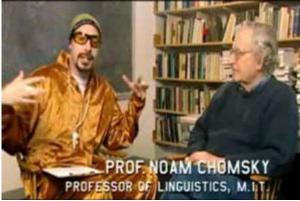




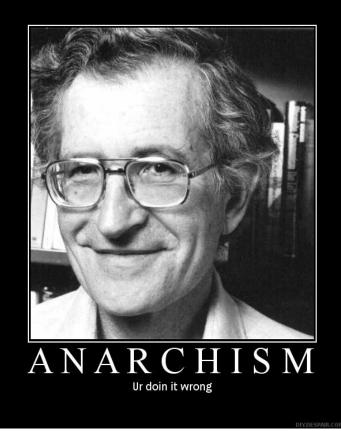


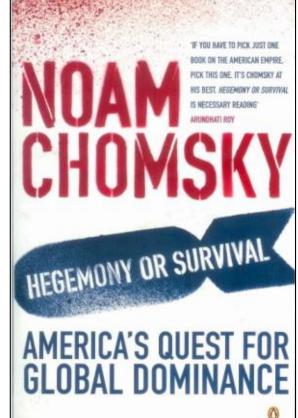


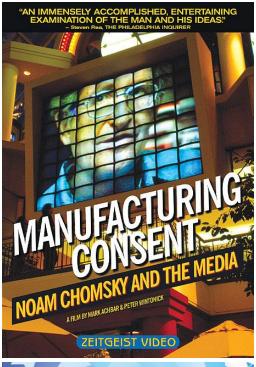


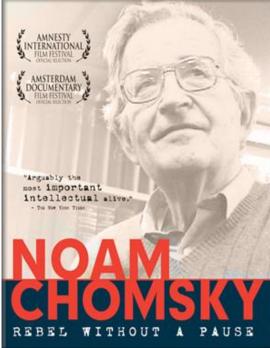






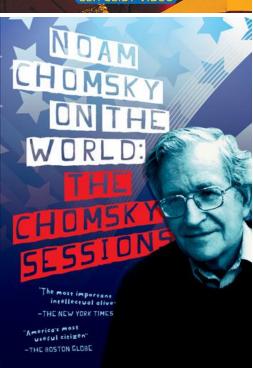


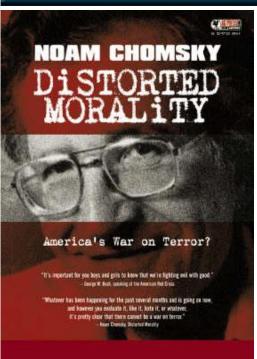


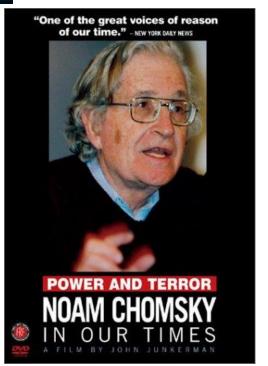


"...I must admit to taking a copy of Noam Chomsky's 'Syntactic Structures' along with me on my honeymoon in 1961 ... Here was a marvelous thing: a mathematical theory of language in which I could use as a computer programmer's intuition!"

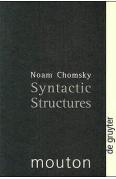
- Don Knuth on Chomsky's influence

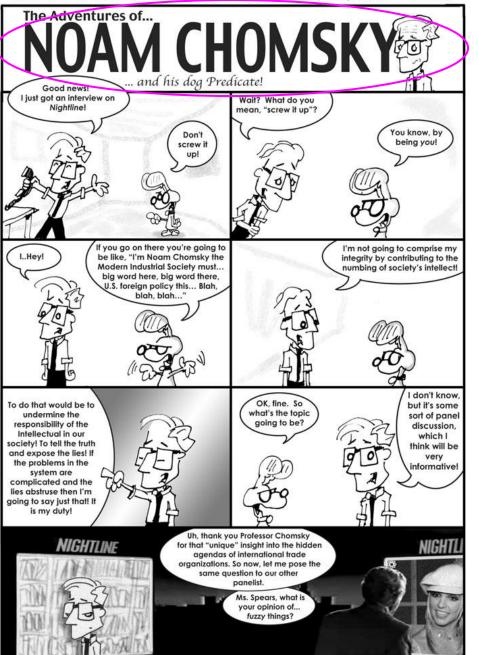






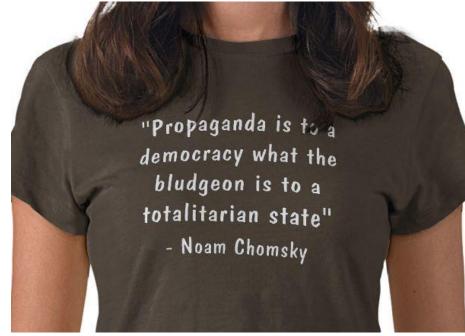




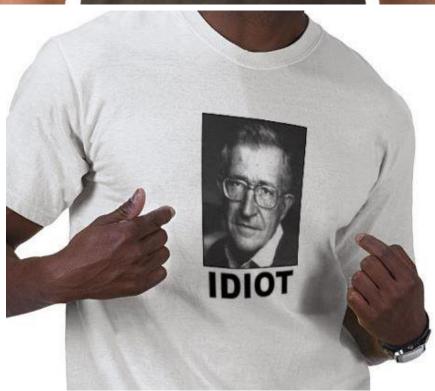




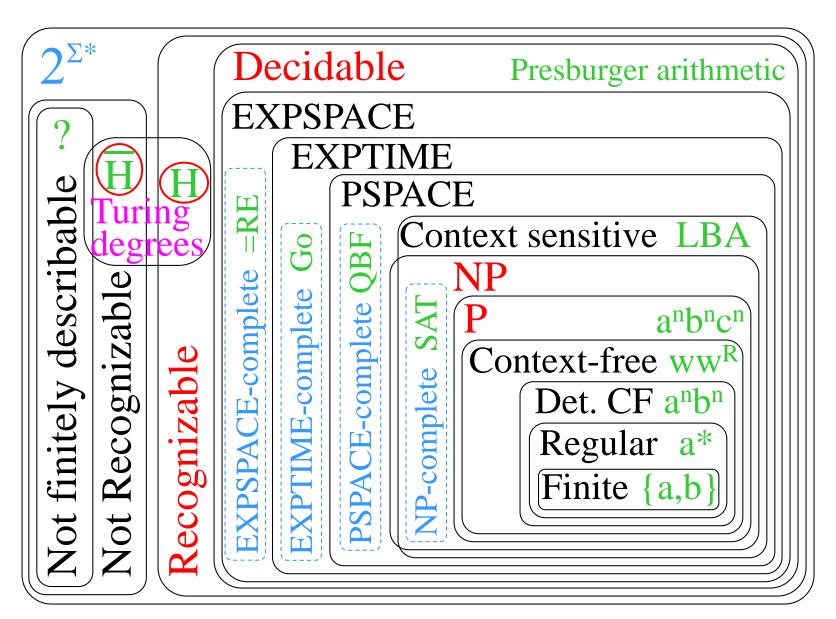


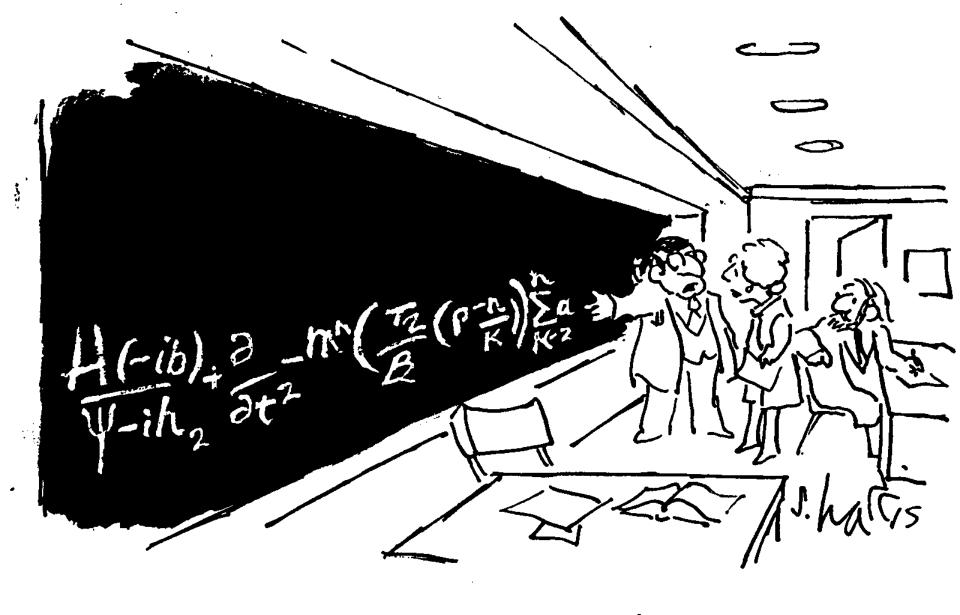






The Chomsky Hierarchy



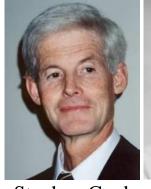


"But this is the simplified version for the general public."

NP Completeness

- Tractability
- Polynomial time









Stephen Cook Leonid Levin Richard Karp

- Computation vs. verification
- Power of non-determinism
- Encodings
- Transformations & reducibilities
- P vs. NP
- "Completeness"





