last time

pipelining idea

- laundry analogy
- divide work into *stages*
- first: instruction A does stage 1
- then: instruction A does stage 2 while instruction B does stage 1
- ...

latency (start to finish) versus throughput (rate of finishing)

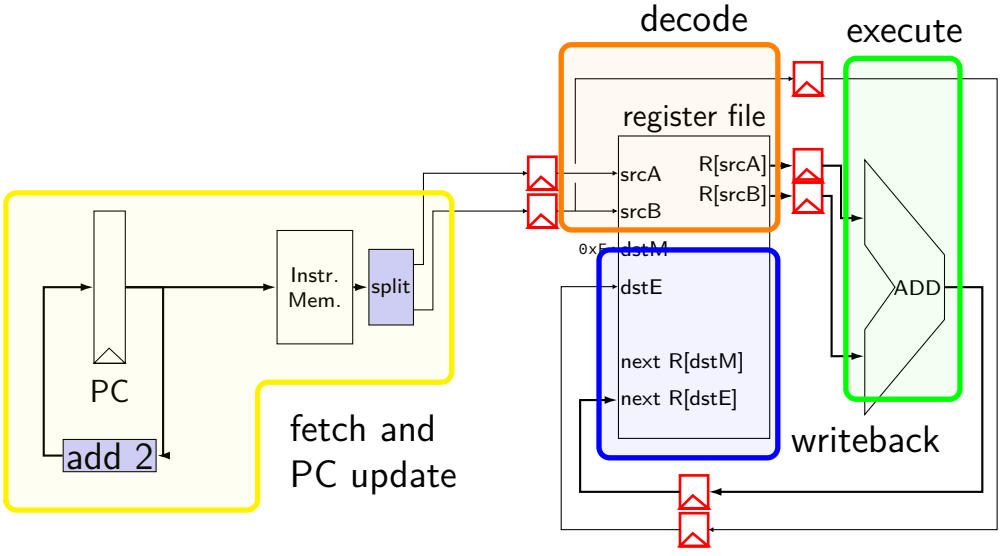
pipelining with circuits

- send values from one stage to next only
- add registers between each pair of stages

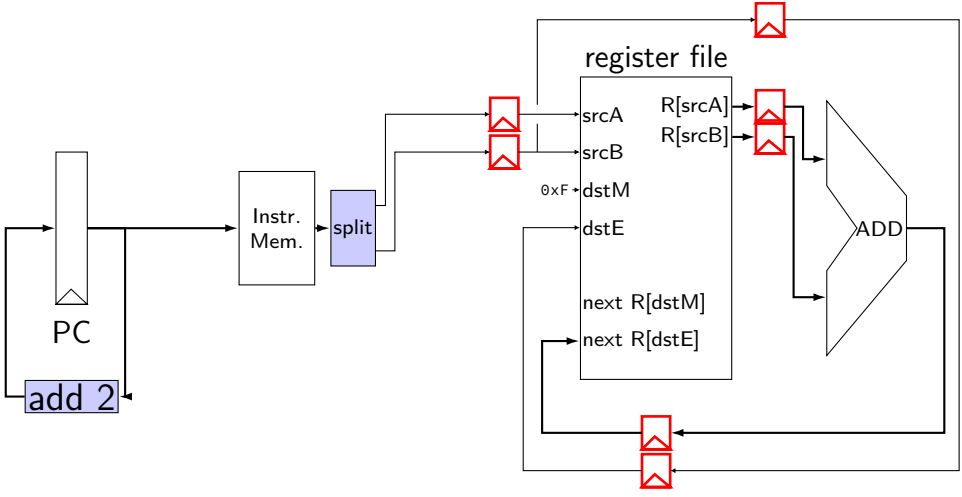
diminishing returns in pipelining

- only as fast as slowest stage
- cannot divide work evenly in practice
- registers take time

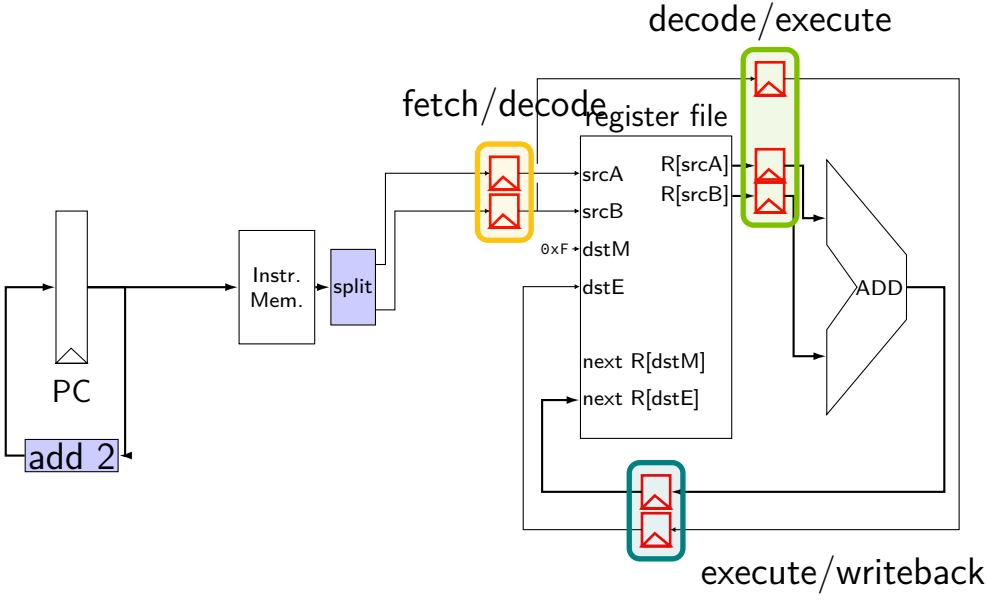
pipelined addq processor



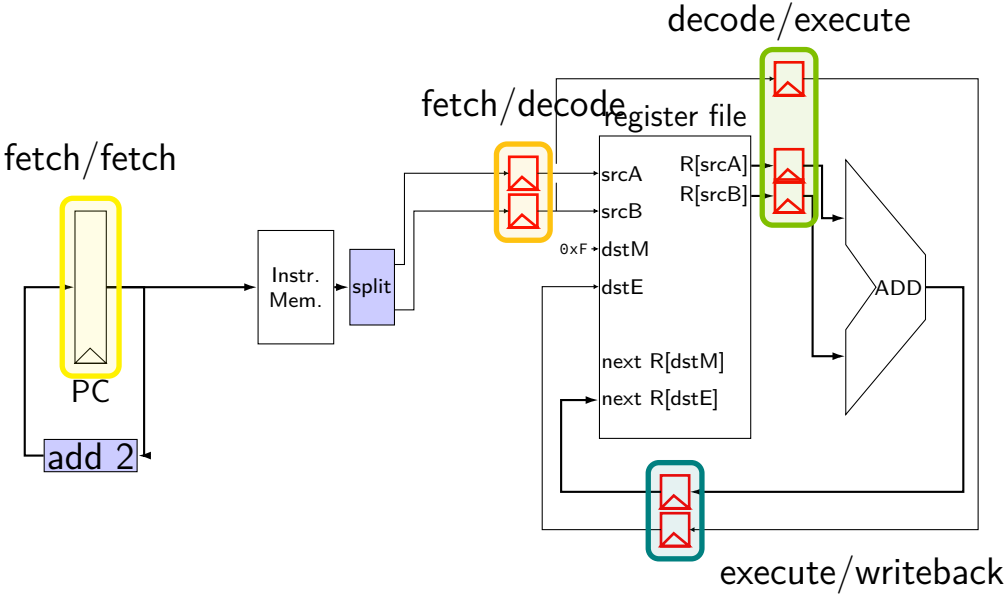
pipelined addq processor



pipelined addq processor

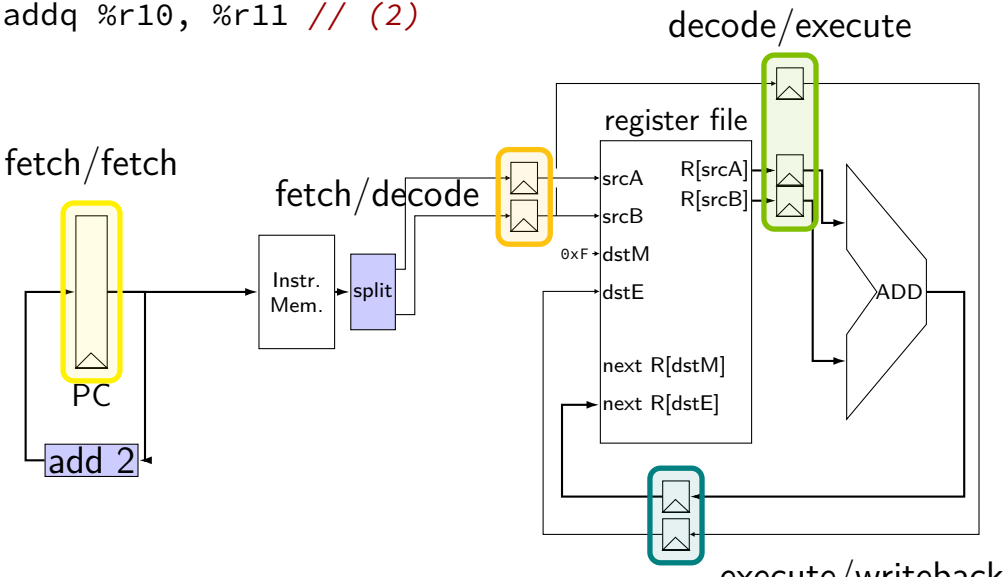


pipelined addq processor



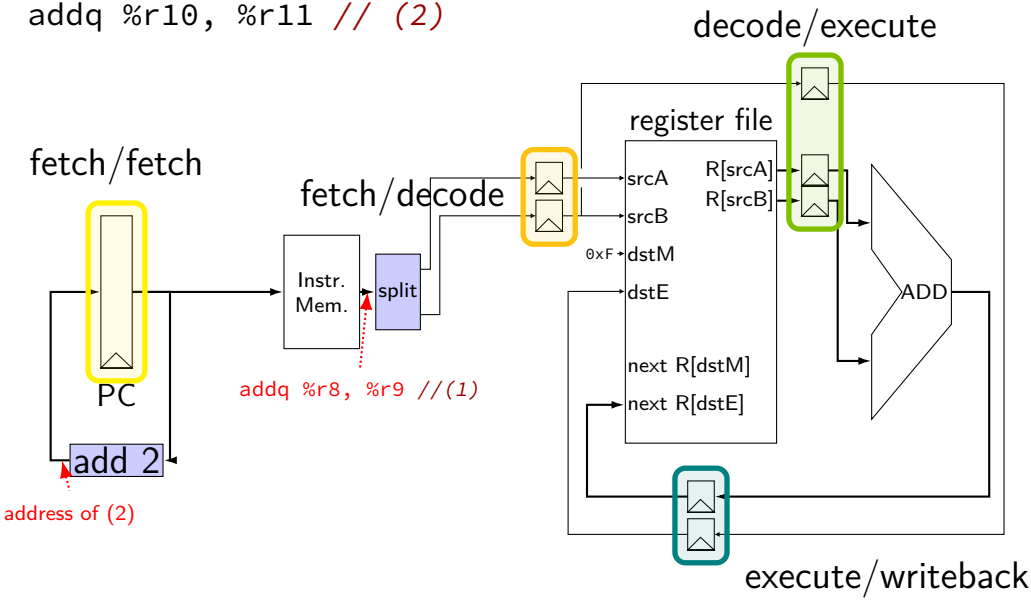
addq execution

```
addq %r8, %r9   // (1)
addq %r10, %r11 // (2)
```



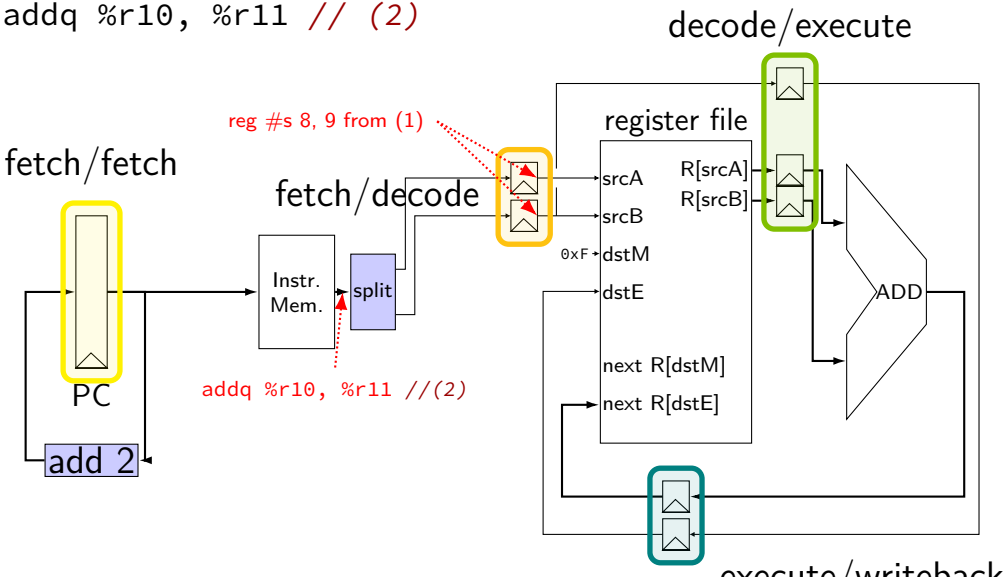
addq execution

```
addq %r8, %r9   // (1)
addq %r10, %r11 // (2)
```



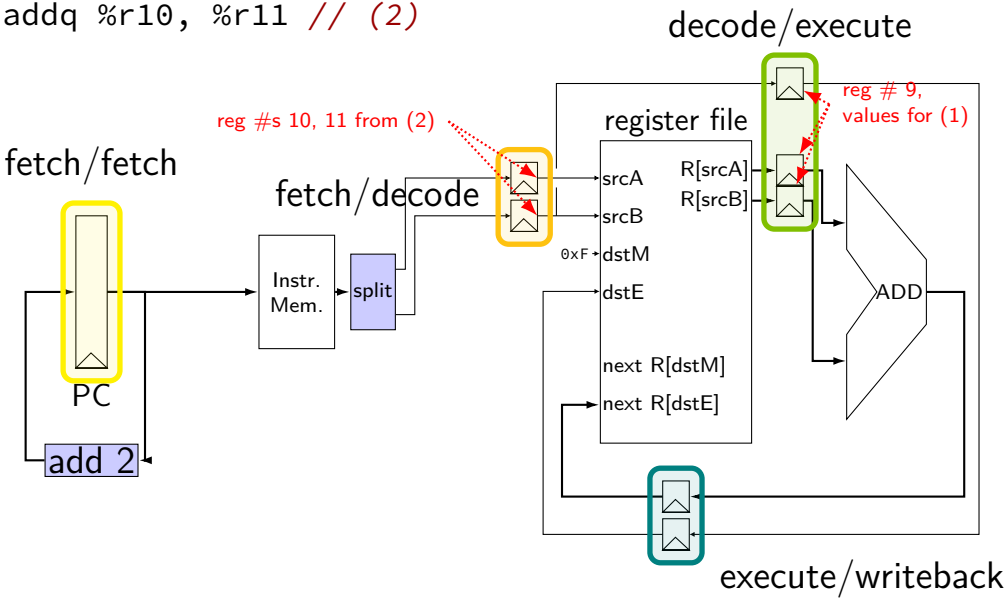
addq execution

```
addq %r8, %r9   // (1)
addq %r10, %r11 // (2)
```



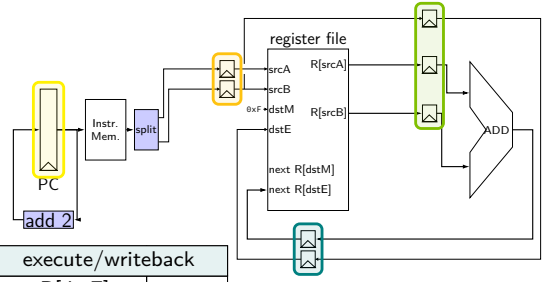
addq execution

```
addq %r8, %r9   // (1)
addq %r10, %r11 // (2)
```



addq processor timing

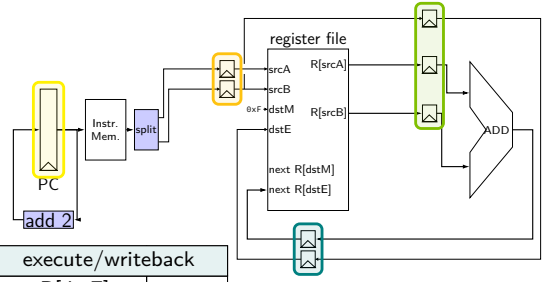
```
// initially %r8 = 800,
//           %r9 = 900, etc.
addq %r8, %r9
addq %r10, %r11
addq %r12, %r13
addq %r9, %r8
```



	fetch	fetch/decode		decode/execute			execute/writeback	
cycle	PC	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0							
1	0x2	8	9					
2	0x4	10	11	800	900	9		
3	0x6	12	13	1000	1100	11	1700	9
4		9	8	1200	1300	13	2100	11
5				1700	800	8	2500	13
6							2500	8

addq processor timing

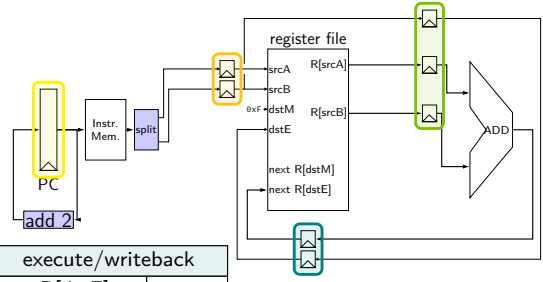
```
// initially %r8 = 800,
//           %r9 = 900, etc.
addq %r8, %r9
addq %r10, %r11
addq %r12, %r13
addq %r9, %r8
```



	fetch	fetch/decode		decode/execute			execute/writeback	
cycle	PC	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0							
1	0x2	8	9					
2	0x4	10	11	800	900	9		
3	0x6	12	13	1000	1100	11	1700	9
4		9	8	1200	1300	13	2100	11
5				1700	800	8	2500	13
6							2500	8

addq processor timing

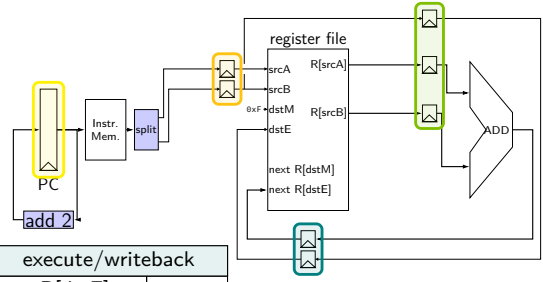
```
// initially %r8 = 800,
//           %r9 = 900, etc.
addq %r8, %r9
addq %r10, %r11
addq %r12, %r13
addq %r9, %r8
```



	fetch	fetch/decode		decode/execute			execute/writeback	
cycle	PC	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0							
1	0x2	8	9					
2	0x4	10	11	800	900	9		
3	0x6	12	13	1000	1100	11	1700	9
4		9	8	1200	1300	13	2100	11
5				1700	800	8	2500	13
6							2500	8

addq processor timing

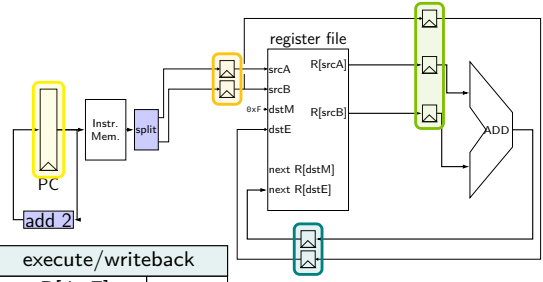
```
// initially %r8 = 800,
//           %r9 = 900, etc.
addq %r8, %r9
addq %r10, %r11
addq %r12, %r13
addq %r9, %r8
```



	fetch	fetch/decode		decode/execute			execute/writeback	
cycle	PC	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0							
1	0x2	8	9					
2	0x4	10	11	800	900	9		
3	0x6	12	13	1000	1100	11	1700	9
4		9	8	1200	1300	13	2100	11
5				1700	800	8	2500	13
6							2500	8

addq processor timing

```
// initially %r8 = 800,
//           %r9 = 900, etc.
addq %r8, %r9
addq %r10, %r11
addq %r12, %r13
addq %r9, %r8
```



	fetch	fetch/decode		decode/execute			execute/writeback	
cycle	PC	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0							
1	0x2	8	9					
2	0x4	10	11	800	900	9		
3	0x6	12	13	1000	1100	11	1700	9
4		9	8	1200	1300	13	2100	11
5				1700	800	8	2500	13
6							2500	8

critical path

every path from state output to state input needs enough time

- output — may change on rising edge of clock
- input — must be stable sufficiently before rising edge of clock

critical path: slowest of all these paths — determines cycle time

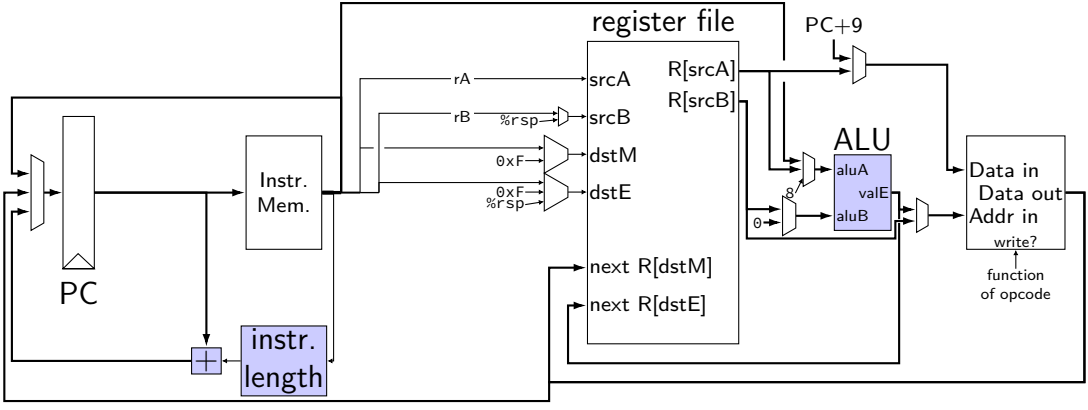
- times three: slowest stage ended up mattering

have to choose *one* clock cycle length

- can't vary clock depending on what instruction is running

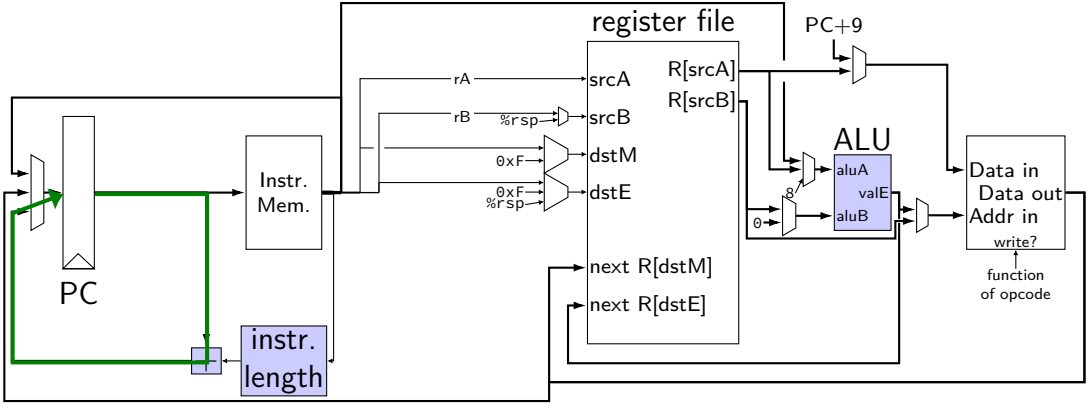
matters with or without pipelining

SEQ paths


register file
PC+9
rA
rB
%rsp
0xF
0xF
%rsp
srcA
srcB
dstM
dstE
R[srcA]
R[srcB]
next R[dstM]
next R[dstE]
ALU
aluA
valE
aluB
8
0
Data in
Data out
Addr in
write?
function
of opcode
Instr.
Mem.
PC
instr.
length

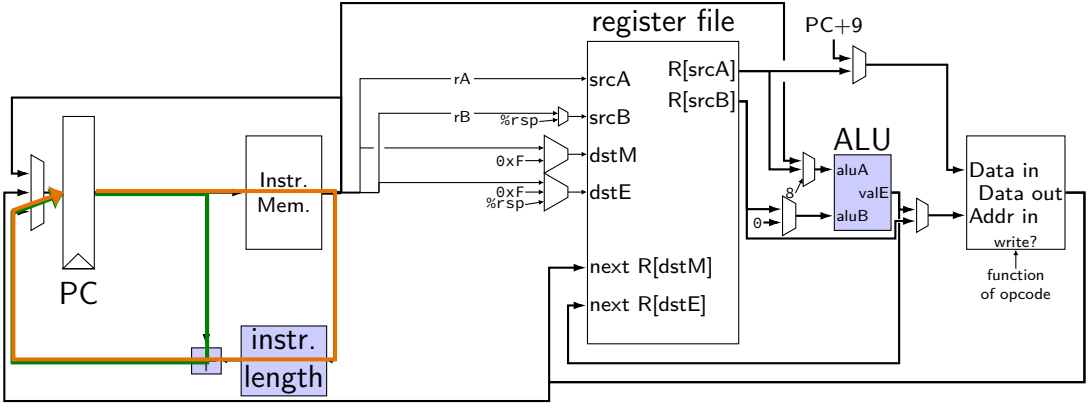
SEQ paths

path 1: 25 picoseconds



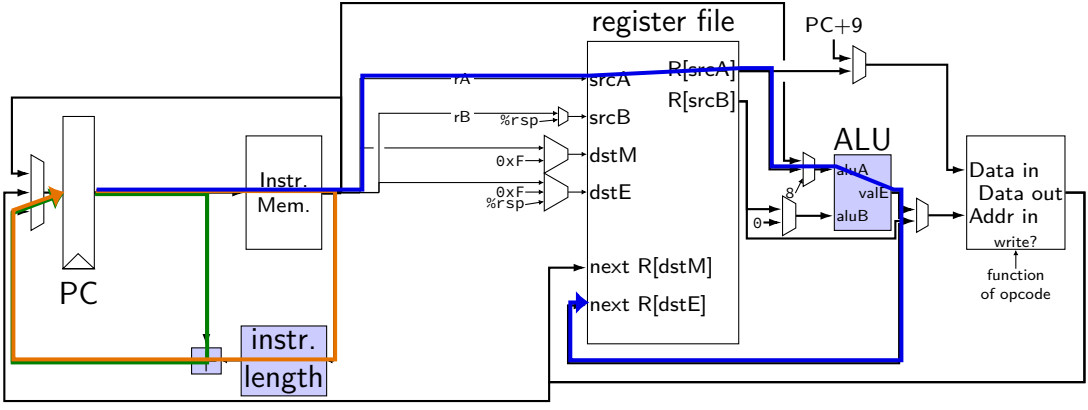
SEQ paths

path 1: 25 picoseconds path 2: 50 picoseconds



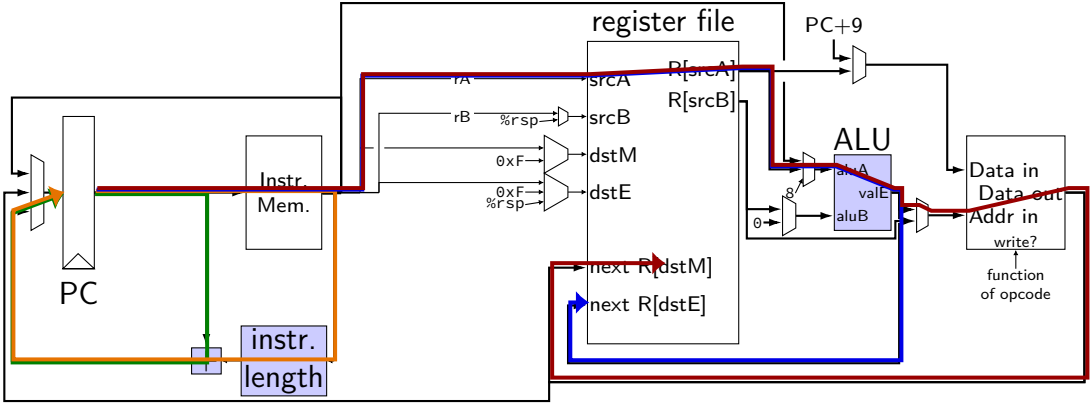
SEQ paths

path 1: 25 picoseconds path 2: 50 picoseconds
path 3: 400 picoseconds



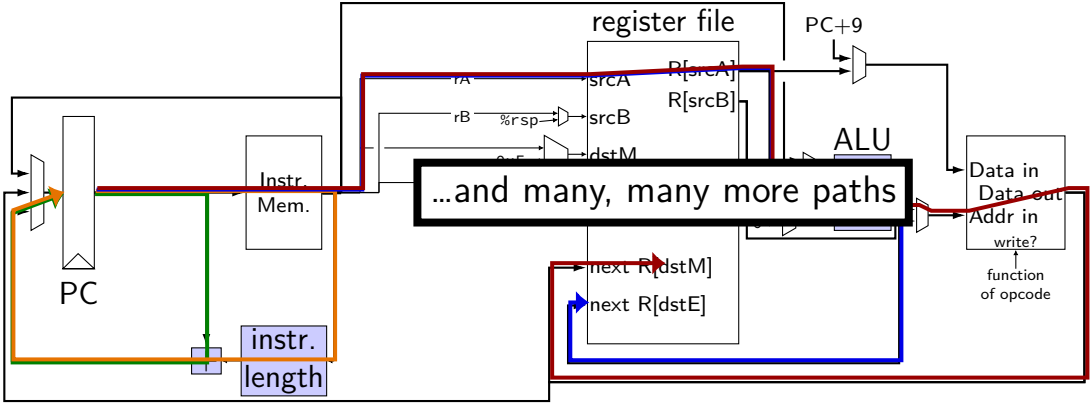
SEQ paths

path 1: 25 picoseconds
path 2: 50 picoseconds
path 3: 400 picoseconds
path 4: 900 picoseconds
...
...

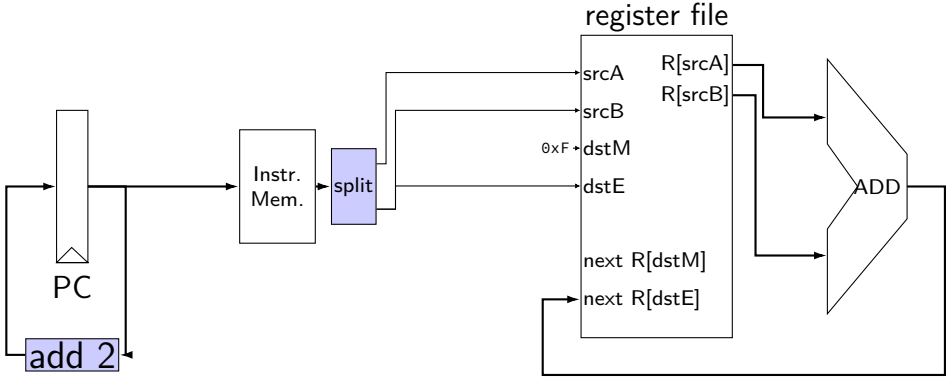


SEQ paths

path 1: 25 picoseconds
path 2: 50 picoseconds
path 3: 400 picoseconds
path 4: 900 picoseconds
...
...

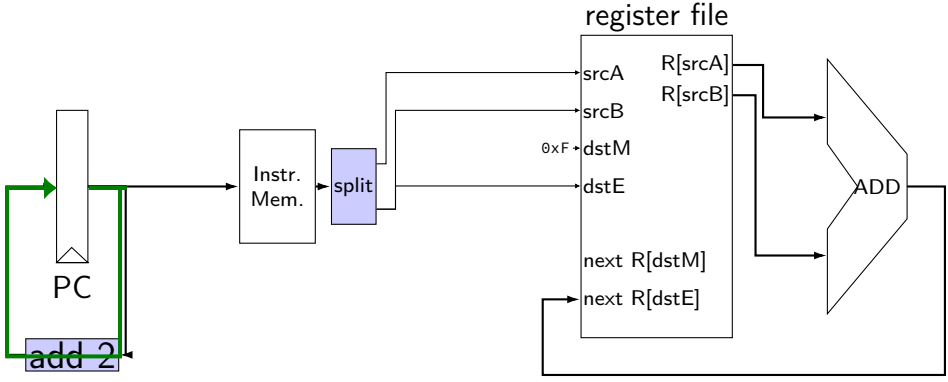


sequential addq paths



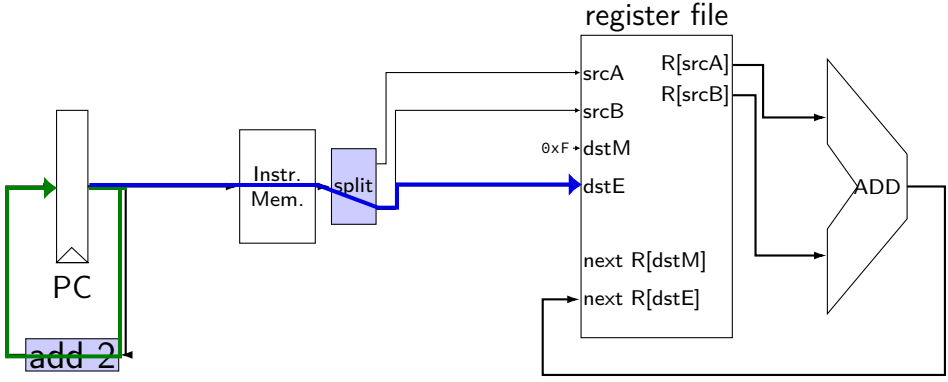
sequential addq paths

path 1: 25 picoseconds



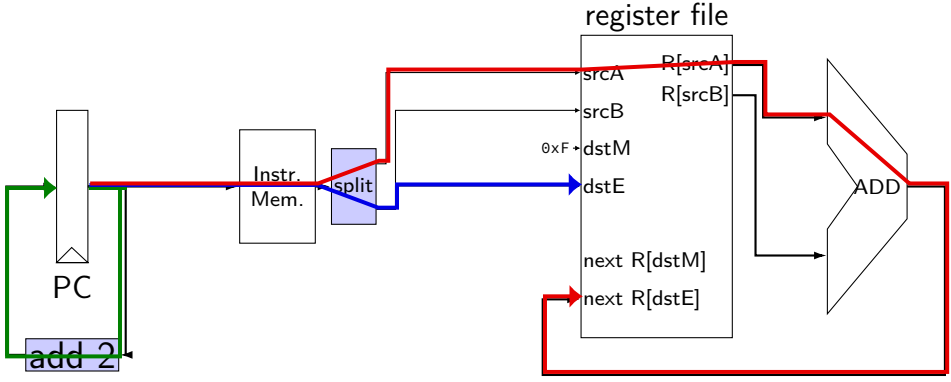
sequential addq paths

path 1: 25 picoseconds
path 2: 375 picoseconds



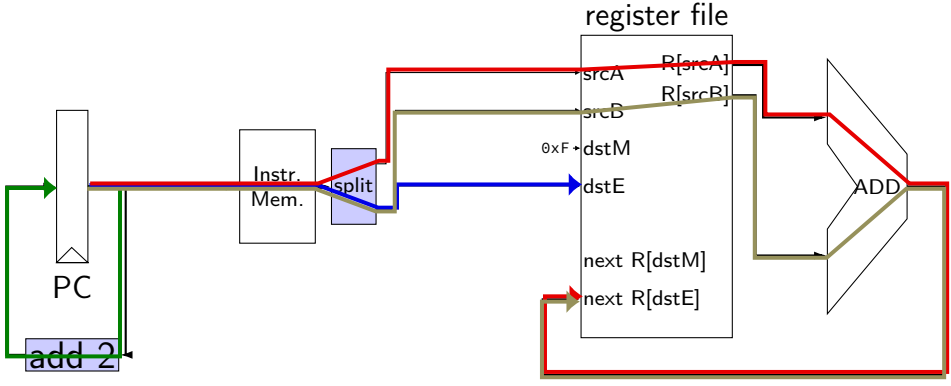
sequential addq paths

path 1: 25 picoseconds
path 2: 375 picoseconds
path 3: 500 picoseconds



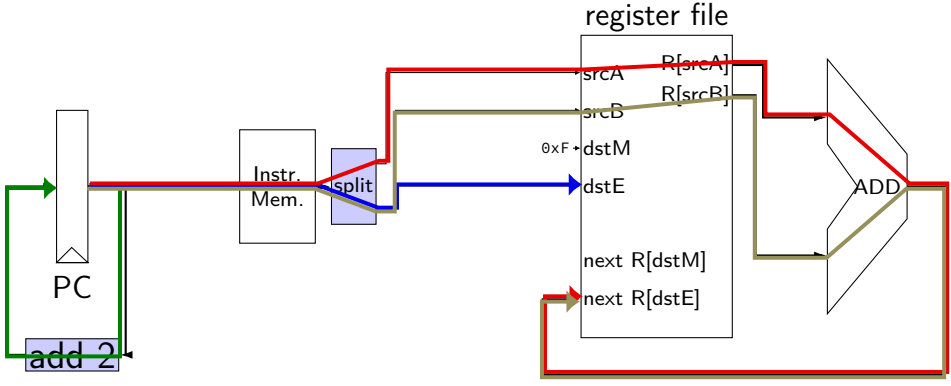
sequential addq paths

path 1: 25 picoseconds
path 2: 375 picoseconds
path 3: 500 picoseconds
path 4: 500 picoseconds

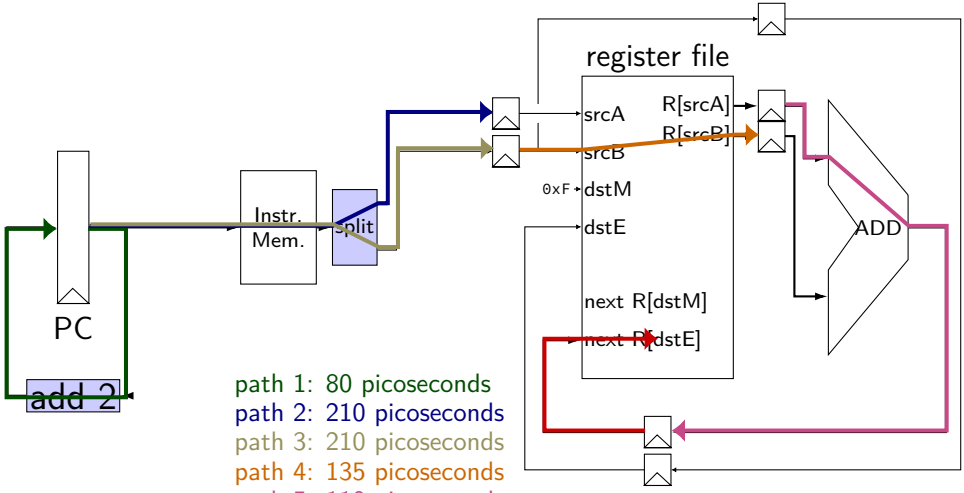


sequential addq paths

path 1: 25 picoseconds
path 2: 375 picoseconds
path 3: **500 picoseconds**
path 4: **500 picoseconds**
overall cycle time: **500 picoseconds** (longest path)

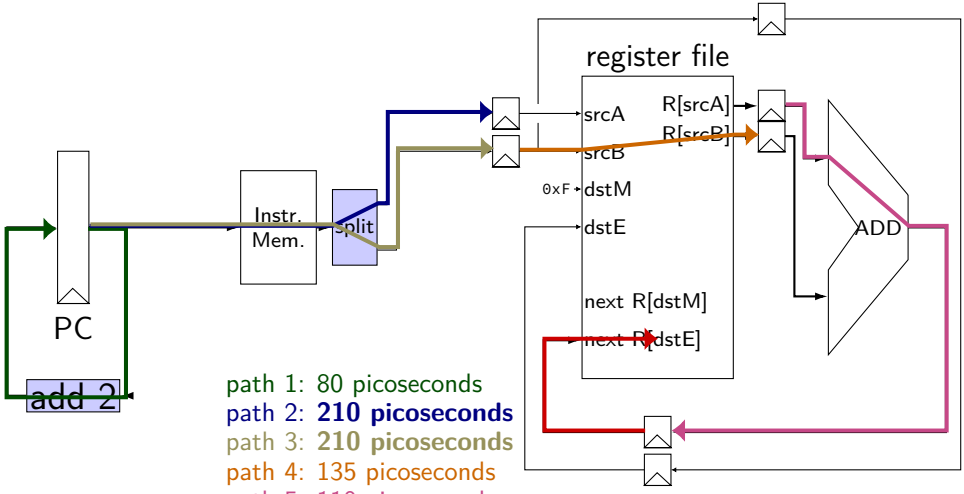


pipelined addq paths



path 1: 80 picoseconds
path 2: 210 picoseconds
path 3: 210 picoseconds
path 4: 135 picoseconds
path 5: 110 picoseconds
path 6: 135 picoseconds
...
overall cycle time: 210 picoseconds

pipelined addq paths

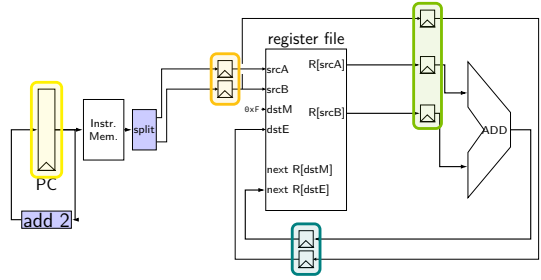


path 1: 80 picoseconds
path 2: **210 picoseconds**
path 3: **210 picoseconds**
path 4: 135 picoseconds
path 5: 110 picoseconds
path 6: 135 picoseconds
...
overall cycle time: **210 picoseconds**

addq processor performance

example delays:

path	time
add 2	80 ps
instruction memory	200 ps
register file read	125 ps
add	100 ps
register file write	125 ps



no pipelining: 1 instruction per 550 ps

add up everything but add 2 (critical (slowest) path)

pipelining: 1 instruction per 200 ps + pipeline register delays

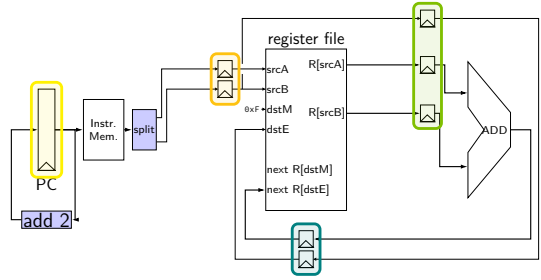
slowest path through stage + pipeline register delays

latency: 800 ps + pipeline register delays (4 cycles)

addq processor timing exercise 1

example delays:

path	time
add 2	80 ps
instruction memory	200 ps
register file read	125 ps
add	100 ps
register file write	125 ps



exercise 1: when instruction 1 stores its result in %rbx, what did instruction 3 *just complete*?

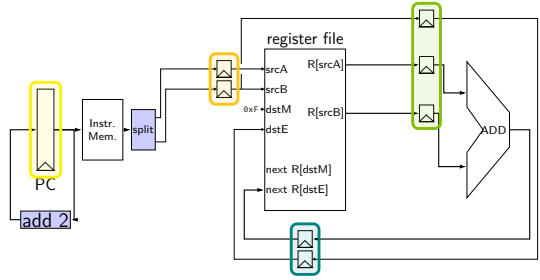
```
addq %rax, %rbx   /* 1 */
addq %rcx, %rdx
addq %r8, %r9     /* 3 */
```

A. fetch **B.** decode (register read) **C.** execute
D. writeback **E.** nothing (it's not running)

addq processor performance exercise 2

example delays:

path	time
add 2	80 ps
instruction memory	200 ps
register file read	125 ps
add	100 ps
register file write	125 ps



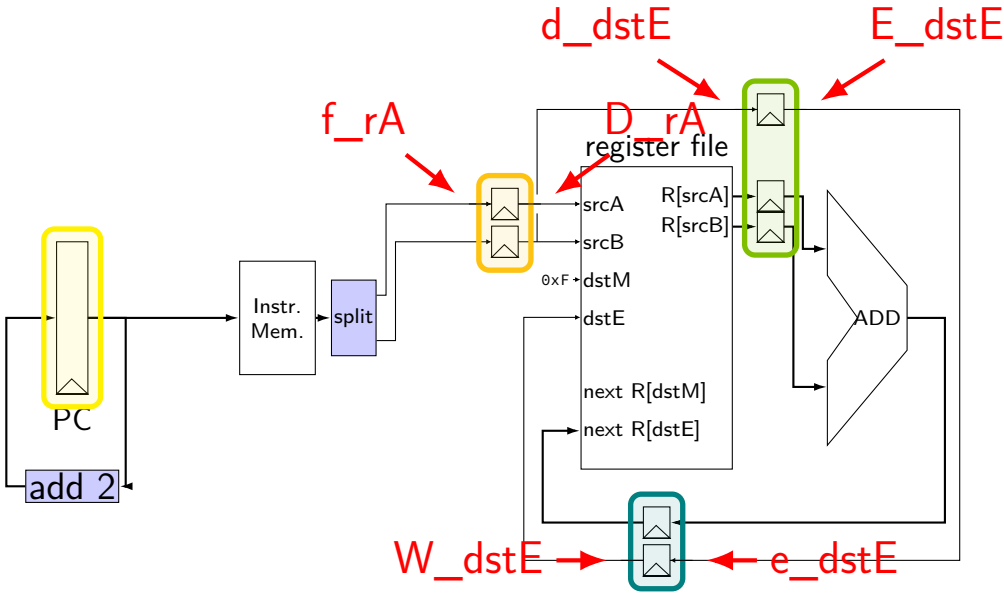
now, cycle time = 200 ps + register delays per cycle

exercise 2:

suppose we combine add and register file read together — new cycle time?

A. 200 ps + reg delay
B. 225 ps + reg delay
C. 250 ps + reg delay
D. 280 ps + reg delay
E. 325 ps + reg delay
E. something else

pipeline register naming convention



pipeline register naming convention

f — fetch sends values here

D — decode receives values here

d — decode sends values here

...

addq HCL

```
...
/* f: from fetch */
f_rA = i10bytes[12..16];
f_rB = i10bytes[8..12];

/* fetch to decode */
/* f_rA -> D_rA, etc. */
register fD {
    rA : 4 = REG_NONE;
    rB : 4 = REG_NONE;
}
```

```
/* D: to decode
   d: from decode */
d_dstE = D_rB;
/* use register file: */
reg_srcA = D_rA;
d_valA = reg_outputA;
...

/* decode to execute */
register dE {
    dstE : 4 = REG_NONE;
    valA : 64 = 0;
    valB : 64 = 0;
}

...
```

addq fetch/decode

unpipelined

```
/* Fetch+PC Update*/
pc = P_pc;
p_pc = pc + 2;
rA = i10bytes[12..16];
rB = i10bytes[8..12];
/* Decode */
reg_srcA = rA;
reg_srcB = rB;
reg_dstE = rB;
valA = reg_outputA;
valB = reg_outputB;
```

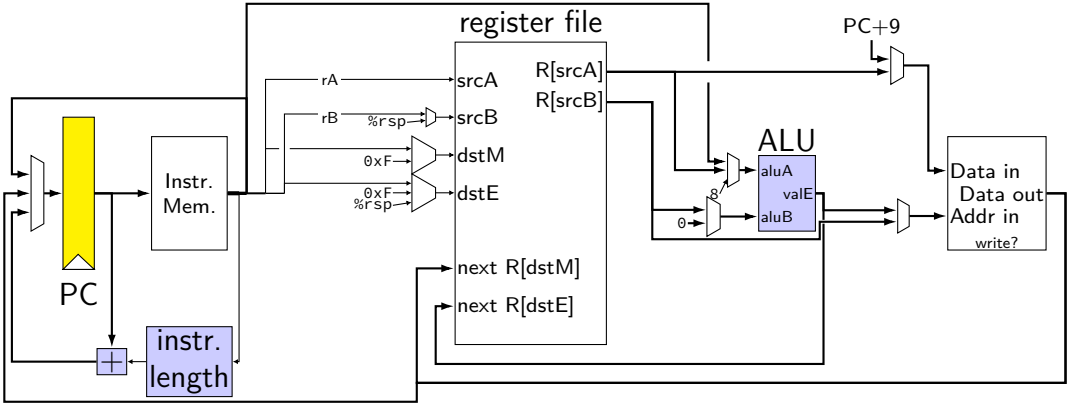
pipelined

```
/* Fetch+PC Update*/
pc = P_pc;
p_pc = pc + 2;
f_rA = i10bytes[12..16];
f_rB = i10bytes[8..12];
/* Decode */
reg_srcA = D_rA;
reg_srcB = D_rB;
d_dstE = D_rB;
d_valA = reg_outputA;
d_valB = reg_outputB;
```

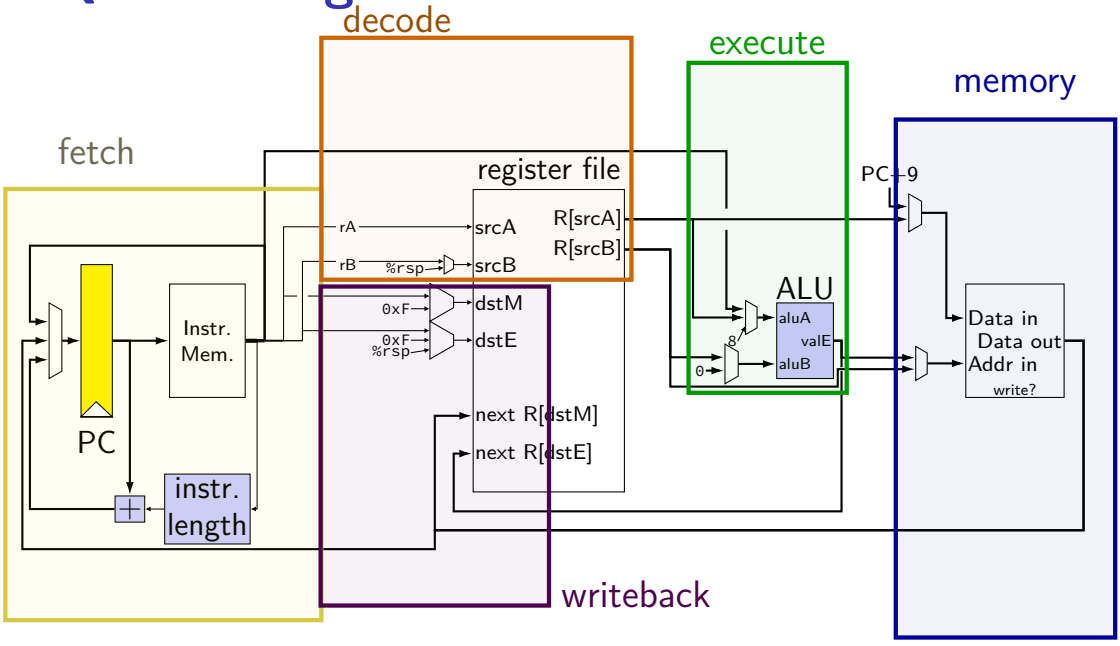
addq pipeline registers

```
register pP {
    pc : 64 = 0;
};
/* Fetch+PC Update*/
register fD {
    rA : 4 = REG_NONE; rB : 4 = REG_NONE;
};
/* Decode */
register dE {
    valA : 64 = 0; valB : 64 = 0; dstE : 4 = REG_NONE;
}
/* Execute */
register eW {
    valE : 64 = 0; dstE : 4 = REG_NONE;
}
/* Writeback */
```

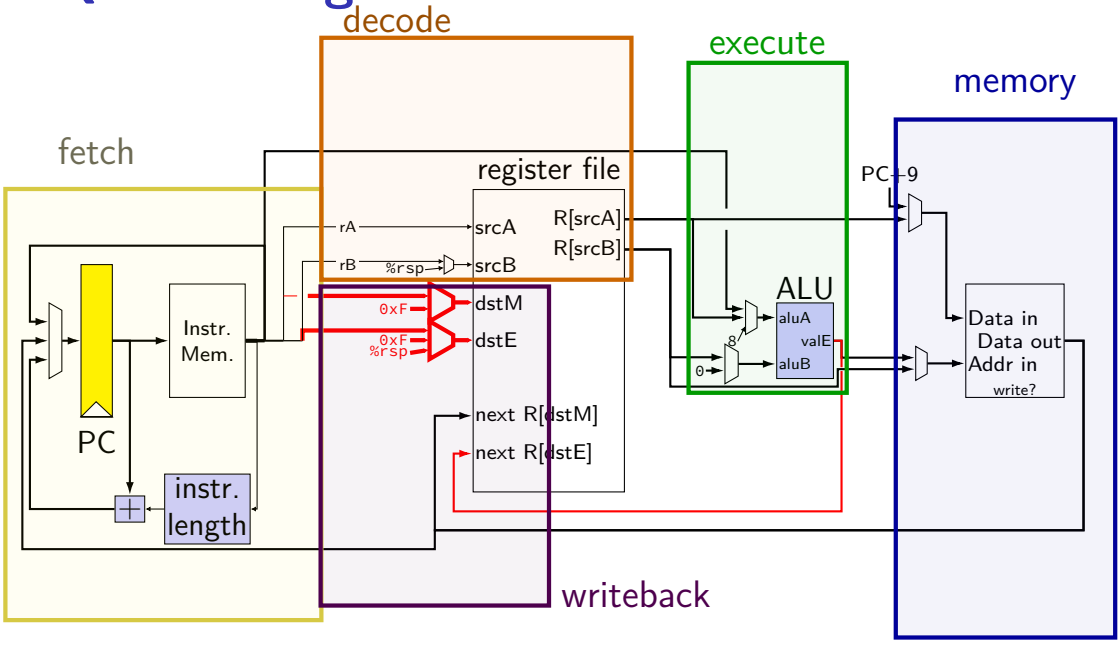
SEQ without stages



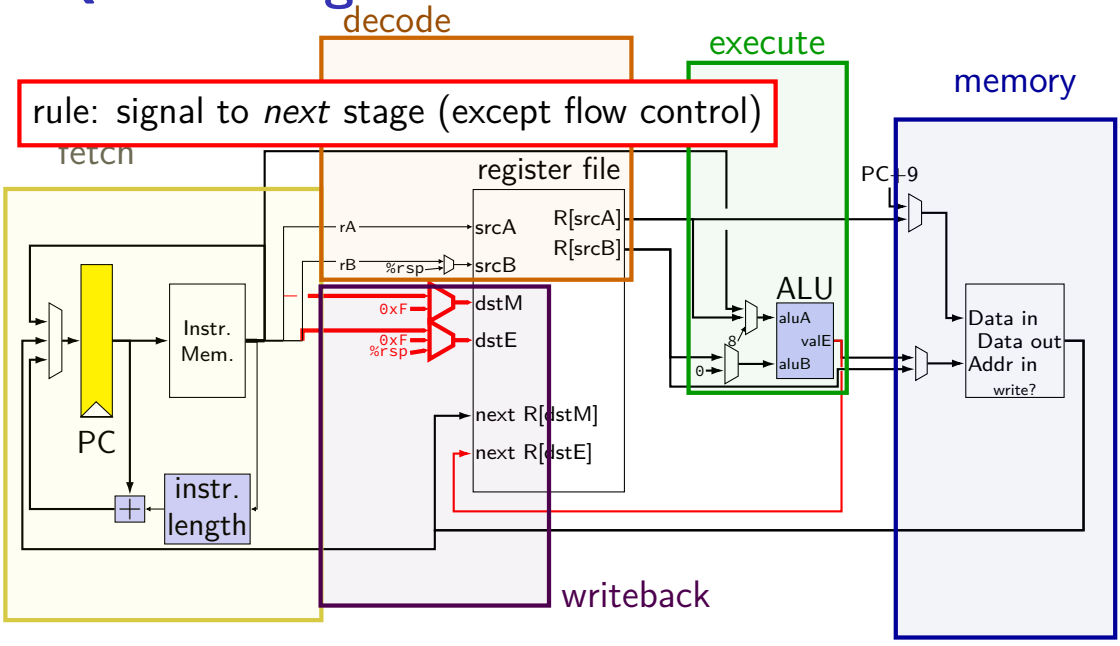
SEQ with stages



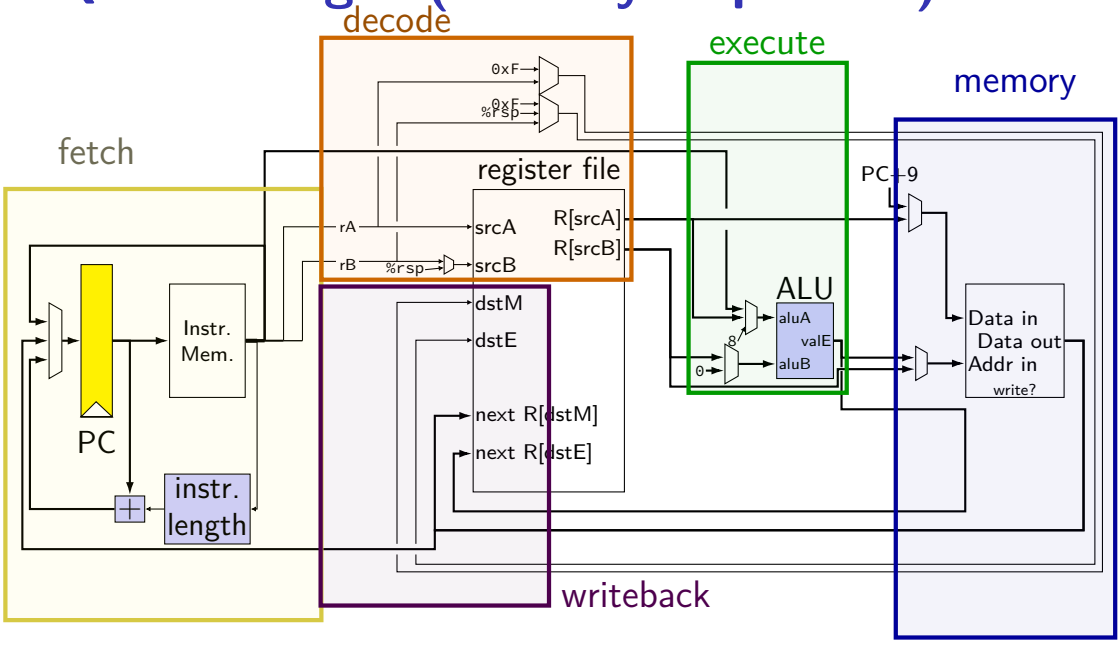
SEQ with stages



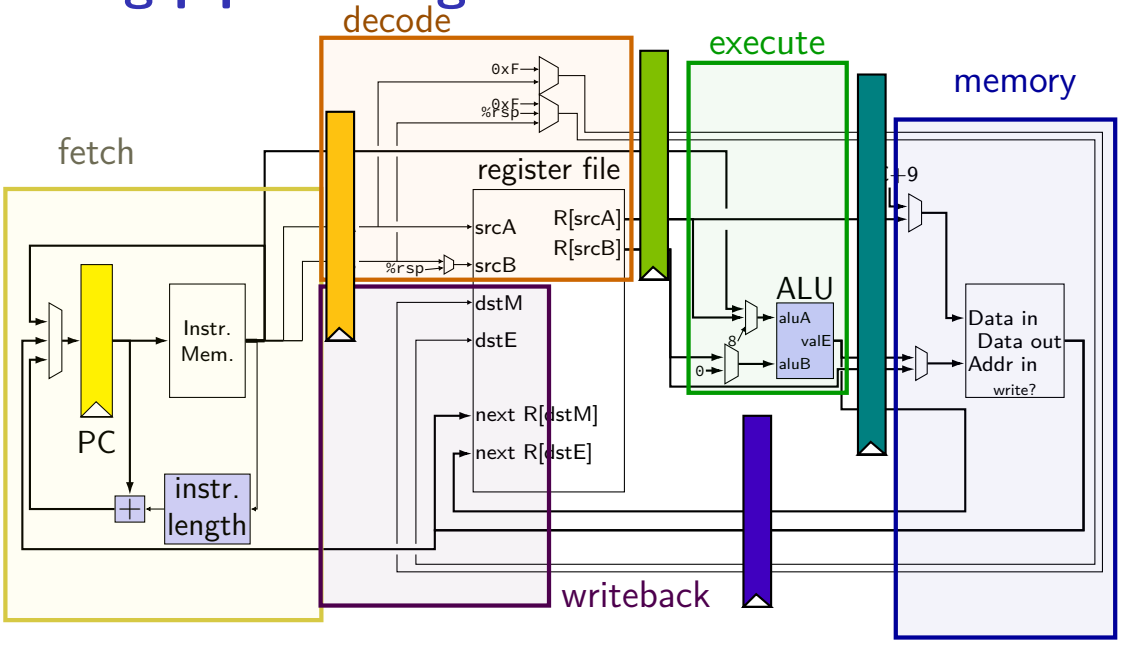
SEQ with stages



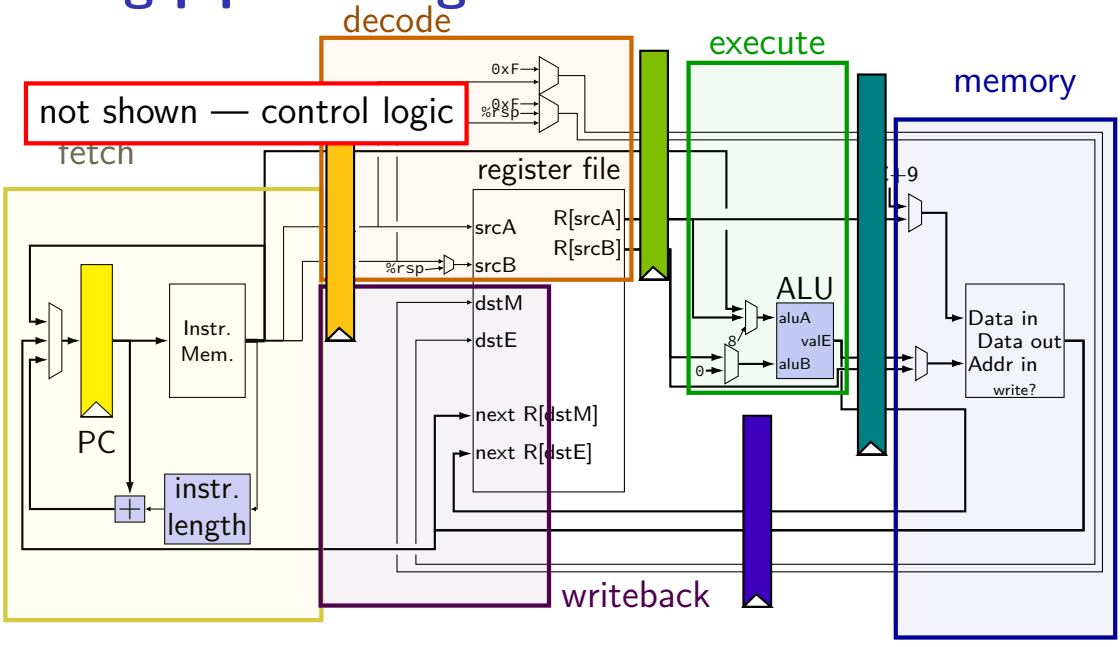
SEQ with stages (actually sequential)



adding pipeline registers



adding pipeline registers



passing values in pipeline

read prior stage's outputs

- e.g. decode: get from fetch via pipeline registers (`D_icode`, ...)

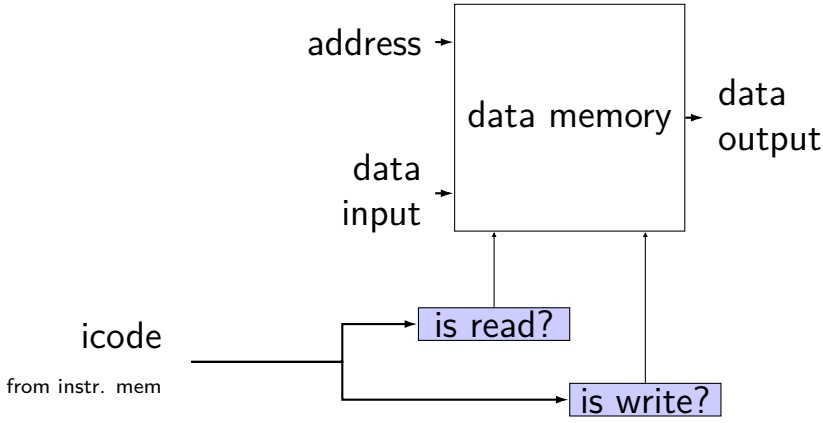
send inputs for next stage

- e.g. decode: send to execute via pipeline registers (`d_icode`, ...)

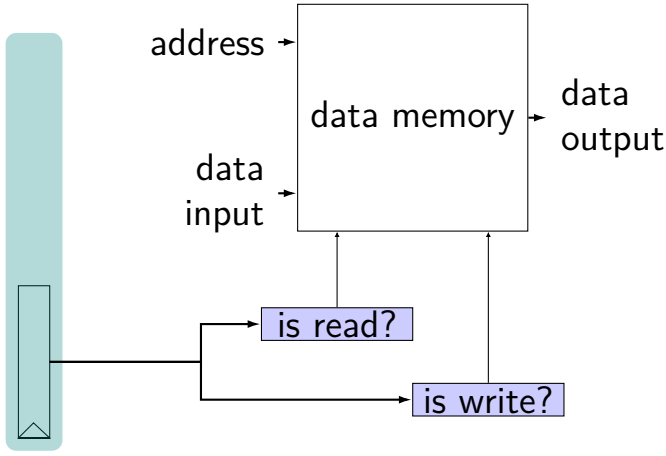
exceptions: deliberate sharing between instructions

- via register file/memory/etc.
- via control flow instructions

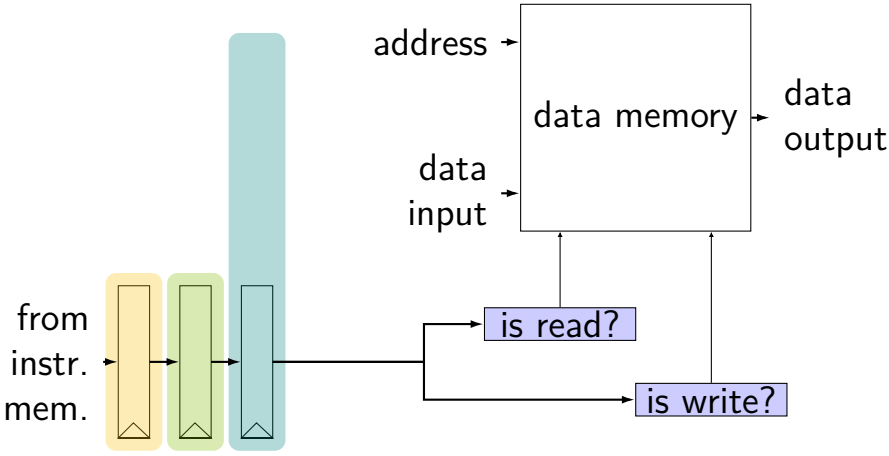
memory read/write logic



memory read/write logic



memory read/write logic



memory read/write: SEQ code

```
icode = i10bytes[4..8];
mem_readbit = [
    icode == MRMOVQ || ...: 1;
    0;
];
```

memory read/write: PIPE code

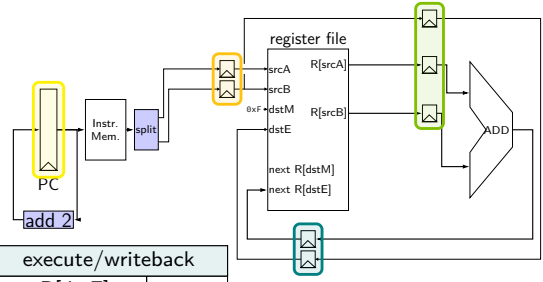
```
f_icode = i10bytes[4..8];
register fD { /* and dE and eM and mW */
    icode : 4 = NOP;
}
d_icode = D_icode;
...
e_icode = E_icode;
mem_readbit = [
    M_icode == MRMOVQ || ...: 1;
    0;
];
```

memory read/write: PIPE code

```
f_icode = i10bytes[4..8];
register fD { /* and dE and eM and mW */
    icode : 4 = NOP;
}
d_icode = D_icode;
...
e_icode = E_icode;
mem_readbit = [
    M_icode == MRMOVQ || ...: 1;
    0;
];
```

addq processor: data hazard

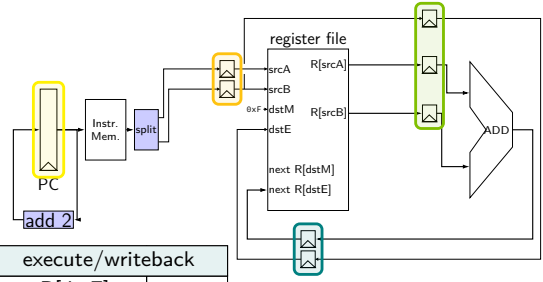
```
// initially %r8 = 800,
//           %r9 = 900, etc.
addq %r8, %r9
addq %r9, %r8
addq ...
addq ...
```



	fetch	fetch/decode		decode/execute			execute/writeback	
cycle	PC	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0							
1	0x2	8	9					
2		9	8	800	900	9		
3				900	800	8	1700	9
4							1700	8

addq processor: data hazard

```
// initially %r8 = 800,
//           %r9 = 900, etc.
addq %r8, %r9
addq %r9, %r8
addq ...
addq ...
```



	fetch	fetch/decode		decode/execute			execute/writeback	
cycle	PC	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0							
1	0x2	8	9					
2		9	8	800	900	9		
3				900	800	8	1700	9
4							1700	8

should be 1700

data hazard

```
addq %r8, %r9  // (1)
addq %r9, %r8  // (2)
```

step#	pipeline implementation	ISA specification
1	read r8, r9 for (1)	read r8, r9 for (1)
2	read r9, r8 for (2)	write r9 for (1)
3	write r9 for (1)	read r9, r8 for (2)
4	write r8 for (2)	write r8 ror (2)

pipeline reads older value...

instead of value ISA says was just written

data hazard compiler solution

```
addq %r8, %r9
nop
nop
addq %r9, %r8
```

one solution: change the ISA

- all addqs take effect three instructions later

make it compiler's job

problem: recompile everytime processor changes?

data hazard hardware solution

```
addq %r8, %r9
// hardware inserts: nop
// hardware inserts: nop
addq %r9, %r8
```

how about hardware add nops?

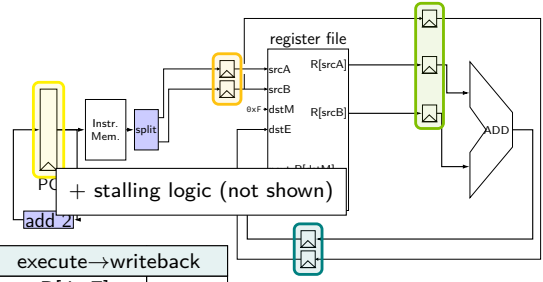
called stalling

extra logic:

- sometimes don't change PC
- sometimes put do-nothing values in pipeline registers

addq processor: data hazard stall

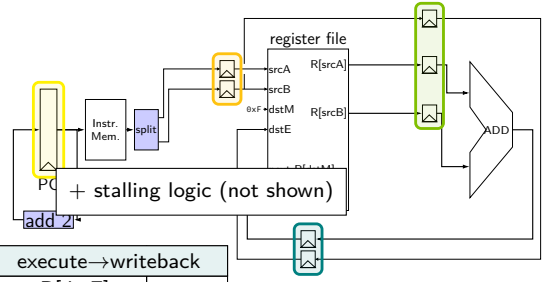
```
// initially %r8 = 800,
//           %r9 = 900, etc.
addq %r8, %r9
// hardware stalls twice
addq %r9, %r8
addq %r10, %r11
```



	fetch	fetch→decode		decode→execute			execute→writeback	
cycle	PC	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0							
1	0x2*	8	9					
2	0x2*	F	F	800	900	9		
3	0x2	F	F	---	---	F	1700	9
4	0x4	9	8	---	---	F	---	F
5		10	11	1700	800	8	---	F
6				1000	1100	11	2500	8

addq processor: data hazard stall

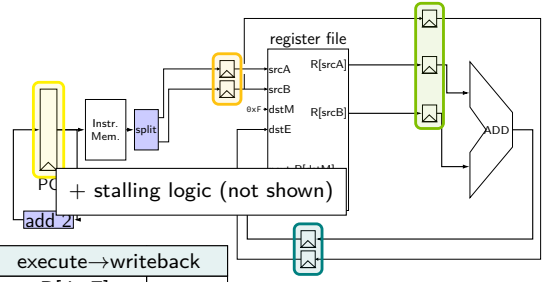
```
// initially %r8 = 800,
//           %r9 = 900, etc.
addq %r8, %r9
// hardware stalls twice
addq %r9, %r8
addq %r10, %r11
```



	fetch	fetch→decode		decode→execute			execute→writeback	
cycle	PC	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0							
1	0x2*	8	9					
2	0x2*	F	F	800	900	9		
3	0x2	F	F	---	---	F	1700	9
4	0x4	9	8	---	---	F	---	F
5		10	11	1700	800	8	---	F
6				1000	1100	11	2500	8

addq processor: data hazard stall

```
// initially %r8 = 800,
//           %r9 = 900, etc.
addq %r8, %r9
// hardware stalls twice
addq %r9, %r8
addq %r10, %r11
```

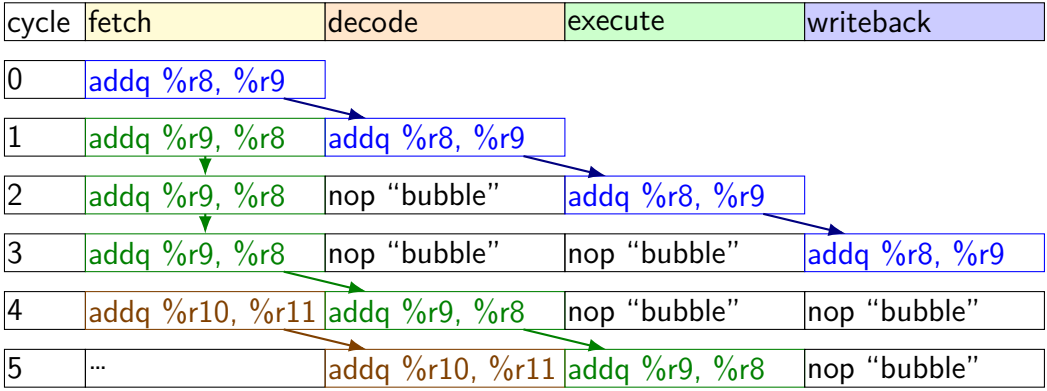


	fetch	fetch→decode		decode→execute			execute→writeback	
cycle	PC	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0							
1	0x2*	8	9					
2	0x2*	F	F	800	900	9		
3	0x2	F	F	---	---	F	1700	9
4	0x4	9	8	---	---	F	---	F
5		10	11	1700	800	8	---	F
6				1000	1100	11	2500	8

R[9] written during cycle 3; read during cycle 4

addq stall

```
addq %r8, %r9
// hardware stalls twice
addq %r9, %r8
addq %r10, %r11
```



hazards versus dependencies

dependency — X needs result of instruction Y?

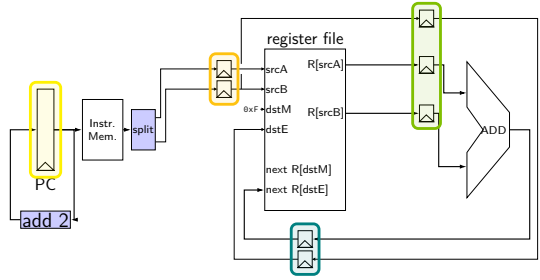
- has potential for being messed up by pipeline
- (since part of X may run before Y finishes)

hazard — will it not work in some pipeline?

- before extra work is done to "resolve" hazards
- multiple kinds: so far, *data hazards*

data hazard exericse

```
addq %r8, %r9
addq %r10, %r11
addq %r9, %r8
addq %r11, %r10
```

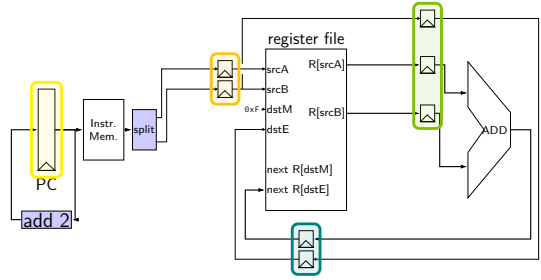


to resolve data hazards with stalling, how many stalls are needed?

hint: complete timeline

instr	cycle: 0	1	2	3	4	5	6	7
addq R8, R9	F	D	E	W				
addq R10, R11		F						
addq R9, R8								
addq R11, R10								

data hazard exericse solution



	cycle #	0	1	2	3	4	5	6	7	8
`addq %r8, %r9`		F	D	E	W					
`addq %r10, %r11`			F	D	E	W				
`addq %r9, %r8`				✕	F	D	E	W		
`addq %r11, %r10`						F	D	E	W	

revisiting data hazards

stalling worked

but very unsatisfying — wait 2 extra cycles to use anything?!

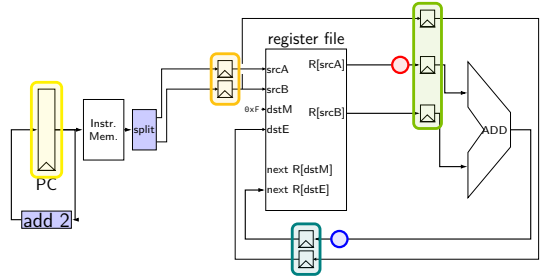
...or more with 5-stage pipeline

observation: value ready before it would be needed

(just not stored in a way that let's us get it)

motivation

location of values during cycle 2:



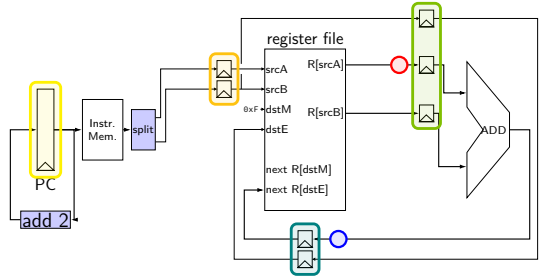

```
// initially %r8 = 800,
//           %r9 = 900, etc.
addq %r8, %r9
addq %r9, %r8
addq ...
addq ...
```

	fetch	fetch/decode		decode/execute			execute/writeback	
cycle	PC	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0							
1	0x2	8	9					
2		9	8	800	900	9		
3				900	800	8	1700	9
4							1700	8

should be 1700

motivation

location of values during cycle 2:



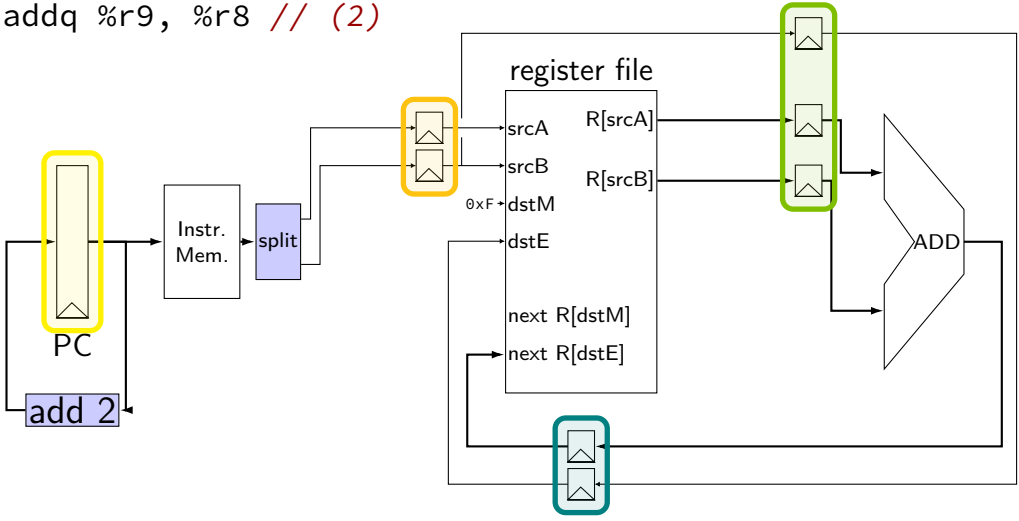

```
// initially %r8 = 800,
//           %r9 = 900, etc.
addq %r8, %r9
addq %r9, %r8
addq ...
addq ...
```

	fetch	fetch/decode		decode/execute			execute/writeback	
cycle	PC	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0							
1	0x2	8	9					
2		9	8	800	900	9		
3				900	800	8	1700	9
4							1700	8

should be 1700

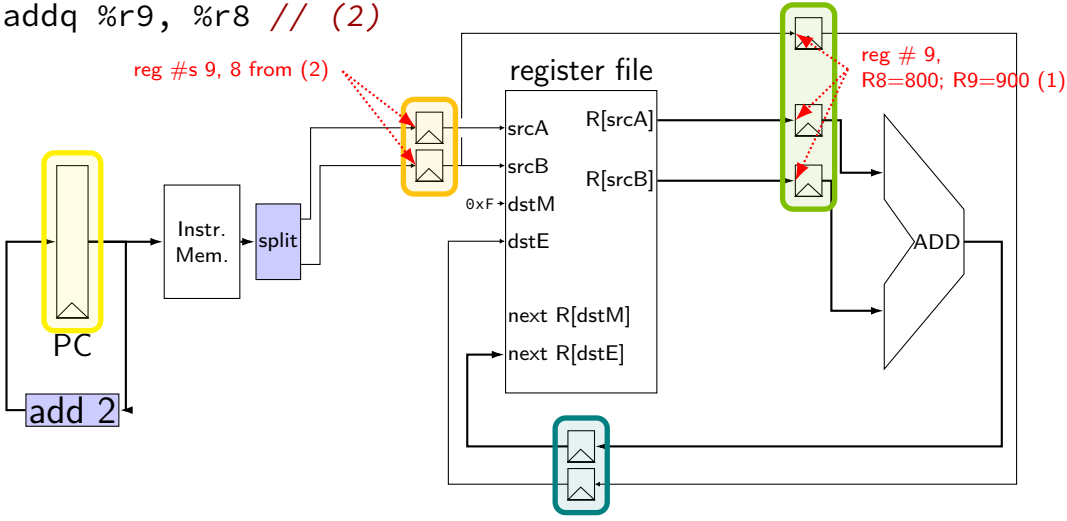
forwarding

```
addq %r8, %r9 // (1)
addq %r9, %r8 // (2)
```



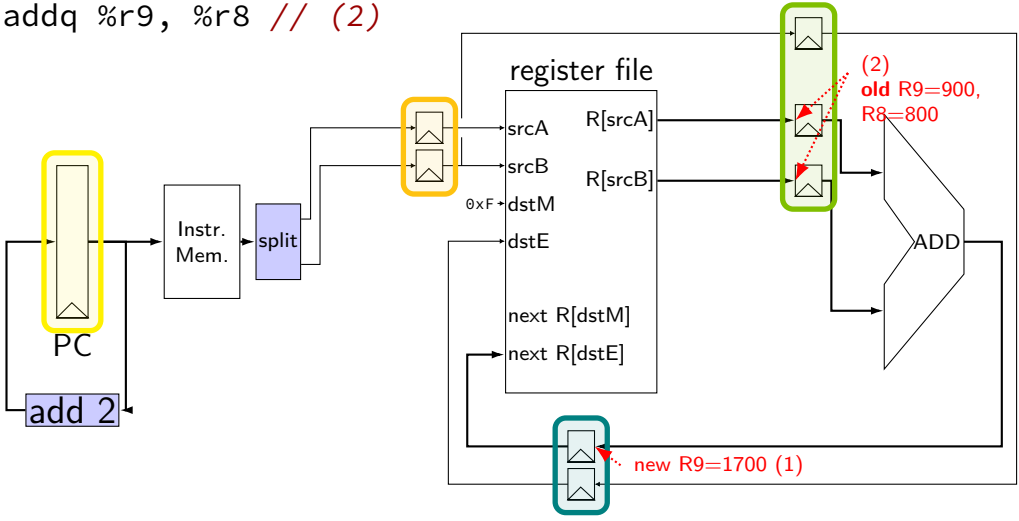
forwarding

```
addq %r8, %r9 // (1)
addq %r9, %r8 // (2)
```



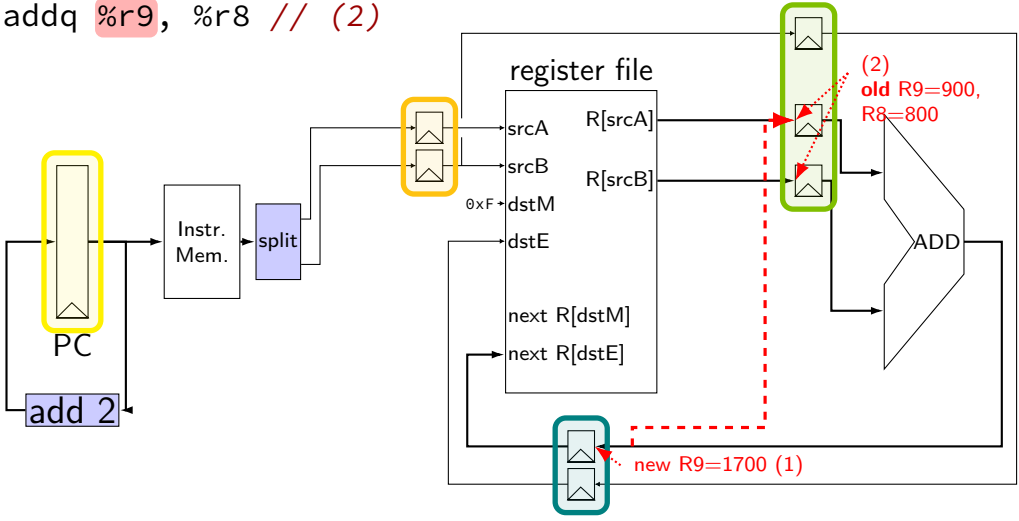
forwarding

```
addq %r8, %r9 // (1)
addq %r9, %r8 // (2)
```



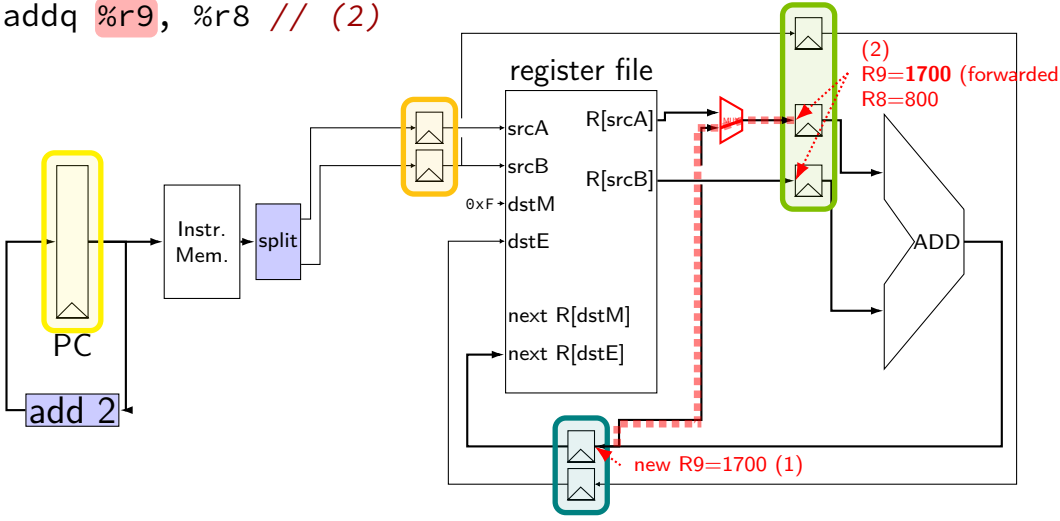
forwarding

```
addq %r8, %r9 // (1)
addq %r9, %r8 // (2)
```



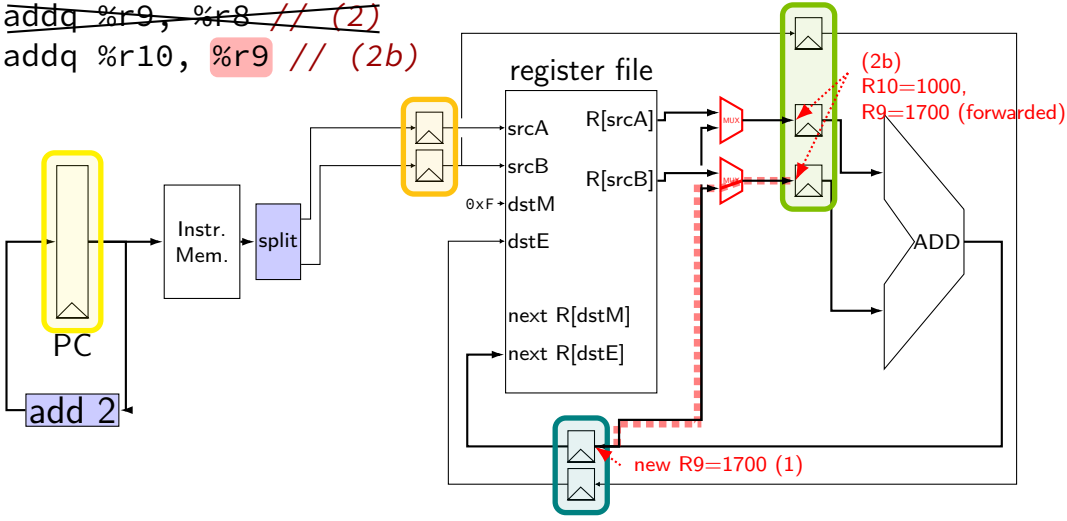
forwarding

```
addq %r8, %r9 // (1)
addq %r9, %r8 // (2)
```



forwarding

```
addq %r8, %r9 // (1)
addq %r9, %r8 // (2)
addq %r10, %r9 // (2b)
```

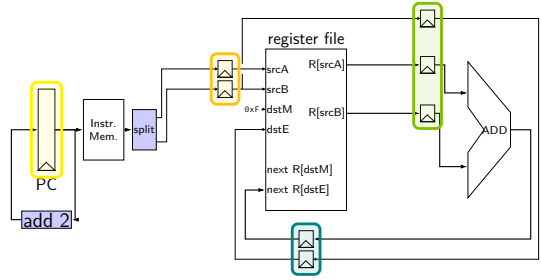


backup slides

addq processor performance

example delays:

path	time
add 2	80 ps
instruction memory	200 ps
register file read	125 ps
add	100 ps
register file write	125 ps



no pipelining: 1 instruction per 550 ps

add up everything but add 2 (critical (slowest) path)

pipelining: 1 instruction per 200 ps + pipeline register delays

slowest path through stage + pipeline register delays

latency: 800 ps + pipeline register delays (4 cycles)