# Schema Refinement Functional Dependencies

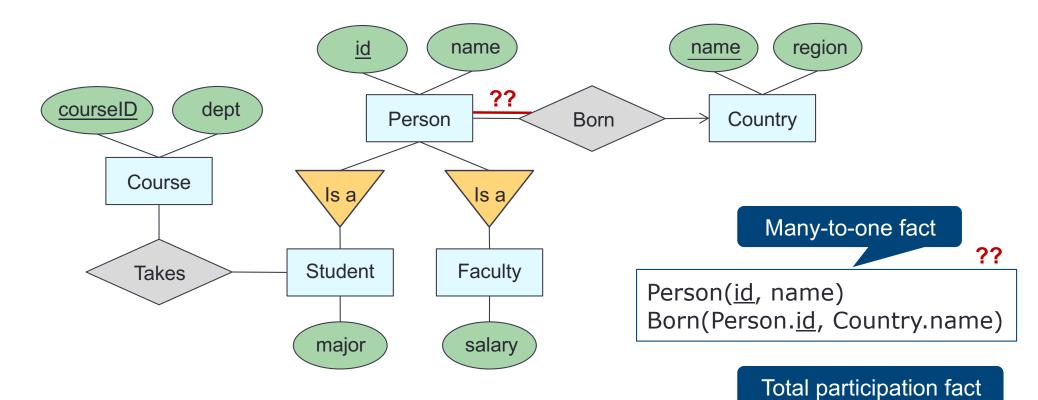
## CS 4750 Database Systems

[A. Silberschatz, H. F. Korth, S. Sudarshan, Database System Concepts, Ch.7] [Ricardo and Urban, Database Illuminated, Ch.6]

[ https://www.w3schools.in/dbms/database-normalization/ ]

#### Recap: E-R Diagram

#### **Convert the following ER into Schema statements**



Country(<u>name</u>, region) Course(<u>courseID</u>, dept) Person(<u>id</u>, name, Country name)

Student(People.id, major)

Faculty(People.id, salary)

Takes(Student.id, Course.courseID)

#### **Database Design Process**

Interact with users and domain experts to characterize the data

Translate requirements into conceptual model (E-R diagrams)

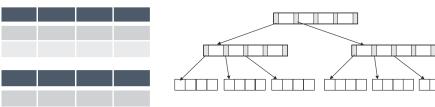
Convert the model to relational model (schema and constraints)



Normalize and develop conceptual (logical) schema of the database

Develop physical schema (partitioning and indexing)





#### Goals for 02/02 - 02/09

Figure out the fundamentals of what makes a good DB schema and being able to apply them to design a DB

- Avoid redundancy and anomalies
- Ensure data interrelationships

#### How:

- Recognize anomalies (things we want to avoid)
- Understand Functional Dependencies (FDs)
- Understand closures and formal definitions of keys
- Understand decomposition and normalization (3NF and BCNF)

#### Why Worry about Sound Structures?

If your database structure isn't sound, what could happen?

Let's share opinion / idea / experience !!

Does "Bad" database design impact any of the following?

- Data manipulation adding, updating, deleting
- Retrieving data
- Data integrity, consistency
- Table relationships

#### Let's Consider: Friend Book

Make a simple friend book that can:

- Hold info about friend's name, email, phone, and city
- Associate friends with the city they live in
- Associate friends with any phone numbers they have

name	email	phone	city
Humpty	humpty@uva.edu	434-111-1111	Charlottesville
Dumpty	dumpty@uva.edu	434-222-1111	Charlottesville
Dumpty	dumpty@uva.edu	434-222-2222	Charlottesville
Mickey	mickey@uva.edu	434-333-3333	Fairfax
Minnie	minnie@uva.edu	434-555-5555	Alexandria

This instance does the job ... but are there issues?

#### **Friend Book: Redundancy Anomaly**

Make a simple friend book that can:

- Hold info about friend's name, email, phone, and city
- Associate friends with the city they live in
- Associate friends with any phone numbers they have

name	email	phone	city
Humpty	humpty@uva.edu	434-111-1111	Charlottesville
Dumpty	dumpty@uva.edu	434-222-1111	Charlottesville
Dumpty	dumpty@uva.edu	434-222-2222	Charlottesville
Mickey	mickey@uva.edu	434-333-3333	Fairfax
Minnie	minnie@uva.edu	434-555-5555	Alexandria

Redundancy – part of data can be derived from other parts

#### **Friend Book: Update Anomaly**

#### Make a simple friend book that can:

- Hold info about friend's name, email, phone, and city
- Associate friends with the city they live in
- Associate friends with any phone numbers they have

name	email	phone	city	
Humpty	humpty@uva.edu	434-111-1111	Charlottesville	
Dumpty	dumpty@uva.edu	434-222-1111	-Charlottesville	Norfolk ???
Dumpty	dumpty@uva.edu	434-222-2222	Charlottesville	
Mickey	mickey@uva.edu	434-333-3333	Fairfax	
Minnie	minnie@uva.edu	434-555-5555	Alexandria	

#### What if Dumpty moves to Norfolk

- Redundancy → possible inconsistency, slow update
- Update once? Update all?

#### **Friend Book: Deletion Anomaly**

#### Make a simple friend book that can:

- Hold info about friend's name, email, phone, and city
- Associate friends with the city they live in
- Associate friends with any phone numbers they have

name	email	phone	city
Humpty	humpty@uva.edu	434-111-1111	Charlottesville
Dumpty	dumpty@uva.edu	434-222-1111	Charlottesville
Dumpty	dumpty@uva.edu	434-222-2222	Charlottesville
Mickey	mickey@uva.edu	434-333-3333	Fairfax
Minnie	minnie@uva.edu	434-555-5555	Alexandria

#### How to delete Minnie's phone

- Delete the entire tuple → lose Minnie
- phone → NULL?

#### **Friend Book: Prevent Data Anomalies**

#### Decompose the relation, separate unrelated attributes

name	email	phone	city
Humpty	humpty@uva.edu	434-111-1111	Charlottesville
Dumpty	dumpty@uva.edu	434-222-1111	Charlottesville
Dumpty	dumpty@uva.edu	434-222-2222	Charlottesville
Mickey	mickey@uva.edu	434-333-3333	Fairfax
Minnie	minnie@uva.edu	434-555-5555	Alexandria



name	email	city
Humpty	humpty@uva.edu	Charlottesville
Dumpty	dumpty@uva.edu	Charlottesville
Mickey	mickey@uva.edu	Fairfax
Minnie	minnie@uva.edu	Alexandria



email	phone
humpty@uva.edu	434-111-1111
dumpty@uva.edu	434-222-1111
dumpty@uva.edu	434-222-2222
mickey@uva.edu	434-333-3333
minnie@uva.edu	434-555-5555

How can we systematically avoid redundancy and anomaly?

#### Functional Dependencies

## Another Example: TA Info Problems with "Bad" DB Design

#### Consider info about TAs

Associate year with the hourly\_rate

computingID	name	year	hourly_rate	hours_worked
ht1y	Humpty	4	12	20
dt2y	Dumpty	3	10	20
md3y	Mickey	4	12	15
mn4e	Minnie	4	12	16
dh5h	Duhhuh	3	10	10

The hourly\_rate of Humpty can be derived from the hourly\_rate of Mickey (or Minnie) since they are all 4<sup>th</sup> year and we know year determines hourly\_rate.

Redundancy exists because of the existence of integrity constraints, in particular Functional Dependencies (FD)

[More functional dependencies later]

### **TA Info: Update Anomaly** (2)

computingID	name	year	hourly_rate	hours_worked
ht1y	Humpty	4	<del>-12</del> 13	20
dt2y	Dumpty	3	10	20
md3y	Mickey	4	12	15
mn4e	Minnie	4	12	16
dh5h	Duhhuh	3	10	10

- What if we attempt to update hourly\_rate of Humpty?
  - Only one copy of hourly\_rate has been updated
- Hourly\_rate determined by year=4 appears in multiple tuples in the table
- Cannot change hourly\_rate in just the 1<sup>st</sup> tuple

### **TA Info: Insertion Anomaly** (3)

computingID	name	year	hourly_rate	hours_worked
ht1y	Humpty	4	12	20
dt2y	Dumpty	3	10	20
md3y	Mickey	4	12	15
mn4e	Minnie	4	12	16
dh5h	Duhhuh	3	10	10
aw6e	Awesome	2	?? Null ?	10

- What if we want to insert a new employee, who is in 2<sup>nd</sup> year, but we don't know the hourly rate for the 2<sup>nd</sup> year?
- Cannot insert a new employee into the table

### **TA Info: Deletion Anomaly** (4)

computingID	name	year	hourly_rate	hours_worked
ht1y	Humpty	4	12	20
d+2v	Dumnty	2	10	20
GCZ y	Dampey	5	10	20
md3y	Mickey	4	12	15
mn4e	Minnie	4	12	16
dhEh	Dubbub	2	10	10
ansn	Dannan	9	10	10

- What if we delete all employees who are in 3<sup>rd</sup> year?
- Lose information about the hourly\_rate for 3<sup>rd</sup> year

#### **TA Info: Potential Solution** (5)

#### Decompose the relation, separate unrelated attributes

computingID	name	year	hourly_rate	hours_worked
ht1y	Humpty	4	12	20
dt2y	Dumpty	3	10	20
md3y	Mickey	4	12	15
mn4e	Minnie	4	12	16
dh5h	Duhhuh	3	10	10

computingID	name	year	hours_worked
ht1y	Humpty	4	20
dt2y	Dumpty	3	20
md3y	Mickey	4	15
mn4e	Minnie	4	16
dh5h	Duhhuh	3	10

year	hourly_rate
4	12
3	10

#### Functional Dependencies – to the rescue!!

#### **General Design Guidelines**

- Semantics of attributes should be self-evident
- Avoid redundancy between tuples, relations
- Avoid NULL values in tuples
- If certain tuples should not exist, don't allow them

Database design = process or organizing data into a database model by considering data needs to be stored and the interrelationship of the data

Database design is about characterizing data and the organizing data

How to describe properties we know or see in the data

How to organize data to promote ease of use and efficiency

#### **Data Interrelationships**

#### Rules that govern data

- Domain knowledge things in the real world
- Pattern analysis

ATA\_Emp(computingID, name, year, hourly\_rate, hours\_worked)

computingID	name	year	hourly_rate	hours_worked
ht1y	Humpty	4	12	20
dt2y	Dumpty	3	10	20
md3y	Mickey	4	12	15
mn4e	Minnie	4	12	16
dh5h	Duhhuh	3	10	10

#### We can:

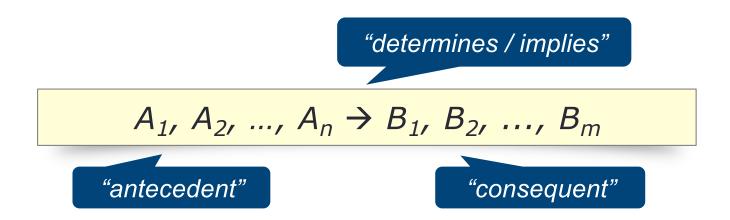
Associate computingID with name comp

Associate year with hourly\_rate

computing → name year → hourly\_rate

### **Functional Dependencies (FDs)**

- Describe data interrelationships
- Constraints on the set of relations
- Determine how to break/decompose a relation



- For each pair of tuples  $t_1$  and  $t_2$  in a relation r
  - If two tuples agree on the attributes,  $A_1$ ,  $A_2$ , ...,  $A_n$
  - Then they must also agree on the attributes  $B_1$ ,  $B_2$ , ...,  $B_m$

### **Functional Dependencies (FDs)**

- A relation can have multiple functional dependencies
  - Example: schema of relation R(A, B, C, D)

FDs: 
$$\{A \rightarrow B, B \rightarrow C, C \rightarrow CD\}$$

- FD holds over a relation R if, for every allowable instance r of R, r satisfies the FD
  - Given some instance r of R, we can check if it violates some
     FD or not

$$t1.X = t2.X$$
 but  $t1.Y \neq t2.Y$ 

- We cannot tell if FD holds over R by looking at an instance (cannot prove non-existence of violation)
- This is the same for all integrity constraints

### **Examples**

computingID	name	year	hourly_rate	hours_worked
ht1y	Humpty	4	12	20
dt2y	Dumpty	3	10	20
md3y	Mickey	4	12	15
mn4e	Minnie	4	12	16
dh5h	Duhhuh	3	10	10

year → hourly\_rate holds

computingID	name	year	hourly_rate	hours_worked
ht1y	Humpty	4	13	20
dt2y	Dumpty	3	10	20
md3y	Mickey	4	12	15
mn4e	Minnie	4	12	16
dh5h	Duhhuh	3	10	10

year → hourly\_rate does not hold

### Let's Try: FDs

Α	В	С
1	aa	X
1	aa	X
2	bb	У
2	СС	У
3	bb	Z

Which of the following is functional dependency?

- (a) A  $\rightarrow$  B
- (b) B  $\rightarrow$  C
  - (c)  $AB \rightarrow C$
  - (d)  $A \rightarrow C$
- (e) C  $\rightarrow$  B

Possible

Not enough information (cannot prove non-existence of violation)

### Let's Try: FDs (2)

EmplD	Name	xPhone	Position
E1001	Mickey	6543	Clerk
E2353	Minnie	1234	Helpdesk
E4567	Daisy	9876	Salesrep
E1234	Donald	9876	Salesrep
E9372	Humpty	1234	Lawyer

List possible FD(s)

EmpID → Name, xPhone, Position

#### **More Example**

ProductName	Category	Color	Department	Price
Beyblade	Gadget	Green	Toys	12
Drone	Gadget	Green	Toys	80

Do all the following FDs hold on this instance?

ProductName → Color

Category → Department

Color, Category -> Price

Possible

If we can be sure that every instance of R will be one in which a given FD is true, then we say that **R satisfies the FD** 

If we say that R satisfies an FD, we are stating a constraint on R

### **Interesting Observation**

If all these FDs are true:

ProductName → Color

Category → Department

Color, Category → Price

Then, this FD also holds:

ProductName, Category → Price

If we find out from application domain that a relation satisfies some FDs, it does not mean that we found all the FDs that it satisfies.

There may be more FDs implied by the ones we have.

#### Reasoning about FDs

To use FDs to break a relation, focus on a key and list all possible FDs

Given some FDs, infer additional FDs using the following rules:

Reflexivity	if b subset a, a → b
Augmentation	if a $\rightarrow$ b, then ac $\rightarrow$ bc
Transitivity	if a $\rightarrow$ b and b $\rightarrow$ c, then a $\rightarrow$ c
Union	if $a \rightarrow b$ and $a \rightarrow c$ , then $a \rightarrow bc$
Decomposition	if a $\rightarrow$ bc, then a $\rightarrow$ b and a $\rightarrow$ c (separately)
<b>Pseudo-transitivity</b>	if a $\rightarrow$ b and cb $\rightarrow$ d, then ac $\rightarrow$ d

There are many rules that let us infer that one FD  $X \to A$  holds in any relation instance that satisfies some other given set of FDs. To verify that  $X \to A$  holds, compute the closure of X, using the given FDs to expand X until it includes A

### **Example: Reasoning**

Supposed we know custID → name

Can we conclude the following? custID, hair\_color → name

Yes!

Adding more attributes to the antecedent can never remove attributes in the consequent

### Example: Reasoning (2)

Supposed we know custID → name

Can we conclude the following? custID → name, hair\_color

No!

Impossible to introduce hair\_color to the consequent without also introducing it to the antecedent

#### **Attribute Closure and F+**

- Attribute Closure  $(\alpha +)$  = all FDs a particular attribute can imply
- Closure of F (F+) = a set of all FDs that are implied by F
- An FD f is logically implied by a set of FDs F if f holds whenever all FDs in F hold
- To compute the closure of a set of functional dependencies F

```
F+ = F
repeat
  for each functional dependency f in F+
     apply reflexivity and augmentation rules on f
     add the resulting functional dependencies to F+
    for each pair of functional dependencies f1 and f2 in F+
     if f1 and f2 can be combined using transitivity
        then add the resulting functional dependency to F+
until F+ does not change any further
```

#### **Example: Attribute Closure**

Let's do this together

Given 
$$R(A,B,C)$$
  
 $FDs = \{A \rightarrow B, B \rightarrow C \}$ 

Compute the attribute closures for all attribute and combination of attributes. Then, think about what can inferred.

	Α	В	С	AB	AC	ВС	ABC
Α	<b>✓</b>	<b>✓</b>	<b>✓</b>	<b>✓</b>	<b>✓</b>	<b>√</b>	<b>√</b>
В							
С							
AB							
AC							
ВС							
ABC							

Summary: attribute closure
A+ = ABC
B+ =
C+ =
AB+ =
AC+ =
BC+ =
ABC+ =

#### **Example: Attribute Closure**

Let's do this together

Given 
$$R(A,B,C)$$
  
 $FDs = \{A \rightarrow B, B \rightarrow C \}$ 

Compute the attribute closures for all attribute and combination of attributes. Then, think about what can inferred.

	Α	В	С	AB	AC	ВС	ABC
Α	<b>✓</b>	<b>√</b>	<b>√</b>	<b>√</b>	<b>√</b>	<b>√</b>	<b>✓</b>
В		$\checkmark$	$\checkmark$			$\checkmark$	
С			<b>√</b>				
AB	$\checkmark$						
AC	<b>✓</b>	<b>√</b>	<b>√</b>	<b>✓</b>	<b>√</b>	<b>√</b>	<b>√</b>
ВС		$\checkmark$	$\checkmark$			$\checkmark$	
ABC	<b>√</b>	<b>√</b>	<b>√</b>	<b>√</b>	<b>√</b>	<b>√</b>	<b>✓</b>

Summary: attribute closure
A+ = ABC
B+=BC
C+ = C
AB+ = ABC
AC+ = ABC
BC+ = BC
ABC+ = ABC

### Example1: Computing F+

Let's do this together

```
Given R(A,B,C,D,E)
           FDs = \{ A \rightarrow C, B \rightarrow B, C \rightarrow BD, D \rightarrow E \}
Compute F+
```

- (1) write all LHS & remaining
  - $\rightarrow$
  - $B \rightarrow$
  - $C \rightarrow$
  - $D \rightarrow$

- - $B \rightarrow B$
  - $C \rightarrow B D$
  - $D \rightarrow$

- (2) copy FDs as is (3) apply reflexivity
  - $A \rightarrow A C$
  - $\rightarrow$  B
  - $C \rightarrow BCD$ 
    - $D \rightarrow$ DF
    - $\rightarrow$ Е

- (4) apply transitivity
  - → ABCDE
  - $\rightarrow$ В
  - $\rightarrow$  BCDE
  - $\rightarrow$ DE
    - $\rightarrow$

 $F+ = \{ A \rightarrow ABCDE, B \rightarrow B, C \rightarrow BCDE, D \rightarrow DE, E \rightarrow E \}$ 

F

E

### Example2: Computing F+

Let's do this together

Given R(A,B,C,D,E) $FDs = \{A \rightarrow BC, B \rightarrow D, CD \rightarrow E \}$ 

Compute F+

Decompose:  $A \rightarrow A$ ,  $A \rightarrow B$ ,  $A \rightarrow C$ 

- (1) write all LHS & remaining
  - $A \rightarrow$
  - $B \rightarrow$
  - $C \rightarrow$
  - $D \rightarrow$
  - *D* /
  - CD →

- (2) copy FDs as is
  - $A \rightarrow BC$

D

Е

- $B \rightarrow$
- $C \rightarrow$
- $D \rightarrow$
- $E \rightarrow$
- $CD \rightarrow$

- (3) apply reflexivity
  - $A \rightarrow ABC$
  - $B \rightarrow B D$
  - $C \rightarrow C$
  - $D \rightarrow D$
  - F →
    - $\rightarrow$
  - $CD \rightarrow CDE$

- (4) apply transitivity
  - $A \rightarrow ABCD$
  - $B \rightarrow B D$
  - $C \rightarrow C$
  - $D \rightarrow D$
  - : → F
  - CD → CDE

### Example2: Computing F+ (cont.)

Decompose:  $A \rightarrow A$ ,  $A \rightarrow B$ ,  $A \rightarrow C$ ,  $A \rightarrow D$ 

Union: A  $\rightarrow$  C and A  $\rightarrow$  D, then A  $\rightarrow$  CD

Let's do this together

(from previous page)

(4) apply transitivity

$$\begin{array}{ccccc} A & \rightarrow & ABCD \\ B & \rightarrow & B & D \\ C & \rightarrow & C \\ D & \rightarrow & D \\ E & \rightarrow & E \\ \hline CD & \rightarrow & CDE \\ \end{array}$$

(5) apply transitivity

$$\begin{array}{ccccc} A & \rightarrow & ABCDE \\ B & \rightarrow & B & D \\ C & \rightarrow & C \\ D & \rightarrow & D \\ E & \rightarrow & E \\ CD & \rightarrow & CDE \end{array}$$

 $F+ = \{ A \rightarrow ABCDE, B \rightarrow BD, C \rightarrow C, D \rightarrow D, E \rightarrow E, CD \rightarrow CDE \}$ 

### **Example3: F+ to Candidate Key**

Consider a relation Stocks(B, O, I, S, Q, D), whose attributes may be thought of informally as broker, office (of the broker), investor, stock, quantity (of the stock owned by the investor), and dividend (of the stock). Let the set of FDs for Stocks be

$$FDs = \{ S \rightarrow D, I \rightarrow B, IS \rightarrow Q, B \rightarrow O \}$$

List all candidate keys for the Stocks relation

**Usual procedure:** reasoning / computing the attribute closures.

**Observation:** None of the RHS of FDs contains I and S. Thus, we know that attribute I and S must be part of any keys.

Let's reasoning FDs

S → S D

I → BOI

IS → BOISQD →

B → BO

What if we want to find all superkeys?

IS is the only minimal superkey (candidate key) for the Stocks relation

#### Wrap-Up

- Problems with "Bad" DB design
- Characterizing data / describe properties of data with Functional dependencies (FDs)
- Reasoning about FDs
- Attribute closure and F+

#### What's next?

Fine-tuning database structures and normalization