Name:	CompID:	
CS 2102 - DMT1 - Fall 2019 — Luther Tychonievich Administered in class friday november 15, 2019		Quiz 10
problem 1 Arithmetic		
1. The prime factorization of 60 is		
2. Re-write $\log_3(x) = y$ without a log function:		
3. Re-write $\log_a(b)$ with a base- $c \log$:	<u> </u>	
4. Re-write $\log_2(a^2 \cdot b)$ with no constants or operators in a log's arguing the second state of the seco	ment:	
5. Suppose $\log_a(b) = \frac{2}{3}$. What is $\log_b(a)$? PROBLEM 2 Proof by Contradiction		
Complete the following proof that $\log_2(3)$ is irrational.		
<i>Proof.</i> Because $3 > 2$, $\log_2(3) > 1$. Assume that $\log_2(3)$ is rational. positive integers. Re-writing this equation we get	Then $\log_2(3) =$	$=\frac{a}{b}$, where a and b are

 $\log_2(3) = \frac{a}{b}$

Since *a* and *b* are positive integers, both sides of the last equation above are integers. But they clearly share no prime factors, which contradicts the fundamental theorem of arithmetic. Because the assumption led to a contradiction, it must be false and $\log_2(3)$ must be irrational. \Box