changelog

22 Feb 2024: two-level page tables: fix column label for valid bit on second-level table

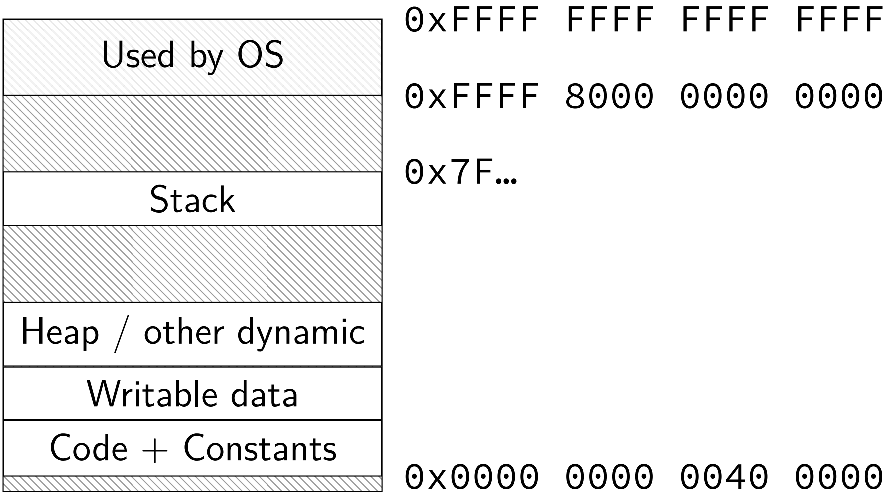
22 Feb 2024: pagetable assignmet API: use size_t only, no void

last time

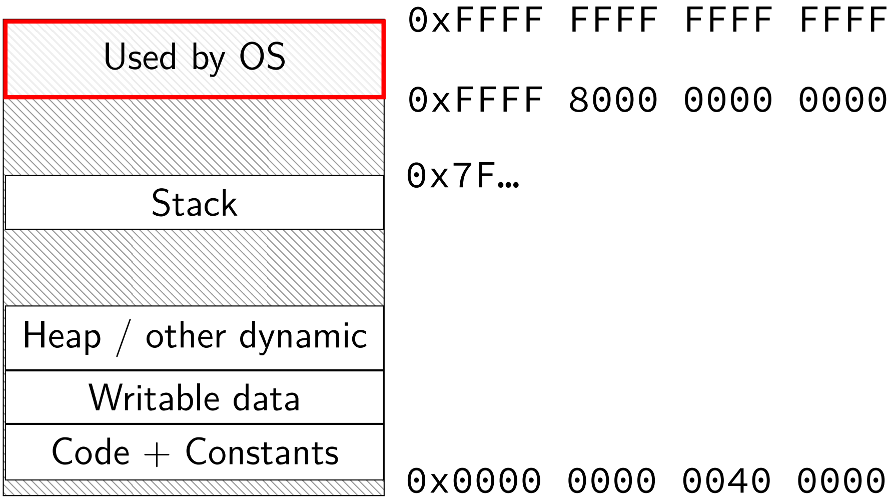
- more page table tricks
  - generalized idea: on exception, maybe fix page table
  - OS tracking memory as list of mappings (separate from page table)
  - page table from HW for hardware

  - loading from/unloading to files on disk
  - copy-on-write
  - …
- storing page tables in memory
  - page table base register
  - representing entries as integers

program memory



program memory



1-level exercise (2)

6-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 other

page table base register `0x20`; translate virtual address `0x12`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	A0 E2 D1 F3
0x24-7	E4 E5 F6 07
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	CB 0B CB 0B
0x38-B	DC 0C DC 0C
0x3C-F	EC 0C EC 0C

1-level exercise (2)

6-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 other

page table base register `0x20`; translate virtual address `0x12`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	A0 E2 D1 F3
0x24-7	E4 E5 F6 07
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	CB 0B CB 0B
0x38-B	DC 0C DC 0C
0x3C-F	EC 0C EC 0C

`0x12` $=$ `01 0010`

PTE addr:

`0x20` $+ 2 \times 1 =$ `0x22`

PTE value:

`0xD1` $=$ `1101 0001`

PPN `110`, valid `1`

M[`110 001`] $=$ **M[**`0x32`**]**

$\rightarrow$ `0xBA`

1-level exercise (2)

6-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 other

page table base register `0x20`; translate virtual address `0x12`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	A0 E2 D1 F3
0x24-7	E4 E5 F6 07
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	CB 0B CB 0B
0x38-B	DC 0C DC 0C
0x3C-F	EC 0C EC 0C

`0x12` = `01 0010`

PTE addr:

`0x20` + 2 ×1 = `0x22`

PTE value:

`0xD1` = `1101 0001`

PPN `110`, valid 1

M[`110 001`] = **M[**`0x32`**]**

→ `0xBA`

1-level exercise (2)

6-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 other

page table base register `0x20`; translate virtual address `0x12`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	A0 E2 D1 F3
0x24-7	E4 E5 F6 07
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	CB 0B CB 0B
0x38-B	DC 0C DC 0C
0x3C-F	EC 0C EC 0C

$\texttt{0x12} = \texttt{01 0010}$

PTE addr:

$\texttt{0x20} + 2 \times 1 = \texttt{0x22}$

PTE value:

$\texttt{0xD1} = \texttt{1101 0001}$

PPN `110`, valid `1`

$M[\texttt{110 001}] = \mathbf{M[}\texttt{0x32}\mathbf{]}$

$\rightarrow$ `0xBA`

1-level exercise (2)

6-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 other

page table base register `0x20`; translate virtual address `0x12`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	A0 E2 D1 F3
0x24-7	E4 E5 F6 07
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	CB 0B CB 0B
0x38-B	DC 0C DC 0C
0x3C-F	EC 0C EC 0C

`0x12` = `01 0010`

PTE addr:

`0x20` + 2 ×1 = `0x22`

PTE value:

`0xD1` = `1101 0001`

PPN `110`, valid `1`

M[`110 001`] = **M[`0x32`]**

→ `0xBA`

pagetable assignment

pagetable assignment

simulate page tables (on top of normal program memory)

- alternately: implement another layer of page tables on top of the existing system's

in assignment:

virtual address $\sim$ arguments to your functions

physical address $\sim$ your program addresses (normal pointers)

pagetable assignment API

```
/* configuration parameters */
#define POBITS ...
#define LEVELS /* later /
```

```
size_t ptbr; // page table base register
    // points to page table (array of page table entries)

// lookup "virtual" address 'va' in page table ptbr points to
// return (~0L) if invalid
size_t translate(size_t va);

// make it so 'va' is valid, allocating one page for its data
// if it isn't already
void page_allocate(size_t va)
```

translate()

with POBITS=12, LEVELS=1:

ptbr = GetPointerToTable(

VPN	valid?	physical
0	0	—
1	1	0x9999
2	0	—
3	1	0x3333
...	...	...

)

```
translate(0x0FFF) == (void*) ~0L
translate(0x1000) == (void*) 0x9999000
translate(0x1001) == (void*) 0x9999001
translate(0x2000) == (void*) ~0L
translate(0x2001) == (void*) ~0L
translate(0x3000) == (void*) 0x3333000
```

translate()

with POBITS=12, LEVELS=1:

ptbr = GetPointerToTable(

VPN	valid?	physical
0	0	—
1	1	0x9999
2	0	—
3	1	0x3333
...	...	...

)

translate(0x0FFF) == (void*) ~0L
translate(0x1000) == (void*) 0x9999000
translate(0x1001) == (void*) 0x9999001
translate(0x2000) == (void*) ~0L
translate(0x2001) == (void*) ~0L
translate(0x3000) == (void*) 0x3333000

page_allocate()

with POBITS=12, LEVELS=1:

ptbr == 0

page_allocate(0x1000) *or* page_allocate(0x1001) *or* ...

page_allocate()

with POBITS=12, LEVELS=1:

ptbr == 0

page_allocate(0x1000) *or* page_allocate(0x1001) *or* ...

ptbr *now* == GetPointerToTable(

VPN	valid?	physical
0	0	—
1	1	(new)
2	0	—
3	1	—
...	...	...

)

allocated with `posix_memalign`

page_allocate()

with POBITS=12, LEVELS=1:

ptbr == 0

page_allocate(0x1000) *or* page_allocate(0x1001) *or* ...

ptbr *now* == GetPointerToTable(

VPN	valid?	physical
0	0	—
1	1	(new)
2	0	—
3	1	—
...	...	...

)

allocated with `posix_memalign`

posix_memalign

```
void *result;
error_code =
    posix_memalign(&result, alignment, size);
```

allocate `size` bytes

choosing address that is multiple of `alignment`

    can make sure allocation starts at beginning of page

`error_code` indicates if out-of-memory, etc.

fills in `result` (passed via pointer)

posix_memalign

```
void *result;
error_code =
    posix_memalign(&result, alignment, size);
```

allocate `size` bytes

choosing address that is multiple of `alignment`

    can make sure allocation starts at beginning of page

`error_code` indicates if out-of-memory, etc.

fills in `result` (passed via pointer)

posix_memalign

```
void *result;
error_code =
    posix_memalign(&result, alignment, size);
```

allocate `size` bytes

choosing address that is multiple of `alignment`

- can make sure allocation starts at beginning of page

`error_code` indicates if out-of-memory, etc.

fills in `result` (passed via pointer)

parts

part 1 (next week): LEVELS=1, POBITS=12 and

- translate() OR
- page_allocate()

part 2 (two weeks after break): all LEVELS, both functions

- in preparation for code review
- due Weds BEFORE LAB

part 3 (two weeks after break): final submission

- Friday after code review
- most of grade based on this
- will test previous parts again

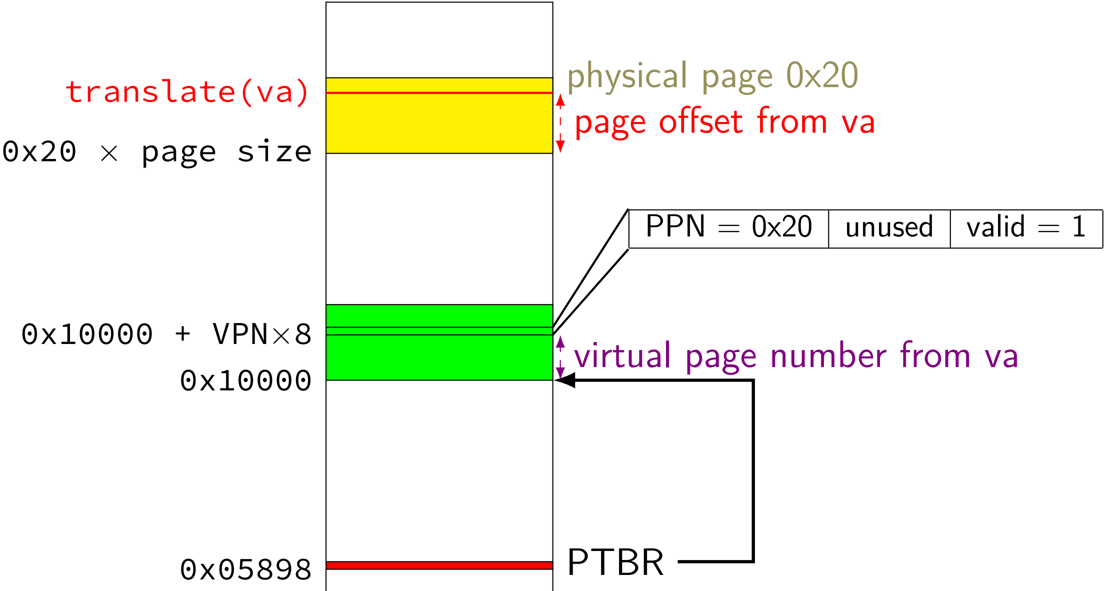
address/page table entry format

(with POBITS=12, LEVELS=1)

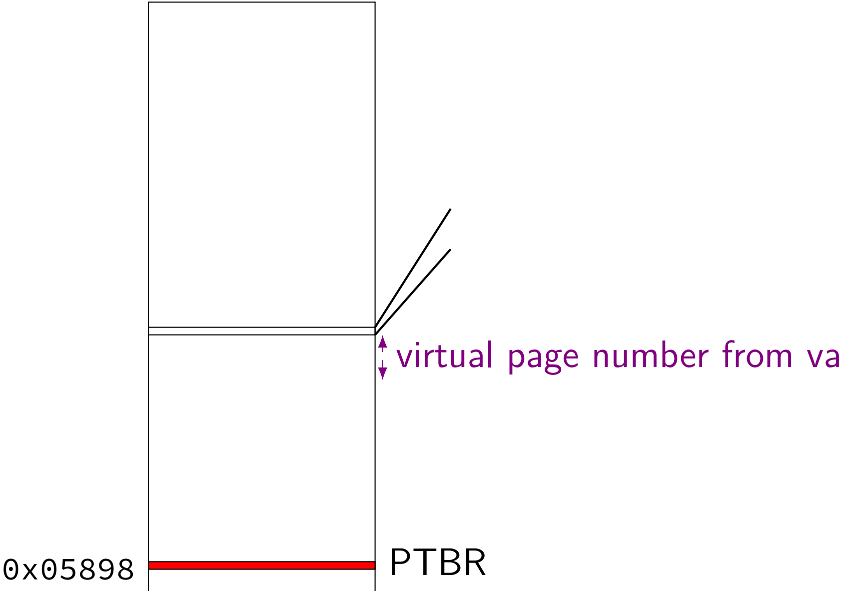
	bits 63–21	bits 20–12	bits 11–1	bit 0
page table entry	physical page number		unused	valid bit
virtual address	unused	virtual page number	page offset	
physical address	physical page number		page offset	

in assignment: value from posix_memalign = physical address

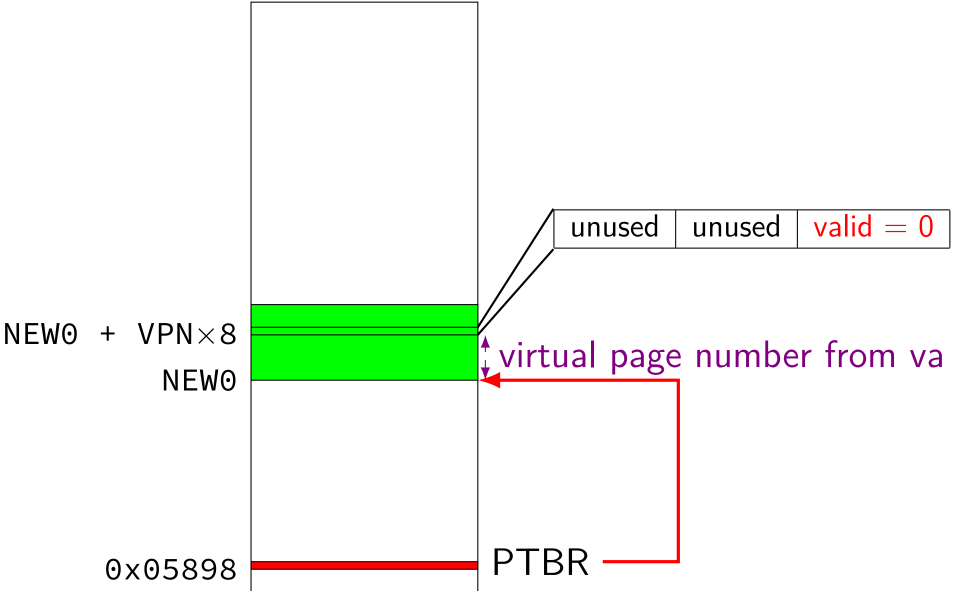
pa = translate(va) [LEVELS=1]



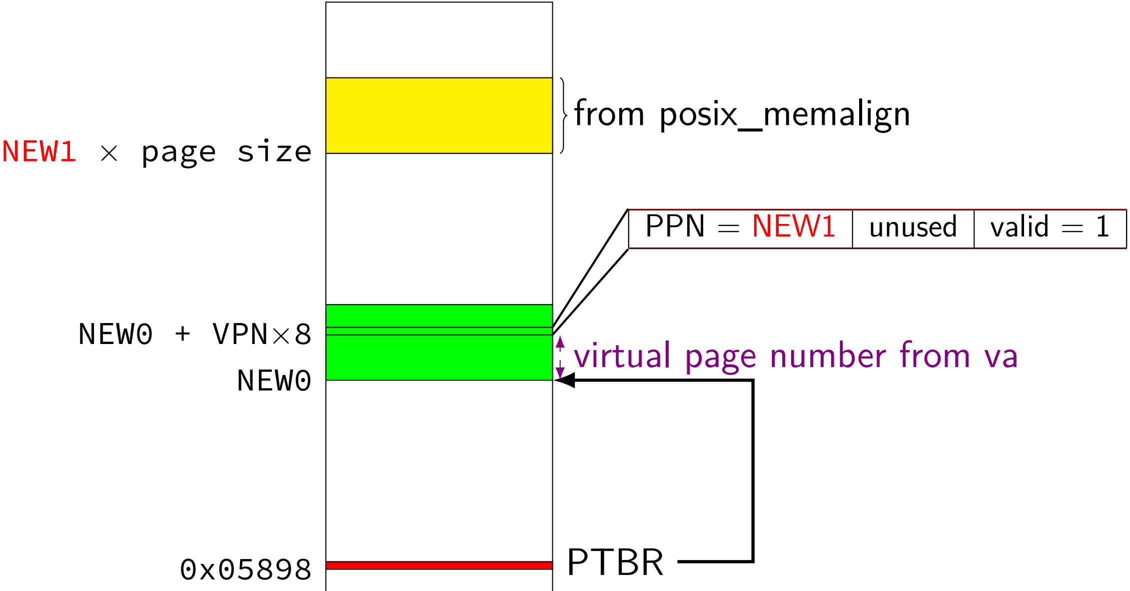
first page_allocate(va) [LEVELS=1]



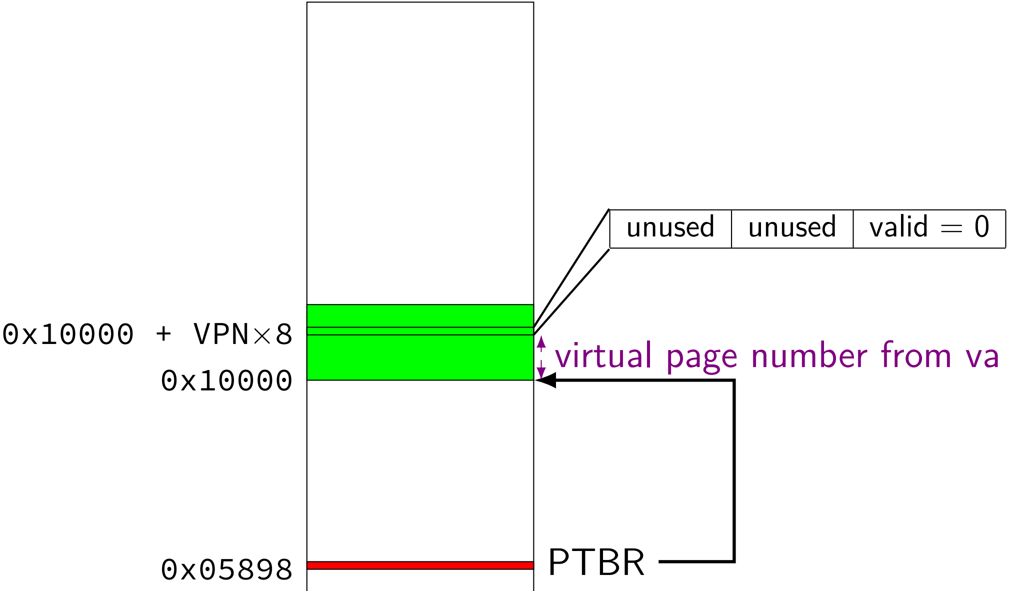
first page_allocate(va) [LEVELS=1]



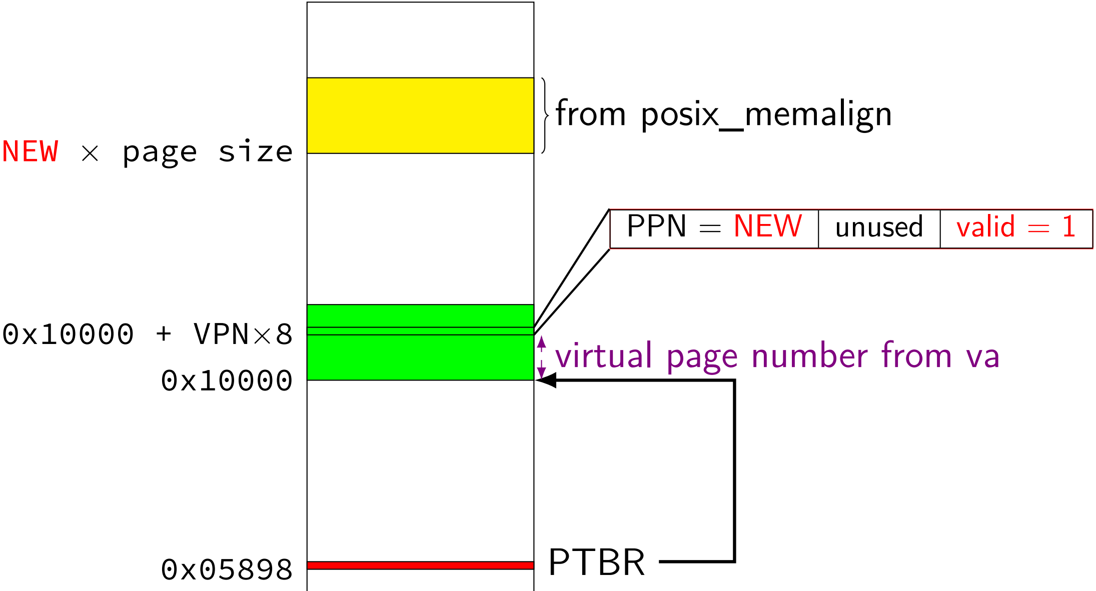
first page_allocate(va) [LEVELS=1]



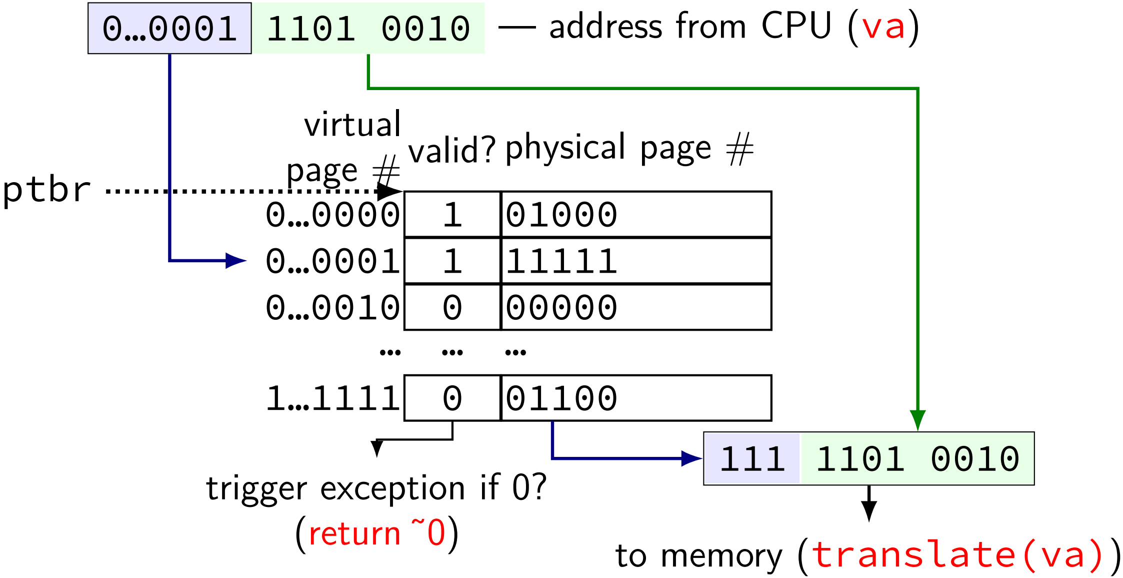
page_allocate(va) [LEVELS=1]



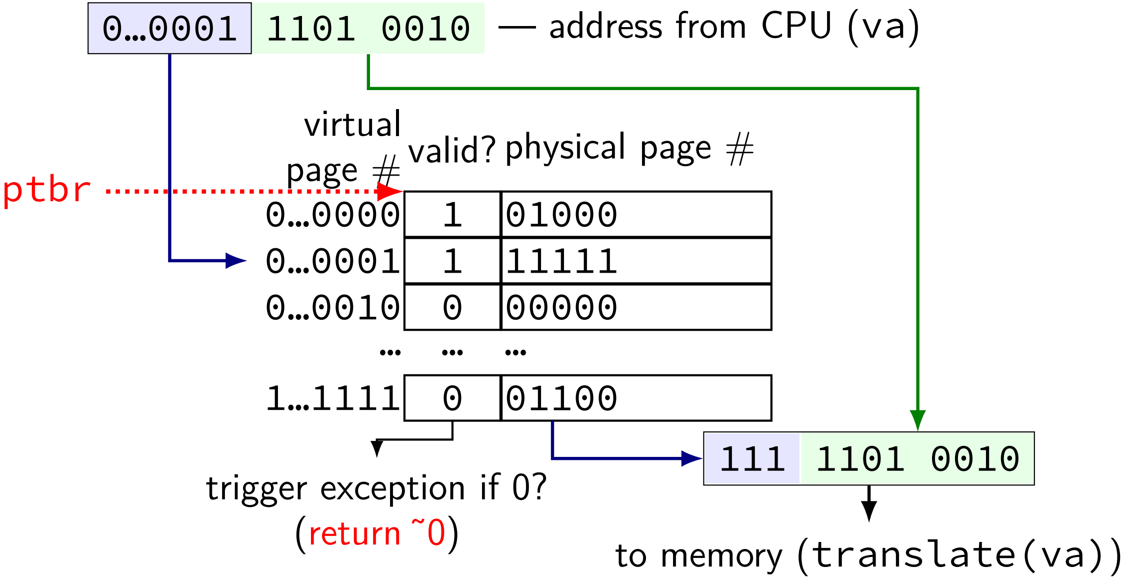
page_allocate(va) [LEVELS=1]



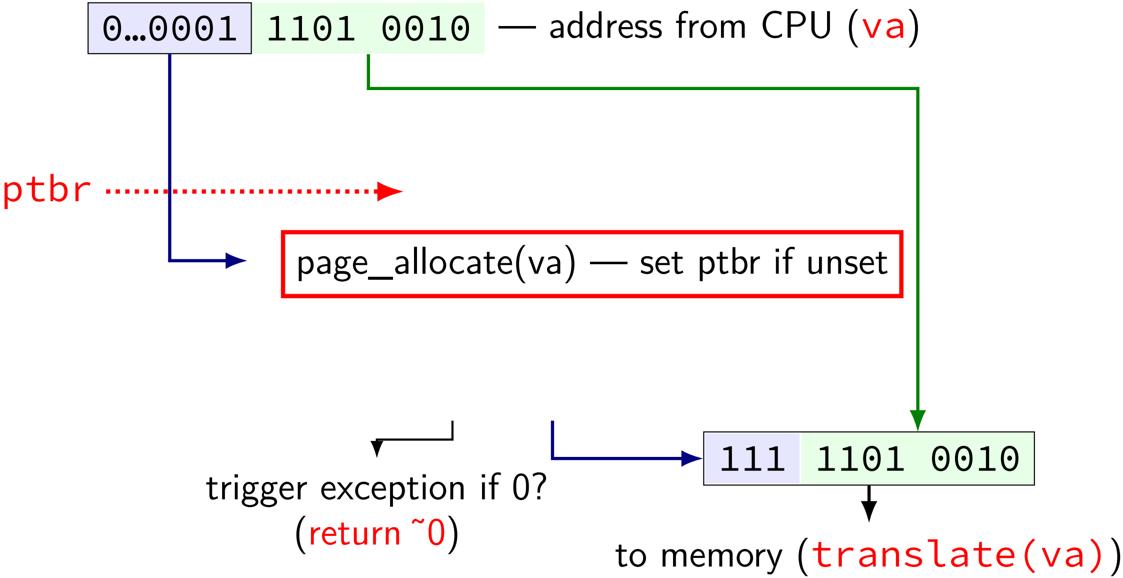
page table lookup (and translate())



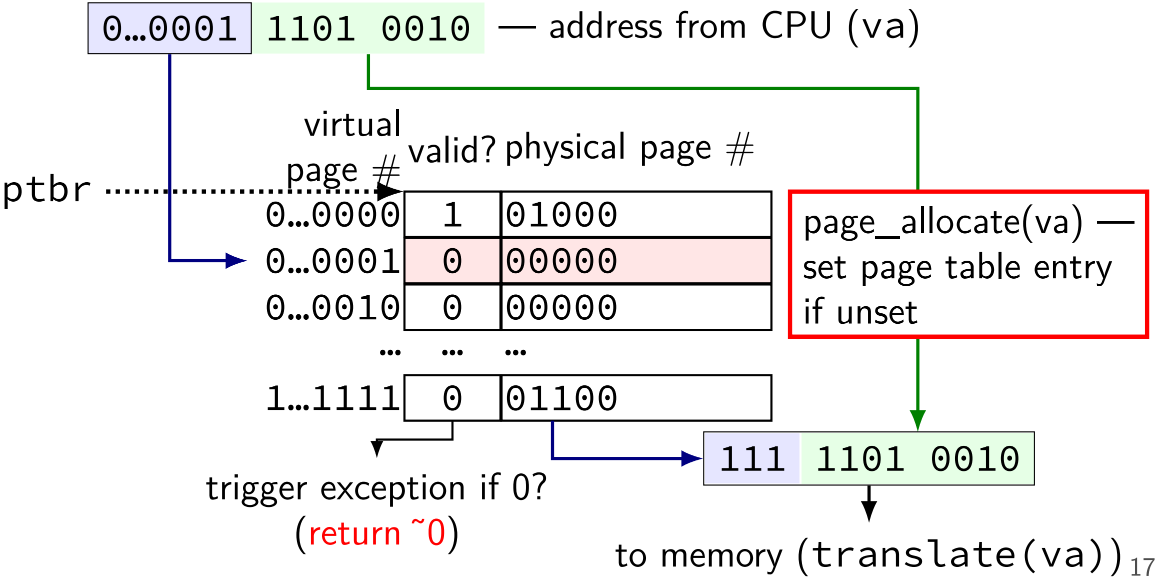
page table lookup (and translate())



page table lookup (and allocate)



page table lookup (and allocate)



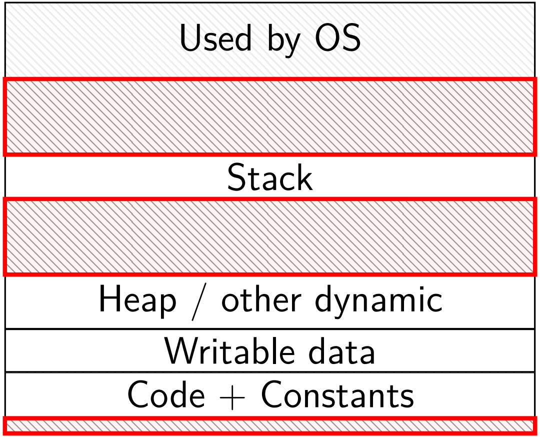
huge page tables

huge virtual address spaces!

impossible to store PTE for every page

how can we save space?

holes



most pages are invalid

saving space

basic idea: don't store (most) invalid page table entries

use a data structure other than a flat array

- want a map — lookup key (virtual page number), get value (PTE)

options?

saving space

basic idea: don't store (most) invalid page table entries

use a data structure other than a flat array

want a map — lookup key (virtual page number), get value (PTE)

options?

hashtable

actually used by some historical processors

but never common

saving space

basic idea: don't store (most) invalid page table entries

use a data structure other than a flat array

- want a map — lookup key (virtual page number), get value (PTE)

options?

hashtable

- actually used by some historical processors
- but never common

tree data structure

- but not quite a search tree

search tree tradeoffs

lookup usually implemented in hardware

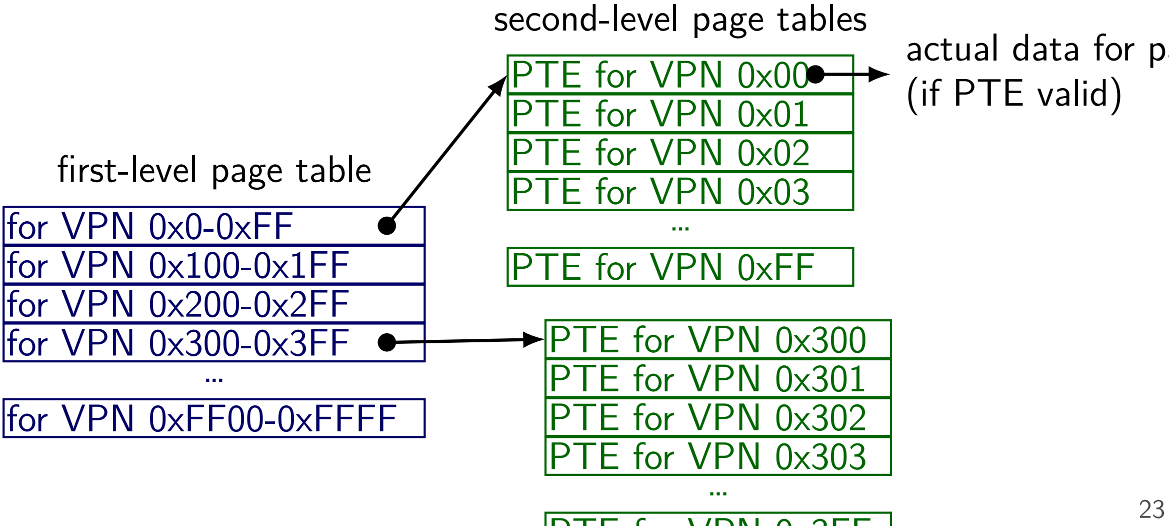
- lookup should be simple
- solution: lookup splits up address bits (no complex calculations)

lookup should not involve many memory accesses

- doing two memory accesses is already very slow
- solution: tree with many children from each node
  - (far from binary tree's left/right child)

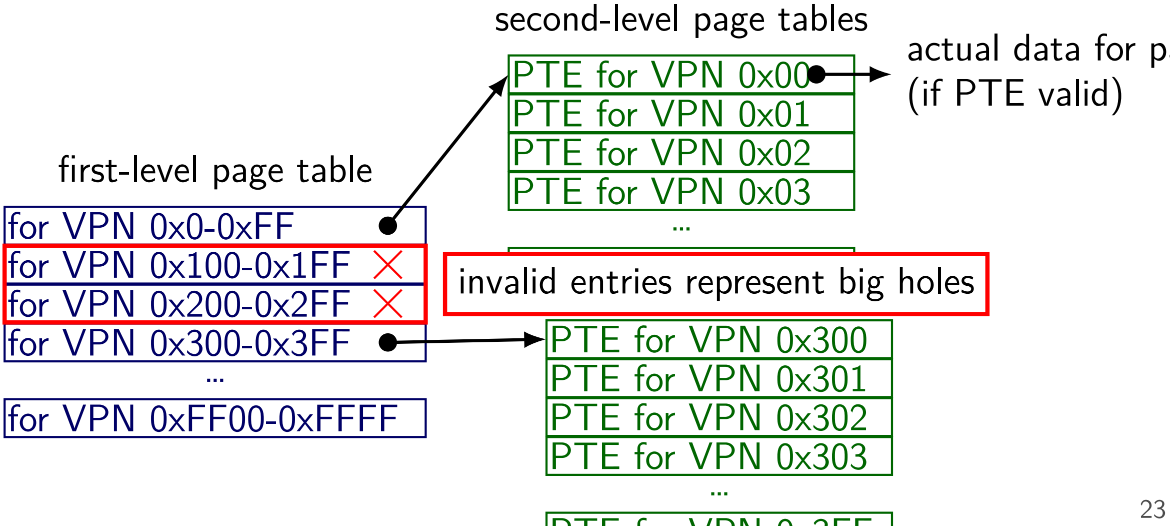
two-level page tables

two-level page tables for 65536 pages (16-bit VPN; 256 entries/table)



two-level page tables

two-level page tables for 65536 pages (16-bit VPN; 256 entries/table)



two-level page tables

two-level page tables for 65536 pages (16-bit VPN; 256 entries/table)

first-level pag

for VPN 0x0-0xF
for VPN 0x100-0
for VPN 0x200-0
for VPN 0x300-0
...
for VPN 0xFF00

for p
d)

first-level page table

VPN range	valid	...	physical page # (of next page table)
0x0000-0x00FF	1	...	0x22343
0x0100-0x01FF	0	...	0x00000
0x0200-0x02FF	0	...	0x00000
0x0300-0x03FF	1	...	0x33454
0x0400-0x04FF	1	...	0xFF043
...	...	...	...
0xFF00-0xFFFF	1	...	0xFF045

PTE for VPN 0x303
...

two-level page tables

two-level page tables for 65536 pages (16-bit VPN; 256 entries/table)

first-level pag

for VPN 0x0-0xF

for VPN 0x100-0

for VPN 0x200-0

for VPN 0x300-0

...

for VPN 0xFF00

for p

d)

first-level page table

VPN range	valid	...	physical page # (of next page table)
0x0000-0x00FF	1	...	0x22343
0x0100-0x01FF	0	...	0x00000
0x0200-0x02FF	0	...	0x00000
0x0300-0x03FF	1	...	0x33454
0x0400-0x04FF	1	...	0xFF043
...	...	...	...
0xFF00-0xFFFF	1	...	0xFF045

PTE for VPN 0x303

...

two-level page tables

two-level page tables for 65536 pages (16-bit VPN; 256 entries/table)

first-level pag

for VPN 0x0-0xF
for VPN 0x100-0
for VPN 0x200-0
for VPN 0x300-0
...
for VPN 0xFF00

for p
d)

first-level page table

VPN range	valid	...	physical page # (of next page table)
0x0000-0x00FF	1	...	0x22343
0x0100-0x01FF	0	...	0x00000
0x0200-0x02FF	0	...	0x00000
0x0300-0x03FF	1	...	0x33454
0x0400-0x04FF	1	...	0xFF043
...	...	...	...
0xFF00-0xFFFF	1	...	0xFF045

PTE for VPN 0x303
...
PTE for VPN 0x3FF

two-level page tables

two-level page tables for 65536 pages (16-bit VPN; 256 entries/table)

first-level page table

for VPN 0x0-0xFF
for VPN 0x100-0x1FF
for VPN 0x200-0x2FF
for VPN 0x300-0x3FF
…
for VPN 0xFF00-0xFFFF

a second-level page table

VPN	valid	…	physical page # (of data)
0x300	1	…	0x42443
0x301	1	…	0x4A9DE
0x302	1	…	0x5C001
0x303	0	…	0x00000
0x304	1	…	0x6C223
…	…	…	…
0x3FF	0	…	0x00000

PTE for VPN 0x303

…

PTE for VPN 0x3FF

two-level page tables

two-level page tables for 65536 pages (16-bit VPN; 256 entries/table)

a second-level page table

VPN	valid	…	physical page # (of data)
0x300	1	…	0x42443
0x301	1	…	0x4A9DE
0x302	1	…	0x5C001
0x303	0	…	0x00000
0x304	1	…	0x6C223
…	…	…	…
0x3FF	0	…	0x00000

first-level page table

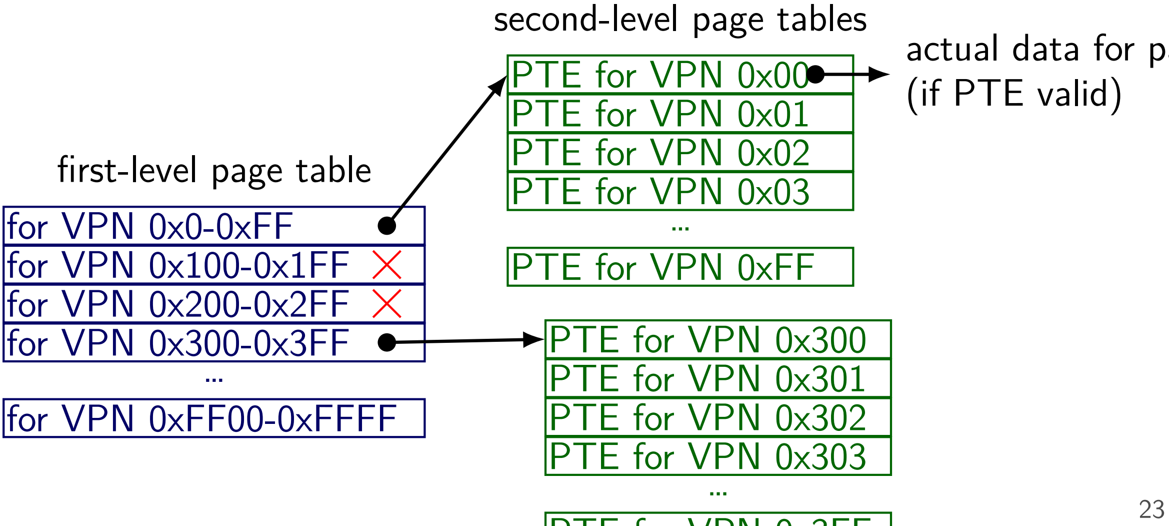
for VPN 0x0-0xFF
for VPN 0x100-0x1FF ✕
for VPN 0x200-0x2FF ✕
for VPN 0x300-0x3FF
…
for VPN 0xFF00-0xFFFF

PTE for VPN 0x303

…

two-level page tables

two-level page tables for 65536 pages (16-bit VPN; 256 entries/table)



two-level page table lookup

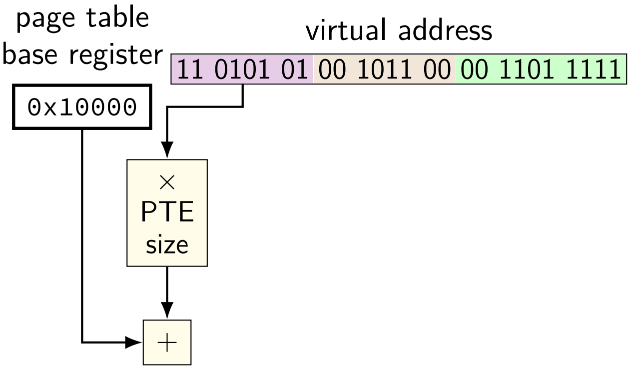
virtual address

11 0101 01	00 1011 00	00 1101 1111

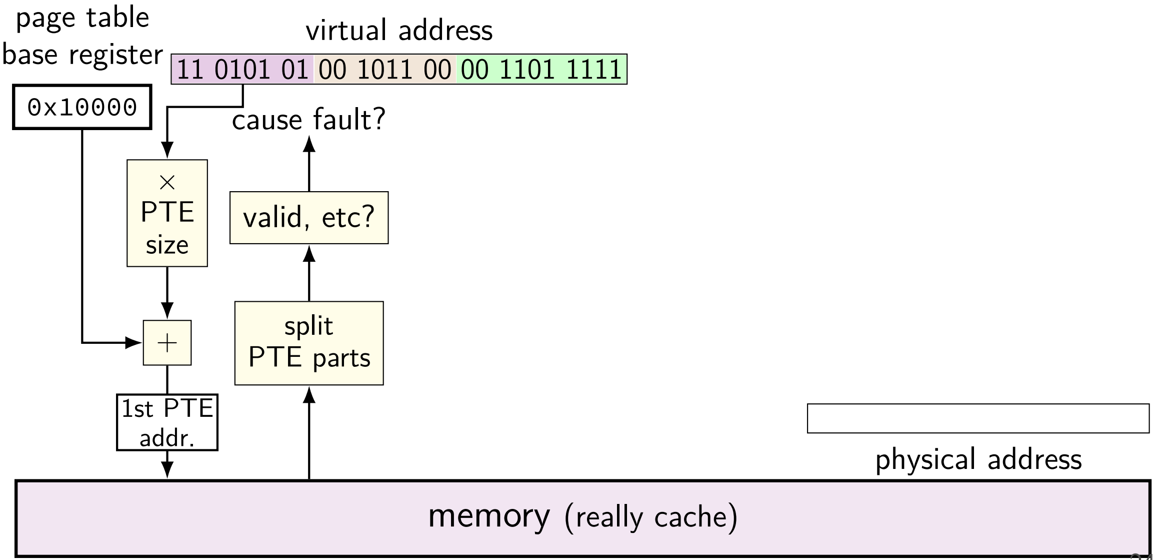
VPN — split into two parts (one per level)

this example: parts equal sized — common, but not required

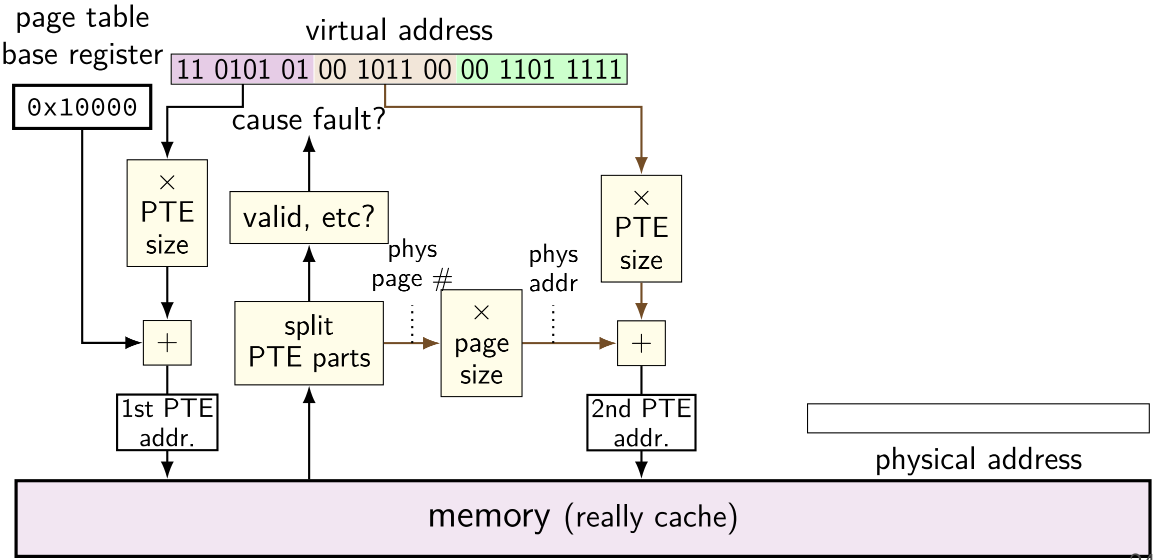
two-level page table lookup



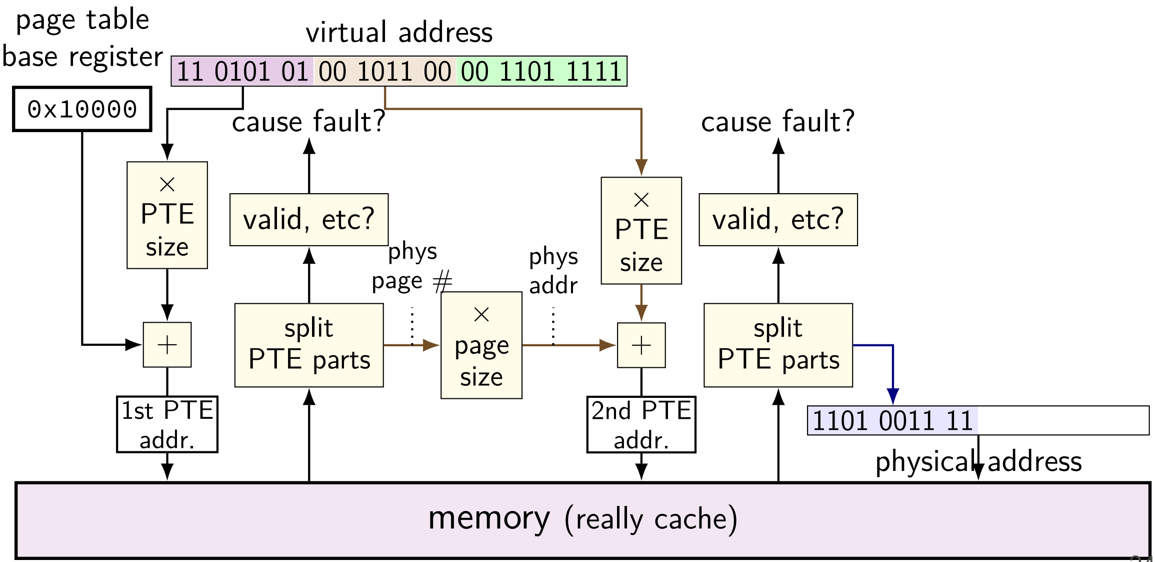
two-level page table lookup



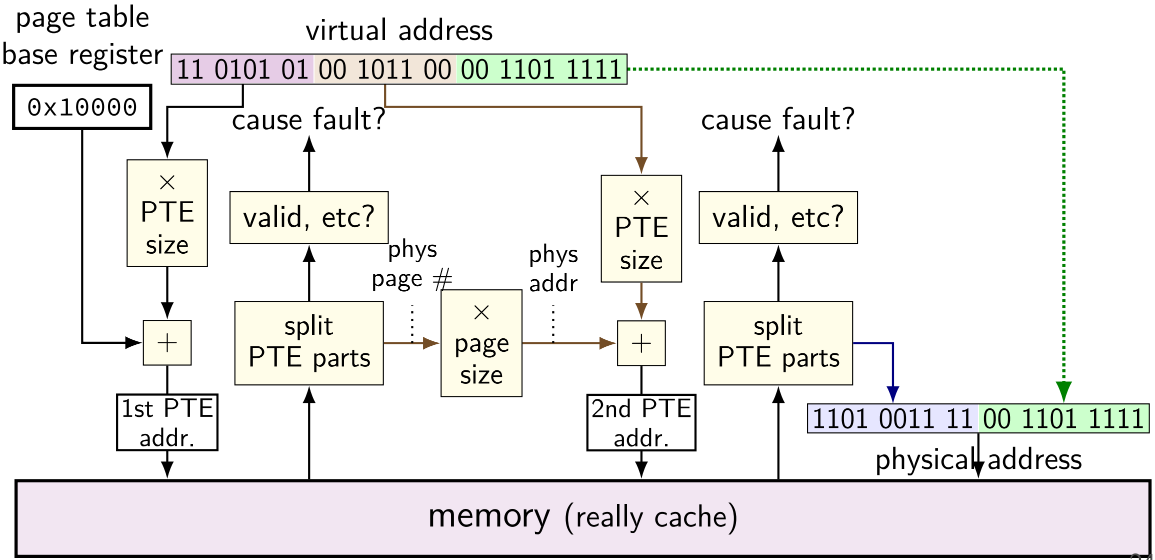
two-level page table lookup



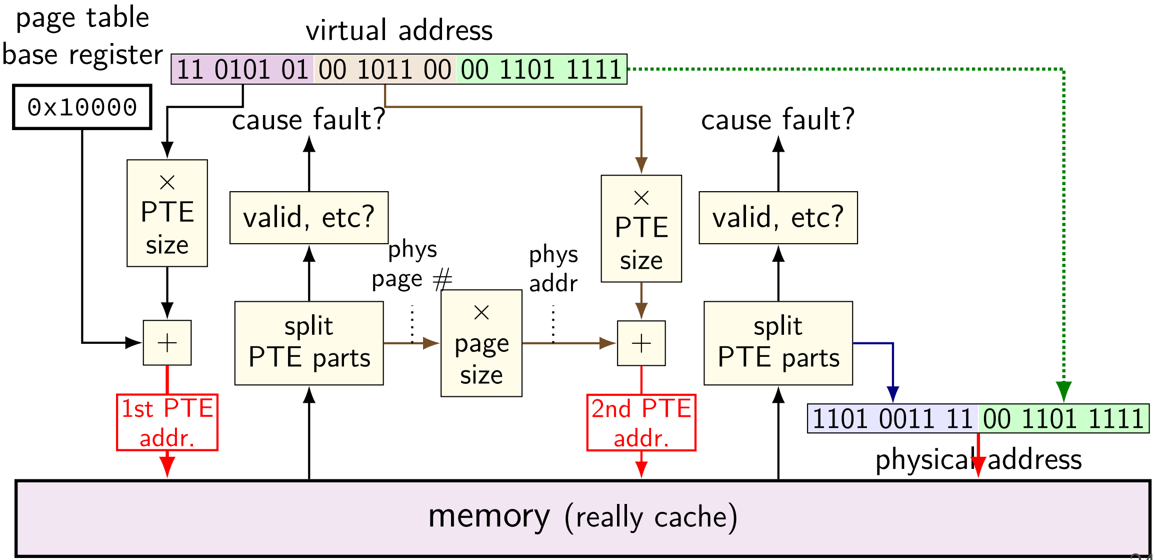
two-level page table lookup



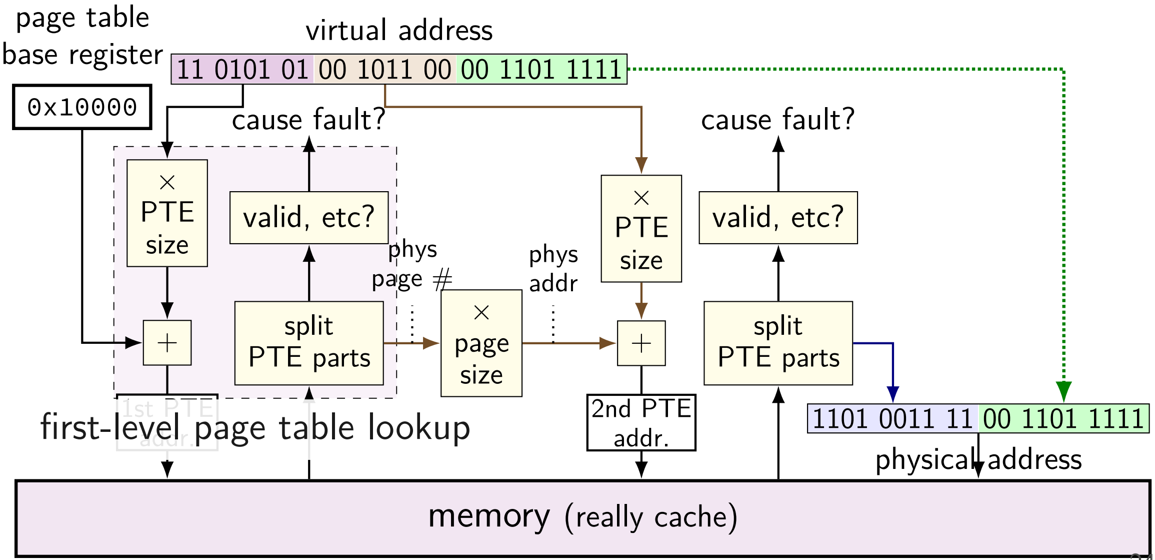
two-level page table lookup



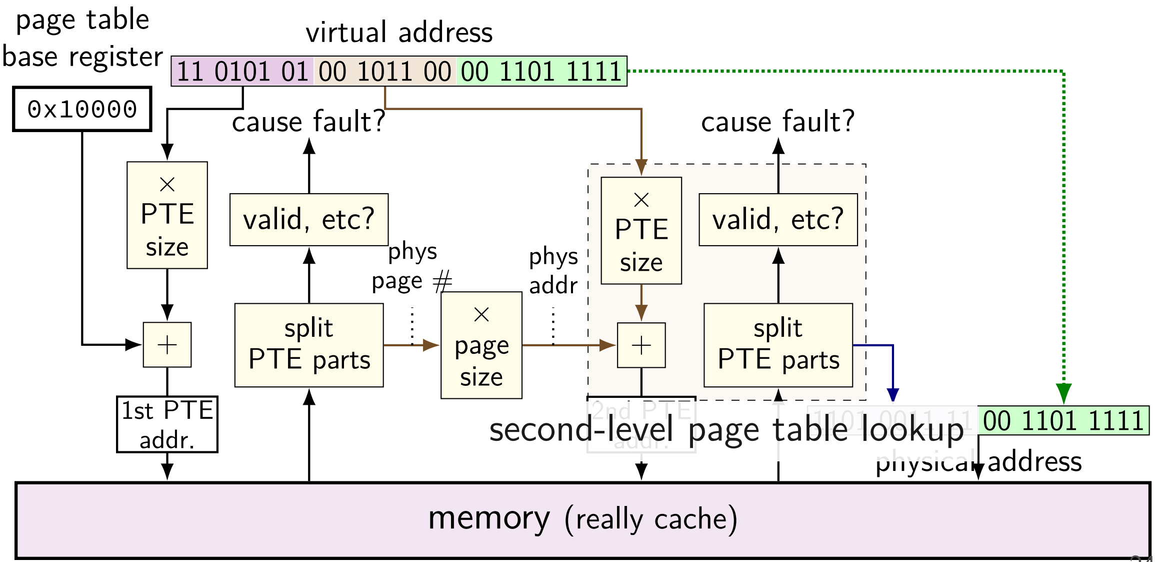
two-level page table lookup



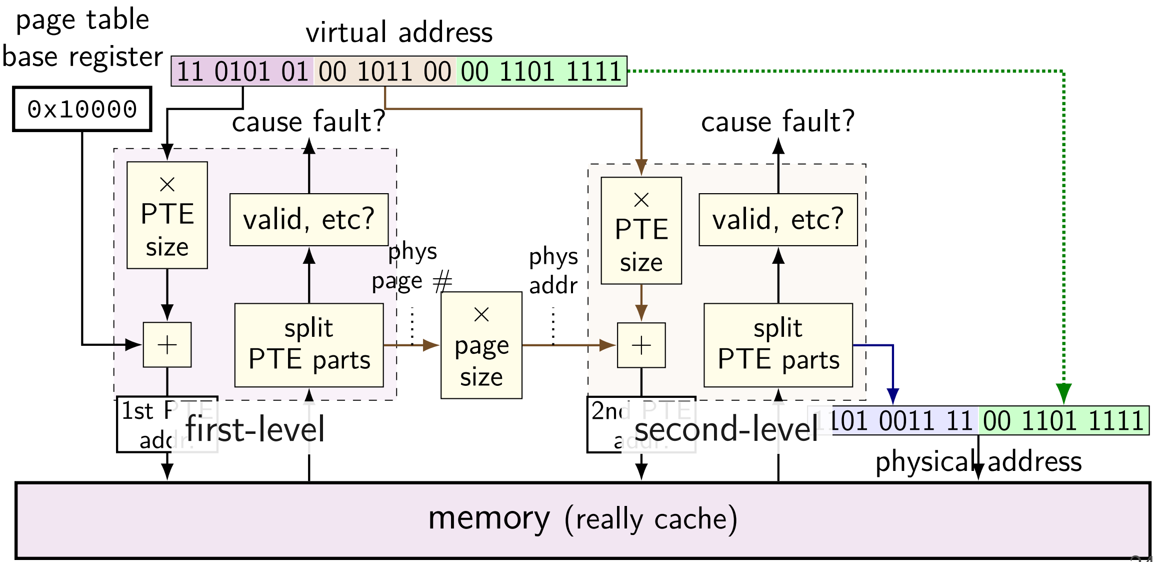
two-level page table lookup



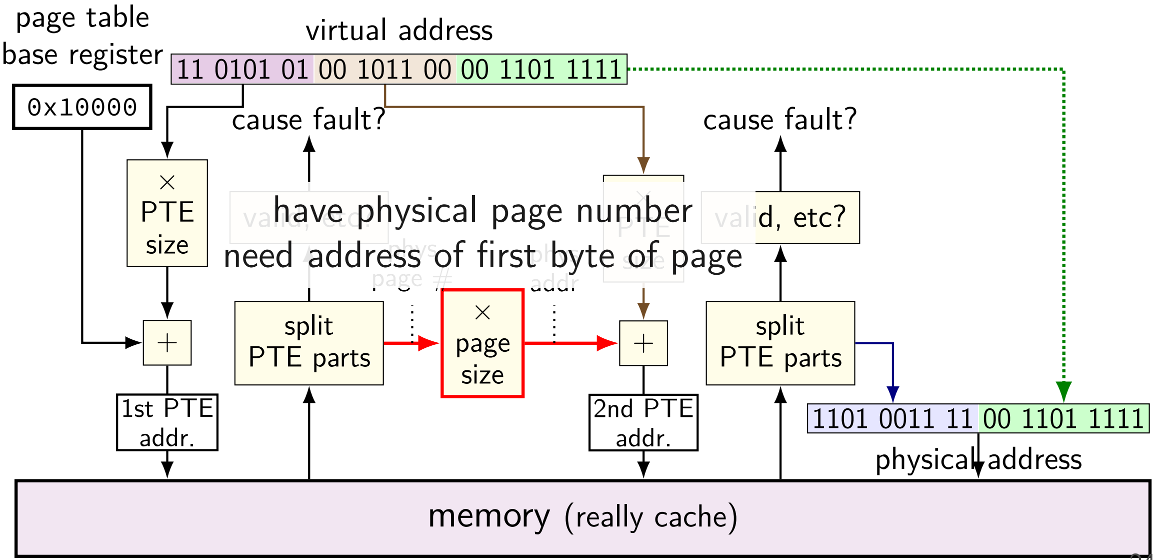
two-level page table lookup



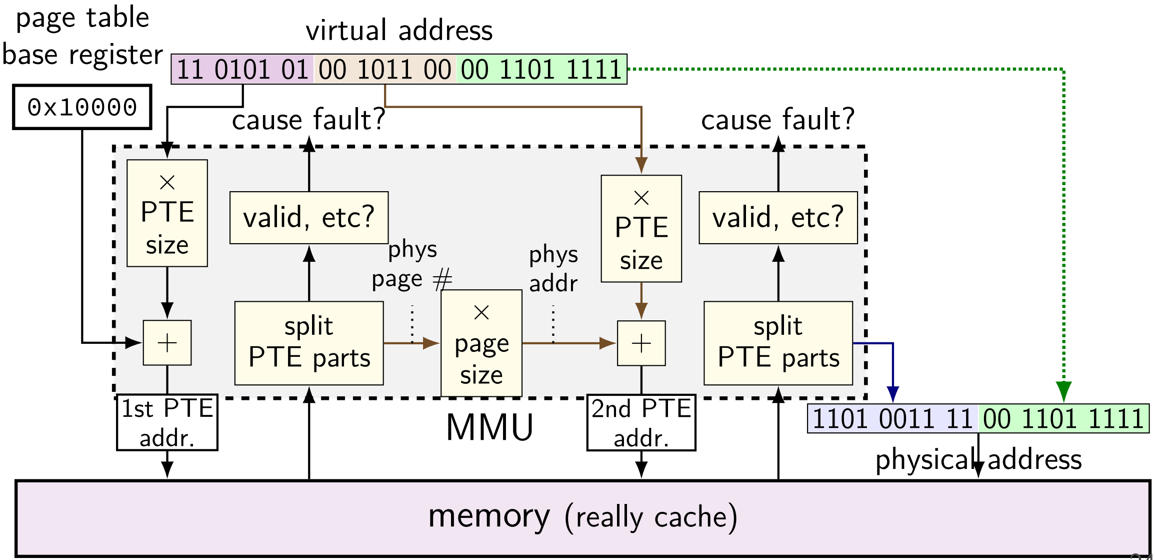
two-level page table lookup



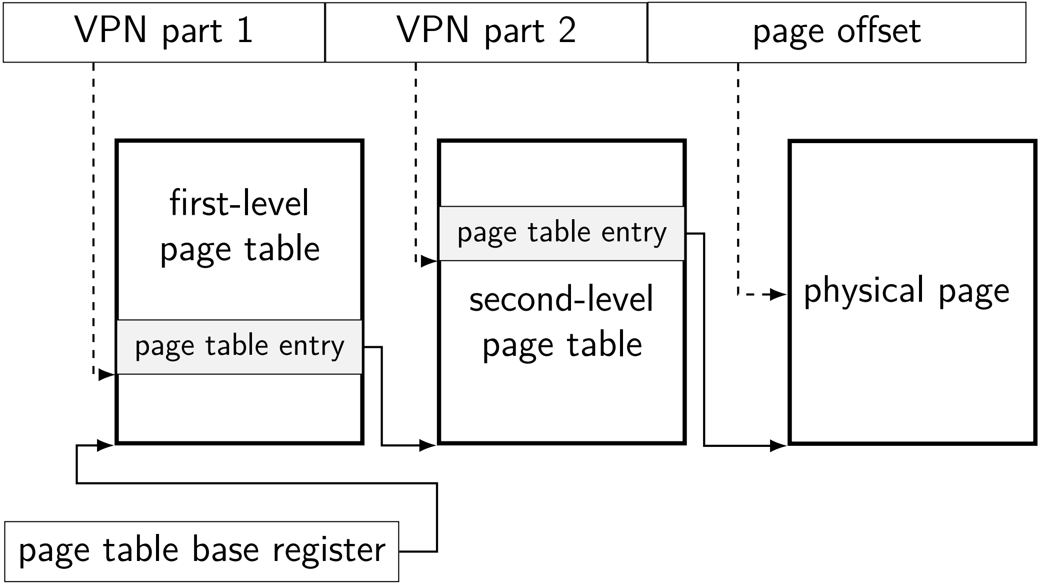
two-level page table lookup



two-level page table lookup



another view



multi-level page tables

VPN split into pieces for each level of page table

top levels: page table entries point to next page table

- usually using physical page number of next page table

bottom level: page table entry points to destination page

validity checks at each level

note on VPN splitting

indexes used for lookup parts of the virtual page number

(there are not multiple VPNs)

assignment

assignment: variable number of LEVELS

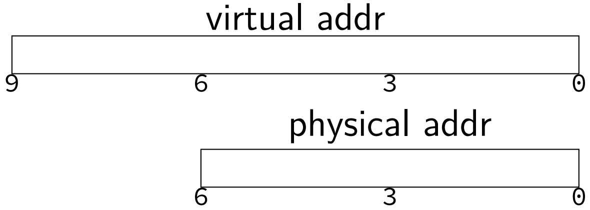
page tables always one page size

means upper bits of virtual address values not used

2-level splitting

9-bit virtual address

6-bit physical address



2-level splitting

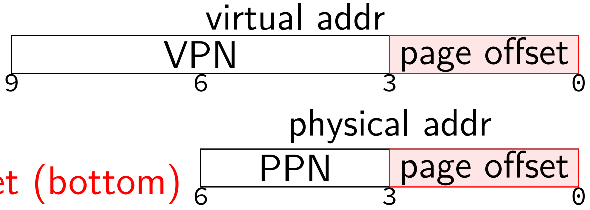
9-bit virtual address

6-bit physical address

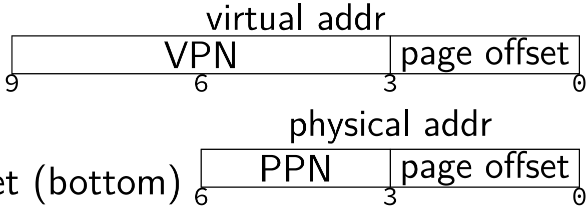
8-byte pages → 3-bit page offset (bottom)

9-bit VA: 6 bit VPN + 3 bit PO

6-bit PA: 3 bit PPN + 3 bit PO



2-level splitting



9-bit virtual address

6-bit physical address

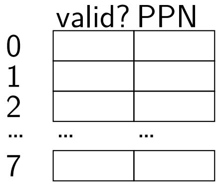
8-byte pages → 3-bit page offset (bottom)

9-bit VA: 6 bit VPN + 3 bit PO

6-bit PA: 3 bit PPN + 3 bit PO

1 page page tables w/ 1 byte entry → 8 entry PTs

page table (either level)



2-level splitting

9-bit virtual address

6-bit physical address

8-byte pages → 3-bit page offset (bottom)

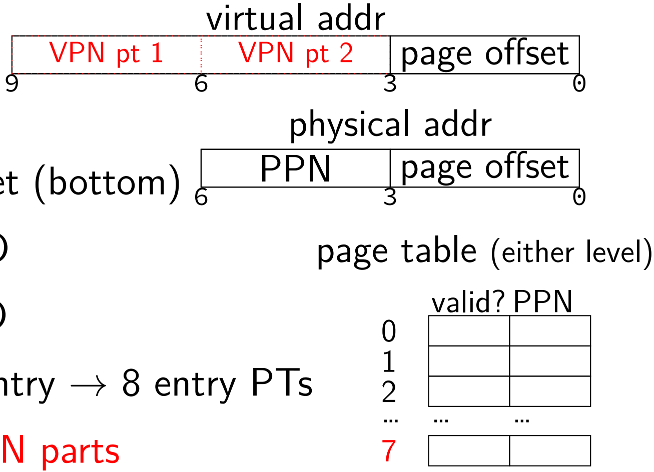
9-bit VA: 6 bit VPN + 3 bit PO

6-bit PA: 3 bit PPN + 3 bit PO

1 page page tables w/ 1 byte entry → 8 entry PTs

8 entry page tables → 3-bit VPN parts

9-bit VA: 3 bit VPN part 1; 3 bit VPN part 2



2-level example

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused

page table base register `0x20`; translate virtual address `0x129`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	00 91 72 13
0x24-7	F4 A5 36 07
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	AC DC DC 0C

2-level example

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused

page table base register `0x20`; translate virtual address `0x129`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	00 91 72 13
0x24-7	F4 A5 36 07
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	AC DC DC 0C

$\texttt{0x129} = \texttt{1 0010 1001}$

$\texttt{0x20} + \texttt{0x4} \times 1 = \texttt{0x24}$

PTE 1 value:

$\texttt{0xF4} = \texttt{1111 0100}$

PPN 111, valid 1

2-level example

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused

page table base register `0x20`; translate virtual address `0x129`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	00 91 72 13
0x24-7	F4 A5 36 07
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	AC DC DC 0C

$\texttt{0x129} = \texttt{1 0010 1001}$

$\texttt{0x20} + \texttt{0x4} \times 1 = \texttt{0x24}$

PTE 1 value:

$\texttt{0xF4} = \texttt{1111 0100}$

PPN 111, valid 1

PTE 2 addr:

$\texttt{111 000} + \texttt{101} \times 1 = \texttt{0x3D}$

PTE 2 value: 0xDC

2-level example

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused

page table base register `0x20`; translate virtual address `0x129`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	00 91 72 13
0x24-7	F4 A5 36 07
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	AC DC DC 0C

$\texttt{0x129} = \texttt{1 0010 1001}$

$\texttt{0x20} + \texttt{0x4} \times 1 = \texttt{0x24}$

PTE 1 value:

$\texttt{0xF4} = \texttt{1111 0100}$

PPN `111`, valid 1

PTE 2 addr:

$\texttt{111 000} + \texttt{101} \times 1 = \texttt{0x3D}$

PTE 2 value: `0xDC`

PPN `110`; valid 1

M[`110 001` (`0x31`)] = `0x0A`

2-level example

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused

page table base register `0x20`; translate virtual address `0x129`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	00 91 72 13
0x24-7	F4 A5 36 07
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	AC DC DC 0C

`0x129` $=$ `1 0010 1001`

`0x20` $+$ `0x4` $\times 1 =$ `0x24`

PTE 1 value:

`0xF4` $=$ `1111 0100`

PPN `111`, valid 1

PTE 2 addr:

`111 000` $+$ `101` $\times$ `1` $=$ `0x3D`

PTE 2 value: `0xDC`

PPN `110`; valid 1

M[`110 001` (`0x31`)] $=$ `0x0A`

2-level example

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused

page table base register `0x20`; translate virtual address `0x129`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	00 91 72 13
0x24-7	F4 A5 36 07
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	AC DC DC 0C

$\texttt{0x129} = \texttt{1 0010 1001}$

$\texttt{0x20} + \texttt{0x4} \times 1 = \texttt{0x24}$

PTE 1 value:

$\texttt{0xF4} = \texttt{1111 0100}$

PPN `111`, valid 1

PTE 2 addr:

$\texttt{111 000} + \texttt{101} \times 1 = \texttt{0x3D}$

PTE 2 value: `0xDC`

PPN `110`; valid 1

$M[\texttt{110 001 (0x31)}] = \texttt{0x0A}$

2-level exercise (2)

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused;

page table base register `0x10`; translate virtual address `0x109`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 5A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	D0 D1 D2 D3
0x24-7	D4 D5 D6 D7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

2-level exercise (2)

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused;

page table base register `0x10`; translate virtual address `0x109`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 5A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	D0 D1 D2 D3
0x24-7	D4 D5 D6 D7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

`0x109` = `100 011 001`

(PTE 1 at:
0x10 + PTE size times 4 (100))

PTE 1: `0x1B` at `0x14`

PTE 1: PPN `000` (0) valid 1

(second table at:
0 (000) times page size = 0x00)

PTE 2: `0x33` at `0x03`

PTE 2: PPN `001` (1) valid 1

`001 001` = `0x09` → `0x99`

2-level exercise (2)

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused;

page table base register `0x10`; translate virtual address `0x109`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 5A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	D0 D1 D2 D3
0x24-7	D4 D5 D6 D7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

`0x109` = `100 011 001`

(PTE 1 at:

0x10 + PTE size times 4 (100))

PTE 1: `0x1B` at `0x14`

PTE 1: PPN `000` (0) valid 1

(second table at:

0 (000) times page size = 0x00)

PTE 2: `0x33` at `0x03`

PTE 2: PPN `001` (1) valid 1

`001 001` = `0x09` → `0x99`

2-level exercise (2)

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused;

page table base register `0x10`; translate virtual address `0x109`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 5A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	D0 D1 D2 D3
0x24-7	D4 D5 D6 D7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

`0x109` = `100 011 001`

(PTE 1 at:

0x10 + PTE size times 4 (100))

PTE 1: `0x1B` at `0x14`

PTE 1: PPN `000` (0) valid 1

(second table at:

0 (000) times page size = 0x00)

PTE 2: `0x33` at `0x03`

PTE 2: PPN `001` (1) valid 1

`001 001` = `0x09` → `0x99`

2-level exercise (2)

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused;

page table base register `0x10`; translate virtual address `0x109`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 5A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	D0 D1 D2 D3
0x24-7	D4 D5 D6 D7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

`0x109` = `100 011 001`

(PTE 1 at:

0x10 + PTE size times 4 (100))

PTE 1: `0x1B` at `0x14`

PTE 1: PPN `000` (0) valid 1

(second table at:

0 (000) times page size = 0x00)

PTE 2: `0x33` at `0x03`

PTE 2: PPN `001` (1) valid 1

`001 001` = `0x09` → `0x99`

2-level exercise (1)

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused;

page table base register `0x08`; translate virtual address `0x0FB`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	D0 D1 D2 D3
0x24-7	D4 D5 D6 D7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

2-level exercise (1)

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused;

page table base register `0x08`; translate virtual address `0x0FB`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	D0 D1 D2 D3
0x24-7	D4 D5 D6 D7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

`0x0F3` $=$ `011 111 011`

(PTE 1 addr: `0x08` $+$ PTE size times 011 (3))

PTE 1: `0xBB` at `0x0B`

PTE 1: PPN `101` (5) valid `1`

PTE 2: `0xF0` at `0x2F`

PTE 2: PPN `111` (7) valid `1`

`111 011` $=$ `0x3B` $\rightarrow$ `0x0C`

2-level exercise (1)

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused;

page table base register `0x08`; translate virtual address `0x0FB`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	D0 D1 D2 D3
0x24-7	D4 D5 D6 D7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

`0x0F3` $=$ `011 111 011`
(PTE 1 addr: `0x08` $+$
PTE size times 011 (3))
PTE 1: `0xBB` at `0x0B`
PTE 1: PPN `101` (5) valid `1`
PTE 2: `0xF0` at `0x2F`
PTE 2: PPN `111` (7) valid `1`
`111 011` $=$ `0x3B` $\rightarrow$ `0x0C`

2-level exercise (1)

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused;

page table base register `0x08`; translate virtual address `0x0FB`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	D0 D1 D2 D3
0x24-7	D4 D5 D6 D7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

`0x0F3` = `011 111 011`

(PTE 1 addr: `0x08` + PTE size times 011 (3))

PTE 1: `0xBB` at `0x0B`

PTE 1: PPN `101` (5) valid 1

PTE 2: `0xF0` at `0x2F`

PTE 2: PPN `111` (7) valid 1

`111 011` = `0x3B` → `0x0C`

2-level exercise (1)

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused;

page table base register `0x08`; translate virtual address `0x0FB`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	D0 D1 D2 D3
0x24-7	D4 D5 D6 D7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

`0x0F3` $=$ `011 111 011`

(PTE 1 addr: `0x08` $+$ PTE size times 011 (3))

PTE 1: `0xBB` at `0x0B`

PTE 1: PPN `101` (5) valid `1`

PTE 2: `0xF0` at `0x2F`

PTE 2: PPN `111` (7) valid `1`

`111 011` $=$ `0x3B` $\rightarrow$ `0x0C`

2-level exercise (3)

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused

page table base register `0x08`; translate virtual address `0x00B`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	D0 D1 D2 D3
0x24-7	D4 D5 D6 D7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

2-level exercise (3)

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused

page table base register `0x08`; translate virtual address `0x00B`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	D0 D1 D2 D3
0x24-7	D4 D5 D6 D7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

`0x0F3` = `000 001 011`

PTE 1: `0x88` at `0x08`

PTE 1: PPN `100` (5) valid `0`

page fault!

2-level exercise (3)

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused

page table base register `0x08`; translate virtual address `0x00B`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	D0 D1 D2 D3
0x24-7	D4 D5 D6 D7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

`0x0F3` = `000 001 011`

PTE 1: `0x88` at `0x08`

PTE 1: PPN `100` (5) valid `0`

page fault!

2-level exercise (4)

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused

page table base register `0x08`; translate virtual address `0x1CB`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	D0 D1 D2 D3
0x24-7	D4 D5 D6 D7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

2-level exercise (4)

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused

page table base register `0x08`; translate virtual address `0x1CB`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	D0 D1 D2 D3
0x24-7	D4 D5 D6 D7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

`0x1CB` = `111 001 011`

PTE 1: `0xFF` at `0x0F`

PTE 1: PPN `111` (7) valid `1`

PTE 2: `0x0C` at `0x39`

PTE 2: PPN `000` (0) valid `0`

page fault!

2-level exercise (4)

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused

page table base register `0x08`; translate virtual address `0x1CB`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	D0 D1 D2 D3
0x24-7	D4 D5 D6 D7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

`0x1CB` = `111 001 011`

PTE 1: `0xFF` at `0x0F`

PTE 1: PPN `111` (7) valid `1`

PTE 2: `0x0C` at `0x39`

PTE 2: PPN `000` (0) valid `0`

page fault!

2-level exercise (4)

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused

page table base register `0x08`; translate virtual address `0x1CB`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	bytes
0x20-3	D0 D1 D2 D3
0x24-7	D4 D5 D6 D7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

`0x1CB` = `111 001 011`

PTE 1: `0xFF` at `0x0F`

PTE 1: PPN `111` (7) valid `1`

PTE 2: `0x0C` at `0x39`

PTE 2: PPN `000` (0) valid `0`

page fault!

2-level exercise (5)

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

page table base register `0x10`; translate virtual address `0x376`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	AC BC DC EC

physical addresses	bytes
0x20-3	D0 E1 D2 D3
0x24-7	D4 E5 D6 E7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

2-level exercise (5)

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

page table base register `0x10`; translate virtual address `0x376`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	AC BC DC EC

physical addresses	bytes
0x20-3	D0 E1 D2 D3
0x24-7	D4 E5 D6 E7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

`0x376` $=$ `110 111 0110`

PTE 1: 0x10 $+ 6 \times 2 =$ `0x1C`: `AC BC`

PTE 1: PPN `10` valid `1`

PTE 2: 0x20 $+ 7 \times 2 =$ `0x2E`: `EF F0`

PTE 2: PPN `11` valid `1`

`11 0110` $=$ `0x36` $\rightarrow$ `DB`

2-level exercise (5)

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

page table base register `0x10`; translate virtual address `0x376`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	AC BC DC EC

physical addresses	bytes
0x20-3	D0 E1 D2 D3
0x24-7	D4 E5 D6 E7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

`0x376` = 110 111 0110

PTE 1: 0x10 + 6×2 = `0x1C`:

AC BC

PTE 1: PPN 10 valid 1

PTE 2: 0x20 + 7×2 = `0x2E`:

EF F0

PTE 2: PPN 11 valid 1

11 0110 = 0x36 → DB

2-level exercise (5)

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

page table base register `0x10`; translate virtual address `0x376`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	AC BC DC EC

physical addresses	bytes
0x20-3	D0 E1 D2 D3
0x24-7	D4 E5 D6 E7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

`0x376` = `110 111 0110`

PTE 1: $0x10 + 6 \times 2 =$ `0x1C`:

AC BC

PTE 1: PPN `10` valid `1`

PTE 2: $0x20 + 7 \times 2 =$ `0x2E`:

EF F0

PTE 2: PPN `11` valid `1`

`11 0110` = `0x36` → `DB`

2-level exercise (5)

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

page table base register `0x10`; translate virtual address `0x376`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	AC BC DC EC

physical addresses	bytes
0x20-3	D0 E1 D2 D3
0x24-7	D4 E5 D6 E7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

`0x376` $=$ `110 111 0110`

PTE 1: $0x10 + 6 \times 2 =$ `0x1C`:

`AC BC`

PTE 1: PPN `10` valid `1`

PTE 2: $0x20 + 7 \times 2 =$ `0x2E`:

`EF F0`

PTE 2: PPN `11` valid `1`

`11 0110` $=$ `0x36` $\rightarrow$ `DB`

2-level exercise (5)

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

page table base register `0x10`; translate virtual address `0x376`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	AC BC DC EC

physical addresses	bytes
0x20-3	D0 E1 D2 D3
0x24-7	D4 E5 D6 E7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

`0x376` $=$ `110 111 0110`

PTE 1: 0x10 $+ 6 \times 2 =$ `0x1C`:

`AC BC`

PTE 1: PPN `10` valid `1`

PTE 2: 0x20 $+ 7 \times 2 =$ `0x2E`:

`EF F0`

PTE 2: PPN `11` valid `1`

`11 0110` $=$ `0x36` $\rightarrow$ `DB`

2-level exercise (5)

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

page table base register `0x10`; translate virtual address `0x376`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	AC BC DC EC

physical addresses	bytes
0x20-3	D0 E1 D2 D3
0x24-7	D4 E5 D6 E7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

`0x376` $=$ `110 111 0110`

PTE 1: $\text{0x10} + 6 \times 2 =$ `0x1C`:

`AC BC`

PTE 1: PPN `10` valid `1`

PTE 2: $\text{0x20} + 7 \times 2 =$ `0x2E`:

`EF F0`

PTE 2: PPN `11` valid `1`

`11 0110` $=$ `0x36` $\rightarrow$ `DB`

2-level exercise (5)

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

page table base register `0x10`; translate virtual address `0x376`

physical addresses	bytes
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	AC BC DC EC

physical addresses	bytes
0x20-3	D0 E1 D2 D3
0x24-7	D4 E5 D6 E7
0x28-B	89 9A AB BC
0x2C-F	CD DE EF F0
0x30-3	BA 0A BA 0A
0x34-7	DB 0B DB 0B
0x38-B	EC 0C EC 0C
0x3C-F	FC 0C FC 0C

`0x376` $=$ `110 111 0110`

PTE 1: $0x10 + 6 \times 2 =$ `0x1C`:
`AC BC`

PTE 1: PPN `10` valid `1`

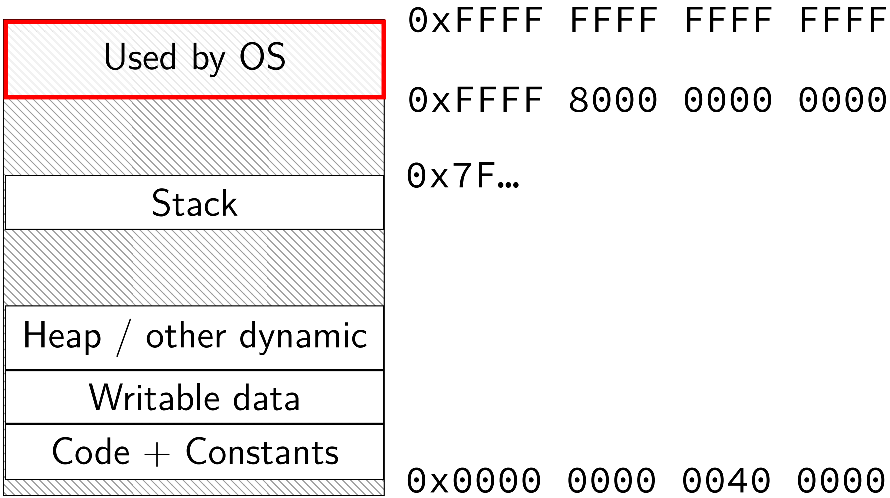
PTE 2: $0x20 + 7 \times 2 =$ `0x2E`:
`EF F0`

PTE 2: PPN `11` valid `1`

`11 0110` $=$ `0x36` $\rightarrow$ `DB`

backup slides

program memory



running OS code

system calls, I/O events, etc. run OS code in kernel mode

running OS code

system calls, I/O events, etc. run OS code in kernel mode

where in memory is this OS code?

running OS code

system calls, I/O events, etc. run OS code in kernel mode

where in memory is this OS code?

- probably have a page table entry pointing to it
- marked not accessible in user mode

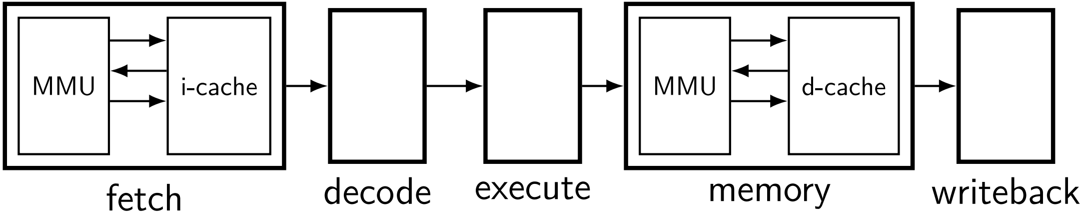
running OS code

system calls, I/O events, etc. run OS code in kernel mode

where in memory is this OS code?
- probably have a page table entry pointing to it
- marked not accessible in user mode

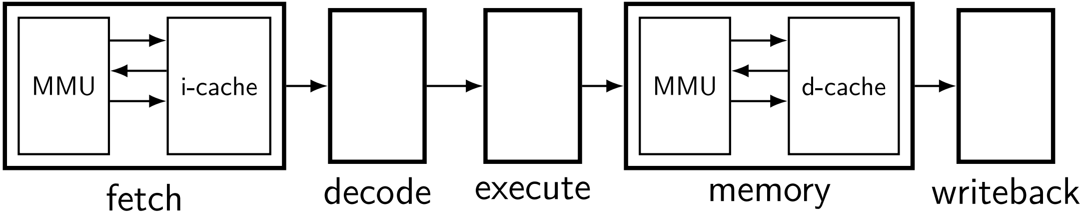
code better not be modified by user program
- otherwise: uncontrolled way to “escape” user mode

MMUs in the pipeline



up to four memory accesses per instruction

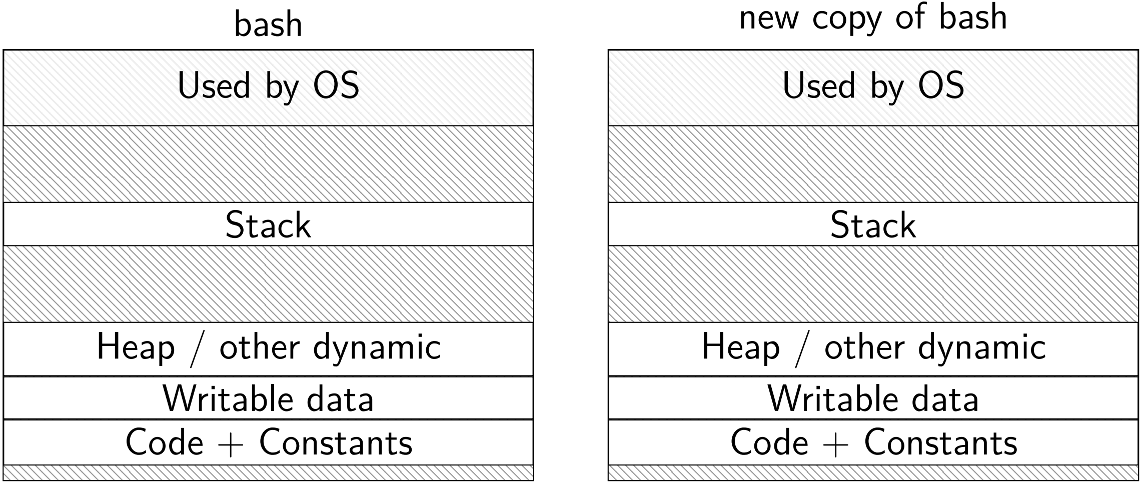
MMUs in the pipeline



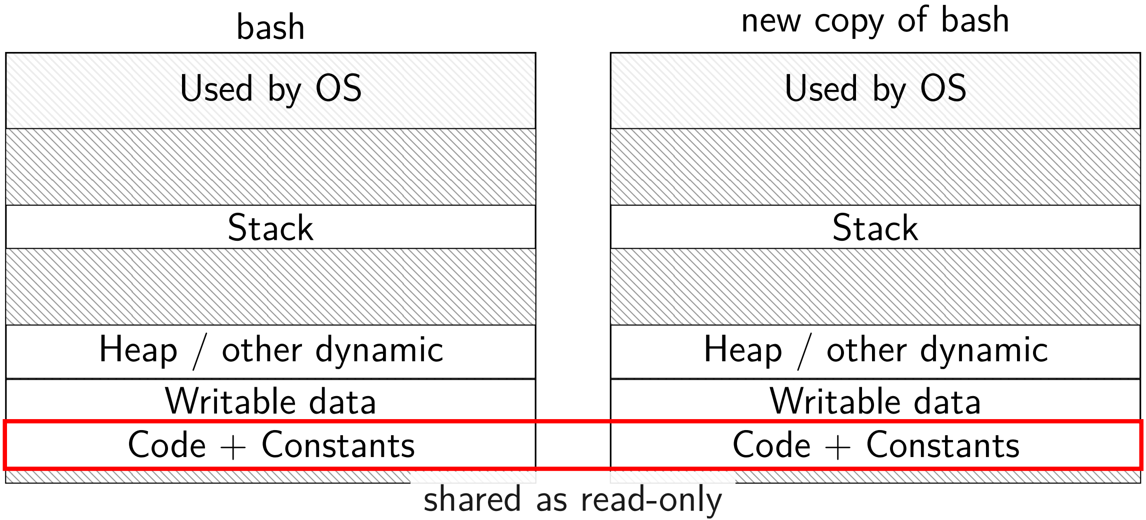
up to four memory accesses per instruction

challenging to make this fast (topic for a future date)

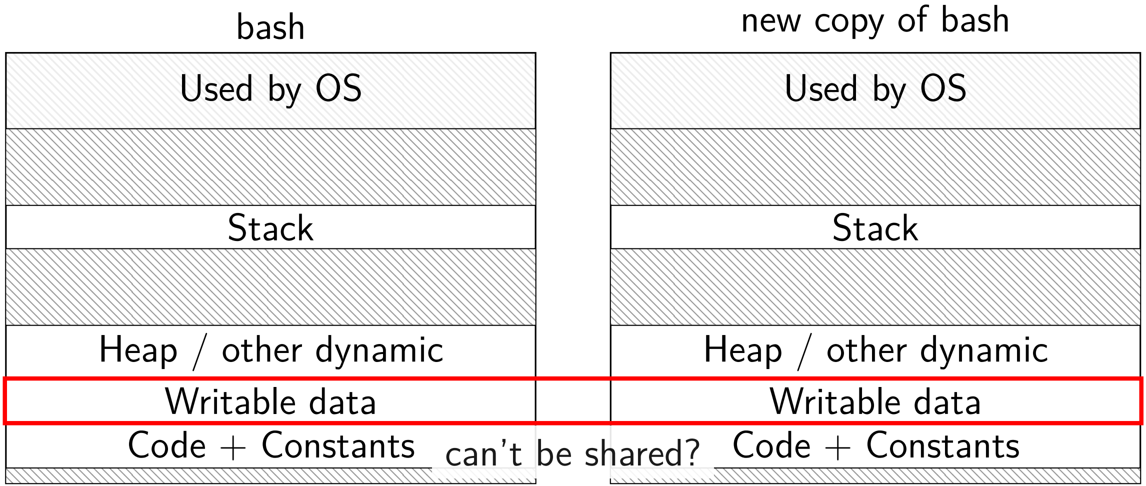
do we really need a complete copy?



do we really need a complete copy?



do we really need a complete copy?



trick for extra sharing

sharing writeable data is fine — until either process modifies it

- example: default value of global variables
- might typically not change
- (or OS might have preloaded executable's data anyways)

can we detect modifications?

trick for extra sharing

sharing writeable data is fine — until either process modifies it

- example: default value of global variables
- might typically not change
- (or OS might have preloaded executable's data anyways)

can we detect modifications?

trick: tell CPU (via page table) shared part is read-only

processor will trigger a fault when it's written

copy-on-write and page tables

VPN	valid?	write?	physical page
…	…	…	…
0x00601	1	1	0x12345
0x00602	1	1	0x12347
0x00603	1	1	0x12340
0x00604	1	1	0x200DF
0x00605	1	1	0x200AF
…	…	…	…

copy-on-write and page tables

VPN	valid?	write?	physical page
…	…	…	…
0x00601	1	0	0x12345
0x00602	1	0	0x12347
0x00603	1	0	0x12340
0x00604	1	0	0x200DF
0x00605	1	0	0x200AF
…	…	…	…

VPN	valid?	write?	physical page
…	…	…	…
0x00601	1	0	0x12345
0x00602	1	0	0x12347
0x00603	1	0	0x12340
0x00604	1	0	0x200DF
0x00605	1	0	0x200AF
…	…	…	…

copy operation actually duplicates page table
both processes share all physical pages
but marks pages in both copies as read-only

copy-on-write and page tables

VPN	valid?	write?	physical page
…	…	…	…
0x00601	1	0	0x12345
0x00602	1	0	0x12347
0x00603	1	0	0x12340
0x00604	1	0	0x200DF
0x00605	1	0	0x200AF
…	…	…	…

VPN	valid?	write?	physical page
…	…	…	…
0x00601	1	0	0x12345
0x00602	1	0	0x12347
0x00603	1	0	0x12340
0x00604	1	0	0x200DF
0x00605	1	0	0x200AF
…	…	…	…

when either process tries to write read-only page triggers a fault — OS actually copies the page

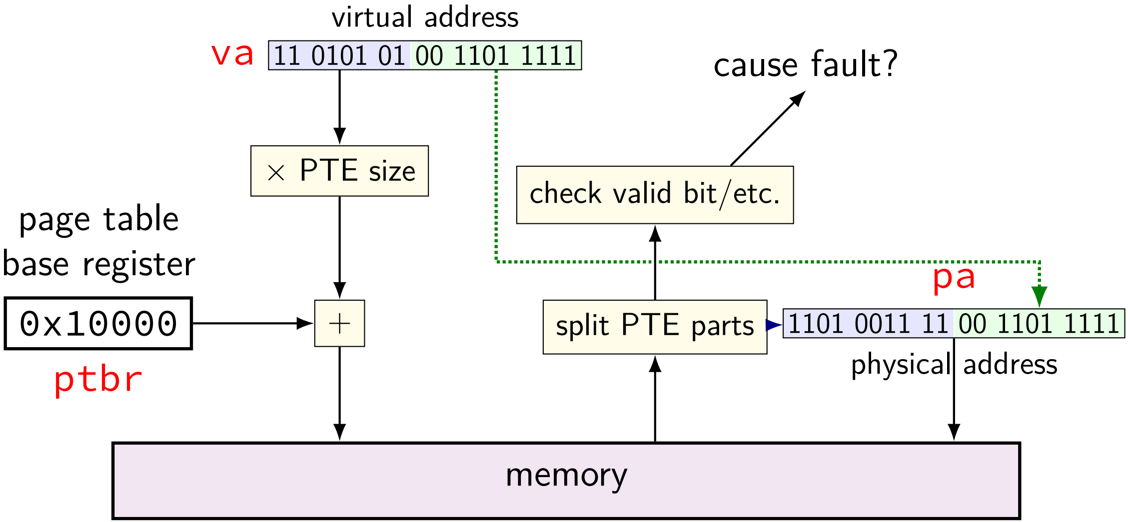
copy-on-write and page tables

VPN	valid?	write?	physical page
…	…	…	…
0x00601	1	0	0x12345
0x00602	1	0	0x12347
0x00603	1	0	0x12340
0x00604	1	0	0x200DF
0x00605	1	0	0x200AF
…	…	…	…

VPN	valid?	write?	physical page
…	…	…	…
0x00601	1	0	0x12345
0x00602	1	0	0x12347
0x00603	1	0	0x12340
0x00604	1	0	0x200DF
0x00605	1	1	0x300FD
…	…	…	…

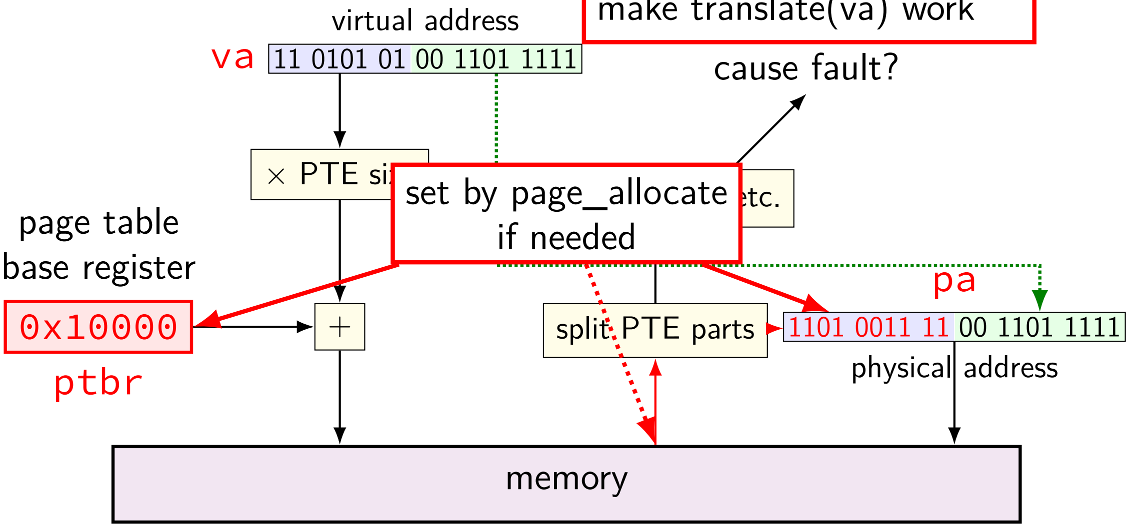
after allocating a copy, OS reruns the write instruction

pa=translate(va)



pa=translate(va)

page_allocate(va) needs to make translate(va) work



swapping

early motivation for virtual memory: swapping

using disk (or SSD, ...) as the next level of the memory hierarchy

- how our textbook and many other sources presents virtual memory

OS allocates program space on disk

- own mapping of virtual addresses to location on disk

DRAM is a cache for disk

swapping

early motivation for virtual memory: swapping

using disk (or SSD, ...) as the next level of the memory hierarchy

  how our textbook and many other sources presents virtual memory

OS allocates program space on disk

  own mapping of virtual addresses to location on disk

DRAM is a cache for disk

swapping components

"swap in" a page — exactly like allocating on demand!

- OS gets page fault — invalid in page table
- check where page actually is (from virtual address)
- read from disk
- eventually restart process

"swap out" a page

- OS marks as invalid in the page table(s)
- copy to disk (if modified)

HDD/SDDs are slow

HDD reads and writes: milliseconds to tens of milliseconds

- minimum size: 512 bytes
- writing tens of kilobytes basically as fast as writing 512 bytes

SSD writes and writes: hundreds of microseconds

- designed for writes/reads of kilobytes (not much smaller)

HDD/SDDs are slow

HDD reads and writes: milliseconds to tens of milliseconds

- minimum size: 512 bytes
- writing tens of kilobytes basically as fast as writing 512 bytes

SSD writes and writes: hundreds of microseconds

- designed for writes/reads of kilobytes (not much smaller)

HDD/SDDs are slow

HDD reads and writes: milliseconds to tens of milliseconds

- minimum size: 512 bytes
- writing tens of kilobytes basically as fast as writing 512 bytes

SSD writes and writes: hundreds of microseconds

- designed for writes/reads of kilobytes (not much smaller)

HDD/SDDs are slow

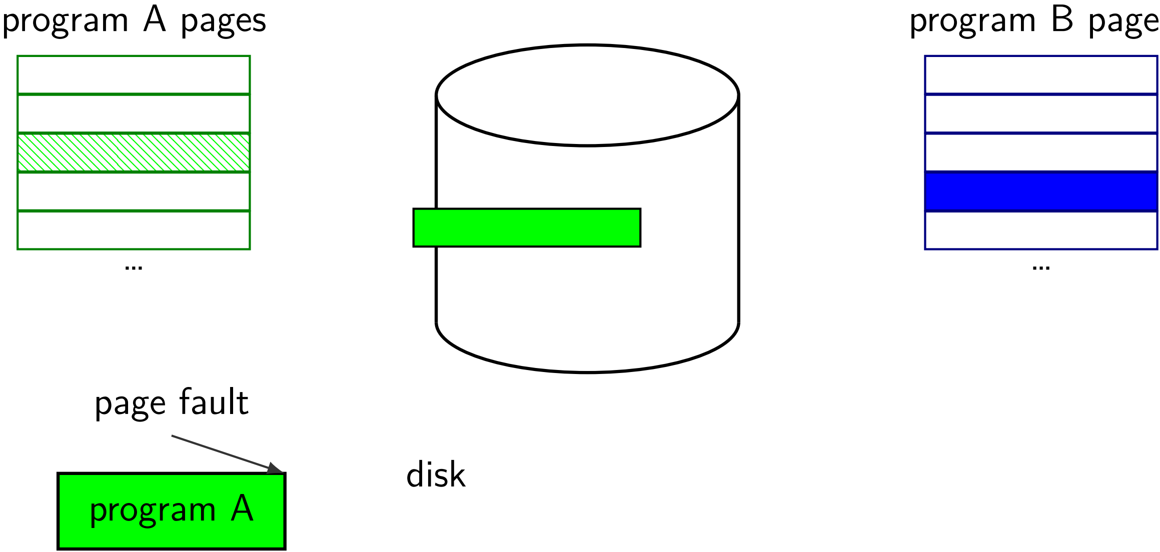
HDD reads and writes: milliseconds to tens of milliseconds

- minimum size: 512 bytes
- writing tens of kilobytes basically as fast as writing 512 bytes

SSD writes and writes: hundreds of microseconds

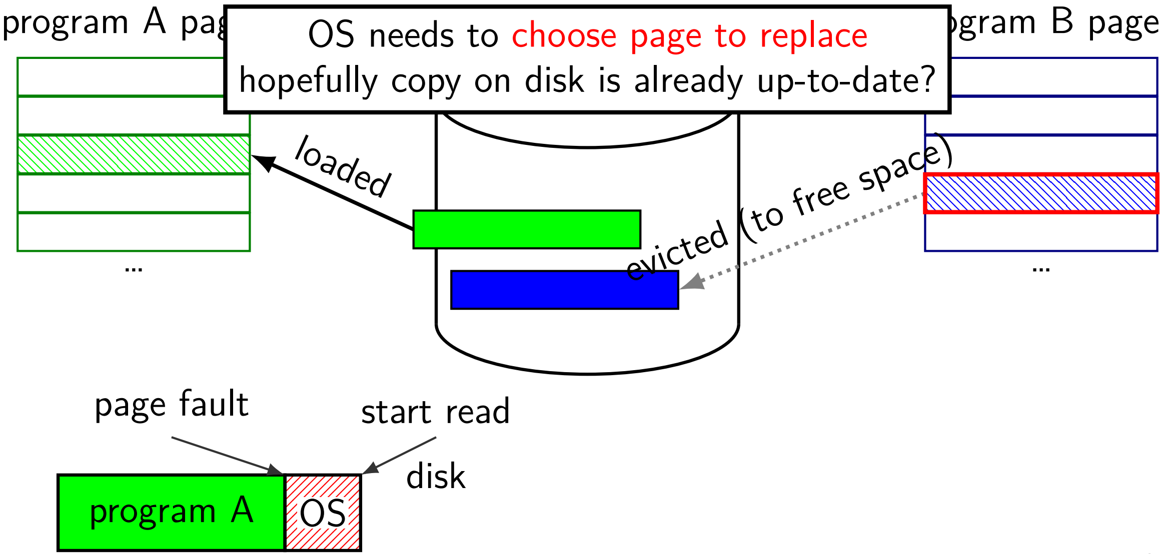
- designed for writes/reads of kilobytes (not much smaller)

swapping timeline

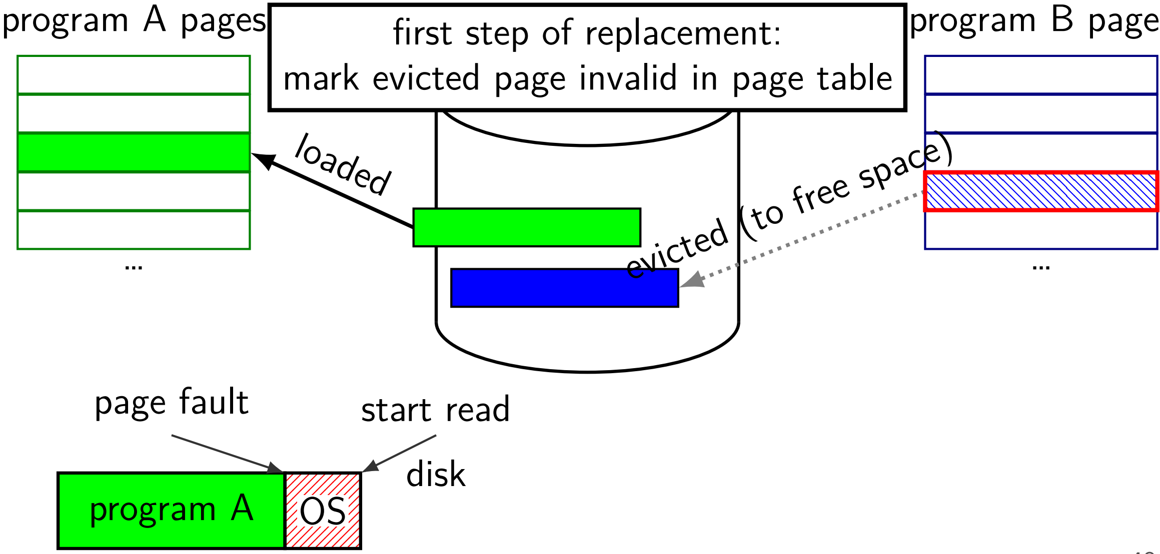


swapping timeline

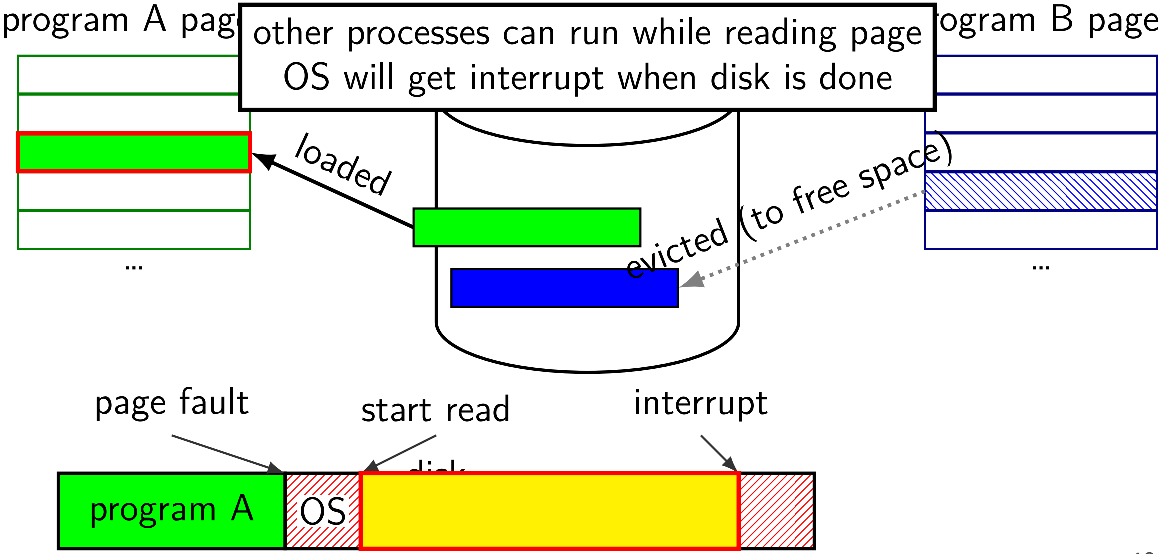
OS needs to choose page to replace
hopefully copy on disk is already up-to-date?



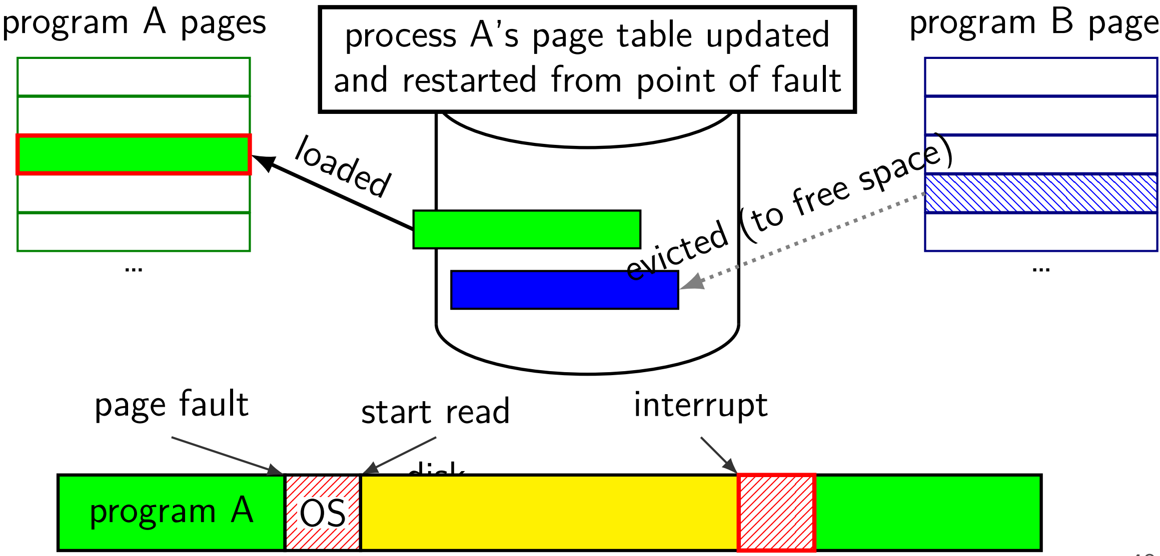
swapping timeline



swapping timeline



swapping timeline



swapping almost mmap

access mapped file for first time, read from disk
- (like swapping when memory was swapped out)

write "mapped" memory, write to disk eventually
- (like writeback policy in swapping)
- use "dirty" bit

extra detail: other processes should see changes
- all accesses to file use same physical memory

exercise: 64-bit system

my desktop: 39-bit physical addresses; 48-bit virtual addresses

4096 byte pages

exercise: 64-bit system

my desktop: 39-bit physical addresses; 48-bit virtual addresses

4096 byte pages

top 16 bits of 64-bit addresses not used for translation

exercise: 64-bit system

my desktop: 39-bit physical addresses; 48-bit virtual addresses

4096 byte pages

exercise: how many page table entries? (assuming page table like shown before)

exercise: how large are physical page numbers?

exercise: 64-bit system

my desktop: 39-bit physical addresses; 48-bit virtual addresses

4096 byte pages

exercise: how many page table entries? (assuming page table like shown before) $2^{48}/2^{12} = 2^{36}$ entries

exercise: how large are physical page numbers? $39 - 12 = 27$ bits

exercise: 64-bit system

my desktop: 39-bit physical addresses; 48-bit virtual addresses

4096 byte pages

exercise: how many page table entries? (assuming page table like shown before) $2^{48}/2^{12} = 2^{36}$ entries

exercise: how large are physical page numbers? $39 - 12 = 27$ bits

page table entries are 8 bytes (room for expansion, metadata)

- trick: power of two size makes table lookup faster

would take up 2^{39} bytes?? (512GB??)

backup slides