



$\{\}$

0

$$P(\{\}) = \{\{\}\}$$

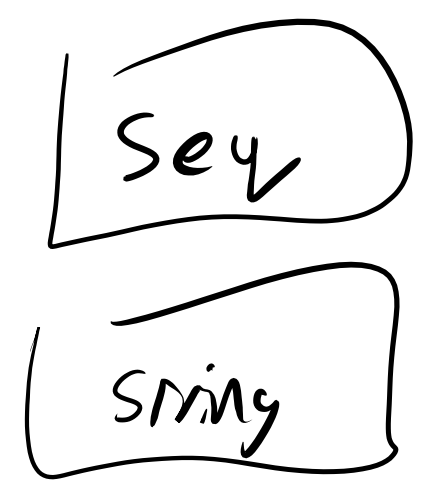
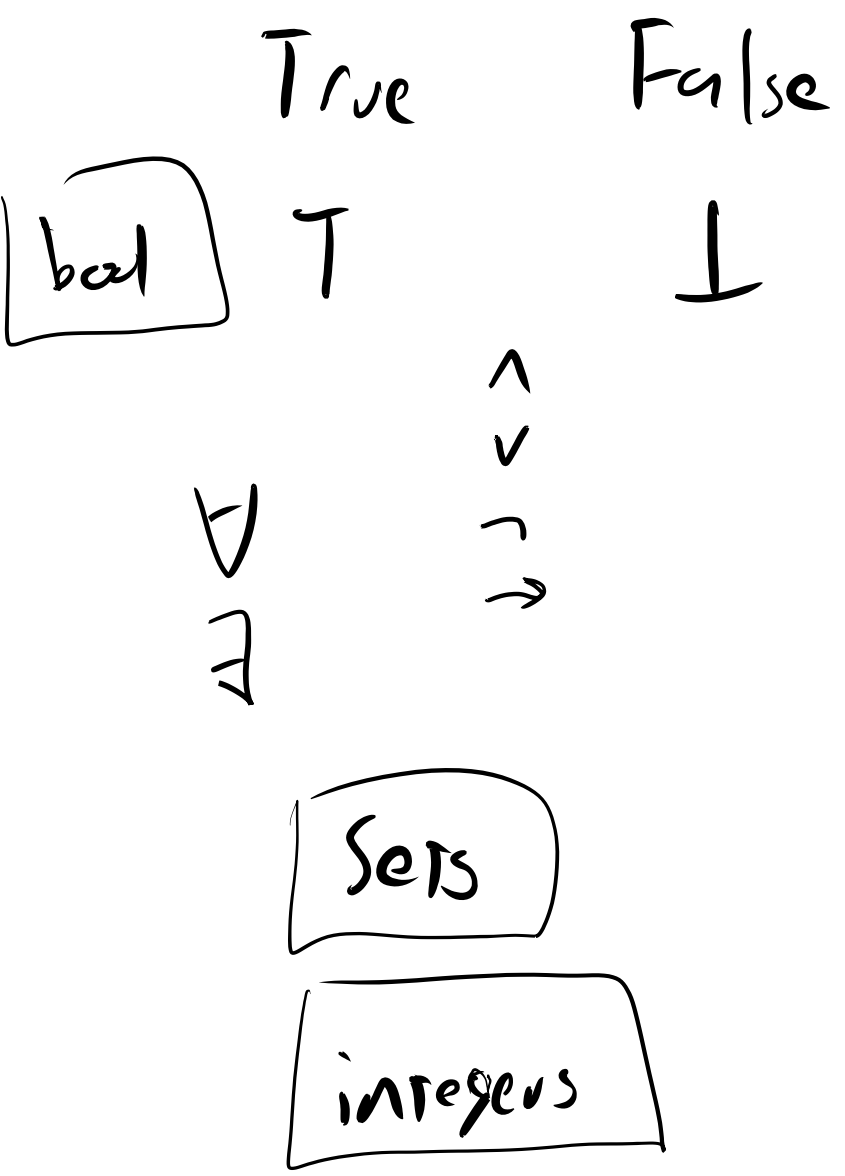
1

$$P(P(\{\})) = \{\underbrace{\{\}}, \underbrace{\{\{\}\}}\} \quad 2$$

$$x = \{3, \{4, 5\}\}$$

$$\{4\}$$

$$\{\underbrace{\{3, \{4, 5\}\}}, 11\}$$



functions

relations

Symbol

{0, 1}

{0, 1}

{a, b}

0 = 0

0 ≠ a

Sequences

	Change len	Element
tuple	no	no
array	no	yes
list	yes	yes



math!

Sequences

- contain
- in an order
- w/ duplicates allowed

pair

triple

quadruple

⋮

tuple

(3, 1, 4, 1, 5, 9, 2, 6, 5, 3, 9)

$$(3) = 3$$

Seq of 1 thing is that thing

Seq of zero things $\begin{cases} \lambda \\ \epsilon \\ \epsilon \end{cases}$

$$\underbrace{\{3\} \times \{4, 5\}}_{\text{Cartesian Product}} \triangleq \{(3, 4), (3, 5)\}$$

$$\{3, 5\}^2 \triangleq \{(3, 3), (3, 5), (5, 3), (5, 5)\}$$

$$\{3, 5\}' = \{(3), (5)\} = \overset{\{3, 5\}}{\text{Kleene}}$$

$$\{3, 5\}^* = \{s \mid \exists n \in \mathbb{N}. s \in \{3, 5\}^n\}$$

$$\{\epsilon, (3), (5), (3, 3), (3, 5), (5, 5), (5, 3), (3, 3, 3), \dots\}$$

Code

alphabet = Σ

code $\in \Sigma^*$

User type $\in \Sigma^*$

\forall . data $\in \text{Bytes}^*$. \rightarrow Crash (data)

$$\{1, 2\} \times \{6, 9\}$$

$$\{(1, 6), (1, 9), (2, 6), (2, 9)\}$$

$$\{1, 2\} \times \underbrace{\{3, 4\} \times \{5\}}$$

$$\{(3, 5), (4, 5)\}$$

String

≡ sequence of symbols

function

Proy

random()

computable

math

$r() = 18230073$

do not have state

predictable

pure

1 arg \rightarrow 1 ans



domain: \mathbb{R}

$$f(x) = x^2$$

$$\left\{ \begin{array}{l} (0, 0), \\ (1, 1), \\ (2, 4), \\ (3, 9), \\ (4, 16), \\ (5, 25), \\ \vdots \\ (0.2, 0.04) \end{array} \right\}$$