

# More Practice 3NF and BCNF

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**CS 4750**  
**Database Systems**

# Practice 1: 3NF and BCNF

Consider a relation Stocks(B, O, I, S, Q, D), whose attributes may be thought of informally as broker, office (of the broker), investor, stock, quantity (of the stock owned by the investor), and dividend (of the stock). Let the set of FDs for Stocks be

$$\text{FDs} = \{ S \rightarrow D, I \rightarrow B, IS \rightarrow Q, B \rightarrow O \}$$

Minimal basis  
 $\sim F_c$

1. Verify that the given set of FDs is a minimal basis

To verify that the given FDs are their own minimal basis, we need to check:

1. Can any of the FDs be removed without losing the dependencies?

No. If we remove any one of the four FDs, the remaining FDs do not imply the removed FD.

2. Can any attributes be removed from LHS and/or RHS without losing the dependencies?

No. If we remove any attribute, we lose the dependency

We can conclude that the given set of FDs is the minimal basis.

# Practice 1: 3NF and BCNF (2)

Stocks(B, O, I, S, Q, D)

FDs = {  $S \rightarrow D$ ,  $I \rightarrow B$ ,  $IS \rightarrow Q$ ,  $B \rightarrow O$  }

2. Use 3NF, decompose the given Stocks relation into proper relations

The first step is to compute Canonical Cover ( $F_c$ ).

```
S  -> D
I  -> B
IS -> Q
B  -> O
```

There is no trivial FD, no reflexivity, no extraneous attr. Thus,  $F_c$  = the given set of FDs. (note:  $F_c$  is the minimal basis of the given set of FDs).

To convert the given relation into 3NF, put the left-hand-side (LHS) and the right-hand-side (RHS) of each FD in  $F_c$  together in one relation. Thus, Stocks(B, O, I, S, Q, D) becomes  $R_1(S, D)$ ,  $R_2(I, B)$ ,  $R_3(I, S, Q)$ , and  $R_4(B, O)$ . Alternatively, we can write in another format: SD // IB // ISQ // BO

# Practice 1: 3NF and BCNF (3)

Stocks(B, O, I, S, Q, D)

FDs = {  $S \rightarrow D$ ,  $I \rightarrow B$ ,  $IS \rightarrow Q$ ,  $B \rightarrow O$  }

Decomposed relations:  
SD // IB // ISQ // BO

## 3. Show that the decomposed relations are in 3NF

### 1. Lossless join

Start with a relation of the decomposition with a superkey; thus consider ISQ where IS is a key. Compute attribute closure of IS.  $IS^+ = B O I S Q D$  (or  $IS \rightarrow B O I S Q D$ ), thus can reconstruct the original relation.

Check if  $(R1 \text{ intersect } R2) \neq \{ \}$  and  $(R1 \text{ intersect } R2)$  is a superkey of either R1 or R2 (or both), where R1 and R2 are any two decomposed relations.

SD and ISQ:  $S \rightarrow D$  (S is a superkey of SD)  
IB and ISQ:  $I \rightarrow B$  (I is a superkey of IB)  
IB and BO:  $B \rightarrow O$  (B is a superkey of BO)

### 2. Dependency preserving

Consider all decomposed relations. Check if the given set of FDs can be verified within the decomposed relations.

$S \rightarrow D$  can be verified within SD  
 $I \rightarrow B$  can be verified within IB  
 $IS \rightarrow Q$  can be verified within ISQ  
 $B \rightarrow O$  can be verified within BO

No transitive dependency. Thus, satisfy dependency preserving property

# Practice 1: 3NF and BCNF (4)

Stocks(B, O, I, S, Q, D)

FDs = {  $S \rightarrow D$ ,  $I \rightarrow B$ ,  $IS \rightarrow Q$ ,  $B \rightarrow O$  }

Decomposed relations:  
SD // IB // ISQ // BO

4. Are the decomposed relations in BCNF?

In BCNF. No violation.

In addition to checking for lossless join property, we need to verify that there is no non-key dependency in each decomposed relation.

For every non-trivial FD,  $X \rightarrow A$ ,  $X$  is a superkey

Consider each decomposed relation (above), all LHS of the given FD is a superkey of the relation. Thus, no non-key dependency

Ready for the next one ??

Go!!

# Practice 2: 3NF

Consider the following relation and functional dependencies

$R(A, B, C, D)$

$FDs = \{ C \rightarrow A, C \rightarrow D, C \rightarrow C, AB \rightarrow C \}$

1. Decompose the given relation  $R(A, B, C, D)$  using 3NF
2. Discuss to show that the decomposed relations are in 3NF

Fc:

$C \rightarrow AD$

$AB \rightarrow C$

Decomposed relations:

$ACD // ABC$

or written as  $R1(ACD)$  and  $R2(ABC)$

# Practice 2: 3NF (2)

## 2. Discuss to show that the decomposed relations are in 3NF

We need to show that the decomposed relations ACD // ABC satisfy **lossless join** and **dependency preserving**.  $F_c = \{ C \rightarrow AD, AB \rightarrow C \}$

**Lossless join** -- check if  $(R1 \text{ intersect } R2) \neq \{ \}$  and  $(R1 \text{ intersect } R2)$  is a superkey of either R1 or R2 (or both)

- Let  $R1 = ACD$  and  $R2 = ABC$ ,  $(R1 \text{ intersect } R2) = AC$
- Consider ACD and check if  $(R1 \text{ intersect } R2)$  is a superkey of ACD.
- Since we know that  $C \rightarrow AD$ 
  - $C \rightarrow C$ , thus  $C \rightarrow ACD$  (reflexive)
  - $A \rightarrow A$ , we can augment the above FD by adding attribute A to the left hand side, thus  $AC \rightarrow ACD$
- Therefore, we can conclude that AC (which is  $R1 \text{ intersect } R2$ ) is a superkey of ACD ( $R1$ )



# Practice 2: 3NF (3)

## 2. Discuss to show that the decomposed relations are in 3NF

Decomposed relations  $ACD \parallel ABC$ ,  $F_c = \{ C \rightarrow AD, AB \rightarrow C \}$

**Lossless join** -- check no loose, no gain

- First, identify the superkey of the given relation  $R(ABCD)$ .
  - Based on the given FDs, compute attribute closure.
  - Any combination of attributes that contains  $AB$  is a superkey. Thus, the only minimal superkey of  $R(ABCD)$  is  $AB$ .
- Then, start with a relation of the decomposition with a superkey  $AB$ , which is  $ABC$  (refer to  $F_c$ :  $AB \rightarrow C$ ).
- Compute attribute closure of  $AB$ .
- To help us envision, from the decomposed relation  $ABC$ ,
  - Apply  $AB \rightarrow C$  ( $F_c$ ),  $AB \rightarrow AB$  (reflexive), and  $C \rightarrow AD$  (transitive), thus  $AB \rightarrow ABCD$ . That is,  $ABC$  will be expanded to  $ABCD$  ( $\sim$  reconstruct the original relation from this decomposition).
- Since  $AB^+ = ABCD$  (i.e.,  $AB \rightarrow ABCD$ ), the decomposition satisfies lossless join property (no loose, no gain).

# Practice 2: 3NF (4)

## 2. Discuss to show that the decomposed relations are in 3NF

Decomposed relations ACD // ABC,  $F_c = \{ C \rightarrow AD, AB \rightarrow C \}$

### Dependency preserving

- Check if the given FDs =  $\{ C \rightarrow A, C \rightarrow D, C \rightarrow C, AB \rightarrow C \}$  can be verified within a single decomposed relation.
- Given FDs:
  - $C \rightarrow A$  can be verified within ACD
  - $C \rightarrow D$  can be verified within ACD
  - $C \rightarrow C$  can be verified within ACD
    - Always true in any relation that contains C
- Given FD:  $AB \rightarrow C$ , we can verify it within ABC
- No transitive dependency.
- Thus, the decomposition satisfies dependency preserving property.

No 3NF violation

Ready for the next one ??

Go!!

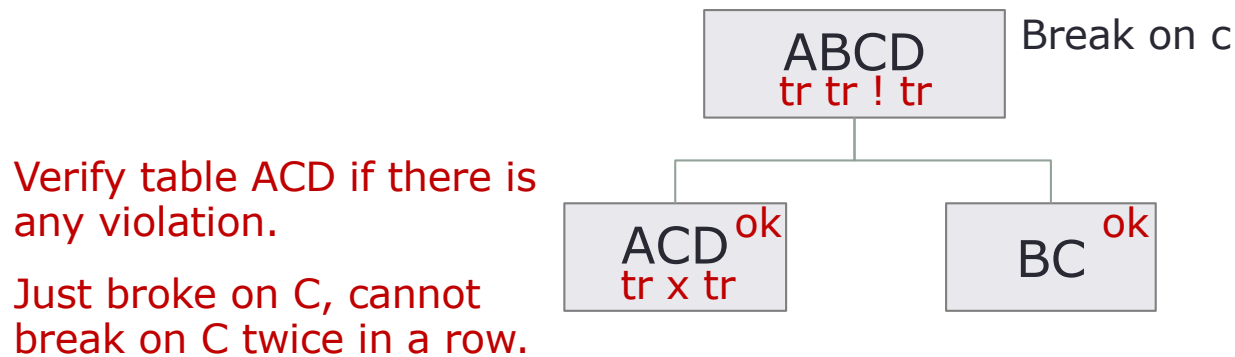
# Practice 3: BCNF

Consider the following relation and functional dependencies

$R(A, B, C, D)$

$FDs = \{ C \rightarrow A, C \rightarrow D, C \rightarrow C, AB \rightarrow C \}$

1. Decompose the given relation  $R(A, B, C, D)$  using BCNF
2. Discuss to show that the decomposed relations are in BCNF



$F^+$

$A \rightarrow A$	tr
$B \rightarrow B$	tr
$C \rightarrow A$	CD
$D \rightarrow D$	tr
$AB \rightarrow ABCD$	sk

Alternatively, we can verify through "for all non-trivial FDs,  $X \rightarrow A$ ,  $X$  must be a superkey"

For ACD, we know that only C has a non-trivial FD and we know that  $C \rightarrow AD$  (given FD), we can conclude that C is a superkey of ACD, cannot break using the superkey (i.e., no violation).

Decomposed relations: ACD // BC

# Practice 3: BCNF (2)

## 2. Discuss to show that the decomposed relations are in BCNF

We need to show that the decomposed relations ACD // BC satisfy **lossless join** and **For every non-trivial FD,  $X \rightarrow \text{Attribute(s)}$ ,  $X$  is a superkey.**

F+		
A	$\rightarrow$	A
B	$\rightarrow$	B
C	$\rightarrow$	A CD
D	$\rightarrow$	D
AB	$\rightarrow$	ABCD
		tr
		tr
		tr
		sk

**Lossless join** -- check if  $(R1 \text{ intersect } R2) \neq \{ \}$  and  $(R1 \text{ intersect } R2)$  is a superkey of either R1 or R2 (or both)

- Let  $R1 = ACD$  and  $R2 = BC$ ,  $(R1 \text{ intersect } R2) = C$
- Consider ACD and check if  $(R1 \text{ intersect } R2)$  is a superkey of ACD.
- From F+, we can conclude that  $(R1 \text{ intersect } R2)$  is a superkey for ACD (R1)
- Thus, the decomposition satisfies lossless join property.

# Practice 3: BCNF (3)

## 2. Discuss to show that the decomposed relations are in BCNF

Decomposed relations  $ACD // BC$ , FDs =  $\{ C \rightarrow A, C \rightarrow D, C \rightarrow C, AB \rightarrow C \}$

**Lossless join** -- check no loose, no gain

- First, identify the superkey of the given relation  $R(ABCD)$ .
  - Based on the given FDs, compute attribute closure.
  - Any combination of attributes that contains  $AB$  is a superkey. Thus, the only minimal superkey of  $R(ABCD)$  is  $AB$ .
- Then, start with a relation of the decomposition with a superkey  $AB$ , which is  $ABC$  ( $AB \rightarrow C$ ).
- Compute attribute closure of  $AB$ .
- To help us envision, from the decomposed relation  $ABC$ ,
  - Apply  $AB \rightarrow C$ ,  $AB \rightarrow AB$  (reflexive), and  $C \rightarrow AD$  (transitive), thus  $AB \rightarrow ABCD$ . That is,  $ABC$  will be expanded to  $ABCD$  ( $\sim$  reconstruct the original relation from this decomposition).
- Since  $AB^+ = ABCD$  (i.e.,  $AB \rightarrow ABCD$ ), the decomposition satisfies lossless join property (no loose, no gain).

F+		
$A \rightarrow A$		tr
$B \rightarrow B$		tr
$C \rightarrow A$	$CD$	
$D \rightarrow D$		tr
$AB \rightarrow ABCD$		sk

# Practice 3: BCNF (4)

## 2. Discuss to show that the decomposed relations are in BCNF

To verify, we need to show that the decomposed relations ACD // BC satisfy **lossless join** and **For every non-trivial FD,  $X \rightarrow \text{Attribute(s)}$ ,  $X$  is a superkey**.

Given FDs =  $\{ C \rightarrow A, C \rightarrow D, C \rightarrow C, AB \rightarrow C \}$

F+		
$A \rightarrow A$		tr
$B \rightarrow B$		tr
$C \rightarrow A \quad CD$		
$D \rightarrow D$		tr
$AB \rightarrow ABCD$		sk

### **For every non-trivial FD, $X \rightarrow \text{Attribute(s)}$ , $X$ is a superkey**

- Consider ACD, we know that  $C \rightarrow ACD$  (A and D have trivial FDs, so ignore)
  - C is the only non-trivial FD and C is a superkey of ACD.
  - No non-key dependency in this decomposed relation.
- Consider BC, no non-key dependency.
  - By default, a relation with 2 attributes is always in BCNF (even if there is no dependency at all).

**No BCNF violation**

Ready for the next one ??

Go!!



# Practice 4: 3NF

Consider the following relation and functional dependencies

$R(A, B, C, D)$

$FDs = \{ A \rightarrow ABC, C \rightarrow D, A \rightarrow C, D \rightarrow D \}$

1. Decompose the given relation  $R(A, B, C, D)$  using 3NF
2. Discuss to show that the decomposed relations are in 3NF

Fc:

$A \rightarrow BC$

$C \rightarrow D$

Decomposed relations:

$ABC // CD$

or written as  $R1(ABC)$  and  $R2(CD)$

# Practice 4: 3NF (2)

## 2. Discuss to show that the decomposed relations are in 3NF

We need to show that the decomposed relations ABC // CD satisfy **lossless join** and **dependency preserving**.  $F_c = \{ A \rightarrow BC, C \rightarrow D \}$

**Lossless join** -- check if  $(R1 \text{ intersect } R2) \neq \{ \}$  and  $(R1 \text{ intersect } R2)$  is a superkey of either R1 or R2 (or both)

- Let  $R1 = ABC$  and  $R2 = CD$ ,  $(R1 \text{ intersect } R2) = C$
- From  $F_c$ , we can conclude that  $(R1 \text{ intersect } R2)$  is a superkey of CD (R2)

# Practice 4: 3NF (3)

## 2. Discuss to show that the decomposed relations are in 3NF

Decomposed relations  $ABC // CD$ ,  $F_c = \{ A \rightarrow BC, C \rightarrow D \}$

**Lossless join** -- check no loose, no gain

- First, identify the superkey of the given relation  $R(ABCD)$ .
  - Based on the given FDs, compute attribute closure.
  - Any combination of attributes that contains  $A$  is a superkey. Thus, the only minimal superkey of  $R(ABCD)$  is  $A$ .
- Then, start with a relation of the decomposition with a superkey  $A$ , which is  $ABC$  (refer to  $F_c: A \rightarrow BC$ ).
- Compute attribute closure of  $A$ .
- To help us envision, from the decomposed relation  $ABC$ ,
  - Apply  $A \rightarrow BC$  ( $F_c$ ),  $A \rightarrow A$  (reflexive), and  $C \rightarrow D$  (transitive), thus  $A \rightarrow ABCD$ . That is,  $ABC$  will be expanded to  $ABCD$  ( $\sim$  reconstruct the original relation from this decomposition).
- Since  $A^+ = ABCD$  (i.e.,  $A \rightarrow ABCD$ ), the decomposition satisfies lossless join property (no loose, no gain).

# Practice 4: 3NF (4)

## 2. Discuss to show that the decomposed relations are in 3NF

Decomposed relations  $ABC \parallel CD, Fc = \{ A \rightarrow BC, C \rightarrow D \}$

### Dependency preserving

- Check if the given FDs  $= \{ A \rightarrow ABC, C \rightarrow D, A \rightarrow C, D \rightarrow D \}$  can be verified within a single decomposed relation.
- Given FDs:
  - $A \rightarrow ABC$  can be verified within ABC
  - $C \rightarrow D$  can be verified within CD
  - $A \rightarrow C$  can be verified within ABC
  - $D \rightarrow D$  can be verified within CD
    - Always true in any relation that contains D
- No transitive dependency.
- Thus, the decomposition satisfies dependency preserving property.

No 3NF violation

Ready for the next one ??

Go!!

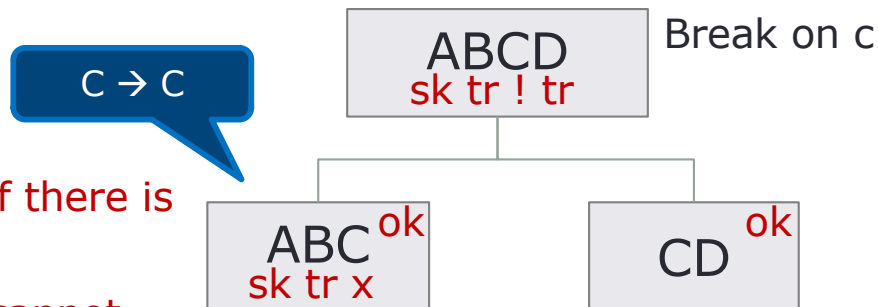
# Practice 5: BCNF

Consider the following relation and functional dependencies

$R(A, B, C, D)$

$FDs = \{ A \rightarrow ABC, C \rightarrow D, A \rightarrow C, D \rightarrow D \}$

1. Decompose the given relation  $R(A, B, C, D)$  using BCNF
2. Discuss to show that the decomposed relations are in BCNF



Verify table ABC if there is any violation.

Just broke on C, cannot break on C twice in a row.

$F^+$

$A \rightarrow ABCD$	sk
$B \rightarrow B$	tr
$C \rightarrow CD$	
$D \rightarrow D$	tr

Alternatively, we can verify through "for all non-trivial FDs,  $X \rightarrow A$ ,  $X$  must be a superkey"

For ABC, we know that only A has a non-trivial FD and we know that  $A \rightarrow BC$  (given FD), we can conclude that A is a superkey of ABC, cannot break using the superkey (i.e., no violation).

Decomposed relations: ABC // CD

# Practice 5: BCNF (2)

## 2. Discuss to show that the decomposed relations are in BCNF

To verify, we need to show that the decomposed relations ABC // CD satisfy **lossless join** and **For every non-trivial FD,  $X \rightarrow \text{Attribute(s)}$ ,  $X$  is a superkey.**

F+		
A	$\rightarrow$	ABCD
B	$\rightarrow$	B
C	$\rightarrow$	CD
D	$\rightarrow$	D
		sk
		tr
		tr

**Lossless join** -- check if  $(R1 \text{ intersect } R2) \neq \{ \}$  and  $(R1 \text{ intersect } R2)$  is a superkey of either R1 or R2 (or both)

- Let  $R1 = ABC$  and  $R2 = CD$ ,  $(R1 \text{ intersect } R2) = C$
- From F+, we can conclude that  $(R1 \text{ intersect } R2)$  is a superkey for CD (R2)
- Thus, no violation

# Practice 5: BCNF (3)

## 2. Discuss to show that the decomposed relations are in BCNF

Decomposed relations ABC // CD, FDs =  $\{ A \rightarrow ABC, C \rightarrow D, A \rightarrow C, D \rightarrow D \}$

**Lossless join** -- check no loose, no gain

- First, identify the superkey of the given relation R(ABCD).
  - Based on the given FDs, compute attribute closure.
  - Any combination of attributes that contains A is a superkey. Thus, the only minimal superkey of R(ABCD) is A.
- Then, start with a relation of the decomposition with a superkey A (ABC).
- Compute attribute closure of A.
- To help us envision, from the decomposed relation ABC,
  - Apply  $A \rightarrow ABC$  (given FD) and  $C \rightarrow D$  (transitive), thus  $A \rightarrow ABCD$ . That is, ABC will be expanded to ABCD (~ reconstruct the original relation from this decomposition).
- Since  $A^+ = ABCD$  (i.e.,  $A \rightarrow ABCD$ ), the decomposition satisfies lossless join property (no loose, no gain).

F+

$A \rightarrow ABCD$

$B \rightarrow B$

$C \rightarrow CD$

$D \rightarrow D$

sk

tr

tr



# Practice 5: BCNF (4)

## 2. Discuss to show that the decomposed relations are in BCNF

To verify, we need to show that the decomposed relations ABC // CD satisfy **lossless join** and **For every non-trivial FD,  $X \rightarrow \text{Attribute}(s)$ ,  $X$  is a superkey**.

Given FDs =  $\{ A \rightarrow ABC, C \rightarrow D, A \rightarrow C, D \rightarrow D \}$

F+		
A $\rightarrow$	ABCD	sk
B $\rightarrow$	B	tr
C $\rightarrow$	CD	
D $\rightarrow$	D	tr

### **For every non-trivial FD, $X \rightarrow \text{Attribute}(s)$ , $X$ is a superkey**

- Consider ABC, we know that  $A \rightarrow ABC$ . (B and C have trivial FDs here, ignore)
  - No non-key dependency in this decomposed relation.
- Consider CD, no non-key dependency.
  - By default, a relation with 2 attributes is always in BCNF (even if there is no dependency at all).

No BCNF violation

Ready for the next one ??

Go!!

# Practice 6: BCNF

Given  $R(A,B,C,D,E)$

FDs =  $\{ B \rightarrow DE, C \rightarrow A, A \rightarrow BC, D \rightarrow E \}$

Convert the relation into BCNF

Compute  $F^+$

(1) write all LHS  
& remaining

A  $\rightarrow$   
B  $\rightarrow$   
C  $\rightarrow$   
D  $\rightarrow$   
E  $\rightarrow$

(2) copy FDs as is

A  $\rightarrow$  BC  
B  $\rightarrow$  DE  
C  $\rightarrow$  A  
D  $\rightarrow$  E  
E  $\rightarrow$

(3) apply reflexivity

A  $\rightarrow$  ABC  
B  $\rightarrow$  B DE  
C  $\rightarrow$  A C  
D  $\rightarrow$  DE  
E  $\rightarrow$  E

(4) apply transitivity

A  $\rightarrow$  ABCDE  
B  $\rightarrow$  B DE  
C  $\rightarrow$  ABCDE  
D  $\rightarrow$  DE  
E  $\rightarrow$  E

$F^+ = \{ A \rightarrow ABCDE, B \rightarrow BDE, C \rightarrow ABCDE, D \rightarrow DE, E \rightarrow E \}$

# Practice 6: BCNF (2)

(from previous page)

(4) apply transitivity

F+	A	→	ABCDE	
	B	→	B DE	Non-trivial FDs. B, D are not super key
	C	→	ABCDE	
	D	→	DE	
	E	→	E	Trivial FDs (let's abbreviate to TR)

Based on F+, let's rewrite using the following format to help us calculate

R ( A B C D E )  
SK ! SK ! TR

TR	– trivial
SK	– super key
X	– neither trivial nor super key
!	– (possibly) need to work on

# Practice 6: BCNF (3)

R ( A B C D E )  
SK ! SK ! TR

F+	A	→	ABCDE
	B	→	B DE
	C	→	ABCDE
	D	→	DE
	E	→	E

Consider non-trivial FDs and attributes that are not SK

Let's consider B:

B is not a super key, not trivial, thus  $B \rightarrow BDE$  violates BCNF, thus we can break a relation on B

Let's consider D:

D is not a super key, not trivial, thus  $D \rightarrow DE$  violates BCNF, thus we can break a relation on D

To choose which FD to work on, two ways:

- Choose the first FD, or
- Choose the longest FD (yield better solution)

**Break on B**

# Practice 6: BCNF (4)

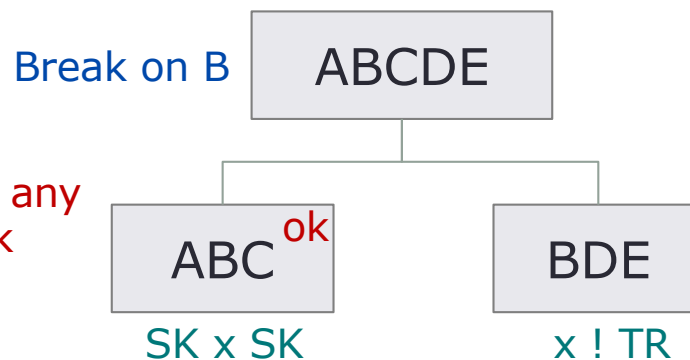
R ( A B C D E )  
           SK ! SK ! TR

F+	A	→	ABCDE
	B	→	B DE
	C	→	ABCDE
	D	→	DE
	E	→	E

B → BDE

*RHS*, make a table: BDE

*LHS*, make a table with B plus (original – (*RHS*)) – thus, ABC



Verify table ABC if there is any violation or if we can break any further.

A and C are super keys. – already satisfy, don't break on them.

Can't break on B twice.

Verify table BDE if there is any violation.

B is a super key. Also, can't break on B twice.

E is trivial, can't break.

**Break on D**

# Practice 6: BCNF (5)

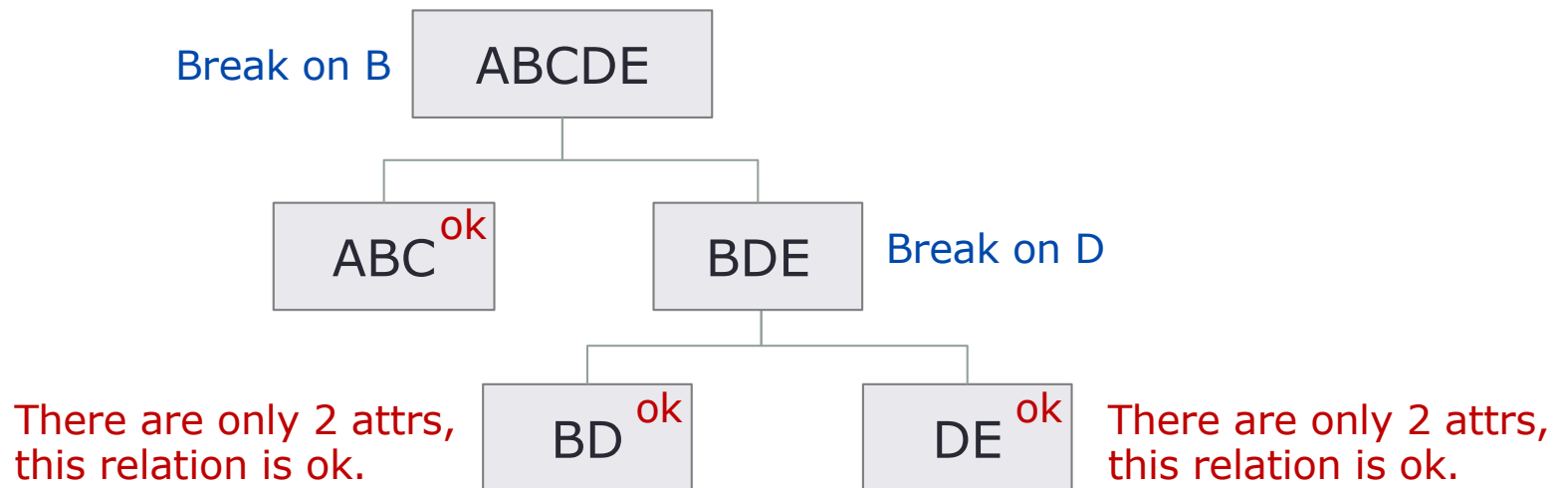
R ( ~~B~~ D ~~E~~ )  
x ! TR

F+	A	→	ABCDE
	B	→	B DE
	C	→	ABCDE
	D	→	DE
	E	→	E

$D \rightarrow DE$

*RHS*, make a table: DE

*LHS*, make a table with D plus (original – (*RHS*)) – thus, BD



Decomposed tables: R1(ABC), R2(BD), R3(DE)

Ready for the next one ??

Go!!



# Practice 7: BCNF

Given  $R(A,B,C,D,E)$

FDs =  $\{ A \rightarrow CE, A \rightarrow B, B \rightarrow D, D \rightarrow CD, C \rightarrow E \}$

Convert the relation into BCNF

Compute  $F^+$

(1) write all LHS  
& remaining

A  $\rightarrow$   
B  $\rightarrow$   
C  $\rightarrow$   
D  $\rightarrow$   
E  $\rightarrow$

(2) copy FDs as is

A  $\rightarrow$  BC E  
B  $\rightarrow$  D  
C  $\rightarrow$  E  
D  $\rightarrow$  CD  
E  $\rightarrow$

(3) apply reflexivity

A  $\rightarrow$  ABC E  
B  $\rightarrow$  B D  
C  $\rightarrow$  C E  
D  $\rightarrow$  CD  
E  $\rightarrow$  E

(4) apply transitivity

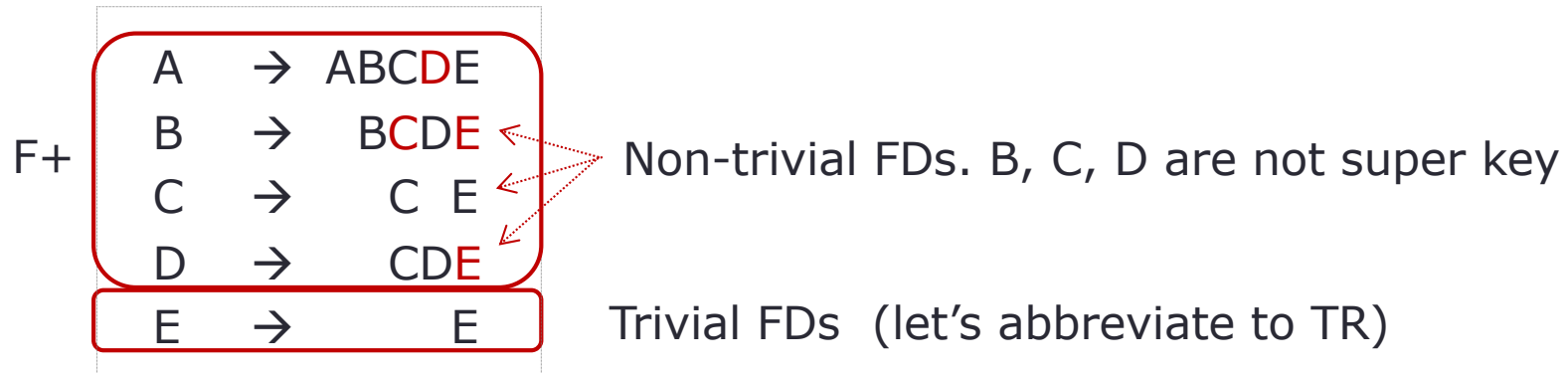
A  $\rightarrow$  ABCDE  
B  $\rightarrow$  BCDE  
C  $\rightarrow$  C E  
D  $\rightarrow$  CDE  
E  $\rightarrow$  E

$F^+ = \{ A \rightarrow ABCDE, B \rightarrow BCDE, C \rightarrow CE, D \rightarrow CDE, E \rightarrow E \}$

# Practice 7: BCNF (2)

(from previous page)

(4) apply transitivity



Based on F+, let's rewrite using the following format to help us calculate

R ( A B C D E )  
SK ! ! ! TR

TR – trivial  
SK – super key  
X – neither trivial nor super key  
! – (possibly) need to work on

# Practice 7: BCNF (3)

R ( ~~A~~ B C D ~~E~~ )  
SK ! ! ! TR

F+	A	→	ABCDE
	B	→	BCDE
	C	→	C E
	D	→	CDE
	E	→	E

Consider non-trivial FDs and attributes that are not SK

B is not a super key, not trivial, thus  $B \rightarrow BCDE$  violates BCNF, thus we can break a relation on B

B is not a super key, not trivial, thus  $C \rightarrow CE$  violates BCNF, thus we can break a relation on C

D is not a super key, not trivial, thus  $D \rightarrow CDE$  violates BCNF, thus we can break a relation on D

To choose which FD to work on, two ways:

- Choose the first FD, or
- Choose the longest FD (yield better solution)

**Break on B**

# Practice 7: BCNF (4)

R ( ~~A~~ B C D ~~E~~ )  
SK ! ! ! TR

Break on B

B → BCDE

F+	A	→	ABCDE
	B	→	BCDE
	C	→	C E
	D	→	CDE
	E	→	E

RHS, make a table: BCDE

LHS, make a table with B plus (original – (RHS)) – thus, AB

There are only 2 attrs, this relation is ok.

R ( ~~B~~ C D ~~E~~ )  
x ! ! TR

Break on D

D → CDE

RHS, make a table: CDE

LHS, make a table with D plus (original – (RHS)) – thus, BD

There are only 2 attrs, this relation is ok.

R ( C ~~D~~ ~~E~~ )  
! x TR

Break on C

C → CE

RHS, make a table: CE

LHS, make a table with C plus (original – (RHS)) – thus, CD

There are only 2 attrs, this relation is ok.

Decomposed tables: R1(AB), R2(BD), R3(CE), R4(CD)

Ready for the next one ??

Go!!

# Practice 8: 3NF

Given  $R(A,B,C,D,E)$

FDs =  $\{ A \rightarrow CE, A \rightarrow B, B \rightarrow D, D \rightarrow CD, C \rightarrow E \}$

Convert the relation into BCNF

Compute Fc without using reflexivity

Compute Fc

(1) write all LHS  
& remaining

A  $\rightarrow$   
B  $\rightarrow$   
C  $\rightarrow$   
D  $\rightarrow$

(2) copy FDs as is

A  $\rightarrow$  BC E  
B  $\rightarrow$  D  
C  $\rightarrow$  E  
D  $\rightarrow$  CD

(3) remove  
reflexivity

A  $\rightarrow$  BC E  
B  $\rightarrow$  D  
C  $\rightarrow$  E  
D  $\rightarrow$  ~~CD~~

(4) remove  
extraneous attr

A  $\rightarrow$  ~~BC~~ ~~E~~  
B  $\rightarrow$  D  
C  $\rightarrow$  E  
D  $\rightarrow$  C

A  $\rightarrow$  B, B  $\rightarrow$  D, D  $\rightarrow$  C, C  $\rightarrow$  E, thus A does not have to directly imply E.  
A  $\rightarrow$  B, B  $\rightarrow$  D, D  $\rightarrow$  C, thus A does not have to directly imply C.  
Alternatively, if we apply A  $\rightarrow$  C, C  $\rightarrow$  E, thus A does not need to directly imply E. If this was done, C would be kept (i.e., A  $\rightarrow$  BC); then, A  $\rightarrow$  B, B  $\rightarrow$  D, D  $\rightarrow$  C, remove C

Fc =  $\{ A \rightarrow B, B \rightarrow D, C \rightarrow E, D \rightarrow C \}$

Decomposed tables: R1(AB), R2(BD), R3(CE), R4(CD)