Hybrid Slicing: Integrating Dynamic Information with Static Analysis

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Program slicing is an effective technique for narrowing the focus of attention to the relevant parts of a program during the debugging process. However, imprecision is a problem in static slices, since they are based on all possible executions that reach a given program point rather than the specific execution under which the program is being debugged. Dynamic slices, based on the specific execution being debugged, are precise but incur high run-time overhead due to the tracing information that is collected during the program’s execution. We present a hybrid slicing technique that integrates dynamic information from a specific execution into a static slice analysis. The hybrid slice produced is more precise than the static slice and less costly than the dynamic slice. The technique exploits dynamic information that is readily available during debugging—namely, breakpoint information and the dynamic call graph. This information is integrated into a static slicing analysis to more accurately estimate the potential paths taken by the program. The breakpoints and call/return points, used as reference points, divide the execution path into intervals. By associating each statement in the slice with an execution interval, hybrid slicing provides information as to when a statement was encountered during execution. Another attractive feature of our approach is that it allows the user to control the cost of hybrid slicing by limiting the amount of dynamic information used in computing the slice. We implemented the hybrid slicing technique to demonstrate the feasibility of our approach.

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General Terms: Algorithms, Experimentation, Theory
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1. INTRODUCTION
Slicing has proven to be a useful tool in the debugging of programs. Static slicing algorithms determine the set of program statements that may affect
the computation of the value of a variable at a specified program point [Agrawal 1994; Choi and Ferrante 1994; Gupta and Soffa 1994; Lyle and Weiser 1987; Weiser 1984]. However, since static slices are computed under all possible executions of the program that reach a specified point, the generated slices are large and imprecise (for a particular execution), which limits their usefulness in practice. Therefore, techniques that improve the precision and reduce the size of the static slice are of significant interest.

One approach for improving the precision of static slices is to employ dynamic slicing [Agrawal and Horgan 1990; Duesterwald et al. 1992b; Korel and Laski 1988]. A dynamic slice is constructed for a fixed input (i.e., for a specific program execution) in contrast to a static slice, which makes no assumptions about the input. However, the construction of a dynamic slice is expensive, since it requires tracing of the program's execution. Therefore, techniques that reduce the expense of dynamic slices without sacrificing too much of the precision are desirable.

An approach to improve the efficiency of dynamic slicing focuses on the use of static information to reduce the run-time overhead by limiting the amount of tracing that is needed during execution [Ball and Larus 1994; Choi et al. 1991; Duesterwald et al. 1992b; Kamkar et al. 1993; Netzer and Weaver 1994]. Information about the program is used to determine a subset of program points that should be traced. Although this approach does reduce the tracing effort, the size of traces can still be quite large.

Our approach in this article is the development of a hybrid slicing technique that integrates a limited amount of dynamic information into a static slicing analysis. The hybrid slice is computed both intraprocedurally and interprocedurally by exploiting information readily available during debugging. Inaccuracies in static slices result from the conservative prediction of potential control flow and data dependencies. Our technique uses dynamic information to more accurately predict control flow and thus eliminate some of the paths that could not have been involved in the specific execution. The particular dynamic information exploited is breakpointing information and dynamic procedure call and return information. The breakpoint information consists of breakpoint positions in the code that are encountered as well as breakpoint positions that are not encountered. For interprocedural slicing, procedure calls and returns are used, including the code position of the call sites.

The hybrid slicing approach improves on the precision of static slicing by computing more accurate and therefore smaller slices. The hybrid slice decomposes the overall slice into subslices by using the dynamic information as reference points, thus dividing the execution path into intervals. Each statement in a slice is associated with the particular execution interval(s) in which it is found. Therefore, the user can examine slices in increments and draw conclusions that cannot be inferred simply by examining an overall static slice, which is the usual approach. Another attractive feature of our approach is that it allows the user to control the cost of slicing by limiting the amount of dynamic information provided to the hybrid slicing algorithm.
The static slicing analysis technique for the computation of hybrid slices is unique in the following two respects. In our analysis, when a dependency being sought is found (e.g., a definition corresponding to a use), it is not immediately assumed to be part of the slice. The algorithm first must ensure that the path on which the dependency is found is feasible with respect to the dynamic information. In order to do so, instead of simply propagating a variable name of interest, the breakpoint or call/return point relative to an execution point is also propagated. The dynamic information and the analysis technique also enable the factoring of the overall slice into subslices and the exclusion of some statements that would have been included if no dynamic information were available.

Intraprocedurally, hybrid slicing degenerates to static slicing if no breakpointing information is provided. It precisely predicts control flow if breakpoints are placed to capture the outcome of each predicate in the program. Hybrid slicing adapts to the user's demands, since more accurate information is provided for program areas that are of most interest to the user, that is, where the user has introduced breakpoints.

We implemented the hybrid slicing technique at both the intraprocedural and interprocedural levels to demonstrate its practicality and effectiveness. We found that the hybrid slice produced is smaller than the static slice and does reduce in size as more breakpoints are added. We also found that there is no measurable difference in execution time between computing static slices and hybrid slices.

Our technique uses the control flow graph as the program representation. Another representation that has been used in slicing is the program dependence graph [Ferrante et al. 1987; Horwitz et al. 1990]. The program dependence graph is not directly applicable to the hybrid slicing technique for it represents control dependence and not control flow. In order to utilize breakpointing information during PDG slicing, a mapping would have to be provided between various points in the control flow graph and the program dependence graph.

Dynamic slicing techniques [Agrawal and Horgan 1990; Duesterwald et al. 1992b; Korel and Laski 1988] can be used to compute precise slices, since accurate control and data flow information can be saved during program execution. Relevant data dependences among statements involving only scalar variables can be accurately determined if the exact program path taken during the execution is known. On the other hand, accurate identification of data dependences in the presence of pointers and arrays requires tracing all read and write operations. Since the breakpoint history used during hybrid slicing only enables us to predict the execution path taken during execution with greater accuracy, its main impact is the improved precision of static slicing for statements involving scalars. In contrast dynamic slicing can also accurately slice programs in the presence of pointers and arrays.

Other approaches to hybrid slicing have been proposed [Choi et al. 1991; Duesterwald et al. 1992a; 1992b; Kamkar et al. 1993; Netzer and Weaver 1994]. These approaches use static information to improve the execution...
time performance of dynamic slicing while maintaining the precision of dynamic slicing. In one approach, dependences that can be computed statically are computed before dynamic slicing and utilized at run-time. Dependences involving array elements or pointers that must be computed at run-time are computed at execution time and recorded in a trace [Duesterwald et al. 1992a; 1992b; Kamkar et al. 1993]. Another approach records only a small amount of trace information during program execution. During debugging, these coarse-grained traces are supplemented with static information to generate fine-grained traces [Choi et al. 1991; Netzer and Weaver 1994].

The notion of a constrained/quasi-static slice is an approach to reduce the size of static slices [Weiser 1984]. An algorithm for computing constrained slices appears in Field et al. [1995]. Constraints on input values are provided, and using this information, a static slice is produced that excludes program executions requiring inputs that do not satisfy the given constraints. In contrast, hybrid slicing integrates dynamic information for improving the precision and cost of slicing during debugging. The usefulness of constrained slicing for understanding legacy codes has been demonstrated in Ning et al. [1994]. While constrained slicing is useful for program understanding, hybrid slicing is more appropriate for program debugging.

A related operation to slicing is chopping [Jackson and Rollins 1994; Reps and Rosay 1995], which computes the elements that cause a program point to have an effect on another program point. It thus provides a more focused approach than slicing for determining the effects of a program point on another. Our approach of using subslices also provides more focused slices according to the program’s execution history.

In Section 2 of this article, we describe the hybrid slicing technique for a single program module that uses breakpoint information. In Section 3 we describe interprocedural slicing that uses call/return information. The algorithms developed for both types of dynamic information can be used separately or combined into a hybrid slicing algorithm that uses both call/return information and breakpoint information to compute the slices. An implementation is briefly described in Section 4, and concluding remarks are given in Section 5.

2. HYBRID SLICING ON A SINGLE PROGRAM MODULE

Program slicing coupled with the breakpointing of a program provides an effective tool for debugging programs. A typical debugging session based upon breakpoints and slicing is characterized as follows:

—The user sets breakpoints and starts the program execution.
—When a breakpoint is encountered, the user examines the values of variables at the breakpoint.
—If the values are as expected, the user resumes the program’s execution. However, before resuming execution the user may disable some existing breakpoints and add new ones.
If the values are incorrect, the user requests slicing information for selected variables to locate the potential cause of the error.

The debugging session continues in this way. However, there is no attempt during the slicing to use the occurrence of a prior breakpoint or the nonoccurrence of a breakpoint in computing the slice or to provide more specific information as to whether a statement was encountered before or after a prior breakpoint. Thus, in our approach to slicing we have two primary goals. One goal is to provide the user with more accurate slices; that is, we would like to exclude statements that could not have affected the values of requested variables at the breakpoint, given the particular execution. Another goal is to split the overall slice into subslices corresponding to relevant statements that could have been executed between every successive pair of breakpoints encountered so far. This approach allows the user to follow the execution of the program as it occurred and therefore leads to a better understanding of how the values of selected variables were computed. For example, if the same statement is executed multiple times, it may be included in multiple subslices. Our approach in computing hybrid slices is to save the breakpoint positions and use them in the computation of more accurate slices as well as in the splitting of a slice into subslices.

In order to define the form of the breakpoint history, we view the program execution as consisting of a series of intervals where each interval represents the execution between two successive breakpoints encountered during the execution. Consider an execution interval during which a set of breakpoints $B$ was active (i.e., set). Further assume that the interval was terminated when a breakpoint $b \in B$ was encountered. The history associated with this execution interval is a pair of the form $(b, N = B - \{b\})$, where $b$ is the breakpoint encountered at the end of the execution interval, and $N$ is the set of breakpoints that were active but not encountered during the interval. The overall breakpoint history is composed of the breakpoint histories of individual execution intervals. The overall hybrid slice is composed of the hybrid subslices corresponding to the execution intervals. The computation of a hybrid slice is initiated with respect to values of variables at the most recent breakpoint. A more precise definition of the breakpoint history and hybrid slices follows.

**Definition 2.1.** The **breakpoint history** of a program execution is of the form

$$BH = \langle (b_0, \phi), (b_1, N_1 = B_1 - \{b_1\}), \ldots (b_m, N_m = B_m - \{b_m\}) \rangle,$$

where $b_0$ is the start node of the program; $b_m$ is the latest breakpoint encountered; $B_i$ is the set of breakpoints that were active during the execution interval from breakpoint $b_{i-1}$ to $b_i$; and $N_i$ is the set of breakpoints that were active but not encountered during the execution interval from $b_{i-1}$ to $b_i$. 
Definition 2.2. A slicing criterion is of the form \( SC = (V, b) \), where \( V \) is a set of variables whose values are of interest at breakpoint \( b \).

Definition 2.3. For a given breakpoint history, \( BH = ((b_0, \phi), (b_1, N_1), \ldots (b_m, N_m)) \), the hybrid slice with respect to a slicing criterion \( SC = (V, b_m) \) is defined as follows:

\[
HSLICE(b_0, b_m) \leftarrow \bigcup_{i=1}^{m} HSLICE(b_{i-1}, b_i),
\]

where \( HSLICE(b_{i-1}, b_i) \) contains those statements that were possibly executed after breakpoint \( b_{i-1} \) and prior to breakpoint \( b_i \) and where their execution, directly or indirectly, influenced the computation of the value of some variable in \( V \) at \( b_m \). The statements that influence the computation of a variable are computed by taking the transitive closure over both data and control dependences. Data slices are computed by taking the transitive closure over only data dependences.

As the breakpoint history for a given program execution grows, so does the number of subslices computed by the hybrid slicing algorithm. The complexity of computing hybrid slices can be limited by restricting the size of the breakpoint history. It is reasonable to expect that the subslices corresponding to the recent breakpoints are of more interest to the user than the earlier ones. Therefore the size of the history can be limited by considering the recent breakpoints and eliminating the earlier breakpoints. For example, let us assume that the complete breakpointing history under a program execution is given by \( BH = ((b_0, \phi), (b_1, N_1), \ldots (b_m, N_m)) \). We can replace this history by the following shortened breakpoint history:

\[
SBH = \left( (b_0, \phi), (b_{m-\Delta-1}, N_{m-\Delta-1} = \bigcap_{i=1}^{m-\Delta-1} N_i), (b_{m-\Delta}, N_{m-\Delta}) \ldots (b_m, N_m) \right).
\]

The shortened history only considers the most recent \( \Delta \) breakpoints. The consequence of this approach is that the accuracy of the subslice corresponding to the execution from \( b_0 \) to \( b_{m-\Delta-1} \) is sacrificed to limit the cost of computing hybrid slices. In fact the subslice for interval \( b_0 \) to \( b_{m-\Delta-1} \) degenerates to the static slice for that interval. The breakpoints in set \( N_{m-\Delta-1} \) of the shortened history include all those breakpoints that were set and never encountered for the program’s execution up to breakpoint \( b_{m-\Delta-1} \).

The example in Figure 1 illustrates the usefulness of hybrid slices. We set breakpoints at statements 4, 9, 10, and 11 before the program execution begins (see Figure 1(a)). The results of computing hybrid data slices for a number of breakpoint histories are shown in Figure 1(b). We focus on the computation of the hybrid slice for variable \( X \) when the breakpoint at statement 11 is encountered. First consider the execution in which no
A breakpoint other than 11 was encountered (see row 1 of Figure 1(b)). Our algorithm is able to utilize this information to conclude that the value of $X$ at 11 is the value that was read at statement 1, and therefore the hybrid

**Fig. 1. Examples of hybrid data slices.**

<table>
<thead>
<tr>
<th>Breakpoints Encountered</th>
<th>Hybrid Subslices</th>
<th>Hybrid Slices</th>
</tr>
</thead>
<tbody>
<tr>
<td>0, 11</td>
<td>HSLICE(0, 11)={1}</td>
<td>HSLICE(0, 11)={1}</td>
</tr>
<tr>
<td>0, 4, 11</td>
<td>HSLICE(0, 4)={1}  \ HSLICE(4, 11)={6}</td>
<td>HSLICE(0, 11)={1, 6}</td>
</tr>
<tr>
<td>0, 4, 10, 11</td>
<td>HSLICE(0, 4)={1, 2}  \ HSLICE(4, 10)={4, 6}  \ HSLICE(10, 11)={10}</td>
<td>HSLICE(0, 11)={1, 2, 4, 6, 10}</td>
</tr>
<tr>
<td>0, 4, 9, 10, 9, 11</td>
<td>HSLICE(0, 4)={1, 2}  \ HSLICE(4, 9)={4, 6}  \ HSLICE(9, 10)={9}  \ HSLICE(10, 9)={10}  \ HSLICE(9, 11)={9}</td>
<td>HSLICE(0, 11)={1, 2, 4, 6, 9, 10}</td>
</tr>
</tbody>
</table>
slice contains only statement 1. On the other hand, a static data-slicing algorithm will report that statements 1, 2, 4, 5, 6, 9, and 10 are all part of the data slice. Therefore by using breakpointing history, the sizes of slices can be considerably reduced.

Let us consider the last data slice shown in Figure 1(b) (row 4). In this execution the overall hybrid slice contains all statements that are in the static slice except for statement 5. By using the breakpoint history, we can determine that the path through node 5 could not have been executed. By examining the subslices in the example, we obtain useful information about the execution of the program. The subslices show that the values of X and Y are initialized at statements 1 and 2 and then updated at statements 6 and 4, respectively. Next the value of X is modified at statement 9. Using this current value of X and the value of Y from statement 4, a new value of X is computed at statement 10. Finally at statement 9 the value of X is updated again, which is then available at statement 11. It should be noted that statement 9 is encountered twice during the execution and therefore contained in 2 subslices. As we can see from this example, by providing subslices we allow the user to understand the flow of values including those values computed during the execution of loops. This flow of values could not have been inferred by simply examining an overall slice for a single module.

Let us now illustrate the effect of shortening the histories on the quality of slicing information. Let us assume that the last history in Figure 1(b) has been shortened to only include the two latest breakpoints, i.e., \( \Delta \) is set to two, and the breakpoints 4, 9, and 10 are no longer part of the history. Using the shortened history we obtain the subslices \( HSLICE(9, 11) = \{9\} \) and \( HSLICE(0, 9) = \{1, 2, 4, 5, 6, 9, 10\} \). As we can see, the subslice \( HSLICE(9, 11) \) is the same as it was for the complete history. However, the slice \( HSLICE(0, 9) \) has increased in size, since an additional statement, statement 5, has been included in the subslice. Thus, the precision of the subslice corresponding to the period of execution over which the history is not maintained is reduced, while the precision of the subslice for the period of execution over which the history is maintained is not affected.

Next we develop the algorithms for computing hybrid slices by first focusing on the computation of data slices. The key problem to be solved for the computation of data slices is that of identifying those immediate data dependences (i.e., use to a definition) that can be established along a path that is feasible under the given breakpointing history. Intuitively, a path is said to be feasible with respect to a breakpoint history if it visits the encountered breakpoints in the appropriate order and if it does not visit the breakpoints that were not encountered in the corresponding execution intervals. In the computation of static slices all paths to a point are considered feasible. In contrast, during hybrid slicing only a subset of such paths are considered feasible. Once an algorithm for identifying immediate dependences has been developed, it can be repeatedly applied for computing the transitive closure over the data dependences.

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Definition 2.4. Given a breakpoint history, \( BH = \langle (b_0, \phi), (b_1, N_1), \ldots (b_m, N_m) \rangle \), a path \( P \) from \( b_0 \) to \( b_m \) is feasible if and only if path \( P \) is composed of subpaths as follows:

\[
P = \text{PATH}(b_0 ; b_1).\text{PATH}(b_1 ; b_2). \cdots \text{PATH}(b_{m-1} ; b_m)
\]

such that, for \( 1 \leq i \leq m \), \( \text{NODES}(\text{PATH}(b_{i-1} ; b_i)) \cap N_i = \phi \), where \( \text{NODES}(\text{PATH}(b_{i-1} ; b_i)) \) includes all nodes along the path from \( b_{i-1} \) to \( b_i \) excluding the endpoints \( b_{i-1} \) and \( b_i \).

Let us assume that we are interested in the slice for variable \( v \) at statement \( s \) when \( s \) is encountered after \( b_{i-1} \) and before \( b_i \) during execution. Further assume that \( s \) is reachable from the definition of variable \( v \) at statement \( s' \). The statement \( s' \) is included in subslice \( \text{HSLICE}(b_{j-1}, b_j) \), where \( j \leq i \), if and only if there exists a feasible path \( P \) such that

— the subpath \( \text{PATH}(b_{j-1} ; b_j) \) in \( P \) contains \( s' \) and
— the subpath from \( s' \) to \( s \) in \( P \) is definition clear with respect to variable \( v \).

The algorithm we present computes immediate data dependences in two steps: detection and verification. The detection step takes as its initial input triples of the form \( (v, s, b_m) \), indicating an interest in the value of variable \( v \) immediately preceding statement \( s \), which is where the latest breakpoint \( b_m \) occurred. In the process of taking the closure over data dependences, a triple \( (v, s, b_j) \) is considered if variable \( v \) is used by statement \( s \) and if statement \( s \) has been included in the hybrid subslice \( \text{HSLICE}(b_{j-1}, b_j) \). The output of the detection step is a set of pairs of the form \( (s', b_j) \) such that there is a path from \( s' \) to \( s \) through which a definition of variable \( v \) in \( s' \) reaches statement \( s \). In addition, this path is feasible with respect to the portion of breakpoint history \( (b_j, N_j), (b_{j+1}, N_{j+1}), \ldots, (b_i, N_i) \). The verification step ensures that there is a path from \( b_{j-1} \) to \( b_j \) along which \( s' \) is encountered, therefore implying that \( s' \) should be included in the slice. In order to take the transitive closure over data dependences, new criteria are generated from the statements included in the slice, and the above steps are repeated.

Our presentation of the hybrid slicing algorithm is organized into three algorithms. The algorithm \( \text{ComputeTentativeSlice} \) implements the detection step, and the algorithm \( \text{ComputeActualSlice} \) implements the verification step. The algorithm \( \text{ComputeHybridSlice} \) in Figure 2 calls these algorithms repeatedly to compute the transitive closure over data dependences. The input to algorithm \( \text{ComputeHybridSlice} \) is the breakpointing history \( (BH) \) and slicing criterion \( (SC) \). Based upon the slicing criterion a set of triples is generated. The immediate data dependences corresponding to these triples are detected by \( \text{ComputeTentativeSlice} \), and a set of pairs is generated for \( \text{ComputeActualSlice} \). The pairs that are successfully verified by \( \text{ComputeActualSlice} \) are included in the appropriate subslices. From the newly added statements to the slice, new sets of triples are generated for the transitive closure, and the above steps are repeated until no more statements are added to the slice. The algorithm \( \text{ComputeHybridSlice} \) also
initializes the data flow sets for algorithms ComputeTentativeSlice and ComputeActualSlice to process a given set of triples and pairs respectively.

The algorithm ComputeTentativeSlice (Figure 3) performs backward propagation of variables whose definitions are being sought, based on the slicing criterion. The data flow sets corresponding to the entry and exit of a node \( n \) are denoted by \( \text{VAR}_{en}^{all}[n] \) and \( \text{VAR}_{ex}^{all}[n] \). Each variable \( v \) in a data flow set is associated with a breakpoint \( b_i \), which indicates that the search for the definition of \( v \) has progressed to a point prior to the execution of \( b_i \). Therefore during propagation, if this variable reaches the statement that is the breakpoint \( b_{i-1} \), then the propagated breakpoint is modified to \( b_{i-1} \) as it is propagated past breakpoint \( b_{i-1} \) (see lines 15–17). On the other hand, if the variable reaches a statement in \( N_i \), then its propagation is discontinued, since this implies the path is infeasible (in line 9 \( \text{VAR}_{ex}^{all}[n] \) is the feasible subset of \( \text{VAR}_{ex}^{all}[n] \)). Finally when variable \( v \) reaches a definition of \( v \), we examine the associated breakpoint. If the associated breakpoint is \( b_j \), then the statement becomes a potential candidate for inclusion in subslice \( \text{HSLICE}(b_{j-1}, b_j) \).

The algorithm ComputeActualSlice (Figure 4) performs backward propagation of statements that are potential candidates for inclusion in the slice. The data flow sets corresponding to the entry and exit of a node \( n \) are denoted by \( \text{THSLICE}_{en}^{all}[n] \) and \( \text{THSLICE}_{ex}^{all}[n] \). A statement \( s \) with associated breakpoint \( b_i \) is included in subslice \( \text{HSLICE}(b_{i-1}, b_i) \) if a path from \( b_{i-1} \) to statement \( s \) can be found along which no node from \( N_i \) is encountered. Therefore if the statement \( s \) reaches a statement in \( N_i \), then its

Fig. 2. Overview of hybrid slicing algorithm.
propagation is discontinued, since this implies that we are on an infeasible path (in line 14, \( \text{THSLICE}^{f}_{\text{ex}}[n] \) is the feasible subset of \( \text{THSLICE}^{all}_{\text{ex}}[n] \)). Once a statement is included in subslice \( \text{HSLICE}(b_{i-1}, b_i) \), new triples are generated corresponding to variables referenced by the statement so that the transitive closure over data dependences can be computed (see line 6).

Next let us consider the control dependences in the computation of slices. Given a statement \( s \) that has just been included in subslice \( \text{HSLICE}(b_{i-1}, b_i) \), the algorithm \text{ComputeControlTriples} in Figure 5 describes the treatment of control dependences involving \( s \). An immediate control ancestor of \( s \), say \( c \), must be included in the hybrid slice, i.e., \( s \) is control dependent on \( c \). However, we must first determine the subslice in which \( c \) must be placed. It is possible that \( c \) may be placed in a subslice several breakpoints back as these breakpoints may have been encountered since the execution of \( c \) and prior to the execution of \( s \). The predicate \( c \) along with breakpoint \( b_i \) is propagated backward starting at statement \( s \). The data flow sets corresponding to the entry and exit of a node \( n \) are denoted by \( \text{CD}^{all}_{\text{ex}}[n] \) and \( \text{CD}_{\text{ex}}[n] \). The propagation along infeasible paths is avoided (see line 12), and breakpoints associated with the statements being propagated are appropriately modified during propagation (see lines 14–16). In each data flow set only the maximum \( k \) for which \((c, b_k)\) is added to the set is retained, for we are interested in the latest execution of \( c \) preceding the execution of \( s \). Finally, the data flow set at the predicated node \( c \) is examined, and \( c \) is

Fig. 3. Identification of potential statements in the slice.
1. algorithm ComputeActualSlice ( )
2. while Tslicerlist ≠ Ø do
3. get n from the Tslicerlist
4. for each \((s, b_i) \in THS\text{LIC}E_{en}^{all}[n]\) and \(b_{i-1} = n\) do
5. \(HSLICE(b_{i-1}, b_i) \leftarrow HSLICE(b_{i-1}, b_i) \cup \{(s)\}\)
6. Generate new triples for taking closure over data dependencies.
7. if \(s = b_{i-1}\) then triples \(\leftarrow\) triples \(\cup\{(v, s, b_{i-1}) : v \in \text{Ref}(s)\}\)
8. else triples \(\leftarrow\) triples \(\cup\{(v, s, b_i) : v \in \text{Ref}(s)\}\) endif
9. if closure over control dependencies is also required then
10. ComputeControlTriples\((s \in HSLICE(b_{i-1}, b_i))\)
11. endif
12. end for
13. for each predecessor \(p \in \text{Pred}(n)\) do
14. if \(THS\text{LIC}E_{ex}^{all}[n] \not\subset THS\text{LIC}E_{ex}^{all}[p]\) then
15. \(THS\text{LIC}E_{ex}^{all}[p] \leftarrow THS\text{LIC}E_{ex}^{all}[p] \cup THS\text{LIC}E_{ex}^{all}[n]\)
16. Eliminate (statement, breakpoint) pairs inconsistent with breakpoint history.
17. end if
18. end for
19. endwhile
20. end ComputeActualSlice

Fig. 4. Identification of actual statements in the slice.

included in the subslice \(HSLICE(b_{k-1}, b_k)\) such that \((c, b_k)\) is contained in the data flow set at the entry of predicate \(c\) (see line 21). Once a statement is included in a slice the appropriate triples are generated for further processing (see line 22). The algorithm \(\text{ComputeControlTriples}\) calls itself recursively, since we must take the transitive closure over control dependences (see line 23).

Figures 6 and 7 illustrate the computation of a hybrid data slice for the third breakpoint history of the example in Figure 1. The computation of the data slice takes three iterations. The pairs/triples resulting from each invocation of the detection/verification step are shown in Figure 6. In the first detection step starting from statement 11, definitions of \(X\) in statements 1, 6, and 10 are identified, and during the verification step statement 10 is included in the slice, while statements 1 and 6 are discarded. Statement 10 uses variables \(X\) and \(Y\) whose definitions are sought in the next iteration. Definitions in statements 1, 4, 5, and 6 are detected, and during the verification step statements 4 and 6 are included in the slice. The statements 6 and 4 reference variables \(X\) and \(Y\) respectively, and in the final iteration the definitions in statements 1 and 2 are included in the slice.

Next we illustrate the treatment of control dependences. Let us consider the last breakpoint history for which the hybrid data slice is shown in Figure 1(b). Consider the invocation \(\text{ComputeControlTriples}(9 \in HSLICE(b_4, b_5))\). Based upon these results predicate 8, which is the immediate
control predecessor of 9, is included in subslice $HSLICE(b_3, b_4)$ (Figure 8). The predicate 8 is included in subslice $HSLICE(b_3, b_4)$ because it was executed during the period of execution that corresponds to this subslice. Once predicate 8 has been included, the algorithm is recursively invoked to compute the transitive closure over control dependences. Also, triples are generated for later processing for variables referenced in 8 to take the closure over data dependences.

**Complexity Analysis of Data Slicing.** For the purpose of this analysis we assume that the program contains $V$ variables, $N$ statements (and the number of statements is of the same order as the number of edges), and that $d$ is the maximum depth of loop nests. We further assume that $B$ is the number of breakpoints in the history. During the detection step the maximum size of a data flow set is $B \times V$. Thus, a single operation on the data flow set requires at most $O(B \times V)$ time. Each node may be examined $MAX(d + 1, B)$ times until the data flow stabilizes. Thus the cost of the detection step is bounded by $O(MAX(d + 1, B) \times N \times B \times V)$. Since the number of source variables is typically smaller than the number of source statements, the time for the detection step is bounded by $O((d + 1) \times N^2 \times V)$.
The size of a data flow set during the verification step is bounded by $N \times B$, and the number of times each node may be examined is bounded by $d + 1$. Thus the cost of the verification step is bounded by $O((d + 1) \times N^2 \times B)$. The total cost of the two steps is therefore given by $O(\text{MAX}(d + 1, B) \times N^2 \times B)$. Since typically $d$ is a small number, it is reasonable to assume that $\text{MAX}(d + 1, B)$ is equal to $B$. Thus, the worst-case cost of the two steps can be considered to be $O(B^2 \times N^2)$. Since the size of a hybrid slice is bounded by $B \times N$, the maximum number of times the detection and verification steps are repeated is also bounded by this value. Therefore the total cost of computing data hybrid slices is $O(B^3 \times N^3)$.

Fig. 6. Detailed example.
From the above analysis it is clear that the complexity of hybrid slicing increases with the length of breakpoint history. Thus, the ability of our approach to allow the use of shortened histories is significant. On the other hand the complexity of dynamic slicing cannot be controlled in the above fashion. In order to obtain precise dynamic slices and subslices for programs with only scalar references, the dynamic trace of all conditional branches must be kept so that the program’s execution path is completely known. In contrast, during hybrid slicing, the breakpoint history is likely to
contain a small subset of recently executed conditional branches. The computation of precise dynamic slices in the presence of pointers and arrays would require a significantly larger overhead for tracing read and write operations by all statements. Thus, while dynamic slicing enables computation of precise slices, the run-time complexity of computing dynamic slices is significantly higher than hybrid slicing.

3. INTERPROCEDURAL HYBRID SLICING

Conceptually the hybrid slicing algorithm using breakpoint history can be extended to interprocedural hybrid slicing. However, this straightforward extension could not adequately handle the calling contexts of procedures and thus would introduce a new source of imprecision in the slice. The interprocedural hybrid slicing that we present uses the dynamic call and return information to correctly handle the calling-context problem. A combination of breakpoints and call/return information can also be used in the definition of the interprocedural hybrid slice. However, to simplify the presentation of the algorithms in this section, we focus on the use of only call/return information to define the interprocedural hybrid slice. In this case, construction of the hybrid slice is guided by the procedure calls and returns. As was the case for breakpoint hybrid slices, the call/return hybrid slices provide more precise information than static slices and provide subslices that give more detailed information as to where in the call/return sequence a particular statement may have been executed.

We first present definitions based on the use of call/return information and then give the algorithms, which are similar to those for breakpoint hybrid slicing. Our algorithms handle local and global variables, reference parameters, and aliases.

**Definition 3.1.** The call history of a program execution is of the form $CH = <CR_0, CR_1, \ldots, CR_m>$, where $CR_i$ is either a procedure call or a return from a procedure, and $CR_0$ is assumed to be a call to start execution of the main program. The forms of call and return are

$\text{CALL}[P_{caller} \rightarrow P_{callee} \text{ at } s]$: indicates that procedure $P_{caller}$ calls procedure $P_{callee}$ at statement $s$.

$\text{RET}[P_{callee} \rightarrow P_{caller} \text{ at } s]$: indicates a return from $P_{callee}$ to $P_{caller}$ at statement $s$ (call site of $P_{callee}$ in $P_{caller}$).

**Definition 3.2.** For a calling history, $CH = <CR_0, CR_1, \ldots, CR_m>$, the overall hybrid slice with respect to a slicing criterion $SC = (V, CR_m)$ is defined as follows:

$$HSLICE(CR_m) \leftarrow \bigcup_{i=1}^{m} HSSLICE(CR_{i-1}, CR_i)$$
where subslice $HSSLICE(CR_{i-1}, CR_i)$ contains those statements that were possibly executed after $CR_{i-1}$ and before $CR_i$, and their execution, directly or indirectly, influenced the computation of the value of some variable in $V$ at $CR_m$.

During the propagation of data flow information across procedure boundaries, the mapping from actuals to formals across a call site and the reverse mapping from formals to actuals at procedure entry are needed. The bindings are obtained by examining the appropriate call site. If $bind$ or $bind^{-1}$ is called with a variable that is not an actual argument or formal parameter, the function returns that variable (used for globals).

Again, we concentrate on data slices in the description of the call/return hybrid slice. Consider the example program given in Figure 9, which consists of a main program and four procedures. Assume the call/return history and the slicing criterion of variable $d$ at statement 28 as given in Figure 9. If static slices are obtained using Weiser’s interprocedural slicing technique [Weiser 1984], which does not take into account the calling contexts of the calls, the following slice is computed: {2, 3, 6, 11, 12, 15, 16, 20, 27, 30}. If a static slice is computed using the calling context [Horwitz et al. 1990; Kamkar et al. 1993], more precise information can be found. Using the calling context, only the call site related to the call is processed. Thus, statement 6 would not be included as part of the slice, as $P_2$ in statement 7 is not a possible call site. Thus, statement 3 defining $y$ would not be included in the slice. Using the calling context, the slice consists of the following statements: {2, 11, 12, 15, 16, 20, 27, 30}.

Using our technique, we are able to compute the precise slice: {2, 11, 12, 16, 20, 27}. In the hybrid slice, statement 15 is not a part of the slice, as this statement is not executed in the above calling sequence for the example program. The path containing the call to $P_2$ at statement 14 is the path that is executed. Likewise, all of the statements in procedure $P_4$ would not be included, as the path where the call to $P_4$ is found is not executed (statement 23). Both of these conditions can be determined by using the dynamic call/return information.

As was the case in the hybrid slicing using breakpoints, we can also construct subslices that indicate where in the call/return history a particular statement could be executed. The subslices computed by our algorithm for the example are also given in Figure 9. Using the subslices, we see that statement 16 appeared on the slice between $CR_5$ and $CR_6$. Thus, the assignment statement is executed after $P_2$ returns to $P_1$ at call site 14, but before $P_1$ calls $P_3$ at statement 17. Statement 27 appears in two subslices. It was executed after $P_2$ called $P_3$ at call site 22, but before $P_3$ returned to $P_2$, that is, between $CR_3$ and $CR_4$. It was also on the execution path after $P_1$ called $P_3$ at call site 17, but before the breakpoint in $P_3$, that is, between $CR_6$ and $CR_7$. This type of detailed information could help the user pinpoint the occurrence of definitions of variables during debugging.

The technique to compute the hybrid slice using call/return history closely follows that of the breakpoint hybrid slices. However, instead of
breakpoints, calls and returns, including the call sites, are used. Initially we do not consider parameter aliasing, but later we show how it can be incorporated.

Fig. 9. Examples of interprocedural hybrid data slices.
Given a call/return history, we define a feasible path as follows:

**Definition 3.3.** Given a call/return history, \( CH = \langle CR_0, CR_1, \ldots, CR_m \rangle \), a path from \( CR_0 \) to \( CR_m \) is feasible if and only if path \( P \) is composed of the following subpaths:

\[
P = \text{PATH}(CR_0 ; CR_1).\text{PATH}(CR_1 ; CR_2).\cdots\text{PATH}(CR_{m-1} ; CR_m),
\]

such that for \( 1 \leq i \leq m \)
- if \( CR_{i-1} \) is a call and \( CR_i \) is a call then \( P^{-1}_{\text{callee}} = P_{\text{caller}} \);
- if \( CR_{i-1} \) is a call and \( CR_i \) is a return then \( P^{-1}_{\text{caller}} = P_{\text{callee}} \) and \( P^{-1}_{\text{callee}} = P_{\text{caller}} \);
- if \( CR_{i-1} \) is a return and \( CR_i \) is a call then \( P^{-1}_{\text{callee}} = P_{\text{caller}} \); and
- if \( CR_{i-1} \) is a return and \( CR_i \) is a return then \( P^{-1}_{\text{call}} = P_{\text{call}} \).

The overall algorithm for interprocedural slicing, \( \text{ComputeInterHybridSlice} \), uses the phases \( \text{ComputeInterTentativeSlice} \) and \( \text{ComputeInterActualSlice} \), which are similar to the phases used in the computation of the hybrid slice using breakpoint history hybrid slice, as are the same data flow sets used. However, in the hybrid interprocedural slicing algorithms, the points of interest are procedure call, entry, and exit points where propagation starts or terminates. In the remainder of the section we provide a brief overview of the algorithms. The detailed algorithms are presented in Figures 10, 11, and 12.

The algorithm \( \text{ComputeInterHybridSlice} \) (Figure 10) iteratively calls algorithms \( \text{ComputeInterTentativeSlice} \) and \( \text{ComputeInterActualSlice} \) to compute the hybrid slice. The algorithm \( \text{ComputeInterTentativeSlice} \) (Figure 11) propagates variables and call/return history points backward until either an entry of the current procedure \( P \) is reached, a call to a procedure is reached, or an assignment to a variable being sliced is encountered. If a call statement is reached, then the call/return history is checked to see if this call matches a return in the history point. If so, variables are bound to the formals in the called procedure; and if the variable being sliced is involved, then the VAR set at the end of the procedure being called is updated, and the appropriate nodes from the procedure are placed on the list for slicing. If the node encountered is an entry node of a procedure, the call/return history is checked to determine if this procedure was called at the appropriate call history point. If so, the variables being sliced are bound by a reverse binding of formals to actuals, and propagation continues at the call point, as determined by the call site information in the call/return history. When a statement is encountered that defines a variable being sliced, a pair is generated, and propagation for this variable terminates. A pair consists of a statement and the call/return history point. If a variable in the criterion is not defined in a procedure, propagation continues in the calling procedure, and the history point is updated to include a previous call return point, that is \( CR_i \rightarrow CR_{i-1} \). \( \text{Findhistory} \) on line 13 in the algorithm is a routine that checks the call/return history to
determine the appropriate point whenever a pair is propagated over a call site. That is, if the slicing variable is a reference parameter that is not included in a particular call, say to $P_s$, then the slicing is not done on $P_s$. The CR point in the pair has to be updated to reflect the number of procedure calls and returns that are being skipped. The history can be checked to match the calls and returns that are found in the history until the correct program point is found.

In the algorithm $\text{ComputeInterActualSlice}$, entry and call nodes are again treated as nodes of interest (see Figure 12). The pairs, each consisting of a statement and the call/return history point and which were found in the $\text{ComputeInterTentativeSlice}$ algorithm, are propagated until it can be determined whether the statement reaches the next valid call/return point and should be included in the slice. When the statement reaches a call or entry point, the call/return history is checked to determine if the node reached is on a feasible path. If so, the statement is added to the slice, and triples are generated for any variables used in the statement being added. Included in the slice is the call/return point where the statement was encountered.

Consider the example given in Figure 9 with the criterion ($d$ at statement 28) and the call and return history given in the example. The definition of $d$ in statement 27 is identified as being a potential statement in the slice associated with the call to $P_3$ from $P_1$ at statement 17. In the algorithm $\text{ComputeInterActualSlice}$, statement 27 along with $CR_7$ is propagated until the entry of procedure $P_3$ is reached. The call/return history is consulted, and the call is identified as being on a valid path so the statement is put in the slice.
the slice. The reference to \( d \) in the statement is bound to the actual parameter \( a \) at the call site (statement 17), and this \( a \), along with the previous call/return point, \( CR_6 \), becomes the slicing criterion in the next phase. Slicing continues from statement 17 using \textit{ComputeInterTentativeSlice}, finding statement 16, to be a potential statement to be added to the slice. The \textit{ComputeInterActualSlice} determines if statement 16 is on a valid path. Finding a call to \( P_2 \) in node 14, which matches the history, it puts statement 16 in the slice. Slicing continues with \textit{ComputeInterTentativeSlice}, with the transitive closure of variables in this statement, which are \( a \) and \( z \). When \textit{ComputeInterTentativeSlice} takes the path through node 15 and propagates the statement 15 defining \( z \), it finds the entry node. A check of the call/return history finds that this is an invalid path and that

![Algorithm ComputeInterTentativeSlice](image)

\[ \text{Algorithm ComputeInterTentativeSlice}() \]
\[
\begin{align*}
1. & \text{while } Varlist \neq \phi \text{ do} \\
2. & \quad \text{get } n \text{ from } Varlist \\
3. & \quad NEWVAR \leftarrow \bigcup_{w \in \text{succ}(n)} \text{VAR}_{\text{en}}^{\text{all}}[w] \\
4. & \quad \text{if } NEWVAR \not\subseteq \text{VAR}_{\text{en}}^{\text{all}}[n] \text{ then} \\
5. & \quad \quad \text{VAR}_{\text{en}}^{\text{all}}[n] \leftarrow \text{VAR}_{\text{en}}^{\text{all}}[n] \cup NEWVAR \\
6. & \quad \text{if } n \text{ is a call statement to } P_f \text{ then} \\
7. & \quad \quad \text{for each } (v, CR_i) \in \text{VAR}_{\text{en}}^{\text{all}}[n] \text{ at } CR_{i-1} = \text{Return from } P_f \text{ to } P_{\text{current}} \text{ at } n \text{ do} \\
8. & \quad \quad \quad \text{Propagate (variable,call-return) pairs to the exit of the callee,} \\
9. & \quad \quad \quad \quad \text{if callc is consistent with call-return history.} \\
10. & \quad \quad \quad \quad \text{if } v \in \text{actualls of } P_f \text{ or global variables then} \\
11. & \quad \quad \quad \quad \quad \text{VAR}_{\text{en}}^{\text{all}}[\text{exit of } P_f] \leftarrow \text{VAR}_{\text{en}}^{\text{all}}[\text{exit of } P_f] \cup \{(\text{bind}, v, CR_{i-1})\} \\
12. & \quad \quad \quad \quad \text{else} \\
13. & \quad \quad \quad \quad \quad \text{VAR}_{\text{en}}^{\text{all}}[n] \leftarrow \text{VAR}_{\text{en}}^{\text{all}}[n] \cup \{(v, \text{findhistory}(CR_i))\} \\
14. & \quad \quad \text{Varlist } \leftarrow \text{Varlist} \cup \text{Pred}(n) \\
15. & \quad \text{endfor} \\
16. & \quad \text{elseif } n \text{ is the entry node of the procedure } P_{\text{current}} \text{ then} \\
17. & \quad \quad \text{for each } (v, CR_i) \in \text{VAR}_{\text{en}}^{\text{all}}[n] \text{ at } CR_{i-1} = \text{Call } P_f \text{ to } P_{\text{current}} \text{ at } s \text{ do} \\
18. & \quad \quad \quad \text{if } v \in \text{formals of } P_{\text{current}} \text{ or global variables then} \\
19. & \quad \quad \quad \quad \text{Propagate (variable,call-return) pairs to the call site in the caller,} \\
20. & \quad \quad \quad \quad \quad \text{if the caller is consistent with call-return history.} \\
21. & \quad \quad \quad \quad \quad \text{VAR}_{\text{en}}^{\text{all}}[s] \leftarrow \text{VAR}_{\text{en}}^{\text{all}}[s] \cup \{(\text{bind}^{-1}, v, CR_{i-1})\} \\
22. & \quad \quad \text{Varlist } \leftarrow \text{Varlist} \cup \text{Pred}(s) \\
23. & \quad \text{endfor} \\
24. & \quad \text{else} \\
25. & \quad \quad \text{VAR}_{\text{en}}^{\text{all}}[n] \leftarrow \text{VAR}_{\text{en}}^{\text{all}}[n] \cup \text{VAR}_{\text{en}}^{\text{all}}[n] \\
26. & \quad \quad \text{for each } (v, CR_i) \in \text{VAR}_{\text{en}}^{\text{all}}[n] \text{ at } v \in \text{Def}(n) \text{ do} \\
27. & \quad \quad \quad \text{Immediate data dependency found;} \\
28. & \quad \quad \quad \quad \text{create (statement,call-return) pair for the verification step.} \\
29. & \quad \quad \quad \text{pairs } \leftarrow \text{pairs} \cup \{(n, CR_i)\} \\
30. & \quad \quad \quad \text{VAR}_{\text{en}}^{\text{all}}[n] \leftarrow \text{VAR}_{\text{en}}^{\text{all}}[n] \setminus \{(n, CR_i)\} \\
31. & \quad \text{endfor} \\
32. & \quad \text{Varlist } \leftarrow \text{Varlist} \cup \text{Pred}(n) \\
33. & \text{endwhile} \\
34. \text{endComputeInterTentativeSlice} \]

Fig. 11. Identification of potential statements in the interprocedural slice.
The hybrid interprocedural algorithm can be extended to include aliases caused by reference parameters and global variables. The computation of the alias sets is performed before slicing begins [Cooper 1985]. The alias sets for a procedure are placed on the program nodes for that procedure. As a variable name is propagated in search of its definition, we include in the slice any definition of an alias as well as any definition of the variable itself.

Through the utilization of interprocedural hybrid slicing algorithms in conjunction with static interprocedural slicing algorithms, we can also allow for shortened call histories. A call history can be shortened by maintaining only the part of the call graph that corresponds to a recent period of program execution which is of interest to the user. To illustrate this approach let us consider the history of the example in Figure 9. Let us assume that the call graph history is shortened to only include CR\textsubscript{6}, i.e., history from CR\textsubscript{1} through CR\textsubscript{5} is excluded. Using our hybrid slicing algorithm we compute the subslice $\text{HSlice}(CR_6, CR_7) = \{27\}$. In addition, we determine that the value of $d$ at the start of P3 is of interest. For the slicing criterion of $d$ at the start of P3, we compute a static slice using an existing static slicing algorithm. For example, let us assume that we use Weiser's [1984] interprocedural static slicing algorithm, which does not
consider the calling context. The result of this algorithm would be 
\[ \text{SLICE}(CR_0, CR_6) = \{2, 3, 6, 11, 12, 15, 16, 20, 27, 30\} \]. Thus, by sacrificing the precision and quality of slicing information for earlier parts of the execution we can reduce the cost of computing hybrid slices.

**Complexity Analysis.** The complexity of the interprocedural hybrid slicing algorithm is equivalent to computing an intraprocedural hybrid slice on an expanded flow graph which is obtained by replacing each procedure call in a caller by the callee’s control flow graph. The breakpoints correspond to the beginning and ending points of each called procedure. Let \( N_{\text{max}} \) be the number of nodes in the control flow graph of the largest program module, and let \( C \) be the length of the call graph history, that is, the number of calls and returns. The size of the expanded flow graph is bounded by \( C \times N_{\text{max}} \), and the number of breakpoints is bounded by \( C \). In the previous section, we showed that the complexity for intraprocedural hybrid slicing is bounded by \( O(B^3 \times N^3) \). Thus, the complexity of interprocedural hybrid slicing is given by \( O(C^3 \times (C \times N_{\text{max}})^3) \) or \( O(C^6 \times N_{\text{max}}^3) \). The user can control the cost of slicing by limiting the size of the history and thus the value of \( C \) to a small number.

**Combined Histories.** In the interprocedural hybrid slicing algorithm presented, the only dynamic information that was used was the call/return history. However, the breakpoint history can also be used in conjunction with call/return history to further improve the precision of the interprocedural slice. The form of the combined history and slice follows.

**Definition 3.4.** The **combined history** of a program execution is of the form \( \mathcal{H} = \langle H_0, H_1, \ldots, H_m \rangle \), where \( H_i \) is one of the following: Breakpoint: \((b_i, N_i)\); Procedure Call: \( \text{CALL}[P_{\text{caller}} \rightarrow P_{\text{callee}} \text{ at } s] \); or Procedure Return: \( \text{RET}[P_{\text{callee}} \rightarrow P_{\text{caller}} \text{ at } s] \).

**Definition 3.5.** For a given combined history, \( \mathcal{H} = \langle H_0, H_1, \ldots, H_m \rangle \), the overall **hybrid slice** with respect to a slicing criterion \( SC = (V, CR_m) \) is defined as follows:

\[
HSLICE(H_m) \leftarrow \bigcup_{i=0}^{m-1} HSSLICE(H_i, H_{i+1})
\]

where subslice \( HSSLICE(H_i, H_{i+1}) \) contains those statements that were possibly executed after \( H_i \) and before \( H_{i+1} \), and their execution, directly or indirectly, influenced the computation of the value of some variable in \( V \) at \( CR_m \).

With this combined history the breakpoint and call/return algorithms can be integrated. The data flow sets as before carry either a breakpoint reference or a call/return reference.

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4. IMPLEMENTATION

We have implemented both the intraprocedural and interprocedural hybrid slicing algorithms to illustrate the feasibility of computing hybrid slices. The implementation incorporates the hybrid slicing algorithms in the Unravel [Lyle et al. 1995] static slicing tool. Unravel, developed at the National Institute of Standards and Technology, was designed to assist in the evaluation of software written in ANSI C. We extended the Unravel tool to accept both breakpoint and call/return histories. These histories are entered either interactively or through an input file containing the histories.

Figure 13 shows the interface between the tool and the user and highlights the statements in the hybrid slice. The breakpoint history is also displayed. During debugging, breakpoints at statements 6, 33, and 45 were set. During execution, breakpoints at statements 6 and 45 were encountered while the breakpoint at statement 33 was not encountered. At the breakpoint at statement 45 a hybrid slice on variable bill was requested. The computed hybrid slice contains statements 18, 24, 31, 40, 42, and 44 in the procedure main. If a static slice at statement 45 would have been requested, statements 34 and 36 would also have been included.

To illustrate the potential of hybrid slices in reducing the number of statements from the static slice, hybrid slices were computed for a number of small programs. Table I shows the results of computing intraprocedural hybrid slices using breakpoint history. The programs include Heapsort, procedures Paintface and ClockShowDate taken from the Clock program, procedures ResolvedGet and SlicePass taken from the static slicing program in Unravel, and procedure ComputeTentativeSlice taken from our implementation of the intraprocedural hybrid slicing algorithm. The second column gives the number of lines of code in the program modules. In the third column of Table I, the range of the number of breakpoints that were set is given, and column four contains the range of the number of statements included in the hybrid slice. In these experiments, all breakpoints except the first and last were placed on a statement following a conditional statement. Execution of the hybrid slicing algorithm with zero breakpoints corresponds to the static slice and resulted in the inclusion of the maximum number of statements in the slice. It can be observed from the table that as the number of breakpoints increased, the size of the hybrid slice decreased due to the greater accuracy of predicting the path taken by the program. In general the decrease in the size of a hybrid slice depends upon the placement of breakpoints as well as the variable and the program point with respect to which the slice is requested. The results in Table I illustrate that at least for some slicing requests and breakpoint placements the decrease in the size of the hybrid slice can be significant, ranging from about 30% to over 50% for these requests.

Table II gives results after running the interprocedural hybrid slicing algorithm on complete programs. The programs include Heapsort, the Hybrid slicing algorithm, the Queens program, and the Clinpack routines.
The program sizes are given in the second column of the table. The slices were computed for various call/return histories and variables. The third column contains the number of statements that occur in the static slice, and the last column gives the number of statements in the interprocedural hybrid slice. As was the case with the intraprocedural slices, the number of statements in the interprocedural hybrids was significantly less than the corresponding static slices. The reductions ranged from 0% to 60%. Thus

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these results illustrate that there are slicing requests that greatly benefit from the availability of call/return histories.

The above results illustrate that for some slicing requests the hybrid slices are significantly smaller than static slices and hence more precise. During the above experiments we observed that there was no measurable difference in the execution times of static and hybrid slicing algorithms. Our experience with hybrid slicing so far indicates that the proposed hybrid slicing algorithms can be implemented with a reasonable amount of effort and that hybrid slicing is a promising approach for improving the precision of static slices. However, to quantify the efficiency and precision of hybrid slicing more extensive experimentation is required.

5. CONCLUDING REMARKS

We have presented the notion of a hybrid slice that utilizes dynamic information readily available during debugging to improve the effectiveness of static slicing. Typically a debugger provides a facility for breakpointing and to trace procedure calls and returns. In order to implement the hybrid slicing, the breakpoint and caller/return history must be saved, and the static slicing tool must have access to this history. This is the only extra run-time cost associated with the hybrid slice that is not typically incurred with debugging. Thus, our technique requires little additional tracing at run-time.

The value of the hybrid slice is that it improves the accuracy of the static slice and provides a more detailed analysis about the statements in the slice. This information enables the user to better identify where values are
computed. An important aspect of the hybrid slice is that the detailed information is guided by the user's breakpoints. Thus, the information presented to the user more clearly focuses on the areas of the program that are of interest to the user. Purely static slices can be produced if no breakpoints are placed, and control flow is precisely predicted if breakpoints are placed at every control predicate. Hybrid slicing also allows the user to control the cost of hybrid slicing by controlling the size of history.

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