

# bitwise (part 1)

# last time

## object files

- contain machine code with things missing...

- relocation table: what to fill in

- symbol table: what other files might need

## C pointer arithmetic and arrays

- `foo[x] = *(x+foo)`

- `foo + X` uses size of what `foo` points to

## typedef struct

## undefined behavior

- C specification says compilers can do whatever

- signed integer overflow

- divide-by-zero

- out-of-bounds pointers

## quiz 2 Q1

suppose  $p$  is  $0x10000$ ,  $x$  is  $0x3$ ,  $*p$  (memory @  $0x10000$ ) is  $0x1$

$$*p = x * 2$$

*result:* memory @  $0x10000$  becomes  $0x3 * 2 = 0x6$ ;  $p$ ,  $x$  unchanged

A. `movq %rax, (%r8); leaq (%r8, 2), %r8`

memory @  $0x10000$  ( $*p$ )  $\leftarrow x = 0x3$

$p \leftarrow p \times 2 = 0x20000$

*actual result:* memory @  $0x10000$  becomes  $0x3$ ;  $p$  also changed

B. `leaq (%rax, 2), %r8; leaq (%r8, 2), %r8`

$p \leftarrow x \times 2 = 0x6$

$p \leftarrow p \times 2 = 0xc$

*actual result:* memory @  $0x10000$  unchanged;  $p$  changed

## quiz 2 Q2

start:

```
    addq %r8, %r9
    cmpq %r9, %r10
    jle start
```

end:

to get to end, need `jle` not to jump back to start

when `jle` jumps back to start, last result was  $\leq 0$ , so  
(ignoring overflow)

when `jle` does not jump to start, last result was  $> 0$   
(ignoring overflow)

ZF = 1 if+only if last result = 0 ✘

SF = 1 if+only if last result is negative ✘

$\implies$  ZF = 0, SF = 0

## quiz 2 Q3

start:

```
    addq %r8, %r9  
    cmpq %r9, %r10  
    jle start
```

end:

cmpq+jle: if  $(r10 - r9 \leq 0)$  goto start

sub is subtract from

do ... while  $(r10 - r9 \leq 0)$

do ... while  $(r10 \leq r9)$

## quiz 2 Q4/5

```
foo:      // <- turns into symbol table entry
          //      pointing to next instruction
          ...
    jmp  bar // <- turns into relocation pointing
          //      to jmp + naming bar
    mov  $bar, %rdi // <- turns into relocation pointing
          //      to mov + naming bar
          ...
quux:
    ...
```

symbol table entry:

there is something called foo

you can find the machine code/data for it in this file at X

relocation table entry:

please find where foo is in memory

and write that location over the machine code/data in this file at X

## quiz 2 Q4/5 aside

in lecture: showed symbol table showing what labels are defined

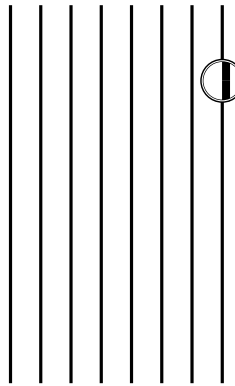
often (including on Linux (ELF format .o files)):

- “blank” symbol table entry for used symbols

- probably to make it easier for linker to know what symbols to look for elsewhere

# moving bits in hardware (one way)

0 1 1 1 0 0 1 0



wire: high voltage = 1, low voltage = 0

0 1 1 1 0 0 1 0

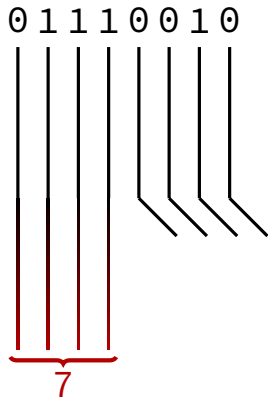


'bundle' of 8 wires: 1 byte



# extracting bits in hardware

0111 0010 = 0x72



# extracting hexadecimal nibble (1)

problem: given 0xAB  
extract 0xA

```
typedef unsigned char byte;  
int get_top_nibble(byte value) {  
    return ???;  
}
```

(hexadecimal digits  
called “nibbles”)

## extracting hexadecimal nibbles (2)

```
typedef unsigned char byte;
int get_top_nibble(byte value) {
    return value / 16;
}
```

## aside: division

division is really slow

Intel “Skylake” microarchitecture:

about **six cycles** per division

...and much worse for eight-byte division

versus: **four additions per cycle**

## aside: division

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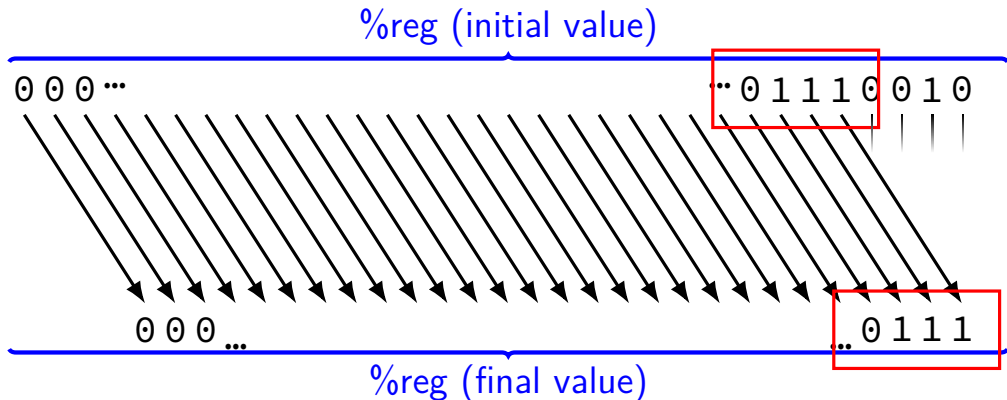
versus: **four additions per cycle**

but this case: it's just extracting 'top wires' — simpler?

# exposing wire selection

x86 instruction: `shr` — shift right

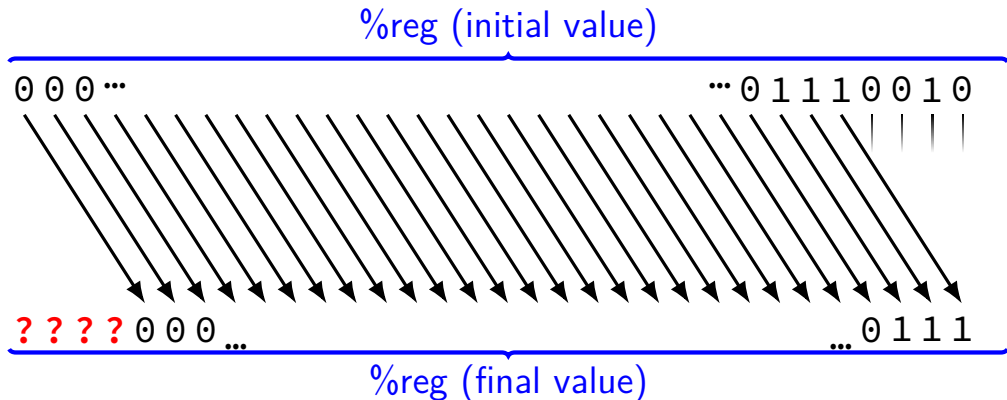
`shr $amount, %reg` (or variable: `shr %cl, %reg`)



# exposing wire selection

x86 instruction: `shr` — shift right

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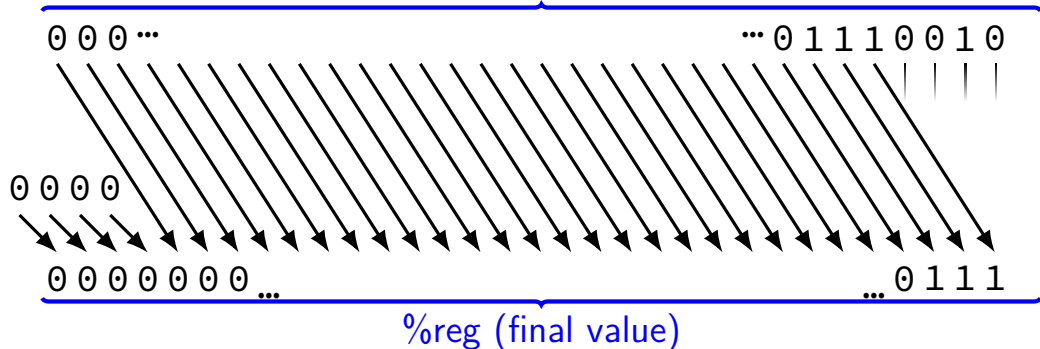


# exposing wire selection

x86 instruction: `shr` — shift right

`shr $amount, %reg` (or variable: `shr %cl, %reg`)

`%reg` (initial value)





## shift right

x86 instruction: `shr` — shift right

```
shr $amount, %reg
```

(or variable: `shr %cl, %reg`)

```
get_top_nibble:
```

```
// eax ← dil (low byte of rdi) w/ zero padding
```

```
movzbl %dil, %eax
```

```
shrl $4, %eax
```

```
ret
```

## shift right

x86 instruction: `shr` — shift right

```
shr $amount, %reg
```

(or variable: `shr %cl, %reg`)

```
get_top_nibble:
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(or variable: `shr %cl, %reg`)

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```

```
movzbl %dil, %eax
```

```
shrl $4, %eax
```

```
ret
```

## right shift in C

```
get_top_nibble:
```

```
// eax ← dil (low byte of rdi) w/ zero padding
```

```
movzbl %dil, %eax
```

```
shrl $4, %eax
```

```
ret
```

```
typedef unsigned char byte;
```

```
int get_top_nibble(byte value) {
```

```
    return value >> 4;
```

```
}
```

## right shift in C

```
typedef unsigned char byte;  
int get_top_nibble1(byte value) { return value >> 4; }  
int get_top_nibble2(byte value) { return value / 16; }
```

## right shift in C

```
typedef unsigned char byte;  
int get_top_nibble1(byte value) { return value >> 4; }  
int get_top_nibble2(byte value) { return value / 16; }
```

example output from optimizing compiler:

```
get_top_nibble1:  
    shrb $4, %dil  
    movzbl %dil, %eax  
    ret
```

```
get_top_nibble2:  
    shrb $4, %dil  
    movzbl %dil, %eax  
    ret
```

## right shift in math

1 >> 0 == 1            0000 0001

1 >> 1 == 0            0000 0000

1 >> 2 == 0            0000 0000

10 >> 0 == 10         0000 1010

10 >> 1 == 5           0000 0101

10 >> 2 == 2           0000 0010

$$x \gg y = \lfloor x \times 2^{-y} \rfloor$$

## exercise

```
int foo(int)
```

```
foo:
```

```
    movl %edi, %eax  
    shrl $1, %eax  
    ret
```

what is the value of `foo(-2)`?

A. -4 B. -2 C. -1 D. 0

E. a small positive number F. a large positive number

G. a large negative number H. something else

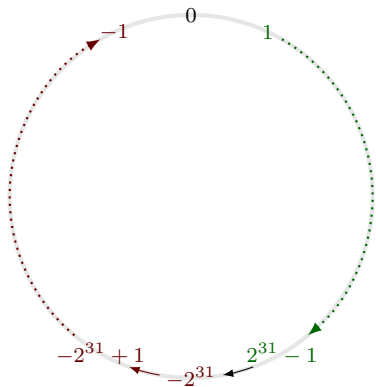


# two's complement refresher

$$-1 = \begin{matrix} & -2^{31} & +2^{30} & +2^{29} & & +2^2 & +2^1 & +2^0 \\ 1 & 1 & 1 & \dots & 1 & 1 & 1 \end{matrix}$$

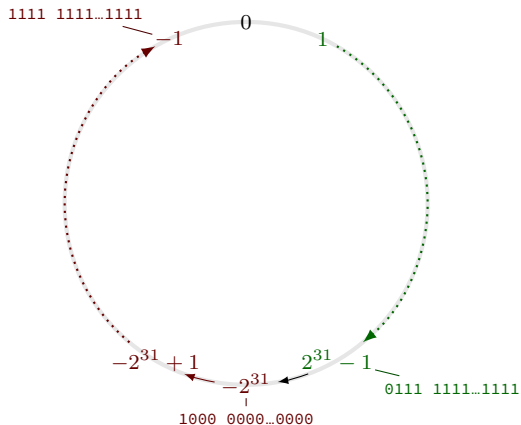
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# dividing negative by two

start with  $-x$

flip all bits and add one to get  $x$

right shift by one to get  $x/2$

flip all bits and add one to get  $-x/2$

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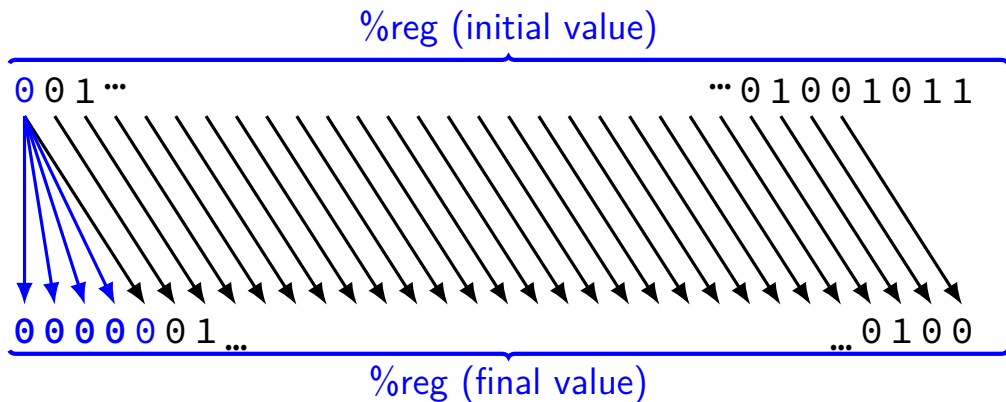
flip all bits and add one to get  $-x/2$

same as right shift by one, adding 1s instead of 0s  
(except for rounding)

# arithmetic right shift

x86 instruction: `sar` — arithmetic shift right

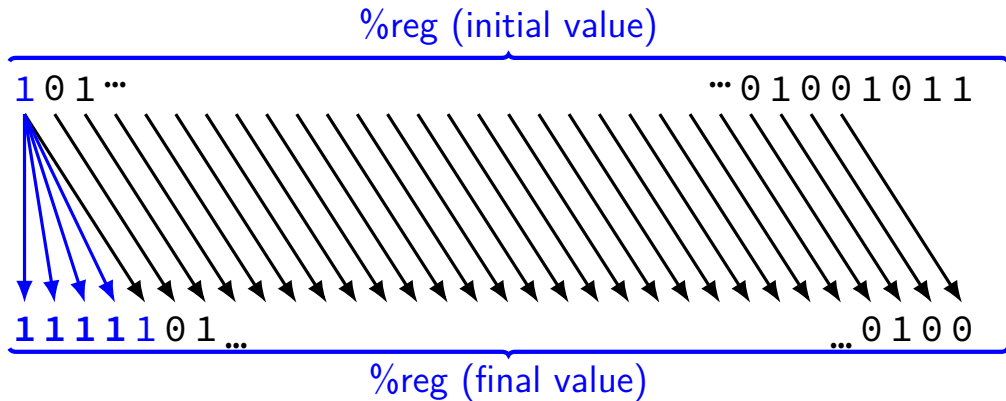
`sar $amount, %reg` (or variable: `sar %cl, %reg`)



# arithmetic right shift

x86 instruction: `sar` — arithmetic shift right

`sar $amount, %reg` (or variable: `sar %cl, %reg`)

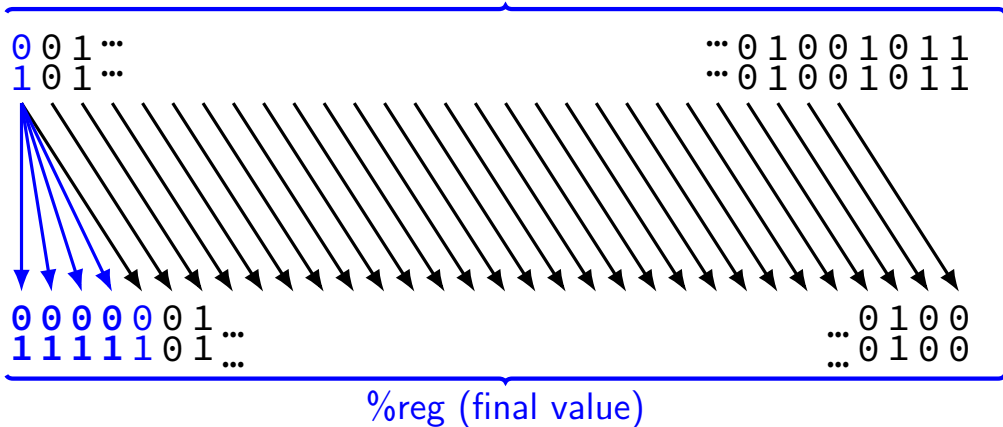


# arithmetic right shift

x86 instruction: `sar` — arithmetic shift right

`sar $amount, %reg` (or variable: `sar %cl, %reg`)

`%reg` (initial value)





## right shift in C

```
int shift_signed(int x) {  
    return x >> 5;  
}
```

```
unsigned shift_unsigned(unsigned x) {  
    return x >> 5;  
}
```

---

```
shift_signed:  
    movl %edi, %eax  
    sarl $5, %eax  
    ret
```

```
shift_unsigned:  
    movl %edi, %eax  
    shrl $5, eax  
    ret
```

# standards and shifts in C

signed right shift is **implementation-defined**

standard lets compilers choose which type of shift to do  
all x86 compilers I know of — arithmetic

we'll assume compiler decides arithmetic in this class

shift amount  $\geq$  width of type: undefined

x86 assembly: only uses lower bits of shift amount

# standards and shifts in C

signed right shift is **implementation-defined**

standard lets compilers choose which type of shift to do  
all x86 compilers I know of — arithmetic

**we'll assume compiler decides arithmetic in this class**

shift amount  $\geq$  width of type: undefined

x86 assembly: only uses lower bits of shift amount

## exercise

```
int shiftTwo(int x) {  
    return x >> 2;  
}
```

shiftTwo(-6) = ???

A. -4 B. -3 C. -2 D. -1 E. 0

F. some positive number G. something else

# explanation

6 = 000...00000110

flip bits 111...11111001

add one

---

-6 = 111...11111010

---

arithmetic shift by 2 11111...111111010

111...111110 (-2)

# dividing negative by two

start with  $-x$

flip all bits and add one to get  $x$

right shift by one to get  $x/2$

flip all bits and add one to get  $-x/2$

same as right shift by one, adding 1s instead of 0s  
(except for rounding)

# divide with proper rounding

C division: rounds towards zero (truncate)

arithmetic shift: rounds towards negative infinity

solution: “bias” adjustments — described in textbook

# divide with proper rounding

C division: rounds towards zero (truncate)

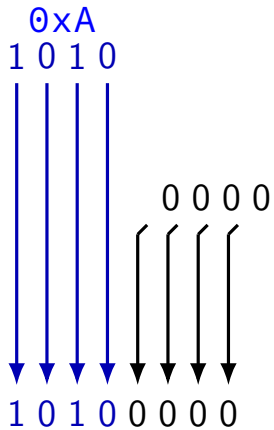
arithmetic shift: rounds towards negative infinity

solution: “bias” adjustments — described in textbook

```
// %eax = int divideBy8(int %edi)  
divideBy8: // GCC generated code  
    leal    7(%rdi), %eax // %eax ← %edi + 7  
    testl   %edi, %edi    // set cond. codes based on %edi  
    cmovns %edi, %eax     // if (SF == 0) %eax ← %edi  
    sarl    $3, %eax      // arithmetic shift  
    ret
```



# multiplying by 16



$$0xA \times 16 = 0xA0$$

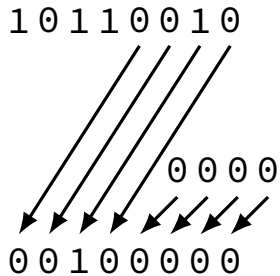
# shift left

~~shr \$-4, %reg~~

instead: **shl** \$4, %reg (“**shift left**”)

~~value >> (-4)~~

instead: value << 4



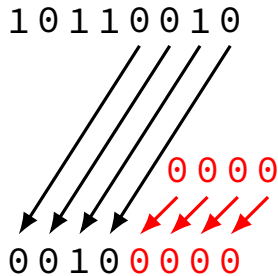
# shift left

~~shr \$-4, %reg~~

instead: `shl $4, %reg` (“**shift left**”)

~~value >> (-4)~~

instead: `value << 4`

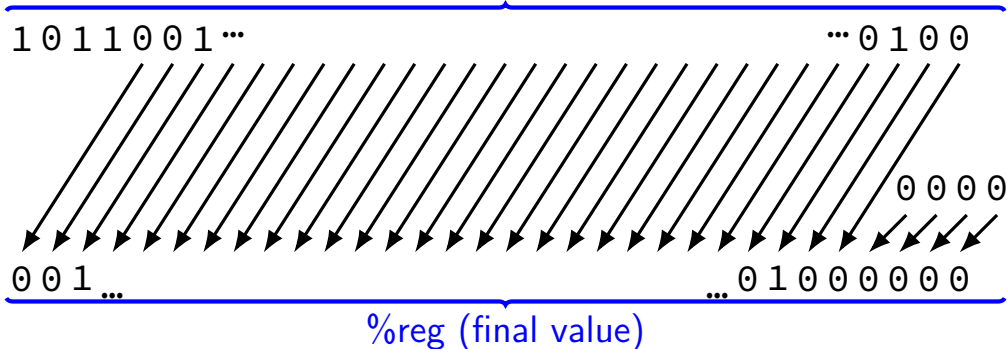


# shift left

x86 instruction: **shl** — shift left

**shl** *\$amount*, %reg (or variable: **shl** %cl, %reg)

%reg (initial value)

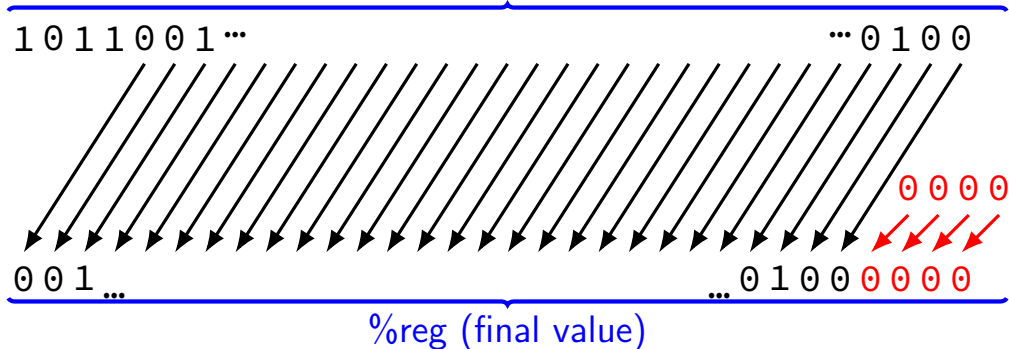


# shift left

x86 instruction: `shl` — shift left

`shl $amount, %reg` (or variable: `shl %cl, %reg`)

`%reg` (initial value)



## left shift in math

$$1 \ll 0 == 1$$

$$1 \ll 1 == 2$$

$$1 \ll 2 == 4$$

0000 0001

0000 0010

0000 0100

$$10 \ll 0 == 10$$

$$10 \ll 1 == 20$$

$$10 \ll 2 == 40$$

0000 1010

0001 0100

0010 1000

$$-10 \ll 0 == -10$$

$$-10 \ll 1 == -20$$

$$-10 \ll 2 == -40$$

1111 0110

1110 1100

1101 1000

## left shift in math

$$1 \ll 0 == 1$$

$$1 \ll 1 == 2$$

$$1 \ll 2 == 4$$

0000 0001

0000 0010

0000 0100

$$10 \ll 0 == 10$$

$$10 \ll 1 == 20$$

$$10 \ll 2 == 40$$

0000 1010

0001 0100

0010 1000

$$-10 \ll 0 == -10$$

$$-10 \ll 1 == -20$$

$$-10 \ll 2 == -40$$

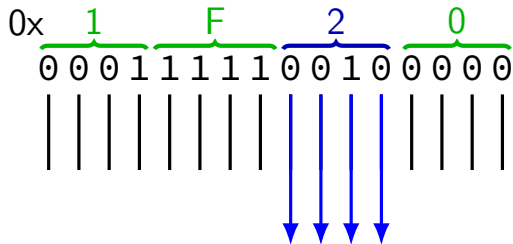
1111 0110

1110 1100

1101 1000

$$x \ll y = x \times 2^y$$

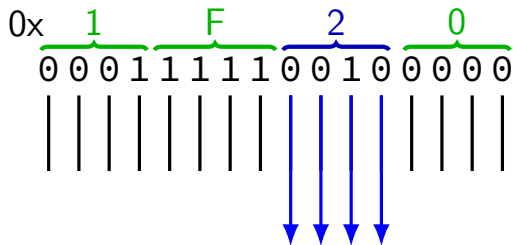
# extracting nibble from more



```
unsigned  
extract_2nd(unsigned value) {  
    return ???;  
}
```



## exercise



```
unsigned  
extract_2nd(unsigned value) {  
    return ???;  
}
```

One idea:  $0x1F20 \rightarrow 0x1F2 \rightarrow 0x2$ .

How can we do each step?

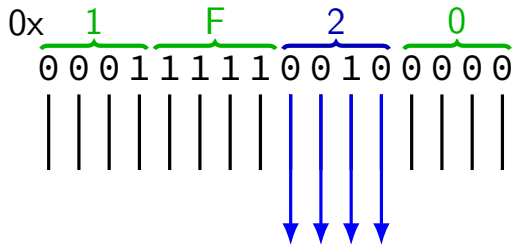
value= $0x1F20 \rightarrow 0x1F2$

**A.** value >> 16    **B.** value >> 4    **C.** value << 2    **D.** value << 4

result= $0x1F2 \rightarrow 0x2$

**A.** result / 256    **B.** result % 256    **C.** result / 16  
**D.** result % 16    **E.** result << 4    **F.** result % 4    **G.** result / 4

# extracting nibble from more



```
unsigned  
extract_2nd(unsigned value) {  
    return ???;  
}
```

*// % -- remainder*

```
unsigned extract_second_nibble(unsigned value) {  
    return (value >> 4) % 16;  
}
```

```
unsigned extract_second_nibble(unsigned value) {  
    return (value % 256) >> 4;  
}
```

# manipulating bits?

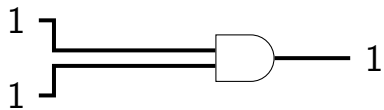
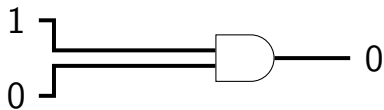
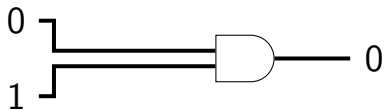
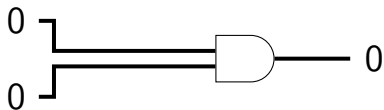
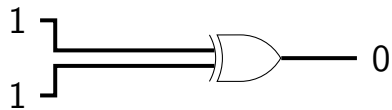
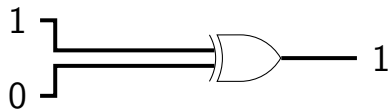
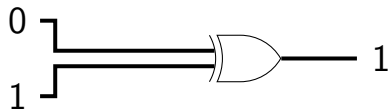
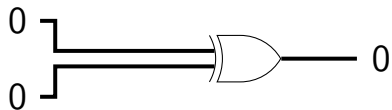
easy to manipulate individual bits in HW

- separate wire for each bit

- just ignore/select wires you care about

how do we expose that to software?

## circuits: gates



## interlude: a truth table

AND	0	1
0	0	0
1	0	1

## interlude: a truth table

AND	0	1
0	0	0
1	0	1

AND with 1: keep a bit the same

## interlude: a truth table

AND	0	1
0	0	0
1	0	1

AND with 1: keep a bit the same

AND with 0: clear a bit

## interlude: a truth table

AND	0	1
0	0	0
1	0	1

AND with 1: keep a bit the same

AND with 0: clear a bit

method: construct “mask” of what to keep/remove



# bitwise AND — &

Treat value as **array of bits**

$$1 \ \& \ 1 \ == \ 1$$

$$1 \ \& \ 0 \ == \ 0$$

$$0 \ \& \ 0 \ == \ 0$$

$$2 \ \& \ 4 \ == \ 0$$

$$10 \ \& \ 7 \ == \ 2$$

# bitwise AND — &

Treat value as **array of bits**

$$1 \ \& \ 1 \ == \ 1$$

$$1 \ \& \ 0 \ == \ 0$$

$$0 \ \& \ 0 \ == \ 0$$

$$2 \ \& \ 4 \ == \ 0$$

$$10 \ \& \ 7 \ == \ 2$$

$$\begin{array}{rcccccc} & & \dots & 0 & 0 & 1 & 0 \\ \& & \dots & 0 & 1 & 0 & 0 \\ \hline & & \dots & 0 & 0 & 0 & 0 \end{array}$$

# bitwise AND — &

Treat value as **array of bits**

$$1 \ \& \ 1 \ == \ 1$$

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$$\begin{array}{rcccccc} & & \dots & 0 & 0 & 1 & 0 \\ \& & \dots & 0 & 1 & 0 & 0 \\ \hline & & \dots & 0 & 0 & 0 & 0 \end{array}$$

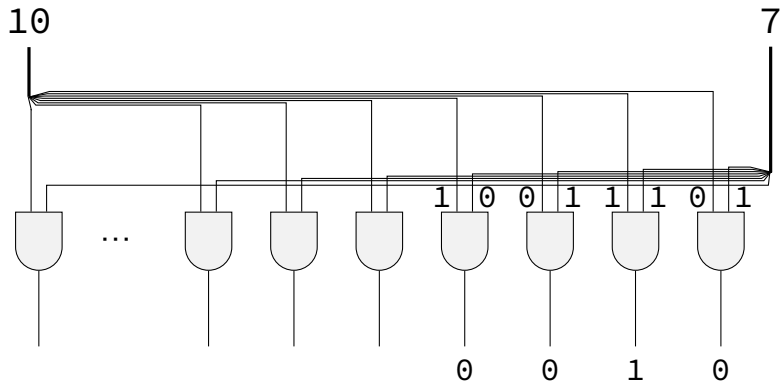
$$\begin{array}{rcccccc} & & \dots & 1 & 0 & 1 & 0 \\ \& & \dots & 0 & 1 & 1 & 1 \\ \hline & & \dots & 0 & 0 & 1 & 0 \end{array}$$

# bitwise AND — C/assembly

x86: `and %reg, %reg`

C: `foo & bar`

# bitwise hardware (10 & 7 == 2)



## extract 0x3 from 0x1234

```
unsigned get_second_nibble1(unsigned value) {  
    return (value >> 4) & 0xF; // 0xF: 00001111  
    // like (value / 16) % 16  
}
```

aaaabbbbccccdddd → aaaabbbbcccc → 00000000cccc

```
unsigned get_second_nibble2(unsigned value) {  
    return (value & 0xF0) >> 4; // 0xF0: 11110000  
    // "mask and shift"  
    // like (value % 256) / 16;  
}
```

aaaabbbbccccdddd → 00000000cccc0000 → 00000000cccc

## extract 0x3 from 0x1234

get\_second\_nibble1\_bitwise:

```
movl %edi, %eax
shrl $4, %eax
andl $0xF, %eax
ret
```

get\_second\_nibble2\_bitwise:

```
movl %edi, %eax
andl $0xF0, %eax
shrl $4, %eax
ret
```

# and/or/xor

AND	0	1
0	0	0
1	0	1

&

conditionally clear bit  
conditionally keep bit

mask: 0s = clear; 1s = keep  
e.g. 101010101...=  
clear every other bit

OR	0	1
0	0	1
1	1	1

|

conditionally set bit

mask: 1s = set; 0s = keep same  
e.g. 101010101...=  
set every other bit

XOR	0	1
0	0	1
1	1	0

^

conditionally flip bit

mask: 1s = flip; 0s = keep same



# bitwise OR — |

$$1 \mid 1 == 1$$

$$1 \mid 0 == 1$$

$$0 \mid 0 == 0$$

$$2 \mid 4 == 6$$

$$10 \mid 7 == 15$$

$$\begin{array}{r} \dots 1 0 1 0 \\ | \dots 0 1 1 1 \\ \hline \dots 1 1 1 1 \end{array}$$

# bitwise xor — ^

$$1 \wedge 1 == 0$$

$$1 \wedge 0 == 1$$

$$0 \wedge 0 == 0$$

$$2 \wedge 4 == 6$$

$$10 \wedge 7 == 13$$

$$\begin{array}{r} \wedge \quad \dots \quad 1 \quad 0 \quad 1 \quad 0 \\ \dots \quad 0 \quad 1 \quad 1 \quad 1 \\ \hline \dots \quad 1 \quad 1 \quad 0 \quad 1 \end{array}$$

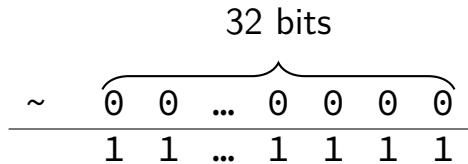
# negation / not — ~

~ ('complement') is bitwise version of !:

!0 == 1

!notZero == 0

~0 == (**int**) 0xFFFFFFFF (aka  
-1)



# negation / not — ~

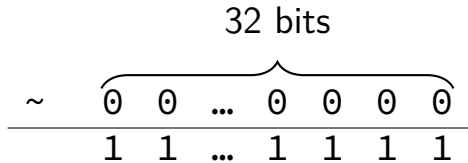
~ ('complement') is bitwise version of !:

`!0 == 1`

`!notZero == 0`

`~0 == (int) 0xFFFFFFFF (aka  
-1)`

`~2 == (int) 0xFFFFFFFDD (aka  
-3)`



# negation / not — ~

~ ('complement') is bitwise version of !:

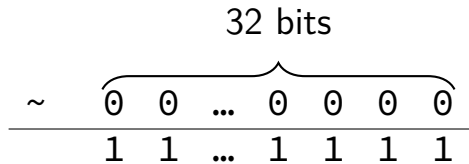
!0 == 1

!notZero == 0

~0 == (**int**) 0xFFFFFFFF (aka  
-1)

~2 == (**int**) 0xFFFFFFFDD (aka  
-3)

~((**unsigned**) 2) == 0xFFFFFFFDD



# bit-puzzles

assignments: bit manipulation puzzles

solve some problem with bitwise ops

maybe that you could do with normal arithmetic, comparisons, etc.

why?

good for thinking about HW design

good for understanding bitwise ops

unreasonably common interview question type

## note: ternary operator

```
w = (x ? y : z)
```

```
if (x) { w = y; } else { w = z; }
```

# ternary as bitwise: simplifying

$(x ? y : z)$  if  $(x)$  return  $y$ ; else return  $z$ ;

task: turn into non-if/else/etc. operators

assembly: no jumps probably

strategy today: build a solution from simpler subproblems

(1) with  $x, y, z$  1 bit:  $(x ? y : 0)$  and  $(x ? 0 : z)$

(2) with  $x, y, z$  1 bit:  $(x ? y : z)$

(3) with  $x$  1 bit:  $(x ? y : z)$

(4)  $(x ? y : z)$



# one-bit ternary

$(x \ ? \ y \ : \ z)$

constraint:  $x, y,$  and  $z$  are 0 or 1

now: reimplement in C without if/else/||/etc.  
(assembly: no jumps probably)

# one-bit ternary

$(x \ ? \ y \ : \ z)$

constraint:  $x, y,$  and  $z$  are 0 or 1

now: reimplement in C without if/else/||/etc.  
(assembly: no jumps probably)

divide-and-conquer:

$(x \ ? \ y \ : \ 0)$

$(x \ ? \ 0 \ : \ z)$

# one-bit ternary parts (1)

constraint:  $x$ ,  $y$ , and  $z$  are 0 or 1

$(x \ ? \ y \ : \ 0)$

# one-bit ternary parts (1)

constraint:  $x$ ,  $y$ , and  $z$  are 0 or 1

$(x \text{ ? } y : 0)$

	<b>y=0</b>	<b>y=1</b>
<b>x=0</b>	0	0
<b>x=1</b>	0	1

$\rightarrow (x \ \& \ y)$

## one-bit ternary parts (2)

$$(x \ ? \ y \ : \ 0) = (x \ \& \ y)$$

## one-bit ternary parts (2)

$$(x \ ? \ y \ : \ 0) = (x \ \& \ y)$$

$$(x \ ? \ 0 \ : \ z)$$

opposite x:  $\sim x$

$$((\sim x) \ \& \ z)$$

# one-bit ternary

constraint:  $x, y,$  and  $z$  are 0 or 1

$(x \text{ ? } y \text{ : } z)$

$(x \text{ ? } y \text{ : } 0) \mid (x \text{ ? } 0 \text{ : } z)$

$(x \ \& \ y) \mid ((\sim x) \ \& \ z)$

## multibit ternary

constraint:  $x$  is 0 or 1

old solution  $((x \& y) \mid (\sim x) \& z)$  only gets least sig. bit

$(x ? y : z)$



## multibit ternary

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$(x ? y : z)$

$(x ? y : 0) \mid (x ? 0 : z)$

# constructing masks

constraint:  $x$  is 0 or 1

$(x \ ? \ y \ : \ 0)$

turn into  $y \ \& \ \text{MASK}$ , where  $\text{MASK} = ???$

“keep certain bits”

# constructing masks

constraint:  $x$  is 0 or 1

$(x \ ? \ y \ : \ 0)$

turn into  $y \ \& \ \text{MASK}$ , where  $\text{MASK} = ???$   
“keep certain bits”

if  $x = 1$ : want 1111111111...1 (keep  $y$ )

if  $x = 0$ : want 0000000000...0 (want 0)

# constructing masks

constraint:  $x$  is 0 or 1

$(x \ ? \ y \ : \ 0)$

turn into  $y \ \& \ \text{MASK}$ , where  $\text{MASK} = ???$   
“keep certain bits”

if  $x = 1$ : want  $1111111111\dots 1$  (keep  $y$ )

if  $x = 0$ : want  $0000000000\dots 0$  (want 0)

a trick:  $-x$  ( $-1$  is  $1111\dots 1$ )

# constructing other masks

constraint:  $x$  is 0 or 1

$(x \ ? \ 0 \ : \ z)$

if  $x = \cancel{0}$ : want 1111111111...1

if  $x = \cancel{1}$ : want 0000000000...0

mask:  $\cancel{>x}$

# constructing other masks

constraint:  $x$  is 0 or 1

$(x \ ? \ 0 \ : \ z)$

if  $x = \cancel{0}$ : want 1111111111...1

if  $x = \cancel{1}$ : want 0000000000...0

mask:  ~~$x$~~   $-(x^1)$

## multibit ternary

constraint:  $x$  is 0 or 1

old solution  $((x \& y) \mid (\sim x) \& z)$  only gets least sig. bit

$(x ? y : z)$

$(x ? y : 0) \mid (x ? 0 : z)$

$((-x) \& y) \mid ((-(x \wedge 1)) \& z)$

# fully multibit

~~constraint:  $x$  is 0 or 1~~

( $x \ ? \ y \ : \ z$ )



## fully multibit

~~constraint:  $x$  is 0 or 1~~

$(x \ ? \ y \ : \ z)$

easy C way:  $!x = 1$  (if  $x = 0$ ) or 0,  $!(!x) = 0$  or 1

x86 assembly: `testq %rax, %rax` then `sete/setne`  
(copy from ZF)

# fully multibit

~~constraint:  $x$  is 0 or 1~~

$(x ? y : z)$

easy C way:  $!x = 1$  (if  $x = 0$ ) or 0,  $!(!x) = 0$  or 1

x86 assembly: `testq %rax, %rax` then `sete/setne`  
(copy from ZF)

$(x ? y : 0) \mid (x ? 0 : z)$

$((-!!x) \& y) \mid ((-!x) \& z)$

**backup slides**

# what's in those files?

hello.c

```
#include <stdio.h>
int main(void) {
    puts("Hello, World!");
    return 0;
}
```

# what's in those files?

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```

hello.s

```
.text
.global main
main:
    sub    $8, %rsp
    mov    $.Lstr, %rdi
    call  puts
    xor    %eax, %eax
    add    $8, %rsp
    ret

.data
.Lstr: .string "Hello, World!"
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    add    $8, %rsp
    ret

.data
.Lstr: .string "Hello, World!"
```

hello.s (Intel syntax)

```
.text
main:
    sub RSP, 8
    mov RDI, .Lstr
    call puts
    xor EAX, EAX
    add RSP, 8
    ret

.data
.Lstr: .string "Hello, Worl"
```

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.Lstr: .string "Hello, World!"
```

Linux x86-64  
calling convention:  
stack addr. must be  
multiple of 16

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sets eax to 0  
(shorter machine  
code than mov)



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```

mark used by other files

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```

hello.o

```
text (code) segment:
48 83 EC 08 BF 00 00 00 00 E8 00 00
00 00 31 C0 48 83 C4 08 C3
```

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```

hello.o

```
text (code) segment:
48 83 EC 08 BF 00 00 00 00 E8 00 00
00 00 31 C0 48 83 C4 08 C3
data segment:
48 65 6C 6C 6F 2C 20 57 6F 72 6C 00
```

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    ret

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```

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```
text (code) segment:
48 83 EC 08 BF 00 00 00 00 E8 00 00
00 00 31 C0 48 83 C4 08 C3
data segment:
48 65 6C 6C 6F 2C 20 57 6F 72 6C 00
relocations:
    take 0s at           and replace with addr. of
    text, byte 5 (|)    data segment, byte 0
    text, byte 10 (|)  puts
```

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int main(void) {
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}
```

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.global main
main:
    sub $8, %rsp
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    call puts
    xor %eax, %eax
    add $8, %rsp
    ret

.data
.Lstr: .string "Hello, World!"
```

hello.o

**text (code) segment:**  
48 83 EC 08 BF 00 00 00 00 E8 00 00  
00 00 31 C0 48 83 C4 08 C3

**data segment:**  
48 65 6C 6C 6F 2C 20 57 6F 72 6C 00

**relocations:**  
take 0s at                      and replace with addr. of  
text, byte 5 (|)                data segment, byte 0  
text, byte 10 (|)               puts

**symbol table:**  
main   text byte 0

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```

hello.s

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.global main
main:
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    call puts
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```
text (code) segment:
48 83 EC 08 BF 00 00 00 00 E8 00 00
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relocations:
    take 0s at          and replace with addr. of
    text, byte 5 (|)    data segment, byte 0
    text, byte 10 (|)   puts
symbol table:
main    text byte 0
```

```
.data
.Lstr: .string "Hello, World!"
```

.Lstr location specified w/o name  
and not usable by other files  
so no symbol table entry needed

(convention: .L...labels always local)

# what's in those files?

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int main(void) {
    puts("Hello, World!");
    return 0;
}
```

hello.s

```
.text
.global main
main:
    sub $8, %rsp
    mov $.Lstr, %rdi
    call puts
    xor %eax, %eax
    add $8, %rsp
    ret
```

hello.o

text (code) segment:

```
48 83 EC 08 BF 00 00 00 00 E8 00 00
00 00 31 C0 48 83 C4 08 C3
```

data segment:

```
48 65 6C 6C 6F 2C 20 57 6F 72 6C 00
```

relocations:

take 0s at                      and replace with addr. of  
text, byte 5 (|)                data segment, byte 0  
text, byte 10 (|)               puts

symbol table:

```
main    text byte 0
```

.data  
.Lstr: .string "Hello, World!"

+ stdio.o

hello.exe

(actually binary, but shown as hexadecimal) ...

```
48 83 EC 08 BF A7 02 04 00
E8 08 4A 00 00 31 C0 48
83 C4 08 C3 ...
...(code from stdio.o) ...
48 65 6C 6C 6F 2C 20 57 6F
72 6C 00 ...
...(data from stdio.o) ...
```



# hello.s

```
.section          .rodata.str1.1,"aMS",@progb  
.LC0:  
    .string "Hello, World!"  
    .text  
    .globl  main  
main:  
    subq    $8, %rsp  
    movl    $.LC0, %edi  
    call    puts  
    movl    $0, %eax  
    addq    $8, %rsp  
    ret
```