

Pipelining 3

March 14, 2023

Last lecture concepts

Pipelining idea

Latency (start to finish for 1 instruction)

Throughput

Diminishing returns in pipelining

- only as fast as slowest stage

- cannot divide work evenly in practice

- registers add latency, area

Pipelining circuits

- send values from one stage to next stage

- add registers between each pair of stages

HCL convention: fD, dE, eM, mW

quiz

Q1: The PC register is a 64-bit register that is always incremented by the number of bytes in the current instruction
not when jXX, call, ret

Q2: The Instruction Memory, register file, and Data Memory access the same underlying memory, therefore data written to the Data Memory can be read from the Instruction Memory or register file
register file is an entirely different mechanism, it is not one with the Instruction/Data memory

Q2: The condition codes values update every time the output of the ALU changes
only during OPq operations

Q4: Latency $(5(800+50))/(3(2000+100))$ vs
 $(800+800+800+800+800 + 5*50)/(1000+2000+2000 + 3*100)$

addq processor: data hazard

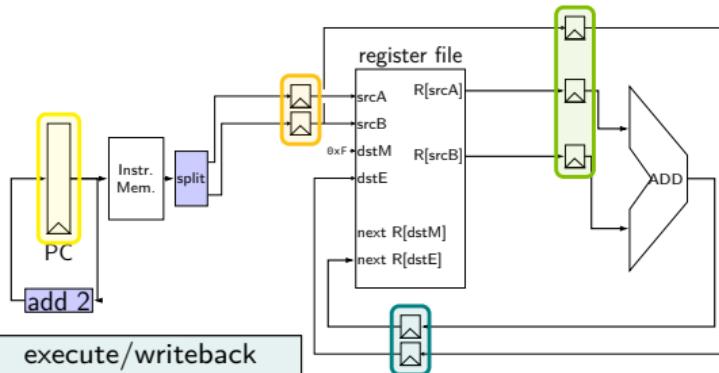
// initially %r8 = 800,
// %r9 = 900, etc.

addq %r8, %r9

addq %r9, %r8

addq ...

addq ...



	fetch	fetch/decode		decode/execute			execute/writeback	
cycle	PC	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0							
1	0x2	8	9					
2		9	8	800	900	9		
3				900	800	8	1700	9
4							1700	8

addq processor: data hazard

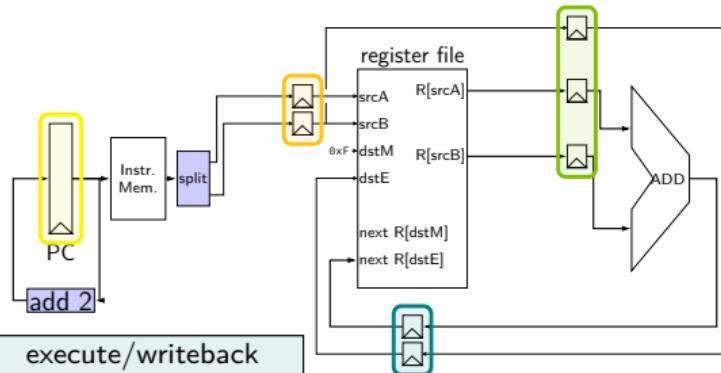
// initially %r8 = 800,
// %r9 = 900, etc.

addq %r8, %r9

addq %r9, %r8

addq ...

addq ...



	fetch	fetch/decode		decode/execute			execute/writeback	
cycle	PC	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0							
1	0x2	8	9					
2		9	8	800	900	9		
3				900	800	8	1700	9
4							1700	8

should be 1700

data hazard

```
addq %r8, %r9 // (1)  
addq %r9, %r8 // (2)
```

step#	pipeline implementation	ISA specification
1	read r8, r9 for (1)	read r8, r9 for (1)
2	read r9, r8 for (2)	write r9 for (1)
3	write r9 for (1)	read r9, r8 for (2)
4	write r8 for (2)	write r8 ror (2)

pipeline reads **older value**...

instead of value ISA says was just written

data hazard compiler solution

```
addq %r8, %r9  
nop  
nop  
addq %r9, %r8
```

one solution: change the ISA

all addqs take effect three instructions later

make it compiler's job

problem: recompile everytime processor changes?

data hazard hardware solution

```
addq %r8, %r9  
// hardware inserts: nop  
// hardware inserts: nop  
addq %r9, %r8
```

how about hardware add nops?

called **stalling**

extra logic:

- sometimes don't change PC

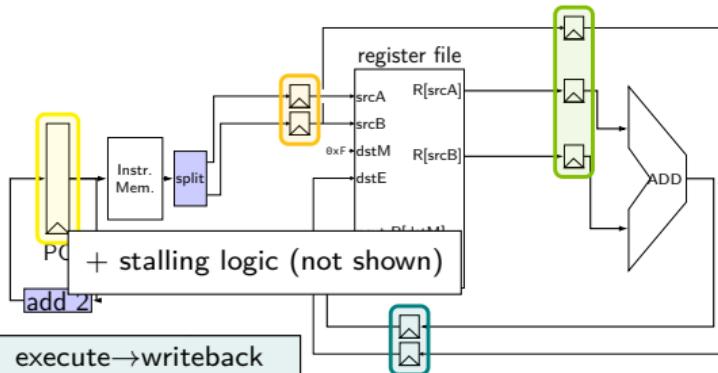
- sometimes put do-nothing values in pipeline registers

addq processor: data hazard stall

```
// initially %r8 = 800,  
// %r9 = 900, etc.  
addq %r8, %r9
```

// hardware stalls twice

```
addq %r9, %r8  
addq %r10, %r11
```



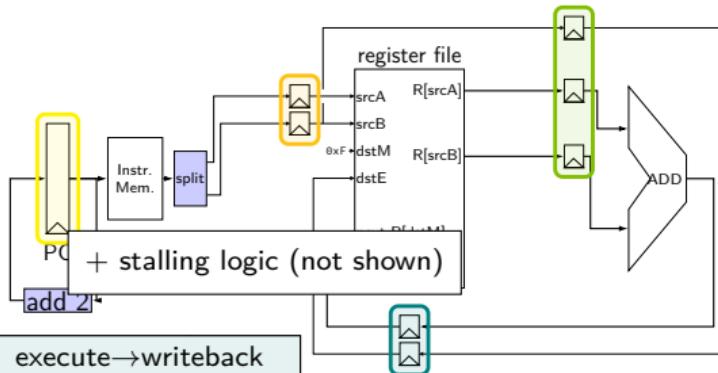
cycle	fetch	fetch→decode		decode→execute			execute→writeback	
	PC	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0							
1	0x2*	8	9					
2	0x2*	F	F	800	900	9		
3	0x2	F	F	---	---	F	1700	9
4	0x4	9	8	---	---	F	---	F
5		10	11	1700	800	8	---	F
6				1000	1100	11	2500	8

addq processor: data hazard stall

```
// initially %r8 = 800,  
// %r9 = 900, etc.  
addq %r8, %r9
```

// hardware stalls twice

```
addq %r9, %r8  
addq %r10, %r11
```



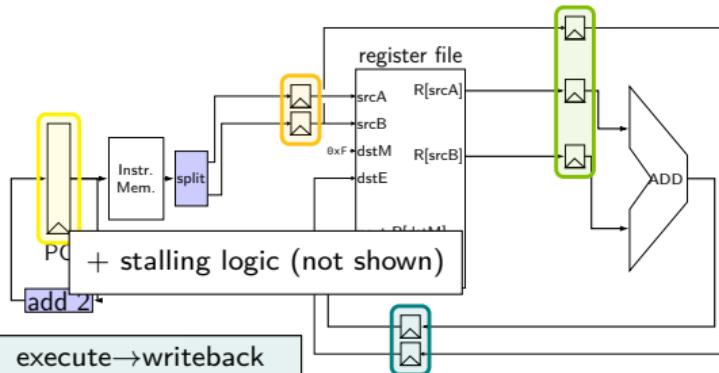
cycle	fetch	fetch→decode		decode→execute			execute→writeback	
	PC	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0							
1	0x2*	8	9					
2	0x2*	F	F	800	900	9		
3	0x2	F	F	---	---	F	1700	9
4	0x4	9	8	---	---	F	---	F
5		10	11	1700	800	8	---	F
6				1000	1100	11	2500	8

addq processor: data hazard stall

```
// initially %r8 = 800,  
// %r9 = 900, etc.  
addq %r8, %r9
```

// hardware stalls twice

```
addq %r9, %r8  
addq %r10, %r11
```

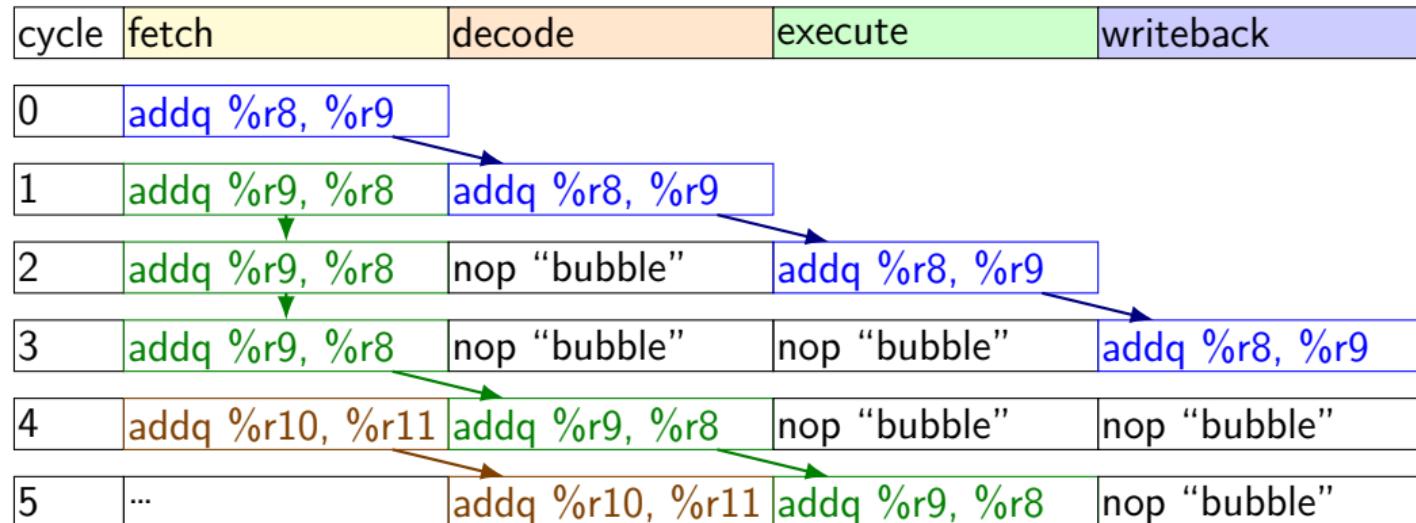


cycle	fetch	fetch→decode		decode→execute			execute→writeback	
	PC	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0							
1	0x2*	8	9					
2	0x2*	F	F	800	900	9		
3	0x2	F	F	---	---	F	1700	9
4	0x4	9	8	---	---	F	---	F
5		10	11	1700	800	8	---	F
6				1000	1100	11	2500	8

R[9] written during cycle 3; read during cycle 4

addq stall

```
addq %r8, %r9  
// hardware stalls twice  
addq %r9, %r8  
addq %r10, %r11
```



hazards versus dependencies

dependency — X needs result of instruction Y?

has potential for being messed up by pipeline
(since part of X may run before Y finishes)

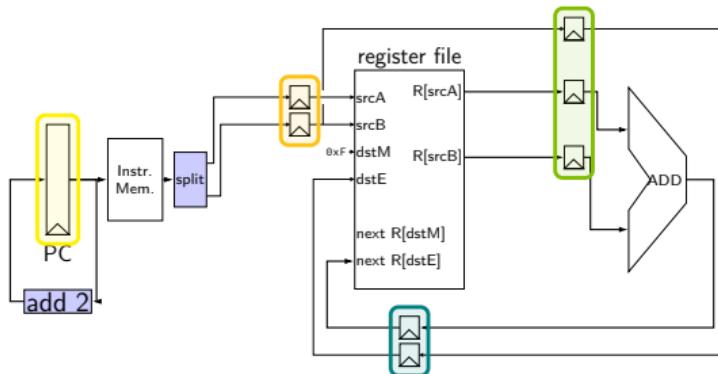
hazard — will it not work in some pipeline?

before extra work is done to “resolve” hazards

multiple kinds: so far, *data hazards*

data hazard exercise

```
addq %r8, %r9  
addq %r10, %r11  
addq %r9, %r8  
addq %r11, %r10
```

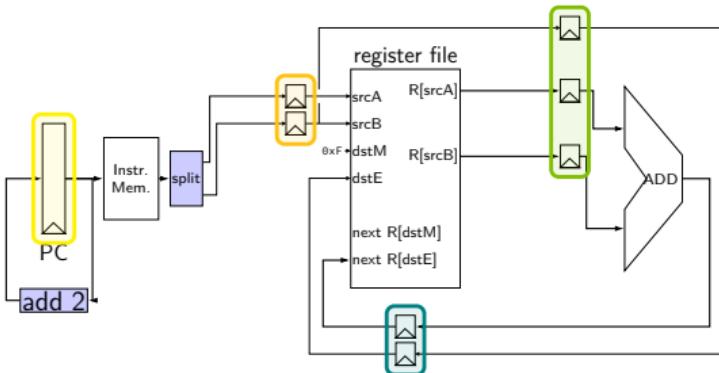


to resolve data hazards with stalling, how many stalls are needed?

hint: complete timeline

instr	cycle: 0	1	2	3	4	5	6	7
addq R8, R9	F	D	E	W				
addq R10, R11			F					
addq R9, R8								
addq R11, R10								

data hazard exercise solution



	cycle #	0	1	2	3	4	5	6	7	8
addq %r8, %r9		F	D	E	W					
addq %r10, %r11		F	D	E	W					
addq %r9, %r8				X	F	D	E	W		
addq %r11, %r10					F	D	E	W		

revisiting data hazards

stalling worked

but very unsatisfying — wait 2 extra cycles to use anything?!
...or more with 5-stage pipeline

observation: **value** ready before it would be needed
(just not stored in a way that let's us get it)

motivation

location of values during cycle 2:

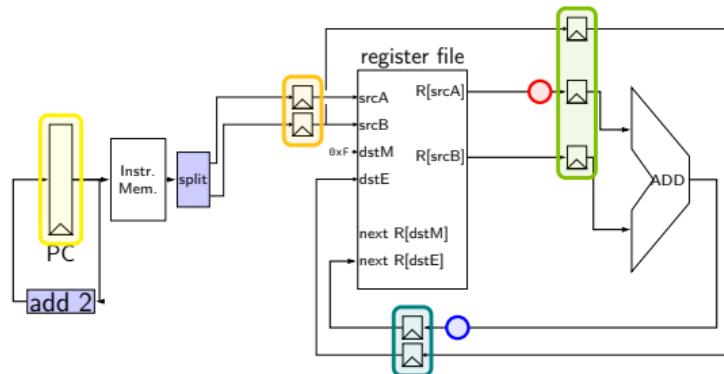
// initially %r8 = 800,
// %r9 = 900, etc.

addq %r8, %r9

addq %r9, %r8

addq ...

addq ...



	fetch	fetch/decode		decode/execute			execute/writeback	
cycle	PC	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0							
1	0x2	8	9					
2		9	8	800	900	9		
3				900	800	8	1700	9
4							1700	8

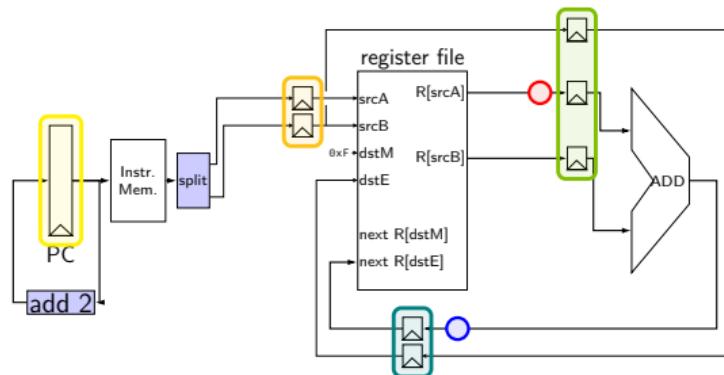
should be 1700

motivation

// initially %r8 = 800,
// %r9 = 900, etc.

addq %r8, %r9
addq %r9, %r8
addq ...
addq ...

location of values during cycle 2:

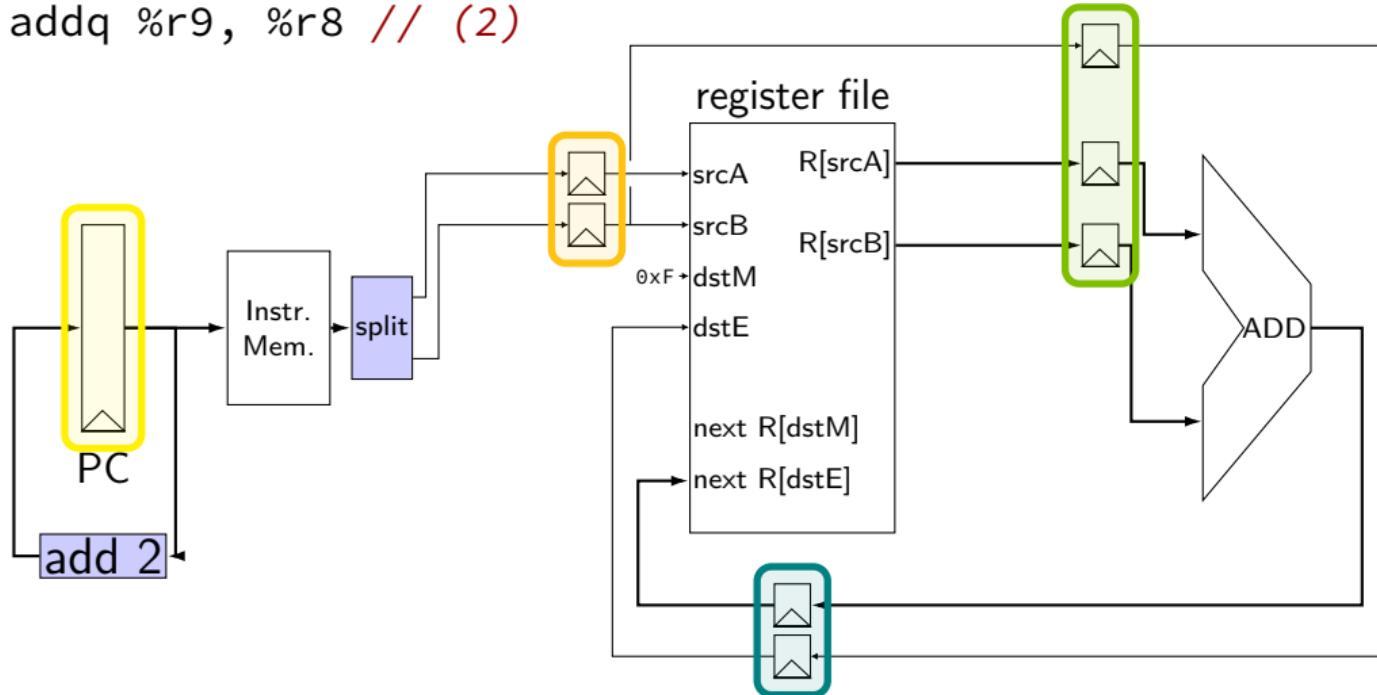


	fetch	fetch/decode		decode/execute			execute/writeback	
cycle	PC	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0							
1	0x2	8	9					
2		9	8	800	900	9		
3				900	800	8	1700	9
4							1700	8

should be 1700

forwarding

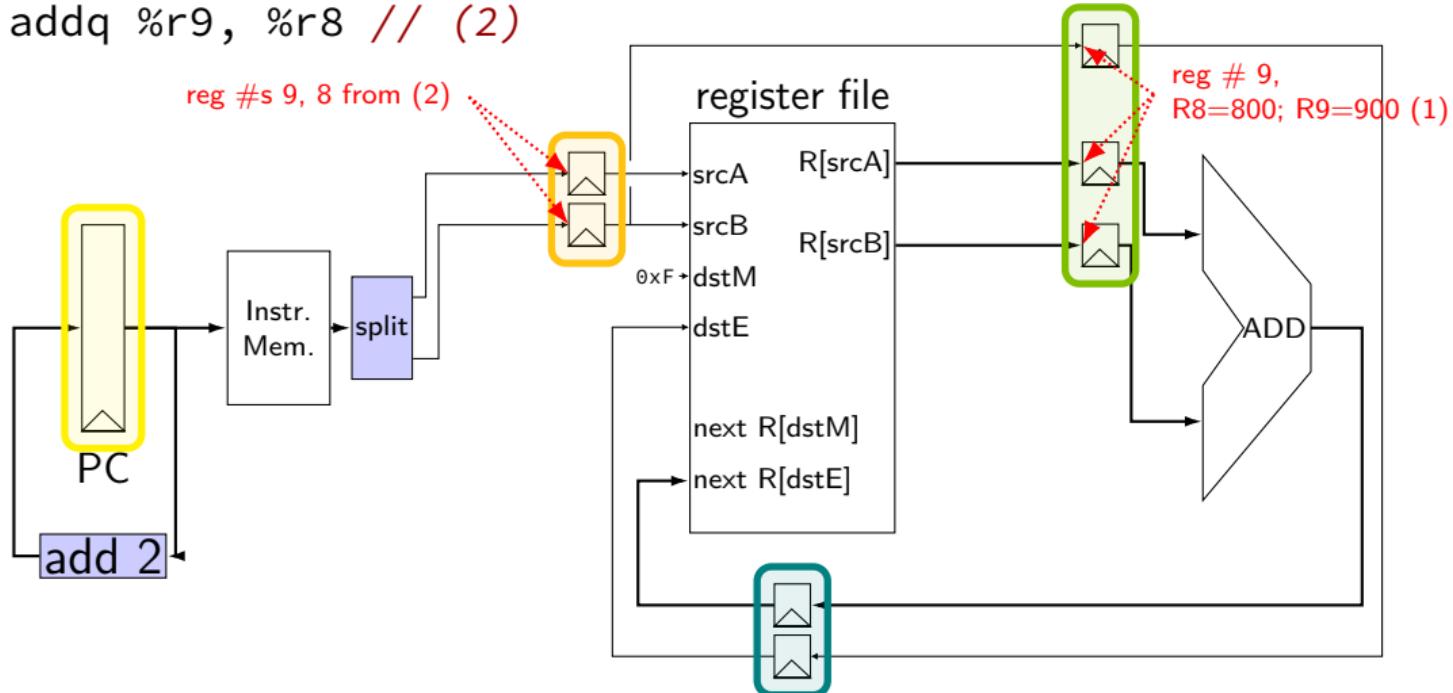
addq %r8, %r9 // (1)
addq %r9, %r8 // (2)



forwarding

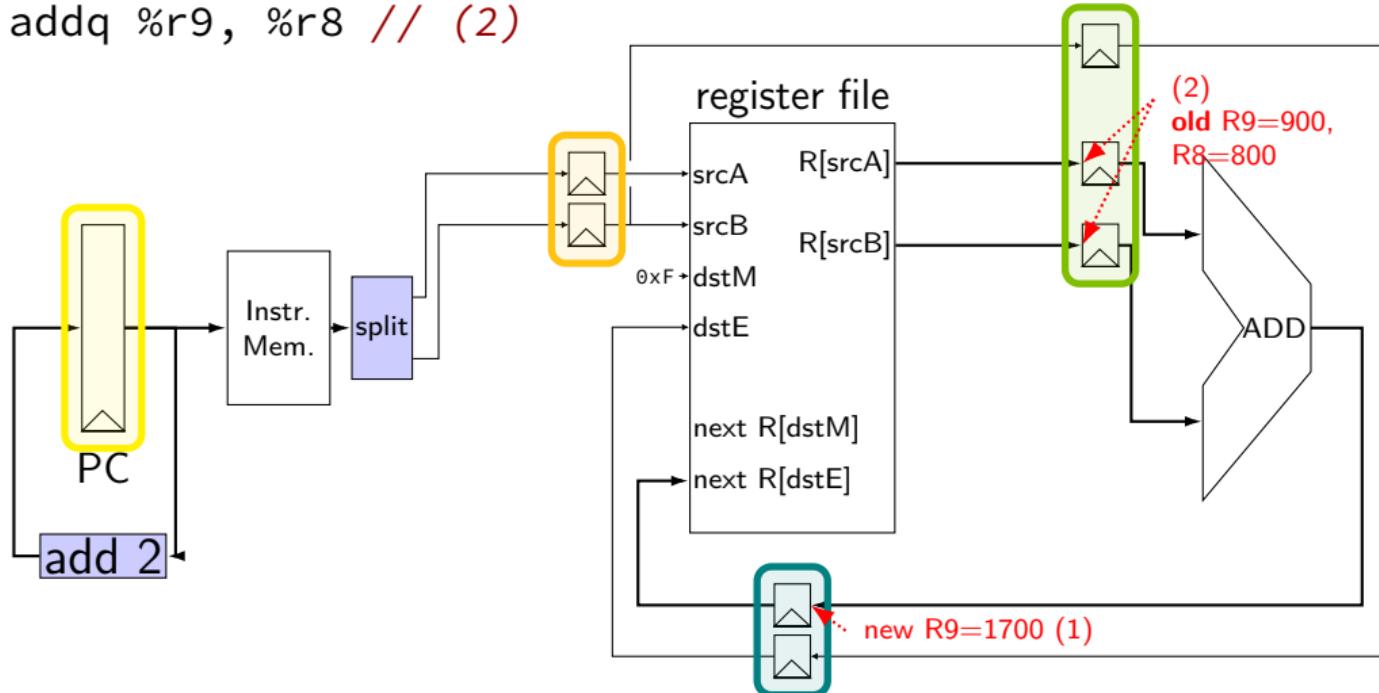
```
addq %r8, %r9 // (1)  
addq %r9, %r8 // (2)
```

reg #s 9, 8 from (2)



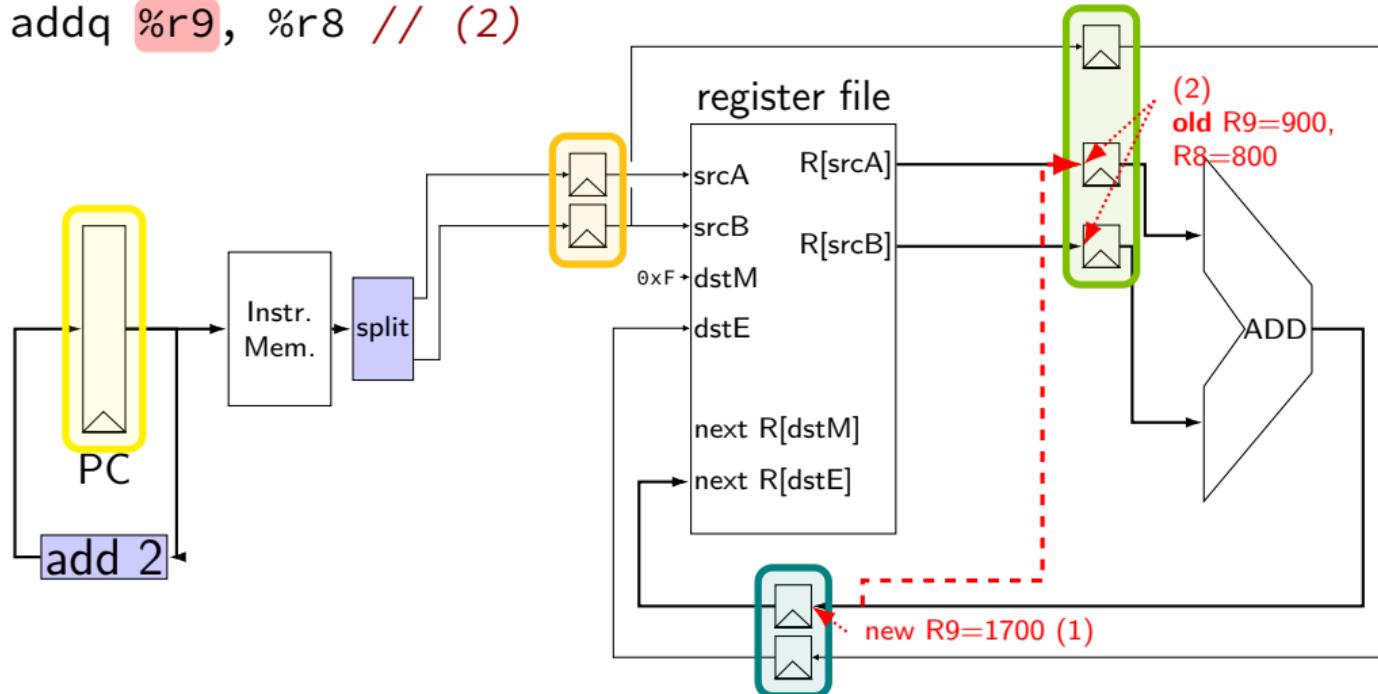
forwarding

addq %r8, %r9 // (1)
addq %r9, %r8 // (2)



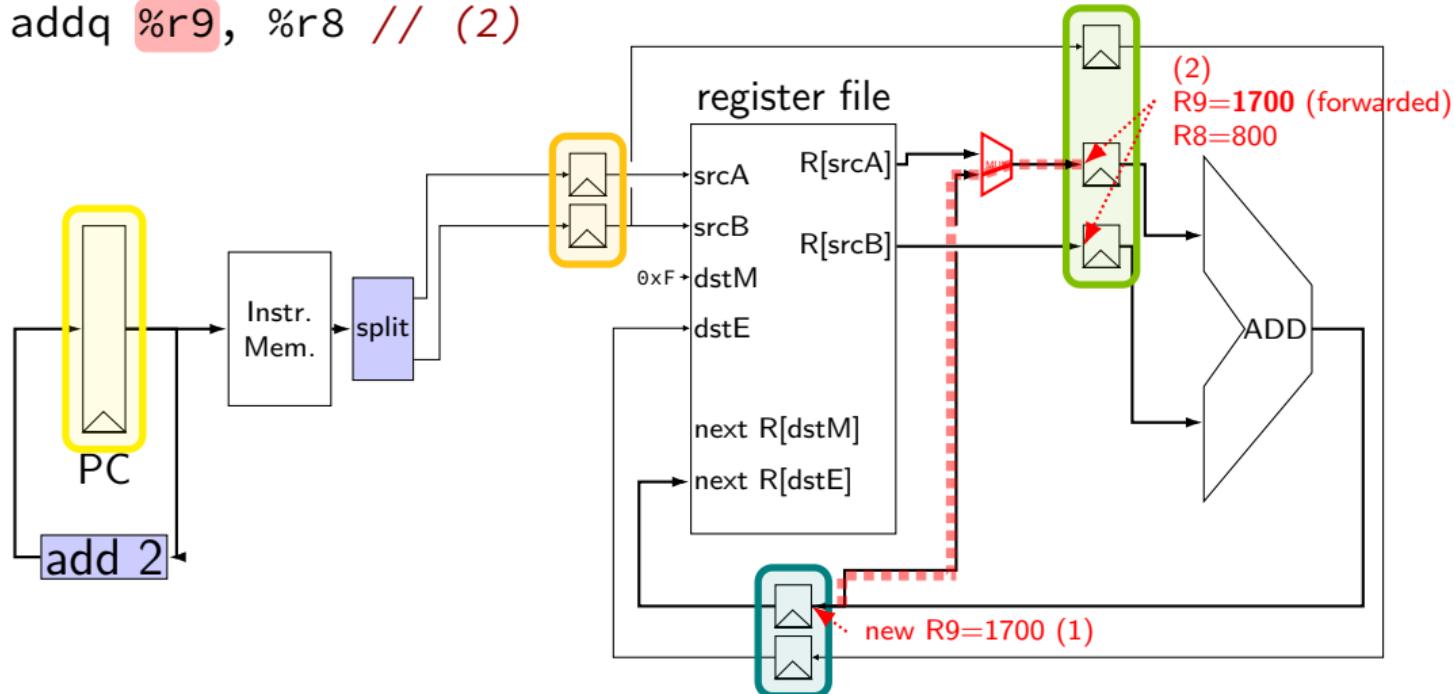
forwarding

addq %r8, %r9 // (1)
addq %r9, %r8 // (2)



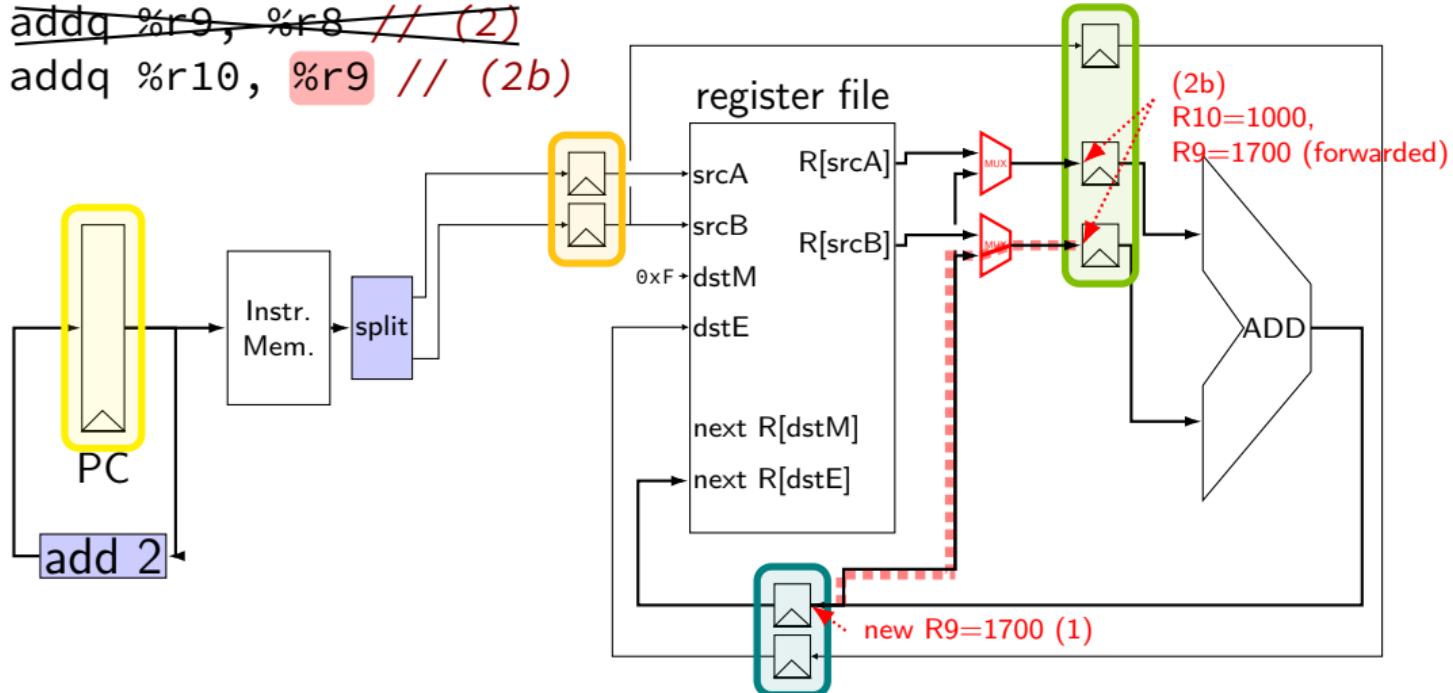
forwarding

addq %r8, %r9 // (1)
addq %r9, %r8 // (2)



forwarding

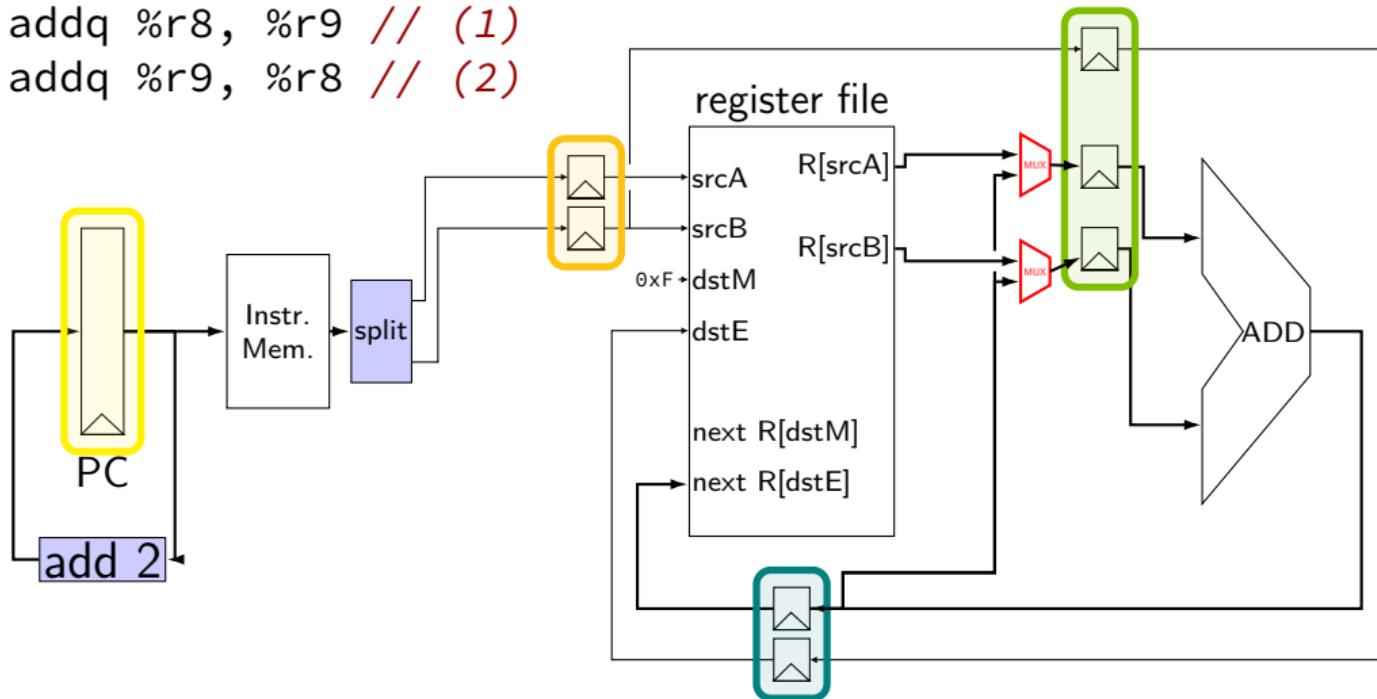
addq %r8, %r9 // (1)
~~addq %r9, %r8 // (2)~~
addq %r10, %r9 // (2b)



forwarding: MUX conditions

addq %r8, %r9 // (1)

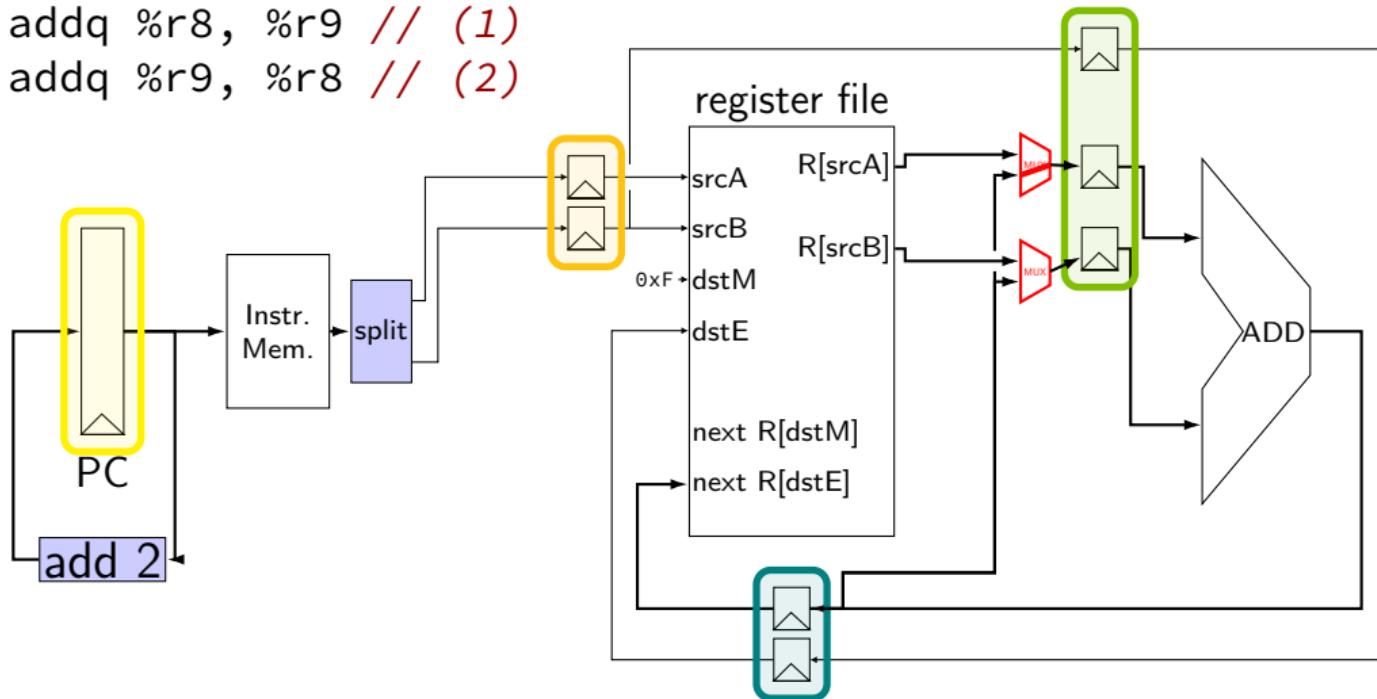
addq %r9, %r8 // (2)



forwarding: MUX conditions

addq %r8, %r9 // (1)

addq %r9, %r8 // (2)



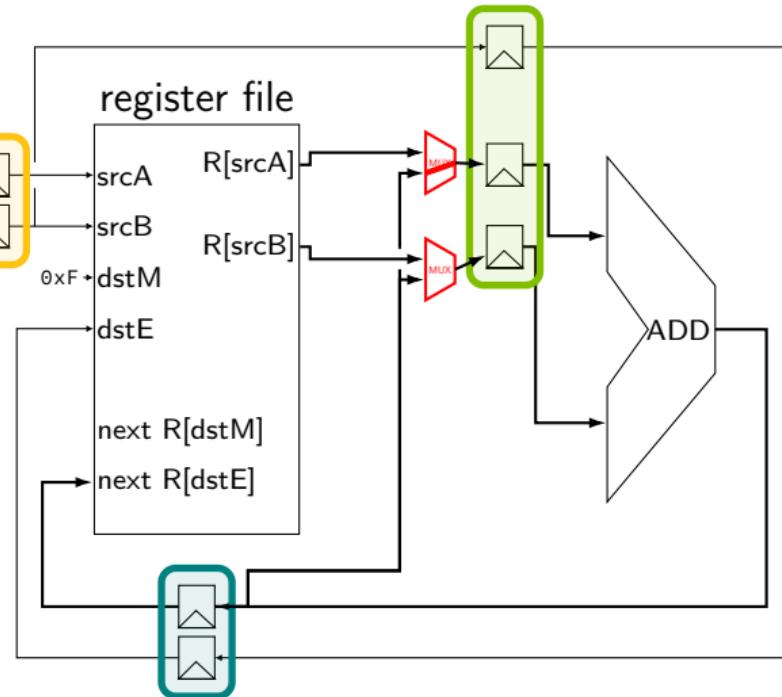
forwarding: MUX conditions

```
addq %r8, %r9 // (1)  
addq %r9, %r8 // (2)
```

```
d_valA = [  
    condition : e_valE;  
    1 : reg_outputA;  
];
```

What could **condition** be?

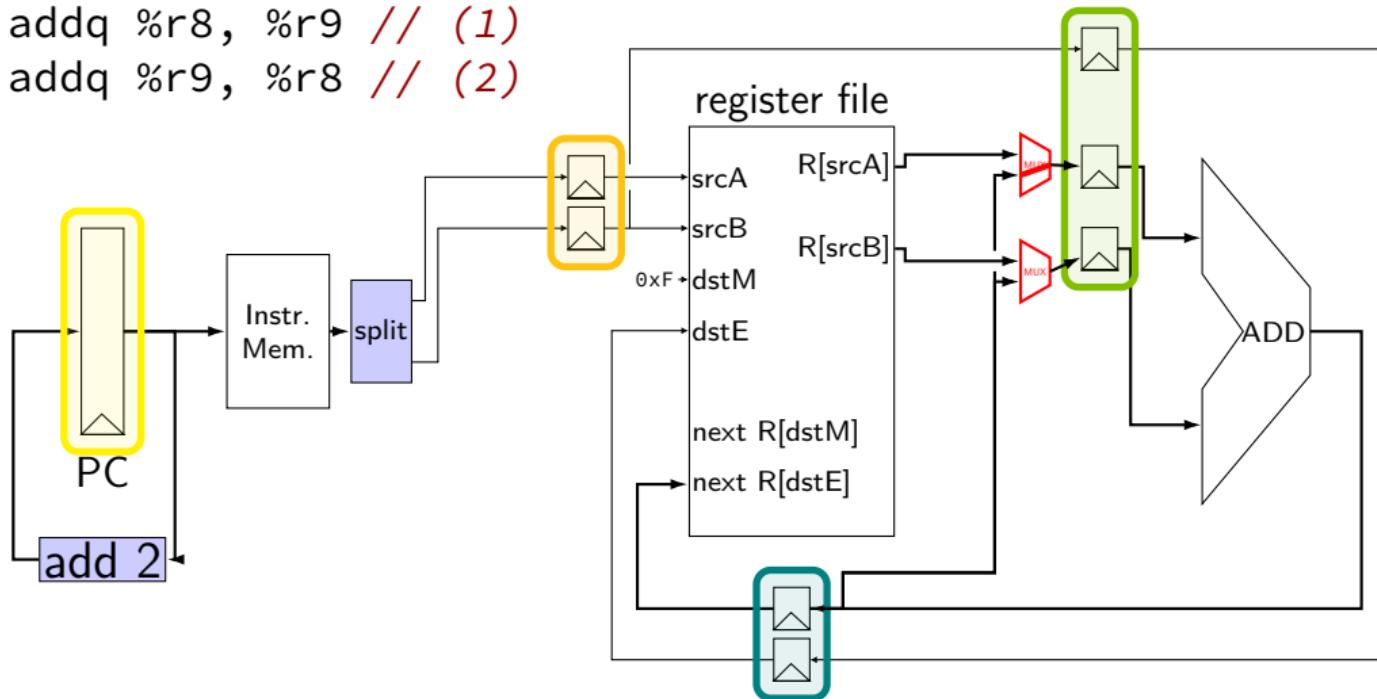
- a. $W_{rA} == \text{reg_srcA}$
- b. $W_{dstE} == \text{reg_srcA}$
- c. $e_{dstE} == \text{reg_srcA}$
- d. $d_{rB} == \text{reg_srcA}$
- e. something else



forwarding: MUX conditions

addq %r8, %r9 // (1)

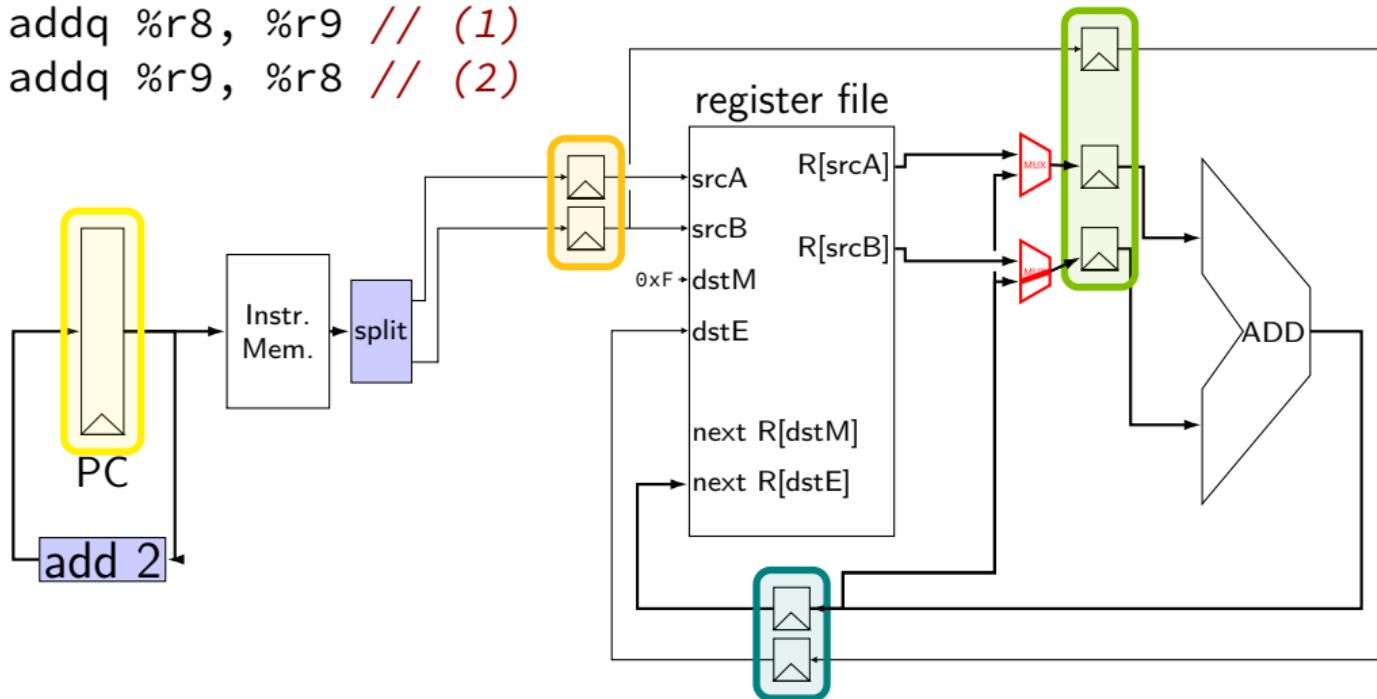
addq %r9, %r8 // (2)



forwarding: MUX conditions

addq %r8, %r9 // (1)

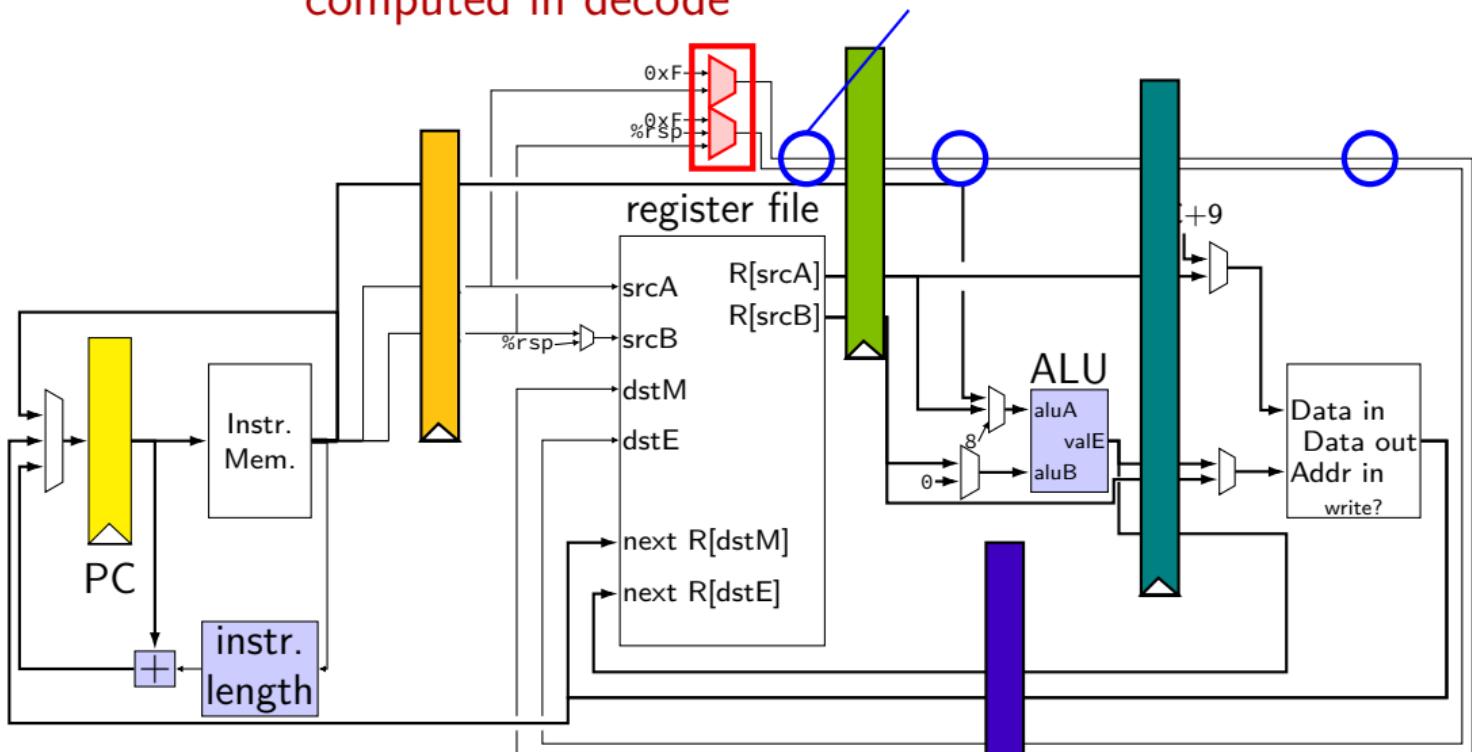
addq %r9, %r8 // (2)



computing destinations early

destination register
computed in decode

available early
for forwarding/etc. logic



textbook convention on destinations

dstE/dstM computed mostly in decode
passed through pipeline as d_dstE, e_dstE, ...

valE/valM only set to value to be stored in dstE/dstM
passed through pipeline as e_valE, m_valE, ...

simplifies forwarding/stalling logic

stalling versus forwarding (1)

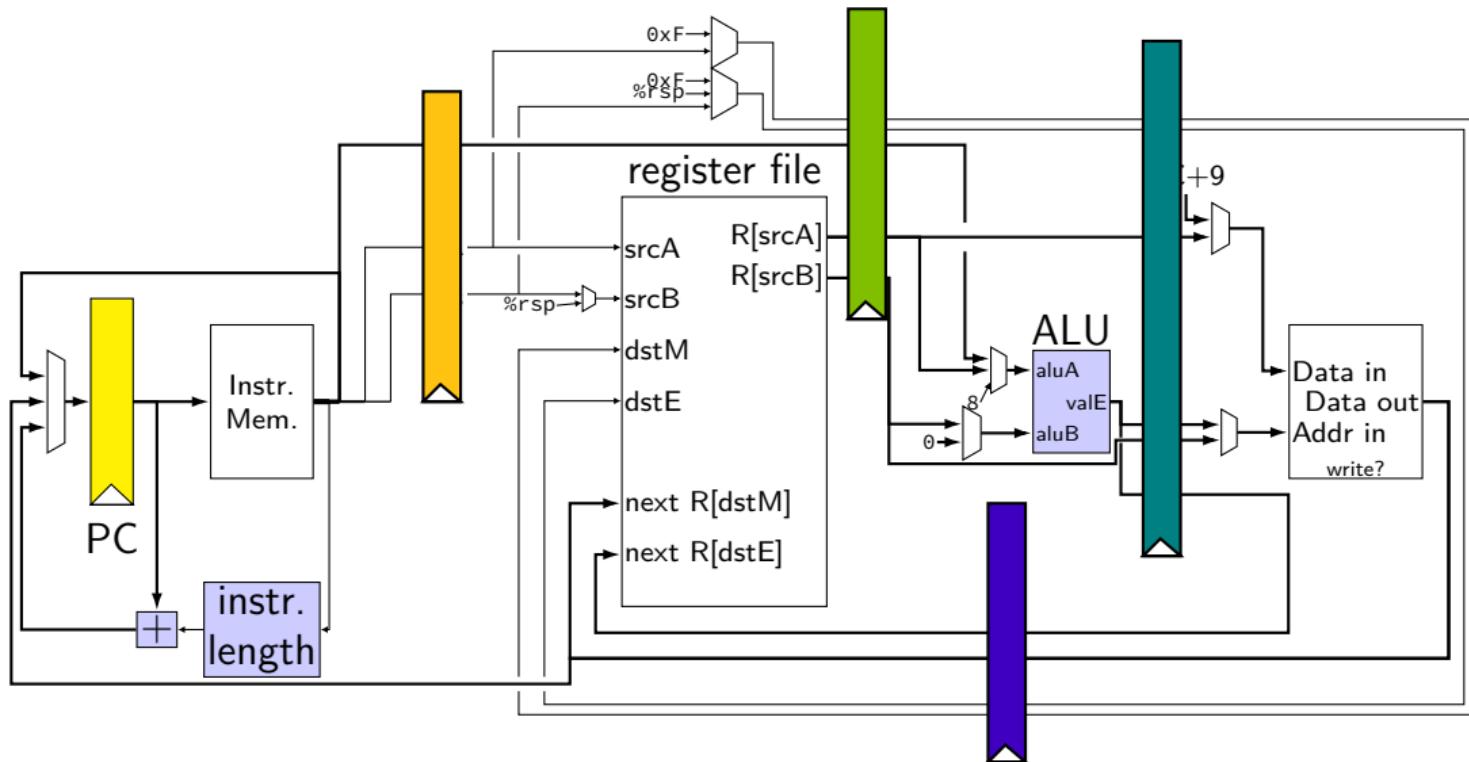
with stalling:

	cycle #	0	1	2	3	4	5	6	7	8
addq %r8, %r9		F	D	E	W					
addq %r9, %r8		X	X	F	D	E	W			

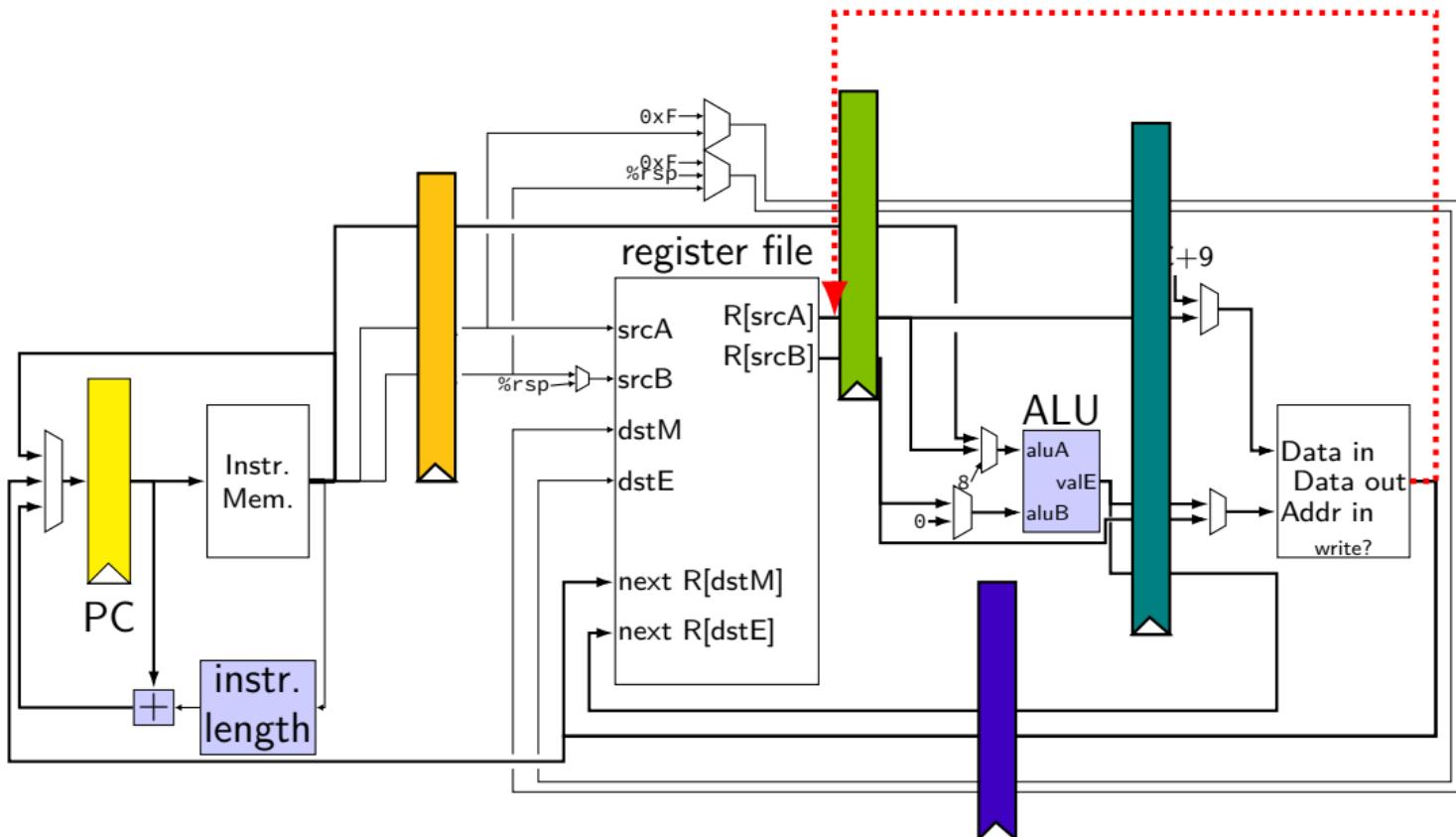
with forwarding:

	cycle #	0	1	2	3	4	5	6	7	8
addq %r8, %r9		F	D	E	W					
addq %r9, %r8		F	D	E	W					

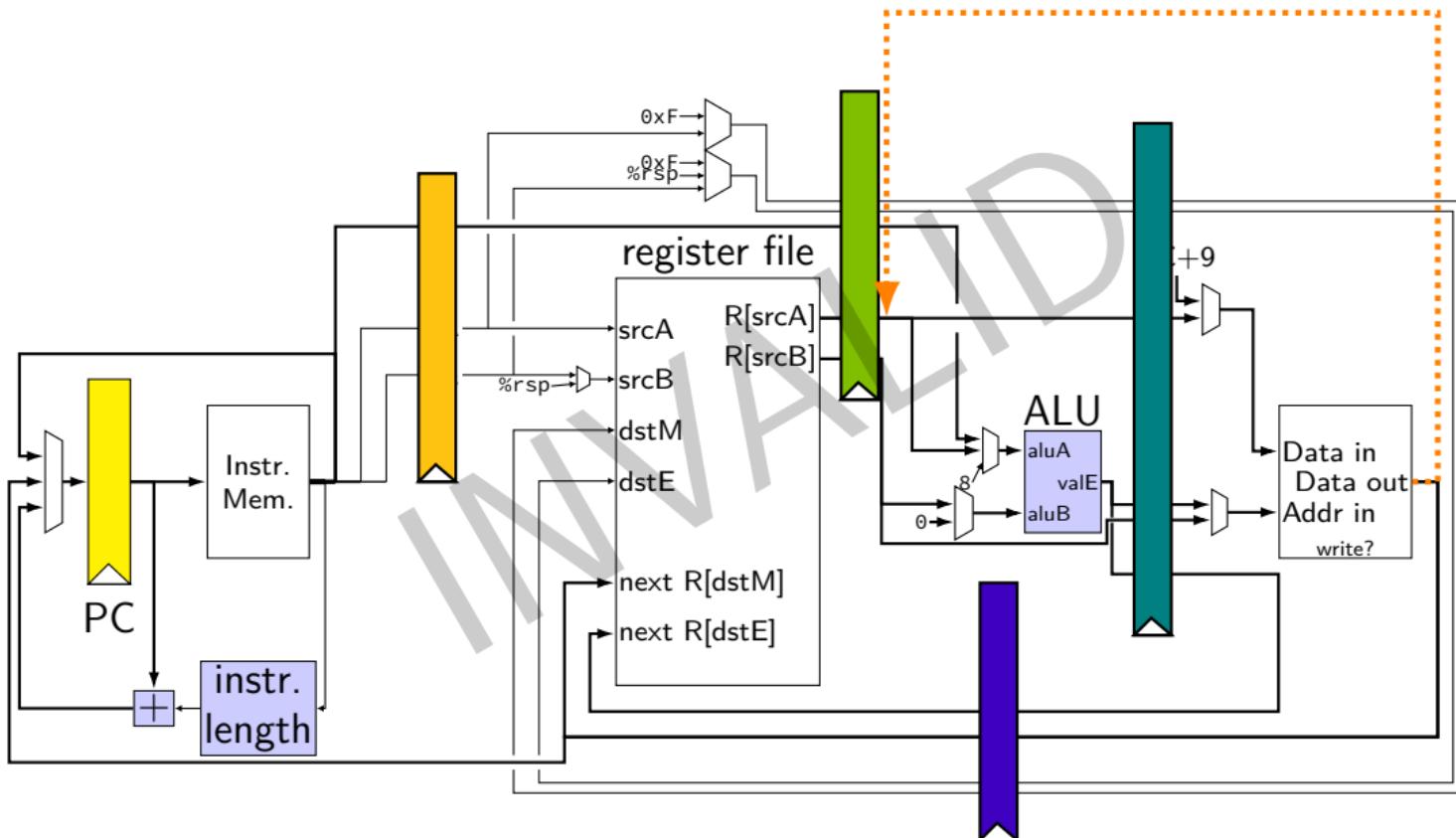
more possible forwarding



more possible forwarding

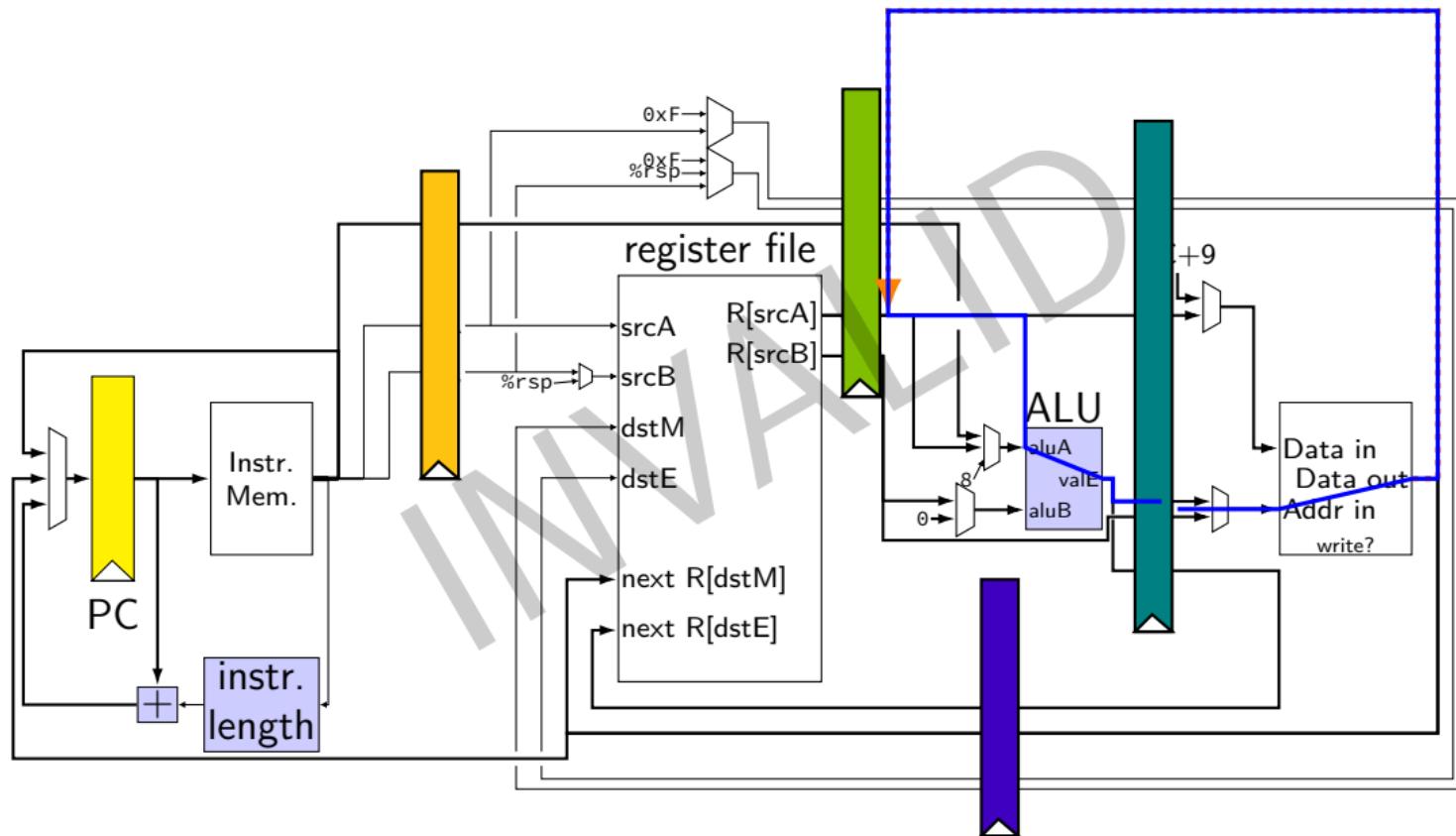


INVALID forwarding path



INVALID forwarding path

oops, extra long
critical path!

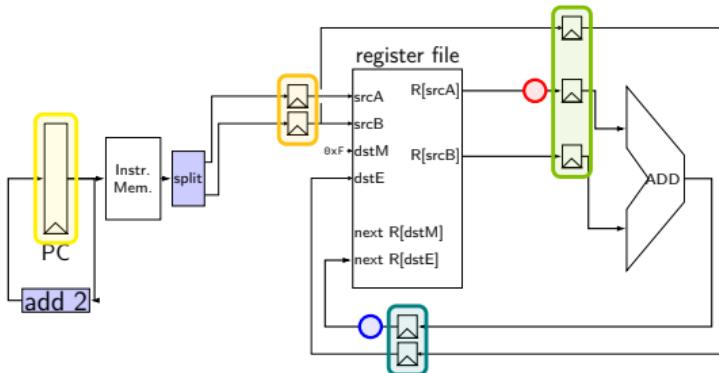


forwarding more?

```
// initially %rax = 0,  
//           %r8 = 800,  
//           %r9 = 900, etc.
```

```
addq %r8, %r9  
addq %rax, %rax  
addq %r9, %r10
```

location of values during cycle 3:

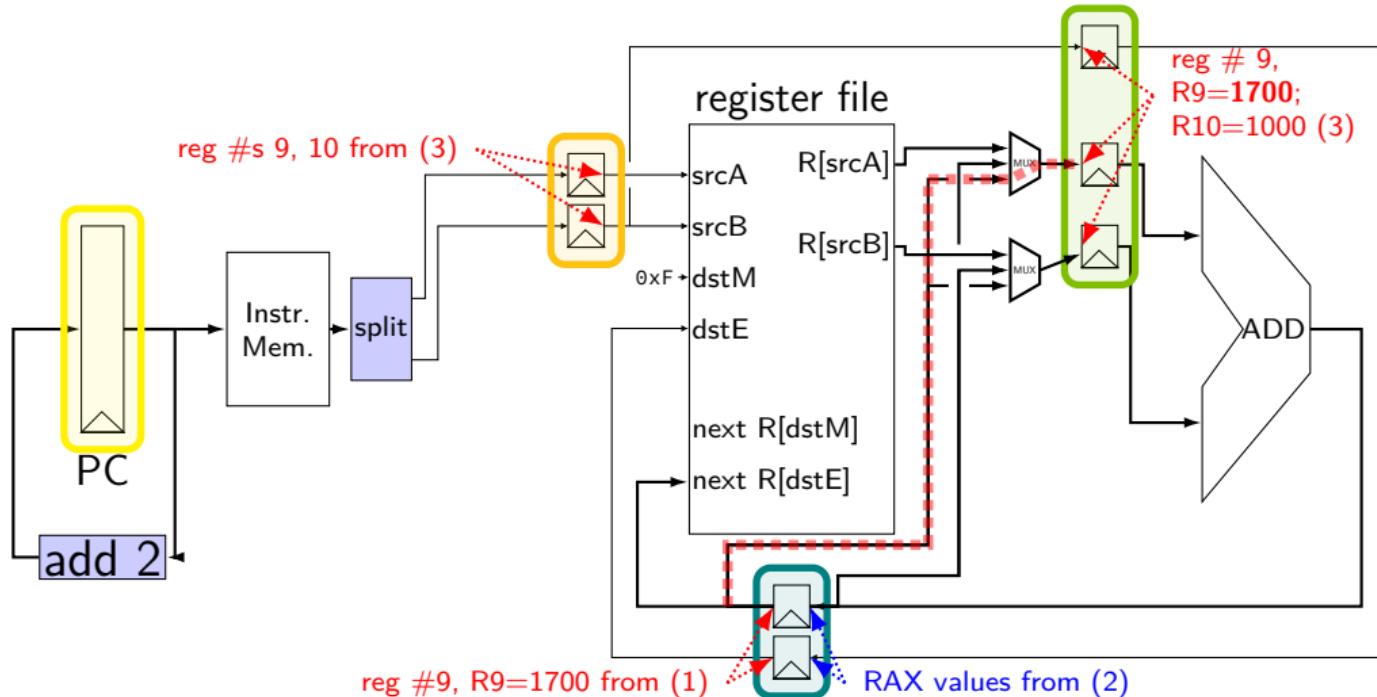


	fetch	fetch/decode		decode/execute			execute/writeback	
cycle	PC	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0							
1	0x2	8	9					
2	0x4	0	0	800	900	9		
3		9	10	0	0	0	1700	9
4				900	1000	10	0	0
5							1900	10

should be 1700

forwarding two stages?

```
addq %r8, %r9    // (1) R9 <- R8 (800) + R9 (900)  
addq %rax, %rax // (2)  
addq %r9, %r10   // (3) R10 <- R9 (1700) + R10 (1000)
```



some forwarding paths

	cycle #	0	1	2	3	4	5	6	7	8
<code>addq %r8, %r9</code>		F	D	E	M	W				
<code>subq %r9, %r11</code>			F	D	E	M	W			
<code>mrmovq 4(%r11), %r10</code>				F	D	E	M	W		
<code>rmmovq %r9, 8(%r11)</code>					F	D	E	M	W	
<code>xorq %r10, %r9</code>						F	D	E	M	W

some forwarding paths

	cycle #	0	1	2	3	4	5	6	7	8
addq %r8, %r9		F	D	E	M	W				
subq %r9, %r11		F	D	E	M	W				
mrmmovq 4(%r11), %r10		F	D	E	M	W				
rmmovq %r9, 8(%r11)		F	D	E	M	W				
xorq %r10, %r9		F	D	E	M	W				

some forwarding paths

	cycle #	0	1	2	3	4	5	6	7	8
addq %r8, %r9		F	D	E	M	W				
subq %r9, %r11		F	D	E	M	W				
mrmmovq 4(%r11), %r10		F	D	E	M	W				
rmmovq %r9, 8(%r11)		F	D	E	M	W				
xorq %r10, %r9		F	D	E	M	W				

some forwarding paths

	cycle #	0	1	2	3	4	5	6	7	8
addq %r8, %r9		F	D	E	M	W				
subq %r9, %r11		F	D	E	M	W				
mrmmovq 4(%r11), %r10		F	D	E	M	W				
rmmovq %r9, 8(%r11)		F	D	E	M	W				
xorq %r10, %r9		F	D	E	M	W				

some forwarding paths

	cycle #	0	1	2	3	4	5	6	7	8
addq %r8, %r9		F	D	E	M	W				
subq %r9, %r11			F	D	E	M	W			
mrmovq 4(%r11), %r10				F	D	E	M	W		
rmmovq %r9, 8(%r11)					F	D	E	M	W	
xorq %r10, %r9						F	D	E	M	W

some forwarding paths

	cycle #	0	1	2	3	4	5	6	7	8
addq %r8, %r9		F	D	E	M	W				
subq %r9, %r11			F	D	E	M	W			
mrmovq 4(%r11), %r10				F	D	E	M	W		
rmmovq %r9, 8(%r11)					F	D	E	M	W	
xorq %r10, %r9						F	D	E	M	W

some forwarding paths

	cycle #	0	1	2	3	4	5	6	7	8
addq %r8, %r9		F	D	E	M	W				
subq %r9, %r11			F	D	E	M	W			
mrmovq 4(%r11), %r10				F	D	E	M	W		
rmmovq %r9, 8(%r11)					F	D	E	M	W	
xorq %r10, %r9						F	D	E	M	W

some forwarding paths

	cycle #	0	1	2	3	4	5	6	7	8
addq %r8, %r9		F	D	E	M	W				
subq %r9, %r11		F	D	E	M	W				
mrmovq 4(%r11), %r10		F	D	E	M	W				
rmmovq %r9, 8(%r11)		F	D	E	M	W				
xorq %r10, %r9		F	D	E	M	W				

some forwarding paths

	cycle #	0	1	2	3	4	5	6	7	8
<code>addq %r8, %r9</code>		F	D	E	M	W				
<code>subq %r9, %r11</code>			F	D	E	M	W			
<code>mrmovq 4(%r11), %r10</code>				F	D	E	M	W		
<code>rmmovq %r9, 8(%r11)</code>					F	D	E	M	W	
<code>xorq %r10, %r9</code>						F	D	E	M	W

multiple forwarding paths (1)

	cycle #	0	1	2	3	4	5	6	7	8
addq %r10, %r8		F	D	E	M	W				
addq %r11, %r8			F	D	E	M	W			
addq %r12, %r8				F	D	E	M	W		

multiple forwarding paths (1)

	cycle #	0	1	2	3	4	5	6	7	8
addq %r10, %r8		F	D	E	M	W				
addq %r11, %r8			F	D	E	M	W			
addq %r12, %r8				F	D	E	M	W		

multiple forwarding HCL (1)

```
/* decode output: valA */
d_valA = [
    ...
    reg_srcA == e_dstE : e_valE;
        /* forward from end of execute */

    reg_srcA == m_dstE : m_valE;
        /* forward from end of memory */

    ...
    1 : reg_outputA;
];
```

multiple forwarding paths (2)

cycle #	0	1	2	3	4	5	6	7	8
addq %r10, %r8	F	D	E	M	W				
addq %r11, %r12		F	D	E	M	W			
addq %r12, %r8			F	D	E	M	W		

multiple forwarding paths (2)

	cycle #	0	1	2	3	4	5	6	7	8
addq %r10, %r8		F	D	E	M	W				
addq %r11, %r12			F	D	E	M	W			
addq %r12, %r8				F	D	E	M	W		

multiple forwarding paths (2)

cycle #	0	1	2	3	4	5	6	7	8
addq %r10, %r8	F	D	E	M	W				
addq %r11, %r12		F	D	E	M	W			
addq %r12, %r8			F	D	E	M	W		

multiple forwarding HCL (2)

```
d_valA = [  
    ...  
    reg_srcA == e_dstE : e_valE;  
    ...  
    1 : reg_outputA;  
];  
...  
d_valB = [  
    ...  
    reg_srcB == m_dstE : m_valE;  
    ...  
    1 : reg_outputB;  
];
```

exercise: forwarding paths

	cycle #	0	1	2	3	4	5	6	7	8
addq %r8, %r9		F	D	E	M	W				
subq %r8, %r10		F	D	E	M	W				
xorq %r8, %r9		F	D	E	M	W				
andq %r9, %r8		F	D	E	M	W				

in subq, %r8 is _____ addq.

in xorq, %r9 is _____ addq.

in andq, %r9 is _____ addq.

in andq, %r9 is _____ xorq.

A: not forwarded from

B-D: forwarded to decode from {execute, memory, writeback} stage of

unsolved problem

cycle #	0	1	2	3	4	5	6	7	8
mrmovq 0(%rax), %rbx	F	D	E	M	W				
subq %rbx, %rcx		F	D	E	M	W			

combine stalling and forwarding to resolve hazard

assumption in diagram: hazard detected in subq's decode stage
(since easier than detecting it in fetch stage)

typically what you'll implement

intuition: try to forward, but detect that it won't work

unsolved problem

	cycle #	0	1	2	3	4	5	6	7	8
<code>mrmovq %rax, %rbx</code>		F	D	E	M	W				
<code>subq %rbx, %rcx</code>			F	D	E	M	W			
<code>subq %rbx, %rcx</code>		F	D	D	E	M	W			

stall

The diagram illustrates a pipeline hazard between two `subq` instructions. The first `subq` instruction is fetched in cycle 0, decodes in cycle 1, and executes in cycle 4. The second `subq` instruction is fetched in cycle 2, decodes in cycle 3, and executes in cycle 5. A dependency arrow points from the first `subq`'s execute stage (cycle 4) to the second `subq`'s decode stage (cycle 3). A red box highlights the stall at cycle 4, where the second `subq`'s execution is delayed due to the hazard.

combine stalling and forwarding to resolve hazard

assumption in diagram: hazard detected in `subq`'s decode stage
(since easier than detecting it in fetch stage)

typically what you'll implement

intuition: try to forward, but detect that it won't work

solveable problem

cycle #	0	1	2	3	4	5	6	7	8
<code>mrmovq 0(%rax), %rbx</code>	F	D	E	M	W				
<code>rmmovq %rbx, 0(%rcx)</code>		F	D	E	M	W			

common for real processors to do this
but our textbook only forwards to the end of decode

aside: forwarding timings

forwarding: adds MUXes for forwarding to critical path
might slightly increase cycle time, considered acceptable

should not add much more to critical path:

example: can't use value read from memory in ALU in same cycle

pipeline with different hazards

example: 4-stage pipeline:

fetch/decode/execute+memory/writeback

		// 4 stage	// 5 stage
addq %rax, %r8	//		// W
subq %rax, %r9	//	W	// M
xorq %rax, %r10	//	EM	// E
andq %r8, %r11	//	D	// D

pipeline with different hazards

example: 4-stage pipeline:

fetch/decode/execute+memory/writeback

	// 4 stage	// 5 stage
addq %rax, %r8	//	// W
subq %rax, %r9	// W	// M
xorq %rax, %r10	// EM	// E
andq %r8, %r11	// D	// D

addq/andq is hazard with 5-stage pipeline

addq/andq is **not** a hazard with 4-stage pipeline

exercise: different pipeline

split execute into two stages: F/D/E1/E2/M/W

result only available near end of second execute stage

where does forwarding, stalls occur?

	cycle #	0	1	2	3	4	5	6	7	8
(1) addq %rcx, %r9		F	D	E1	E2	M	W			
(2) addq %r9, %rbx										
(3) addq %rax, %r9										
(4) rmmovq %r9, (%rbx)										
(5) rrmovq %rcx, %r9										

exercise: different pipeline

split execute into two stages: F/D/E1/E2/M/W

	<i>cycle #</i>	0	1	2	3	4	5	6	7	8
<code>addq %rcx, %r9</code>		F	D	E1	E2	M	W			
<code>addq %r9, %rbx</code>										
<code>addq %rax, %r9</code>										
<code>rmmovq %r9, (%rbx)</code>										

exercise: different pipeline

split execute into two stages: F/D/E1/E2/M/W

	cycle #	0	1	2	3	4	5	6	7	8
addq %rcx, %r9		F	D	E1	E2	M	W			
addq %r9, %rbx		F	D	E1	E2	M	W			
addq %rax, %r9										
rmmovq %r9, (%rbx)						F	D	E1	E2	M

r9 not available yet — can't forward here
so try stalling in addq's decode...

exercise: different pipeline

split execute into two stages: F/D/E1/E2/M/W

	cycle #	0	1	2	3	4	5	6	7	8
addq %rcx, %r9		F	D	E1	E2	M	W			
addq %r9, %rbx			F	D	E1	E2	M	W		
addq %r9, %rbx			F	D	D	E1	E2	M	W	
addq %rax, %r9										
addq %rax, %r9					F	F	D	E1	E2	M
rmmovq %r9, (%rbx)						F	D	E1	E2	M
rmmovq %r9, (%rbx)							F	D	E1	E2

after stalling once, now we can forward

exercise: different pipeline

split execute into two stages: F/D/E1/E2/M/W

	cycle #	0	1	2	3	4	5	6	7	8
addq %rcx, %r9		F	D	E1	E2	M	W			
addq %r9, %rbx			F	D	E1	E2	M	W		
addq %r9, %rbx		F	D	D	E1	E2	M	W		
addq %rax, %r9			F	D	E1	E2	M	W		
addq %rax, %r9		F	F	D	E1	E2	M	W		
rmmovq %r9, (%rbx)			F	D	E1	E2	M	W		
rmmovq %r9, (%rbx)			F	D	E1	E2	M	W		

exercise: different pipeline

split execute into two stages: F/D/E1/E2/M/W

	cycle #	0	1	2	3	4	5	6	7	8
addq %rcx, %r9		F	D	E1	E2	M	W			
addq %r9, %rbx			F	D	E1	E2	M	W		
addq %r9, %rbx			F	D	D	E1	E2	M	W	
addq %rax, %r9				F	D	E1	E2	M	W	
addq %rax, %r9				F	F	D	E1	E2	M	W
rmmovq %r9, (%rbx)					F	D	E1	E2	M	W
rmmovq %r9, (%rbx)					F	D	E1	E2	M	W
rrmovq %rcx, %r9					F	D	E1	E2	M	W

control hazard

```
subq %r8, %r9  
je    0xFFFF  
addq %r10, %r11
```

	fetch	fetch→decode		decode→execute			execute→writeback		
cycle	PC	SF/ZF	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0	0/1							
1	0x2	0/1	8	9					
2	???	0/1	0xF	0xF	800	900	9		

control hazard

```
subq %r8, %r9  
je    0xFFFF  
addq %r10, %r11
```

	fetch	fetch→decode		decode→execute			execute→writeback		
cycle	PC	SF/ZF	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0	0/1							
1	0x2	0/1	8	9					
2	???	0/1	0xF	0xF	800	900	9		

0xFFFF if R[8] = R[9]; 0x12 otherwise

control hazard: stall

```
addq %r8, %r9  
// insert two nops  
je    0xFFFF  
addq %r10, %r11
```

cycle	fetch		fetch→decode		decode→execute			execute→writeback	
	PC	SF/ZF	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0	0/1							
1	0x2*	0/1	8	9					
2	0x2*	0/1	0xF	0xF	800	900	9		
3	0x2	0/0	0xF	0xF	---	---	0xF	1700	9
4	0x10	0/0	0xF	0xF	---	---	0xF	---	0xF
5			10	11	---	---	0xF	---	0xF
6					1000	1100	11	---	0xF

control hazard: stall

```
addq %r8, %r9  
// insert two nops  
je    0xFFFF  
addq %r10, %r11
```

cycle	PC	fetch	fetch→decode		decode→execute		execute→writeback		
		7/1	8	9	800	900	9	1700	9
0	0x0								
1	0x2*	0/1	8	9					
2	0x2*	0/1	0xF	0xF	800	900	9		
3	0x2	0/0	0xF	0xF	---	---	0xF	1700	9
4	0x10	0/0	0xF	0xF	---	---	0xF	---	0xF
5			10	11	---	---	0xF	---	0xF
6					1000	1100	11	---	0xF

control hazard: stall

```
addq %r8, %r9  
// insert two nops  
je    0xFFFF  
addq %r10, %r11
```

	fetch	fetch→decode		decode→execute			execute→writeback		
cycle	PC	SF/ZF	rA	rB	R[srcA]	R[srcB]	dstE	next R[dstE]	dstE
0	0x0	0/1							
1	0x2*				execute je instruction (use SF/ZF)				
2	0x2*	0/1	0xF	0xF	0x00	0x00	9		
3	0x2	0/0	0xF	0xF	---	---	0xF	1700	9
4	0x10	0/0	0xF	0xF	---	---	0xF	---	0xF
5			10	11	---	---	0xF	---	0xF
6					1000	1100	11	---	0xF

stalling costs

with only stalling:

- up to 3 extra cycles for data dependencies

- extra 3 cycles (total 4) for every ret

- extra 2 cycles (total 3) for conditional jmp

ex.: dependencies and hazards (2)

mrmovq 0(%rax) %rbx

addq %rbx %rcx

jne foo

foo: **addq** %rcx %rdx

mrmovq (%rdx) %rcx

where are dependencies?

which are hazards in our pipeline?

which are resolved with forwarding?

making guesses

```
subq    %rcx, %rax
jne     LABEL
xorq    %r10, %r11
xorq    %r12, %r13
...
LABEL: addq    %r8, %r9
       rmmovq %r10, 0(%r11)
```

speculate: **jne** will goto LABEL

right: 2 cycles faster!

wrong: forget before execute finishes

when do instructions change things?

... other than pipeline registers/PC:

stage	changes
fetch	(none)
decode	(none)
execute	condition codes
memory	memory writes
writeback	register writes/stat changes

when do instructions change things?

... other than pipeline registers/PC:

stage	changes
fetch	(none)
decode	(none)
execute	condition codes
memory	memory writes
writeback	register writes/stat changes

to “undo” instruction during fetch/decode:

forget everything in **pipeline registers**

jXX: speculating right

```
subq %r8, %r8  
jne LABEL  
...
```

LABEL: addq %r8, %r9
rmmovq %r10, 0(%r11)
irmovq \$1, %r11

time	fetch	decode	execute	memory	writeback
1	subq				
2	jne	subq			
3	addq [?]	jne	subq (set ZF)		
4	rmmovq [?]	addq [?]	jne (use ZF)	OPq	
5	irmovq	rmmovq	addq	jne (done)	OPq

jXX: speculating right

```
subq %r8, %r8  
jne LABEL  
...
```

LABEL: addq %r8, %r9
rmmovq %r10, 0(%r11)
irmovq \$1, %r11

time	fetch	decode	execute	memory	writeback
1	subq				
2	jne	subq			
3	addq [?]	jne	subq (set ZF)		
4	rmmovq [?]	addq [?]	j were waiting/nothing		
5	irmovq	rmmovq	addq	jne (done)	OPq

jXX: speculating wrong

```
subq %r8, %r8  
jne LABEL  
xorq %r10, %r11  
...
```

LABEL: addq %r8, %r9
rmmovq %r10, 0(%r11)

time	fetch	decode	execute	memory	writeback
1	subq				
2	jne	subq			
3	addq [?]	jne	subq (set ZF)		
4	rmmovq [?]	addq [?]	jne (use ZF)	OPq	
5	xorq	nothing	nothing	jne (done)	OPq

jXX: speculating wrong

```
subq %r8, %r8  
jne LABEL  
xorq %r10, %r11  
...
```

LABEL: addq %r8, %r9
rmmovq %r10, 0(%r11)

time	fetch	decode	execute	memory	writeback
1	subq				
2	jne	“squash” wrong guesses			
3	addq [?]	jne	subq (set ZF)		
4	rmmovq [?]	addq [?]	jne (use ZF)	OPq	
5	xorq	nothing	nothing	jne (done)	OPq

jXX: speculating wrong

```
subq %r8, %r8  
jne LABEL  
xorq %r10, %r11  
...
```

LABEL: addq %r8, %r9
rmmovq %r10, 0(%r11)

time	fetch	decode	execute	memory	writeback
1	subq				
2	jne	subq			
3	addq [?]	j	fetch correct next instruction		
4	rmmovq [?]				
5	xorq	nothing	nothing	jne (done)	OPq

performance

hypothetical instruction mix

kind	portion	cycles (predict)	cycles (stall)
not-taken jXX	3%	3	3
taken jXX	5%	1	3
ret	1%	4	4
others	91%	1*	1*

* — ignoring data hazards

performance

hypothetical instruction mix

kind	portion	cycles (predict)	cycles (stall)
not-taken jXX	3%	3	3
taken jXX	5%	1	3
ret	1%	4	4
others	91%	1*	1*

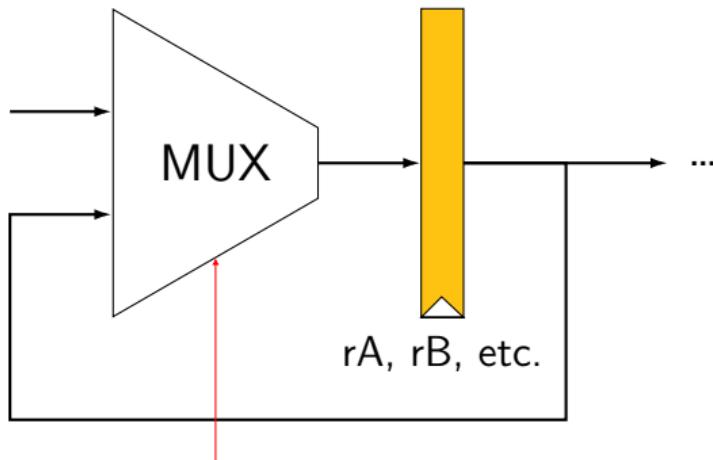
$$\text{predict: } 3 \times .03 + 1 \times .05 + 4 \times .01 + 1 \times .91 = \\ \textcolor{red}{1.09 \text{ cycles/instr.}}$$

$$\text{stall: } 3 \times .03 + 3 \times .05 + 4 \times .01 + 1 \times .91 = \\ \textcolor{red}{1.19 \text{ cycles/instr.}} \quad (1.19 \div \\ 1.09 \approx 1.09\times \text{faster})$$

* — ignoring data hazards

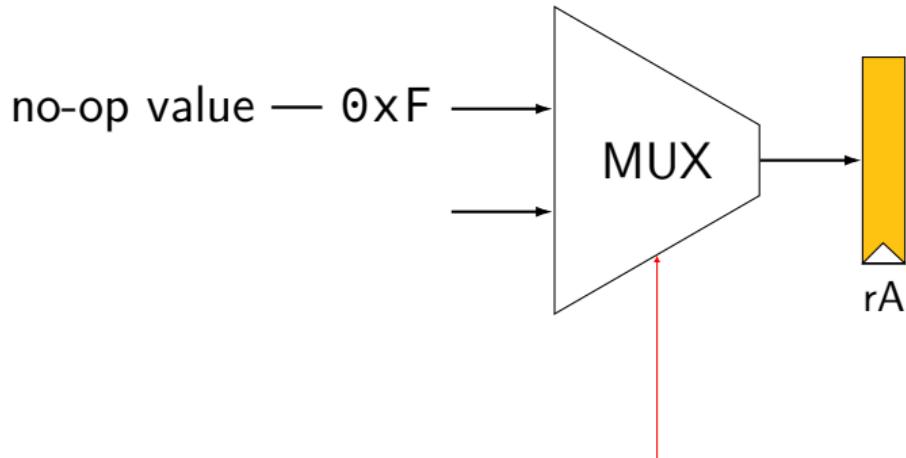
fetch/decode logic — advance or not

from instr. memory



should we stall?

fetch/decode logic — bubble or not



should we send
no-op value ("bubble")?

HCLRS signals

```
register aB {  
    ...  
}
```

HCLRS: every register bank has these MUXes built-in

stall_B: keep **old value** for all registers

register input \leftarrow register output

pipeline: keep same instruction in this stage next cycle

bubble_B: use **default value** for all registers

register input \leftarrow default value

pipeline: put no-operation in this stage next cycle

exercise

```
register aB {  
    value : 8 = 0xFF;  
}  
  
...
```

stall: keep old value
bubble: store default value

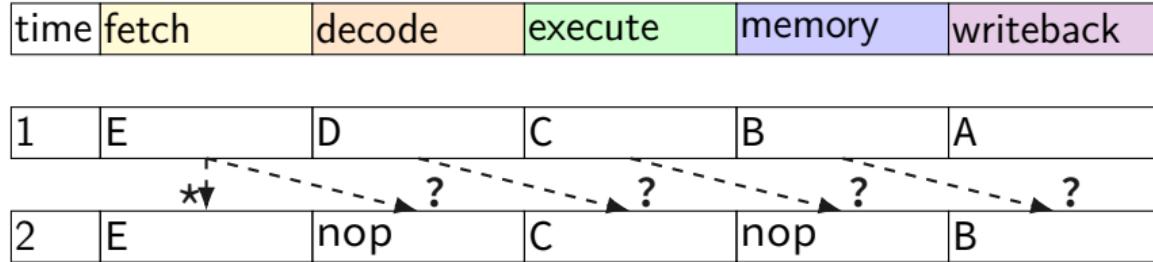
time	a_value	B_value	stall_B	bubble_B
0	0x01	0xFF	0	0
1	0x02	???	1	0
2	0x03	???	0	0
3	0x04	???	0	1
4	0x05	???	0	0
5	0x06	???	0	0
6	0x07	???	1	0
7	0x08	???	1	0
8		???		

exercise result

```
register aB {  
    value : 8 = 0xFF;  
}  
...
```

time	a_value	B_value	stall_B	bubble_B
0	0x01	0xFF	0	0
1	0x02	0x01	1	0
2	0x03	0x01	0	0
3	0x04	0x03	0	1
4	0x05	0xFF	0	0
5	0x06	0x05	0	0
6	0x07	0x06	1	0
7	0x08	0x06	1	0
8		0x06		

exercise: squash + stall (1)

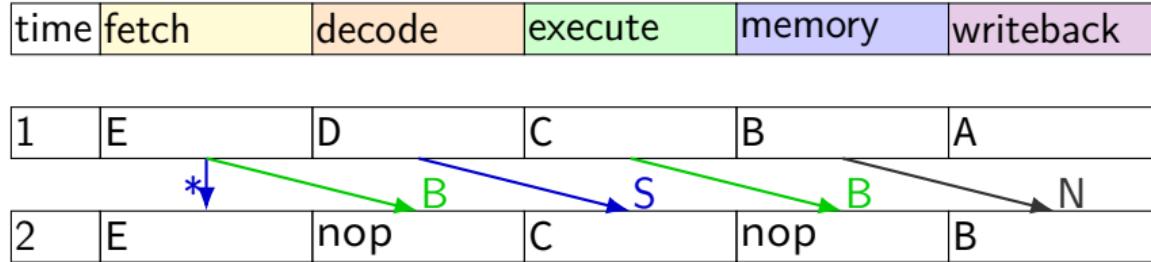


stall (S) = keep old value; normal (N) = use new value

bubble (B) = use default (no-op);

exercise: what are the ?s
write down your answers,
then compare with your neighbors

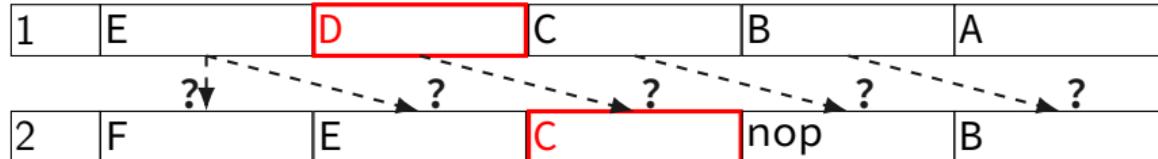
exercise: squash + stall (1)



stall (S) = keep old value; normal (N) = use new value
bubble (B) = use default (no-op);

exercise: squash + stall (2)

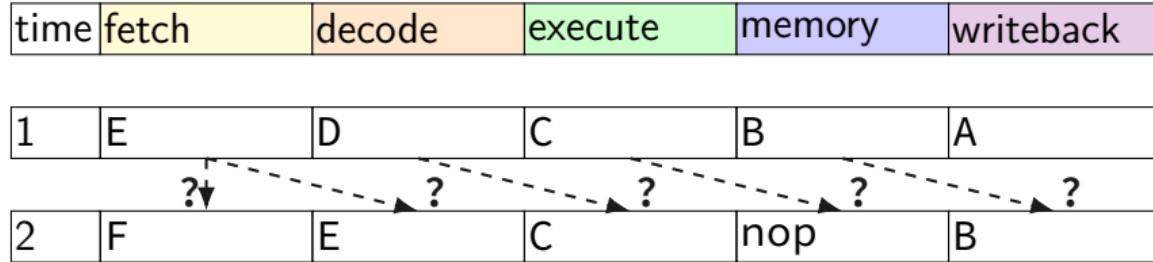
time	fetch	decode	execute	memory	writeback
------	-------	--------	---------	--------	-----------



stall (S) = keep old value; normal (N) = use new value

bubble (B) = use default (no-op);

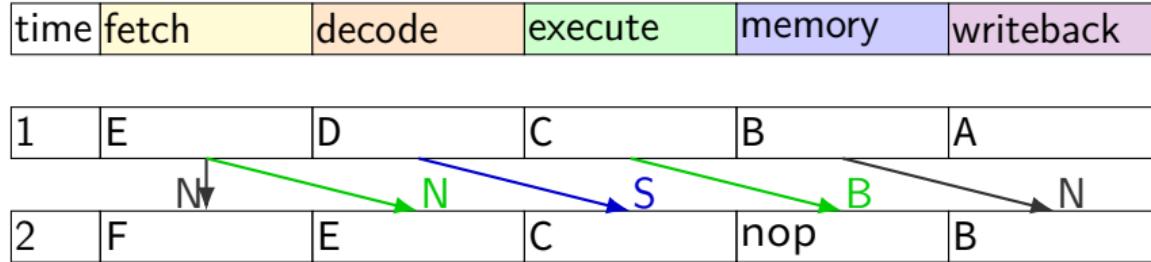
exercise: squash + stall (2)



stall (S) = keep old value; normal (N) = use new value
bubble (B) = use default (no-op);

exercise: what are the ?s
write down your answers,
then compare with your neighbors

exercise: squash + stall (2)



stall (S) = keep old value; normal (N) = use new value

bubble (B) = use default (no-op);

implementing stalling + prediction

need to handle updating PC:

- stalling: retry same PC

- prediction: use predicted PC

- misprediction: correct mispredicted PC

need to update pipeline registers:

- repeat stage in stall: keep same values

- don't go to next stage in stall: insert nop values

- ignore instructions from misprediction: insert nop values

stalling: bubbles + stall

	cycle #	0	1	2	3	4	5	6	7	8
<code>mrmovq 0(%rax), %rbx</code>		F	D	E	M	W				
<code>subq %rbx, %rcx</code>			F	D	D	E	M	W		
inserted nop					E	M	W			
<code>irmovq \$10, %rbx</code>				F	F	D	E	M	W	
...										

need way to keep pipeline register unchanged to repeat a stage
(and to replace instruction with a nop)

stalling: bubbles + stall

	cycle #	0	1	2	3	4	5	6	7	8
<code>mrmovq 0(%rax), %rbx</code>		F	D	E	M	W				
<code>subq %rbx, %rcx</code>			F	D	D	E	M	W		
inserted nop					E	M	W			
<code>irmovq \$10, %rbx</code>			F	F	D	E	M	W		
...										

keep same instruction in cycle 3

during cycle 2:

stall_D = 1

stall_F = 1 or extra f_pc MUX

need way to keep pipeline register unchanged to repeat a stage
(and to replace instruction with a nop)

stalling: bubbles + stall

	cycle #	0	1	2	3	4	5	6	7	8
<code>mrmovq 0(%rax), %rbx</code>		F	D	E	M	W				
<code>subq %rbx, %rcx</code>			F	D	D	E	M	W		
inserted nop					E	M	W			
<code>irmovq \$10, %rbx</code>			F	F	D	E	M	W		

...

insert nop in cycle 3
during cycle 2:
bubble_E = 1

need way to keep pipeline register unchanged to repeat a stage
(and to replace instruction with a nop)

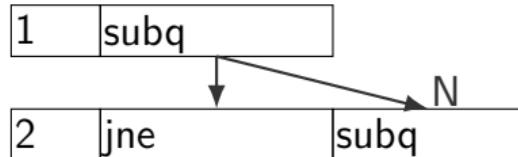
jump misprediction: bubbles

	cycle #	0	1	2	3	4	5	6	7	8
addq %r8, %r9		F	D	E	M	W				
jle target (not taken)		F	D	E	M	W				
target: xorq %rax, %rax (mispredicted)		F	D	—						
inserted nop				E	M	W				
andq %rbx, %rcx (mispredicted)		F	—							
inserted nop			D	E	M	W				
subq %r9, %r10 (instr. after jle)		F	D	E	M	W				

need option: replace instruction with nop (“bubble”)

squashing with stall/bubble

time	fetch	decode	execute	memory	writeback
------	-------	--------	---------	--------	-----------



3	addq [?]	jne	subq (set ZF)
---	----------	-----	---------------

4	rmmovq [?]	addq [?]	jne (use ZF)	subq
---	------------	----------	--------------	------

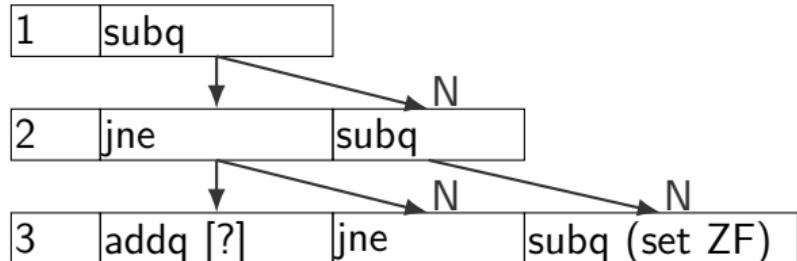
5	xorq	nothing	nothing	jne (done)	subq
---	------	---------	---------	------------	------

stall (S) = keep old value; normal (N) = use new value

bubble (B) = use default (no-op);

squashing with stall/bubble

time	fetch	decode	execute	memory	writeback
------	-------	--------	---------	--------	-----------



4	rmmovq [?]	addq [?]	jne (use ZF)	subq
---	------------	----------	--------------	------

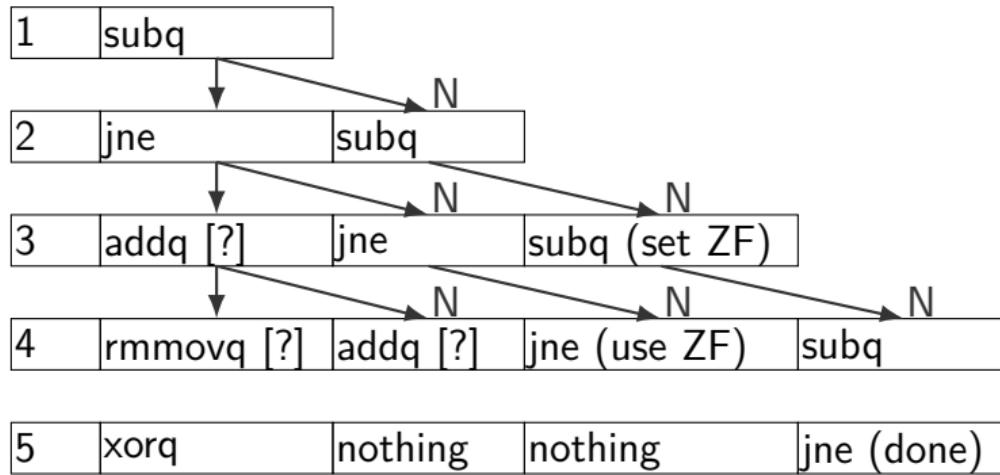
5	xorq	nothing	nothing	jne (done)	subq
---	------	---------	---------	------------	------

stall (S) = keep old value; normal (N) = use new value

bubble (B) = use default (no-op);

squashing with stall/bubble

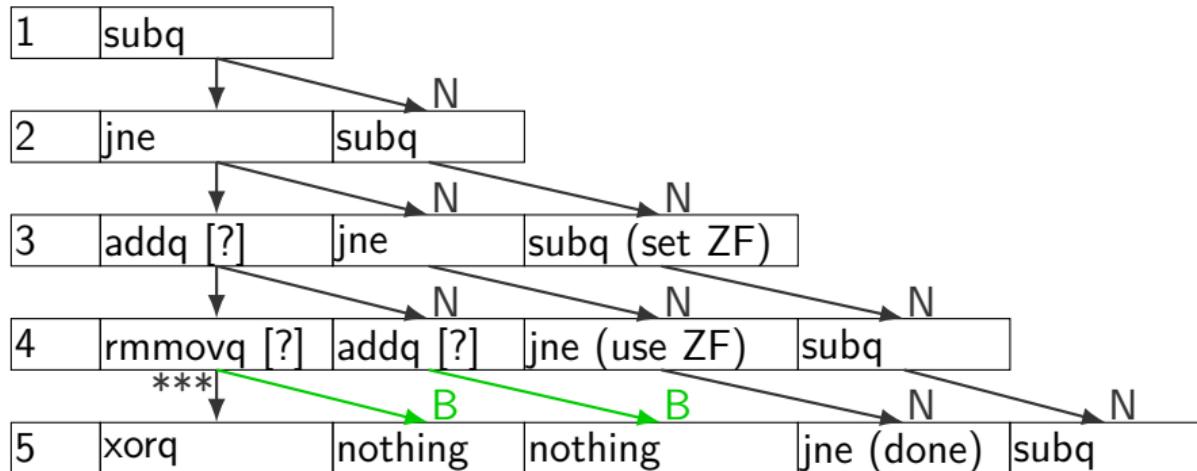
time	fetch	decode	execute	memory	writeback
------	-------	--------	---------	--------	-----------



stall (S) = keep old value; normal (N) = use new value
bubble (B) = use default (no-op);

squashing with stall/bubble

time	fetch	decode	execute	memory	writeback
------	-------	--------	---------	--------	-----------

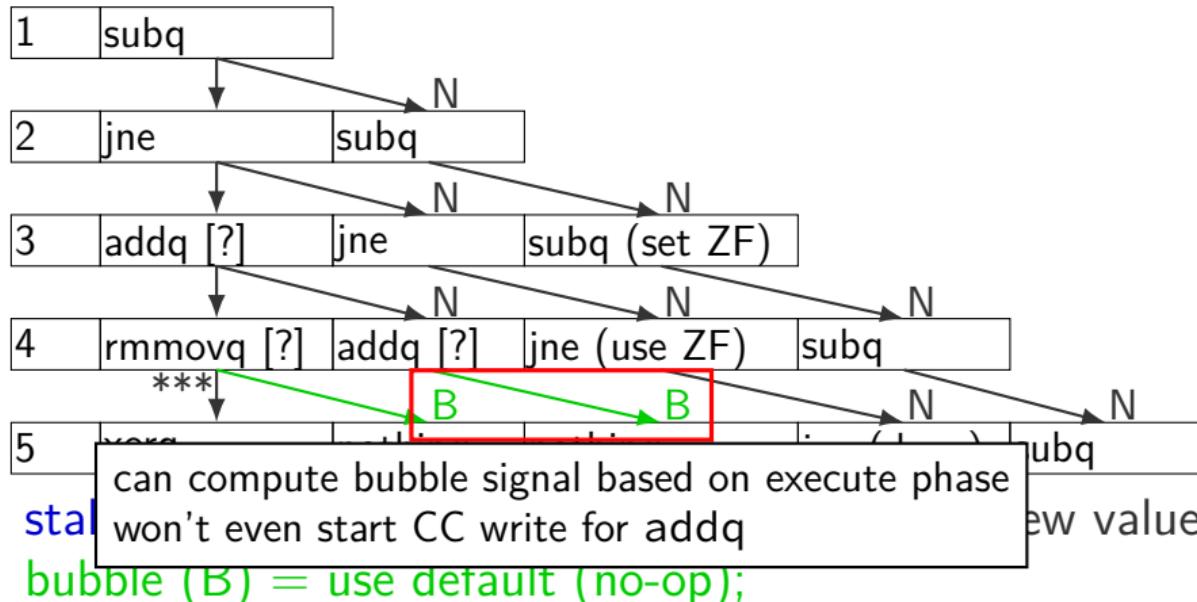


stall (S) = keep old value; normal (N) = use new value

bubble (B) = use default (no-op);

squashing with stall/bubble

time	fetch	decode	execute	memory	writeback
------	-------	--------	---------	--------	-----------



squashing HCLRS

```
just_detected_mispredict =
    e_icode == JXX && !e_branchTaken;
bubble_D = just_detected_mispredict || ...;
bubble_E = just_detected_mispredict || ...;
```

ret bubbles

addq %r8, %r9

ret

???

inserted nop

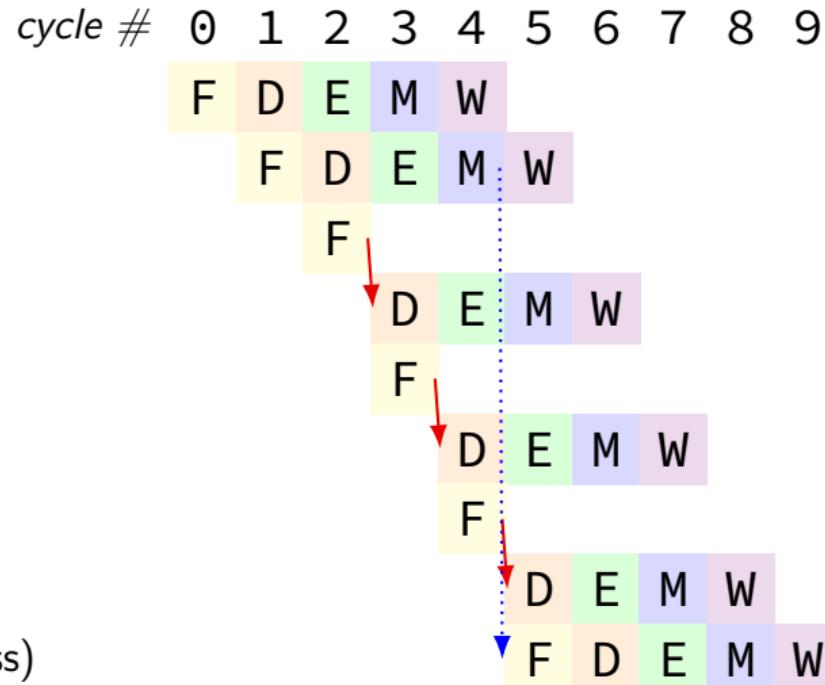
???

inserted nop

???

inserted nop

rrmovq %rax, %r8 (return address)



need option: replace instruction with nop ("bubble")

ret stall

time	fetch	decode	execute	memory	writeback
0	call				
1	ret	call			
2	wait for ret	ret	call		
3	wait for ret	nothing	ret	call (store)	
4	wait for ret	nothing	nothing	ret (load)	call
5	addq	nothing	nothing	nothing	ret

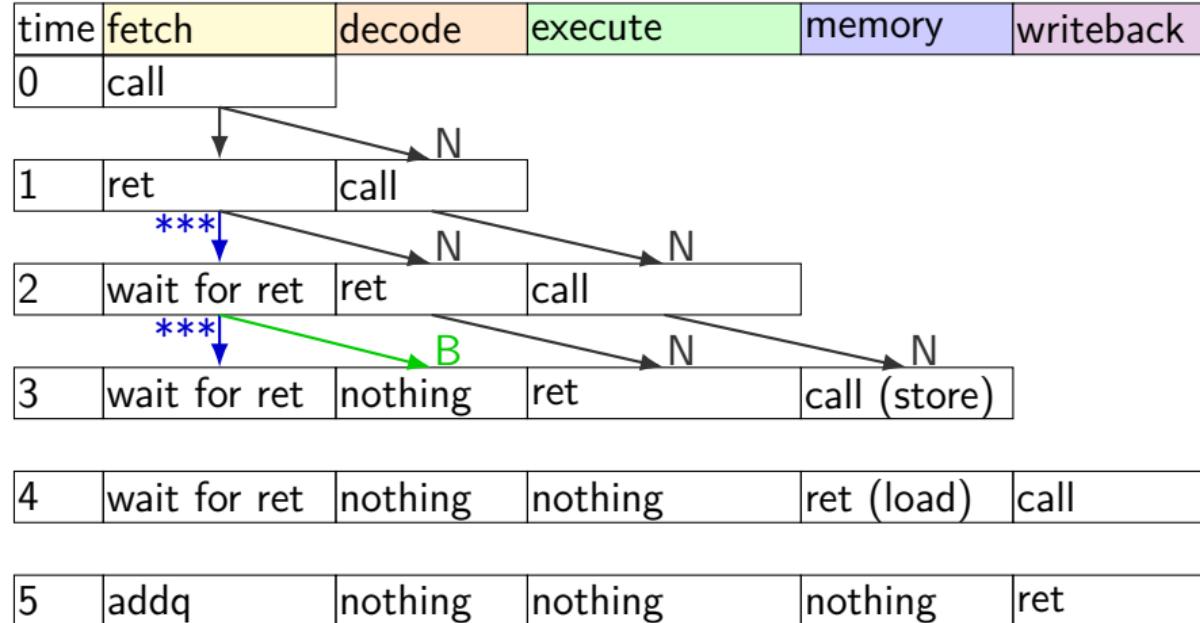
stall (S) = keep old value; normal (N) = use new value
bubble (B) = use default (no-op);

ret stall

time	fetch	decode	execute	memory	writeback
0	call				
1	ret	call			
2	wait for ret	ret	call		
3	wait for ret	nothing	ret	call (store)	
4	wait for ret	nothing	nothing	ret (load)	call
5	addq	nothing	nothing	nothing	ret

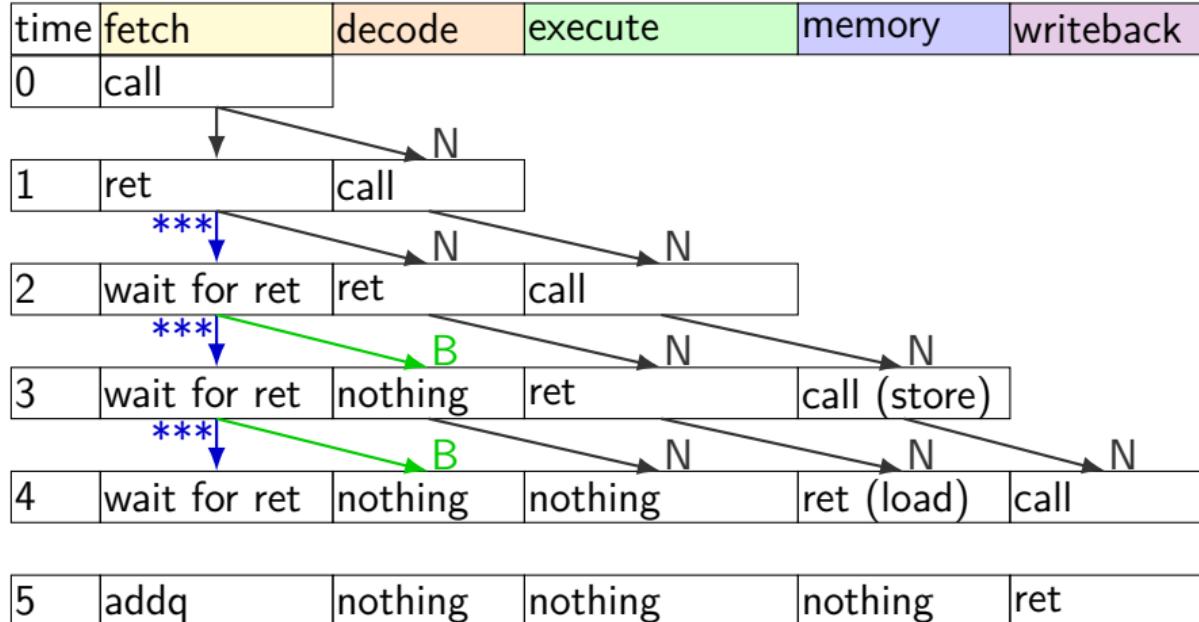
stall (S) = keep old value; normal (N) = use new value
bubble (B) = use default (no-op);

ret stall



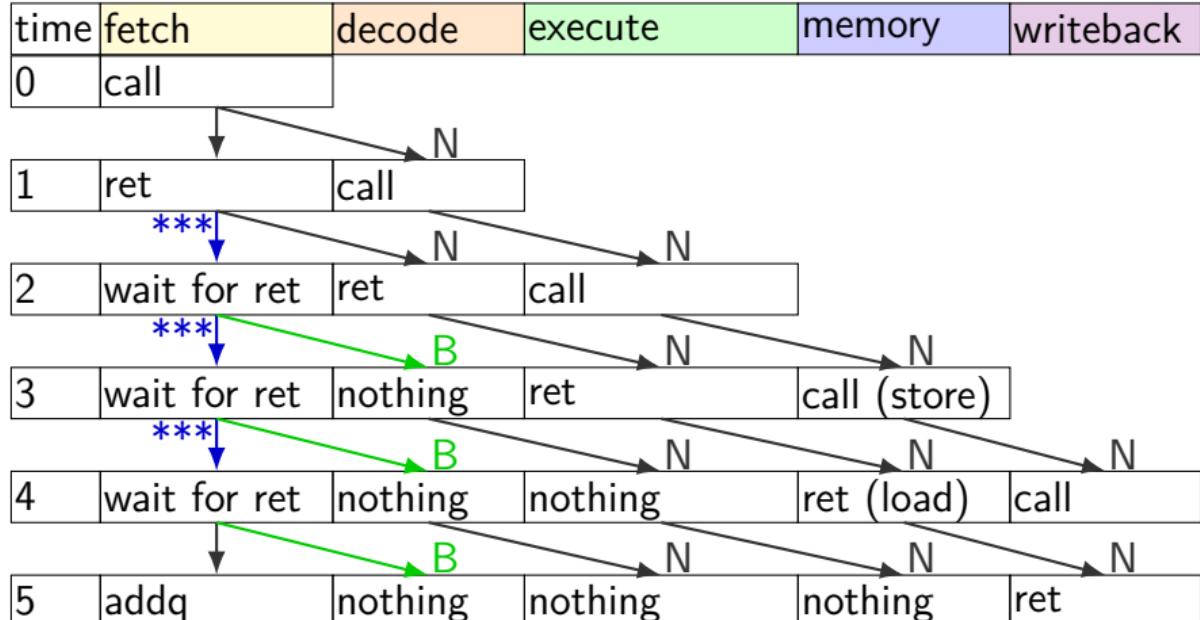
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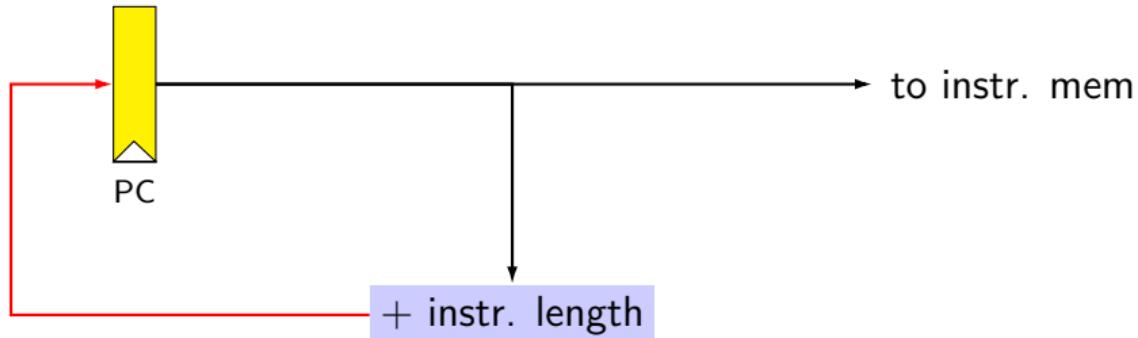
stall (S) = keep old value; normal (N) = use new value
bubble (B) = use default (no-op);

HCLRS bubble example

```
register fD {  
    icode : 4 = NOP;  
    rA : 4 = REG_NONE;  
    rB : 4 = REG_NONE;  
    ...  
};  
wire need_ret_bubble : 1;  
need_ret_bubble = ( D_icode == RET ||  
                    E_icode == RET ||  
                    M_icode == RET );  
  
bubble_D = ( need_ret_bubble ||  
             ... /* other cases */ );
```

building the PC update (one possibility)

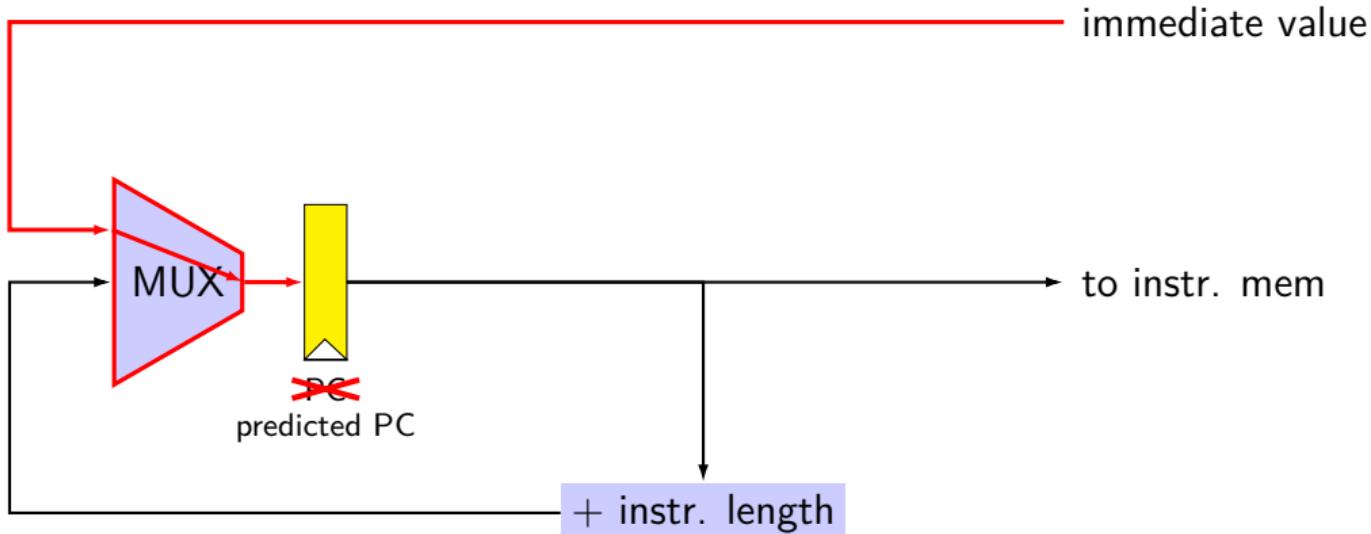
(1) normal case: $\text{PC} \leftarrow \text{PC} + \text{instr. len}$



building the PC update (one possibility)

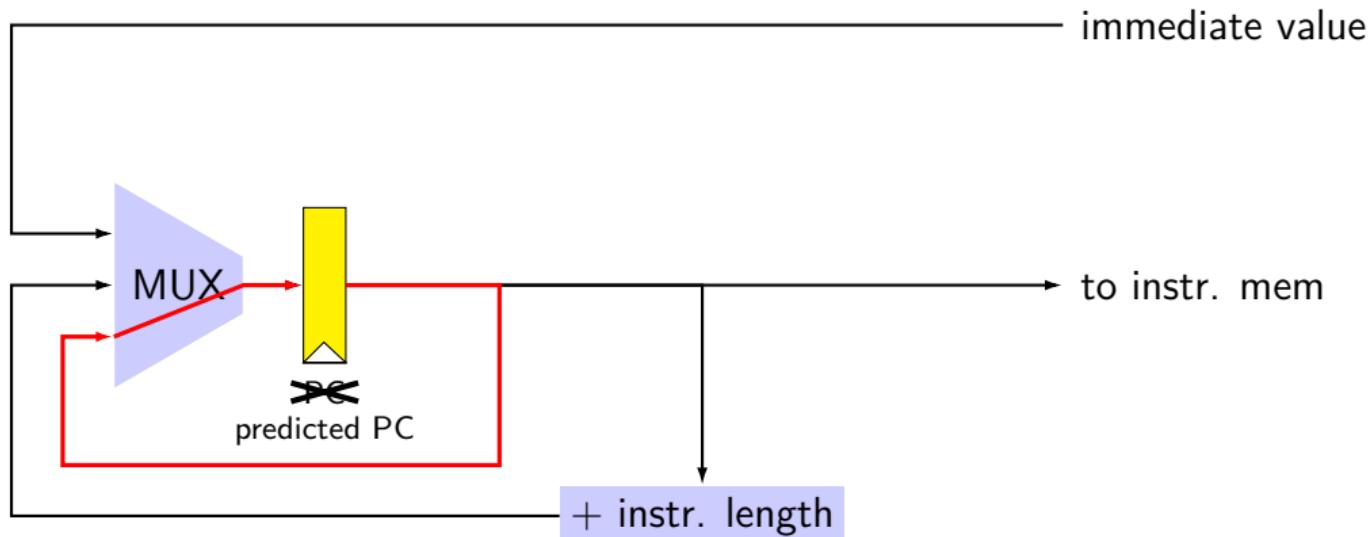
(1) normal case: $\text{PC} \leftarrow \text{PC} + \text{instr len}$

(2) immediate: call/jmp, and *prediction* for cond. jumps



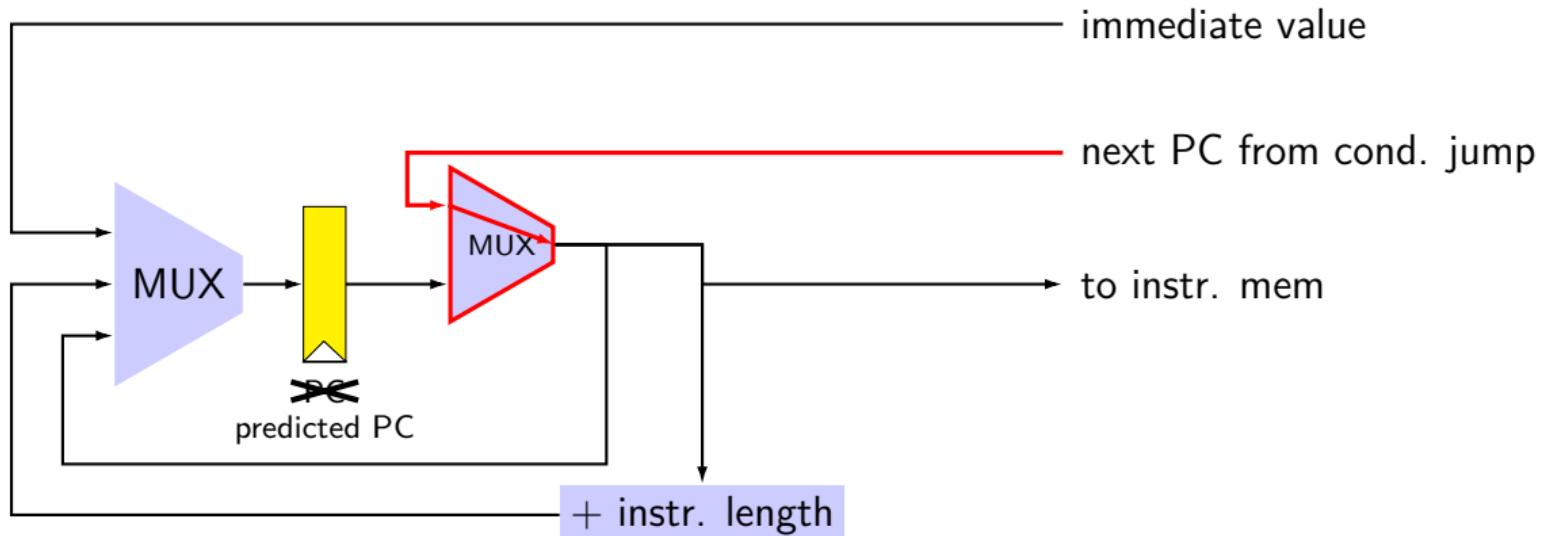
building the PC update (one possibility)

- (1) normal case: $\text{PC} \leftarrow \text{PC} + \text{instr len}$
- (2) immediate: call/jmp, and *prediction* for cond. jumps
- (3) repeat previous PC for stalls (load/use hazard, halt, ret?)



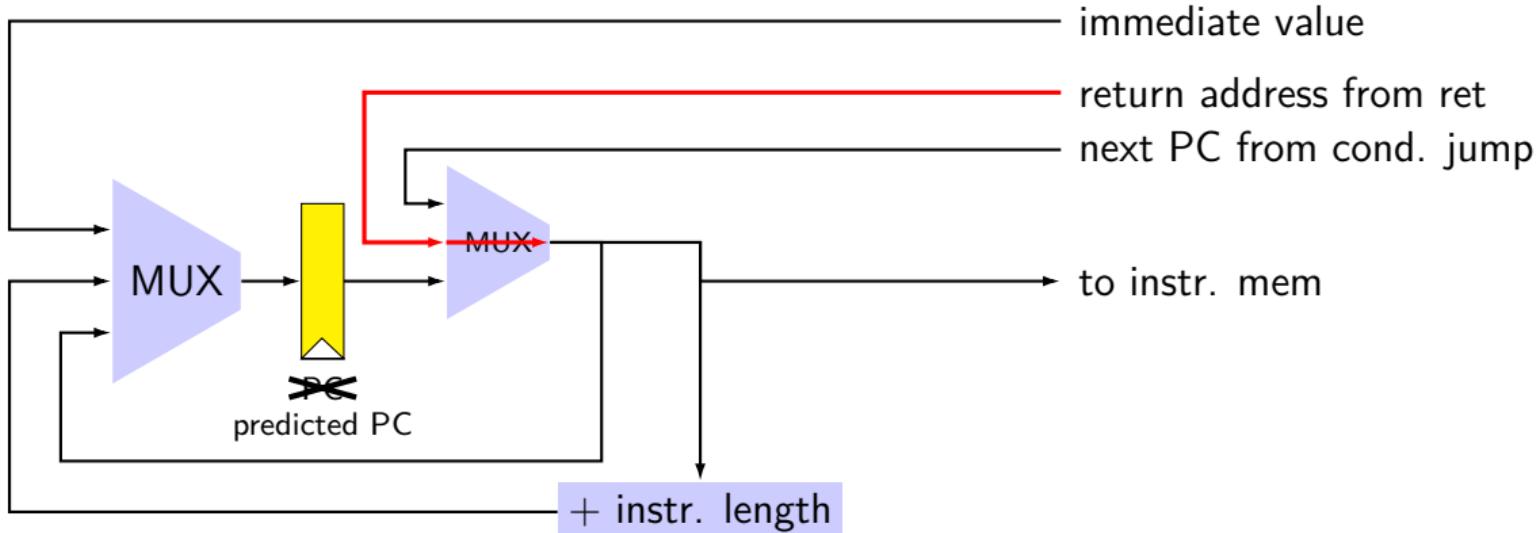
building the PC update (one possibility)

- (1) normal case: $\text{PC} \leftarrow \text{PC} + \text{instr len}$
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- (3) repeat previous PC for stalls (load/use hazard, halt, ret?)
- (4) correct for misprediction of conditional jump



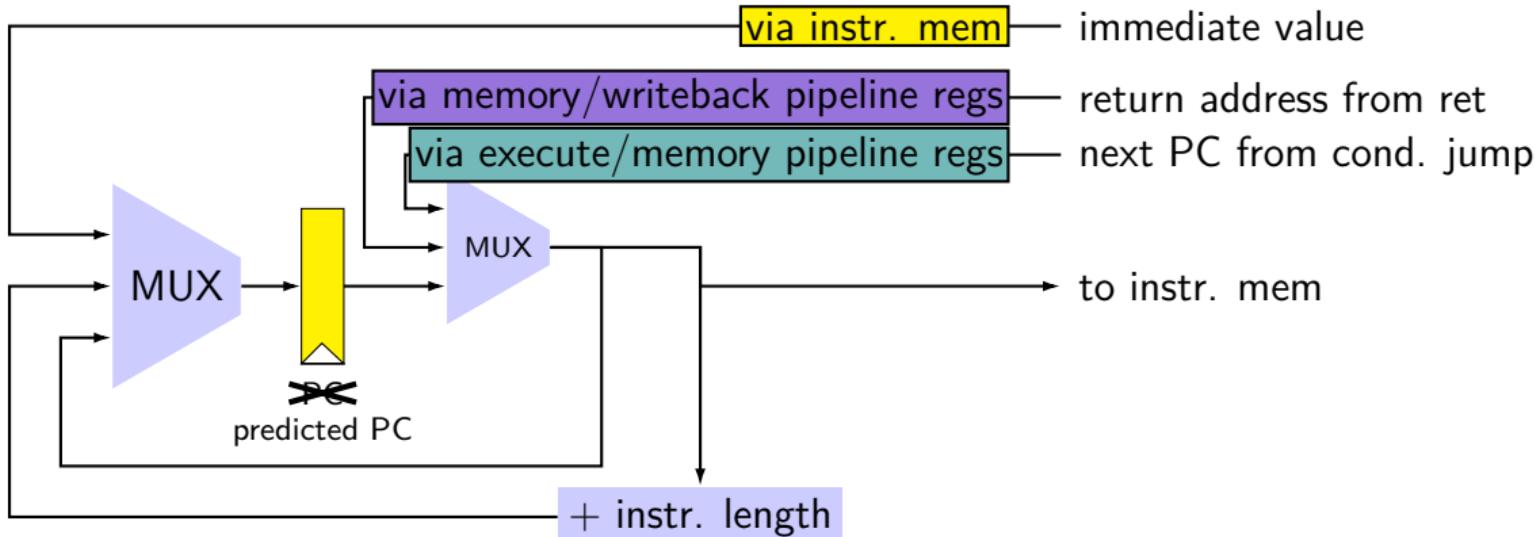
building the PC update (one possibility)

- (1) normal case: $\text{PC} \leftarrow \text{PC} + \text{instr. len}$
- (2) immediate: call/jmp, and *prediction* for cond. jumps
- (3) repeat previous PC for stalls (load/use hazard, halt, ret?)
- (4) correct for misprediction of conditional jump
- (5) correct for missing return address for ret



building the PC update (one possibility)

- (1) normal case: $PC \leftarrow PC + \text{instr len}$
- (2) immediate: call/jmp, and *prediction* for cond. jumps
- (3) repeat previous PC for stalls (load/use hazard, halt, ret?)
- (4) correct for misprediction of conditional jump
- (5) correct for missing return address for ret



PC update overview

predict based on instruction length + immediate

override prediction with stalling sometimes

correct when prediction is wrong just before fetching

retrieve corrections from pipeline register outputs for jCC/ret instruction

above is what textbook does

alternative: could instead correct prediction just before setting PC register

retrieve corrections into PC cycle before corrections used

moves logic from beginning-of-fetch to end-of-previous-fetch

I think this is more intuitive, but consistency with textbook is less confusing...

after forwarding/prediction

where do we still need to stall?

memory output needed in fetch

ret followed by anything

memory output needed in execute

mrmovq or popq + use
(in immediately following instruction)

overall CPU

5 stage pipeline

1 instruction completes **every cycle — except hazards**

most data hazards: solved by forwarding

load/use hazard: 1 cycle of stalling

jXX control hazard: branch prediction + squashing

2 cycle penalty for misprediction

(correct misprediction after jXX finishes execute)

ret control hazard: 3 cycles of stalling

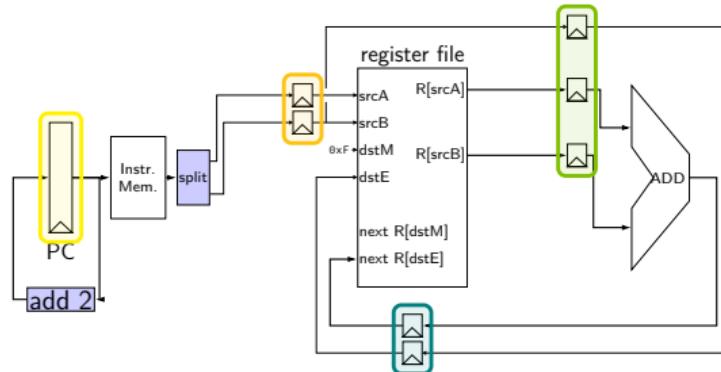
(fetch next instruction after ret finishes memory)

backup slides

addq processor performance

example delays:

path	time
add 2	80 ps
instruction memory	200 ps
register file read	125 ps
add	100 ps
register file write	125 ps



no pipelining: 1 instruction per 550 ps

add up everything but add 2 (**critical (slowest) path**)

pipelining: 1 instruction per 200 ps + pipeline register delays

slowest path through stage + pipeline register delays

latency: 800 ps + pipeline register delays (4 cycles)

stalling for conditional jmps

```
subq %r8, %r8  
je label
```

label: irmovq ...

time	fetch	decode	execute	memory	writeback
1	OPq				
2	jCC	OPq			
3	wait for jCC	jCC	OPq (set ZF)		
4	wait for jCC	nothing	jCC (use ZF)	OPq	
5	irmovq	nothing	nothing	jCC (done)	OPq

stalling for conditional jmps

```
subq %r8, %r8  
je label
```

label: irmovq ...

time	fetch	decode	execute	memory	writeback
1	OPq				
2	jCC	OPq			
3	wait for jCC	jCC	OPq (set ZF)		
4	wait for jCC	nothing	jCC (use ZF)	OPq	
5	irmovq	nothing	nothing	jCC (done)	OPq

stalling for conditional jmps

```
subq %r8, %r8  
je label
```

label: irmovq ...

time	fetch	decode	execute	memory	writeback
1	OPq				
2	jCC	OPq			
3	wait for jCC	jCC	OPq (set ZF)	ZF sent via register	
4	wait for jCC	nothing	jCC (use ZF)	OPq	
5	irmovq	nothing	nothing	jCC (done)	OPq

stalling for conditional jmps

```
subq %r8, %r8  
je label
```

label: irmovq ...

time	fetch	decode	execute	memory	writeback
1	OPq				
2	jCC	OPq			
3	wait for jCC	jCC	OPq (set ZF)		
4	wait for jCC	nothing	jCC (use ZF)	OPq	
5	irmovq	nothing	nothing	jCC (done)	OPq

"taken" sent from execute to fetch

stalling for ret

```
call empty  
addq %r8, %r9
```

empty: ret

time	fetch	decode	execute	memory	writeback
1	call				
2	ret	call			
3	wait for ret	ret	call		
4	wait for ret	nothing	ret	call (store)	
5	wait for ret	nothing	nothing	ret (load)	call
6	addq	nothing	nothing	nothing	ret

stalling for ret

```
call empty  
addq %r8, %r9
```

empty: ret

time	fetch	decode	execute	memory	writeback
1	call				
2	ret	call			
3	wait for ret	ret	call	return address stored here	
4	wait for ret	nothing	ret	call (store)	
5	wait for ret	nothing	nothing	ret (load)	call
6	addq	nothing	nothing	nothing	ret

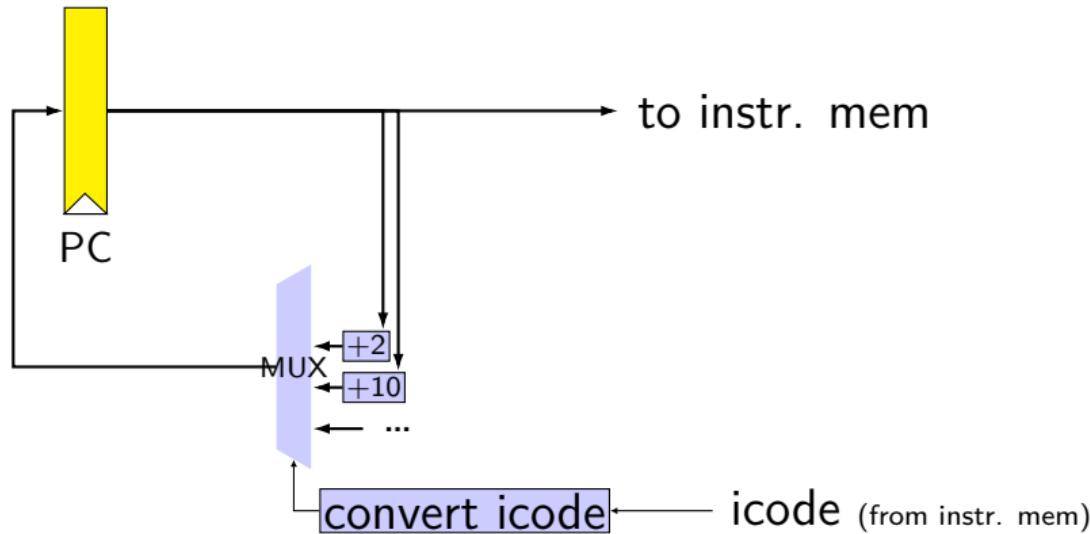
stalling for ret

```
call empty  
addq %r8, %r9
```

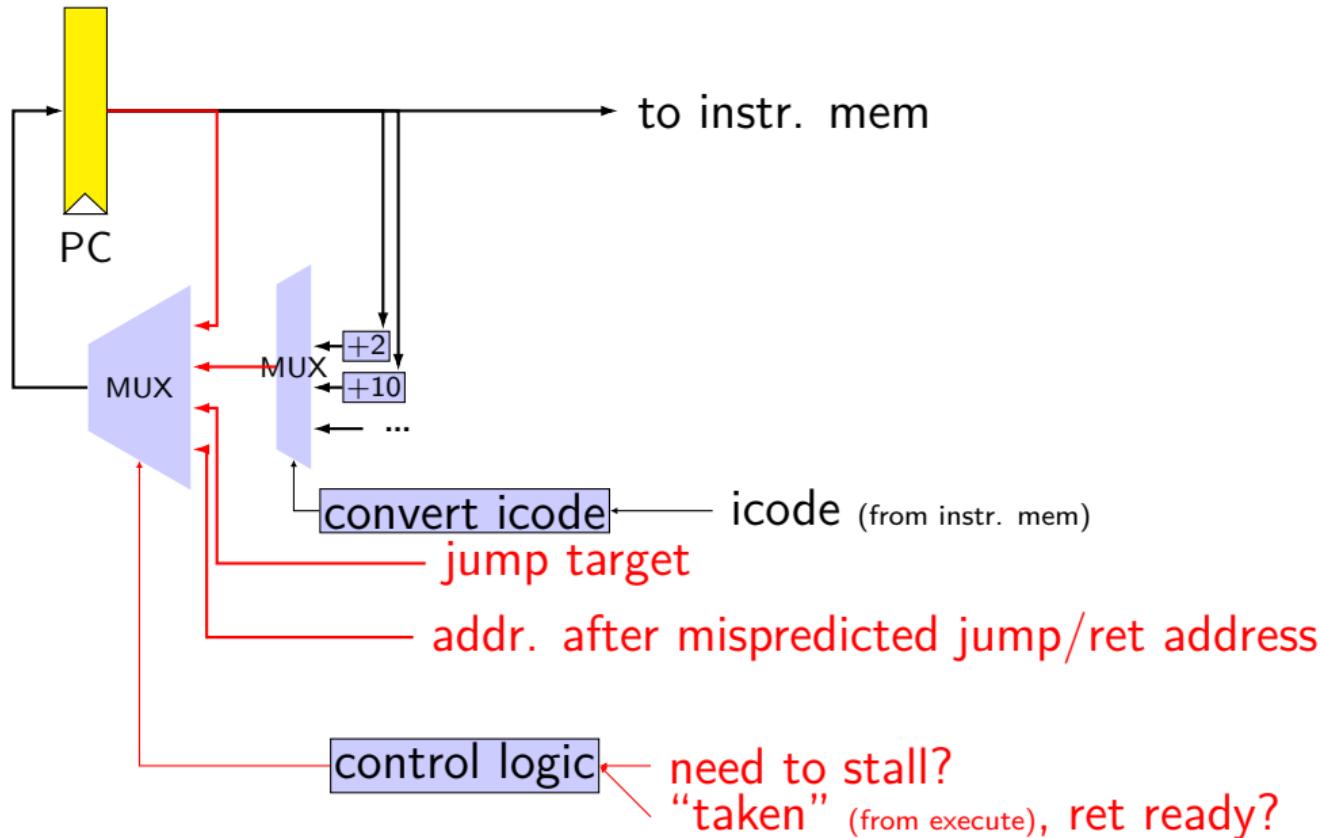
empty: ret

time	fetch	decode	execute	memory	writeback
1	call				
2	ret	call			
3	wait for ret	ret	call		
4	wait for ret	nothing	ret	return address loaded here	
5	wait for ret	nothing	nothing	ret (load)	call
6	addq	nothing	nothing	nothing	ret

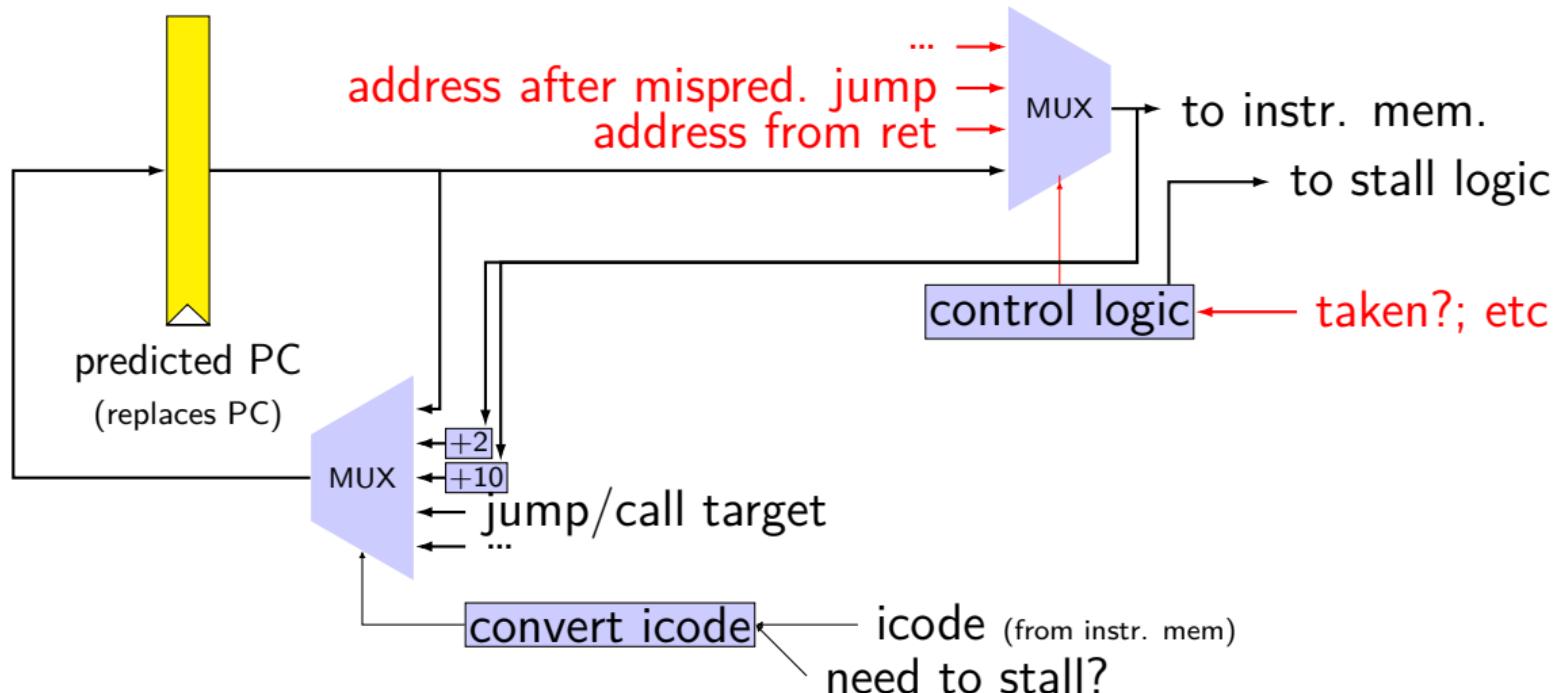
PC update (adding prediction, stall)



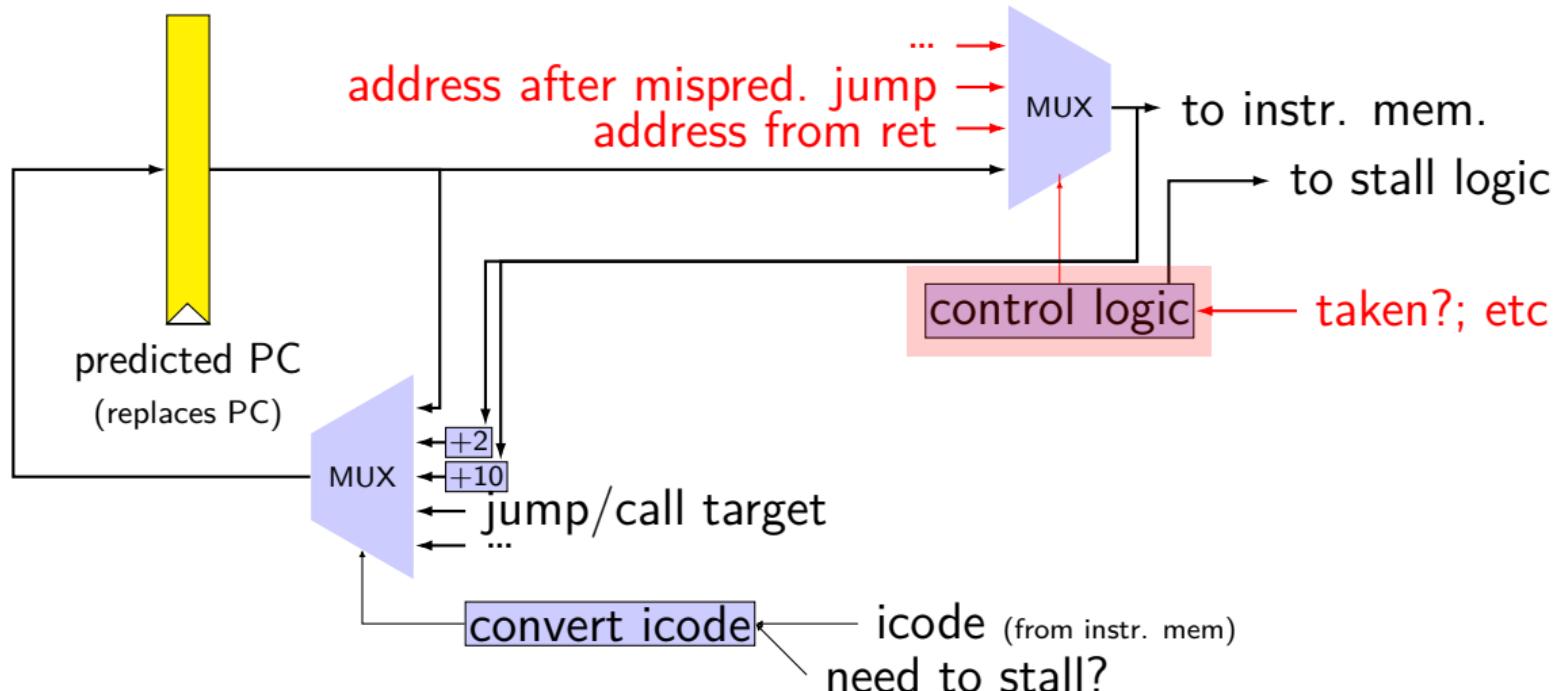
PC update (adding prediction, stall)



PC update (rearranged)

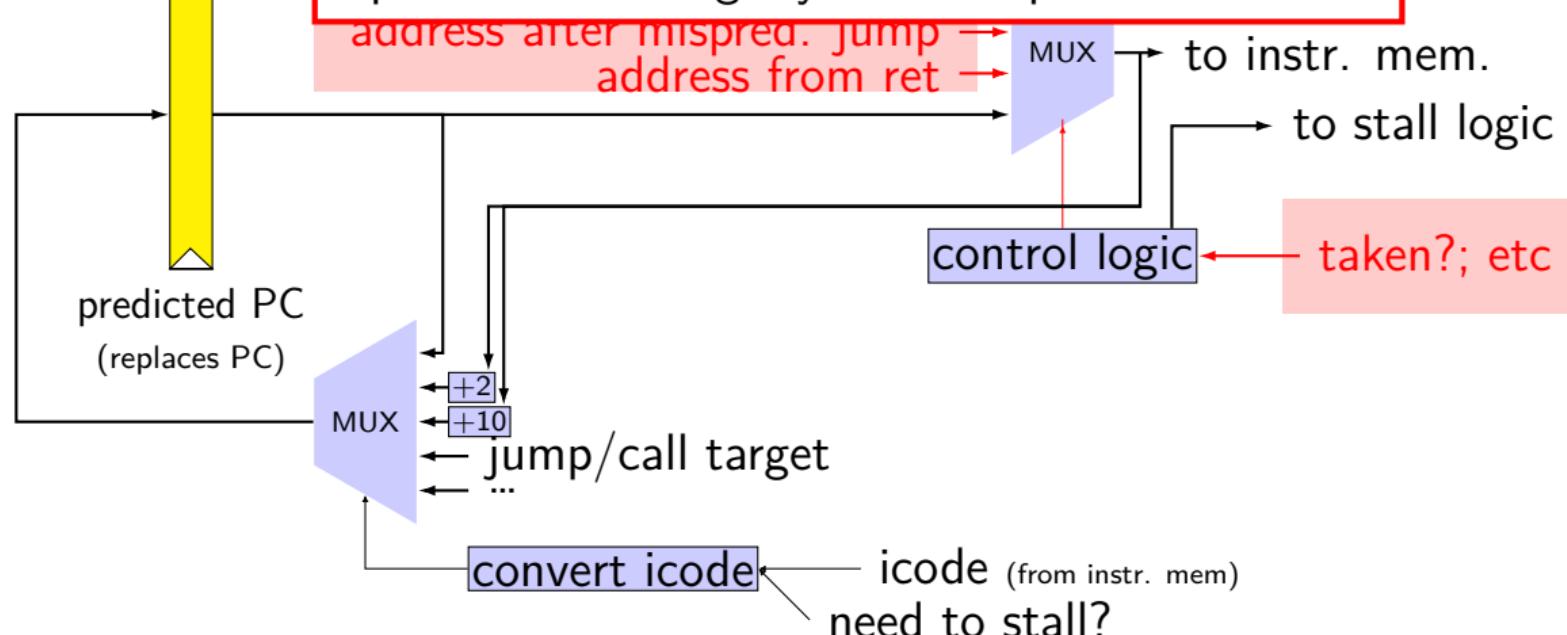


PC update (rearranged)

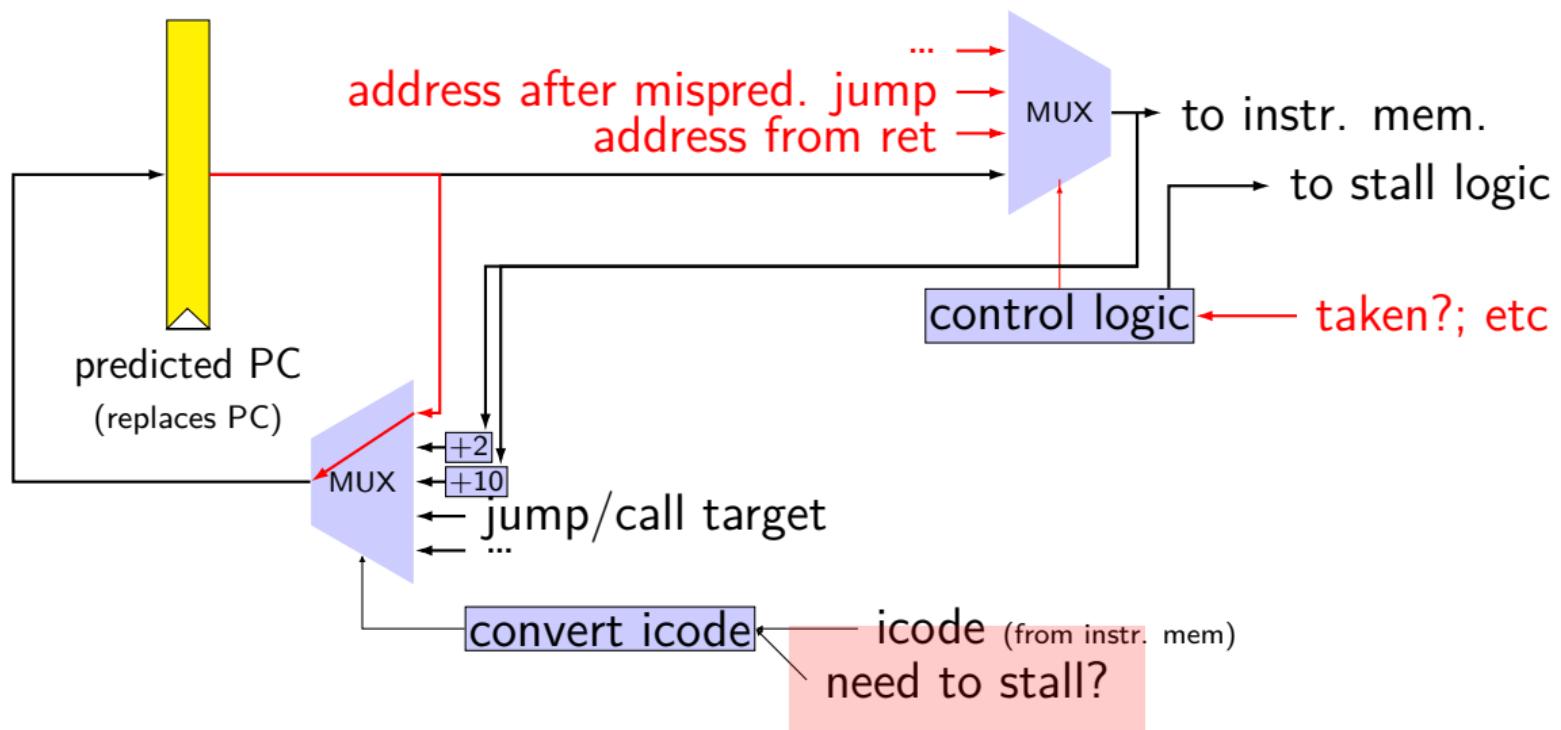


PC update (rearranged)

same logic as before — but happens in next cycle
inputs are from slightly different place...



PC update (rearranged)



rearranged PC update in HCL

```
/* replacing the PC register: */
register fF {
    predictedPC: 64 = 0;
}

/* actual input to instruction memory */
pc = [
    conditionCodesSaidNotTaken : jumpValP;
        /* from later in pipeline */
    ...
    1: F_predictedPC;
];
```

why rearrange PC update?

either works

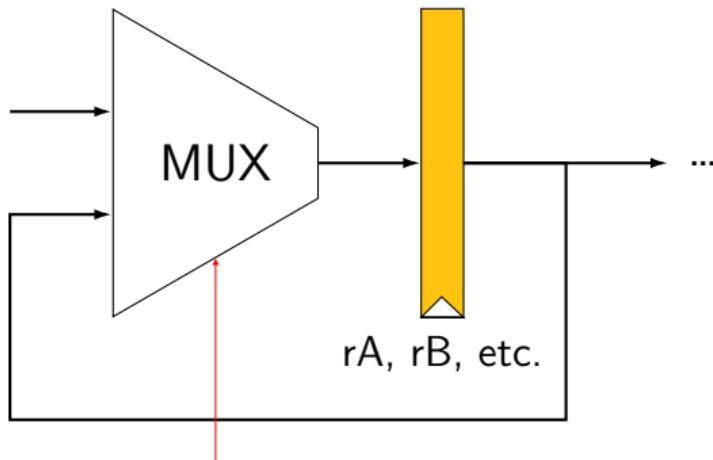
correct PC at beginning or end of cycle?

still some time in cycle to do so...

maybe easier to think about branch prediction this way?

fetch/decode logic — advance or not

from instr. memory



should we stall?

ex.: dependencies and hazards (1)

addq %rax, %rbx

subq %rax, %rcx

irmovq \$100, %rcx

addq %rcx, %r10

addq %rbx, %r10

where are dependencies?

which are hazards in our pipeline?

which are resolved with forwarding?

ex.: dependencies and hazards (1)

addq	%rax ,	%rbx
subq	%rax ,	%rcx
irmovq	\$100 ,	%rcx
addq	%rcx ,	%r10
addq	%rbx ,	%r10

where are dependencies?

which are hazards in our pipeline?

which are resolved with forwarding?

ex.: dependencies and hazards (1)

addq	%rax ,	%rbx
subq	%rax ,	%rcx
irmovq	\$100 ,	%rcx
addq	%rcx ,	%r10
addq	%rbx ,	%r10

where are dependencies?

which are hazards in our pipeline?

which are resolved with forwarding?

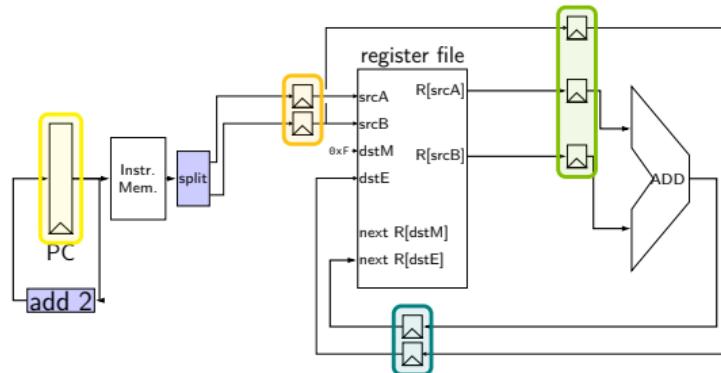
ex.: dependencies and hazards (1)

addq	%rax ,	%rbx
subq	%rax ,	%rcx
irmovq	\$100 ,	%rcx
addq	%rcx ,	%r10
addq	%rbx ,	%r10

where are dependencies?
which are hazards in our pipeline?
which are resolved with forwarding?

exercise

path	time
add 2	50 ps
instruction memory	200 ps
register file read	125 ps
add	100 ps
register file write	125 ps



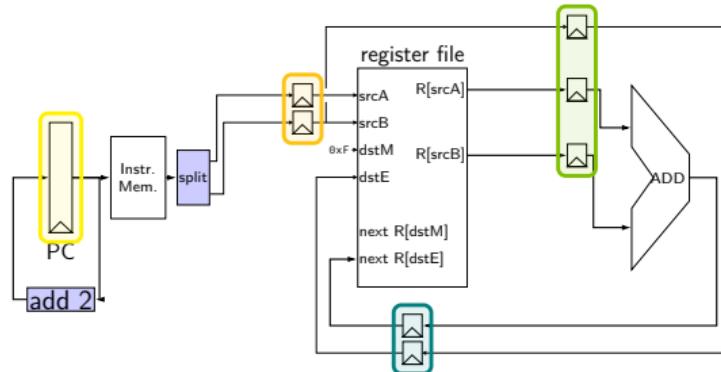
pipeline register delay: 10ps

how will throughput improve if we **double the speed of the instruction memory?**

- A. 2.00x
- B. 1.70x to 1.99x
- C. 1.60x to 1.69x
- D. 1.50x to 1.59x
- E. less than 1.50x

exercise

path	time
add 2	50 ps
instruction memory	200 ps
register file read	125 ps
add	100 ps
register file write	125 ps



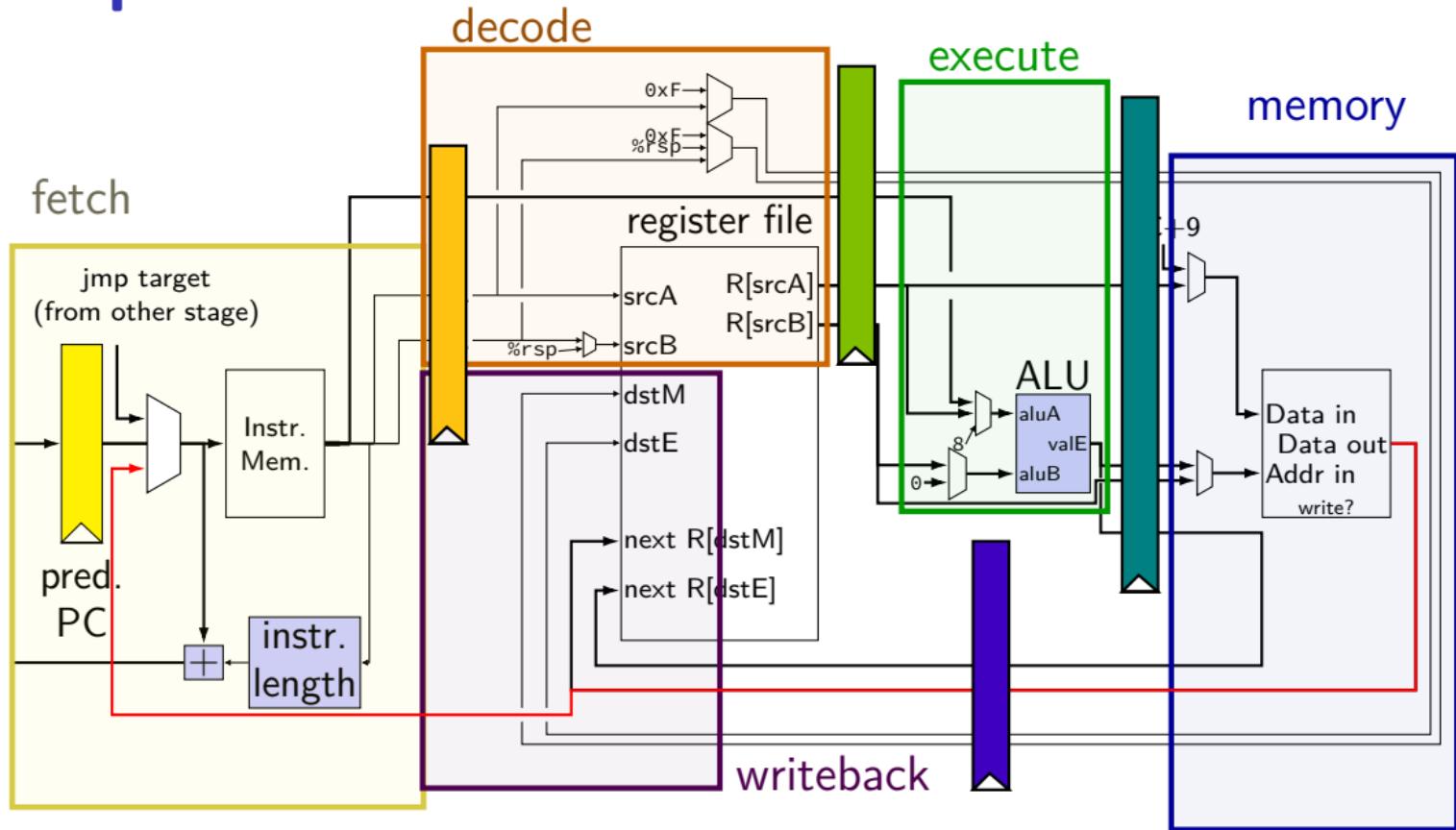
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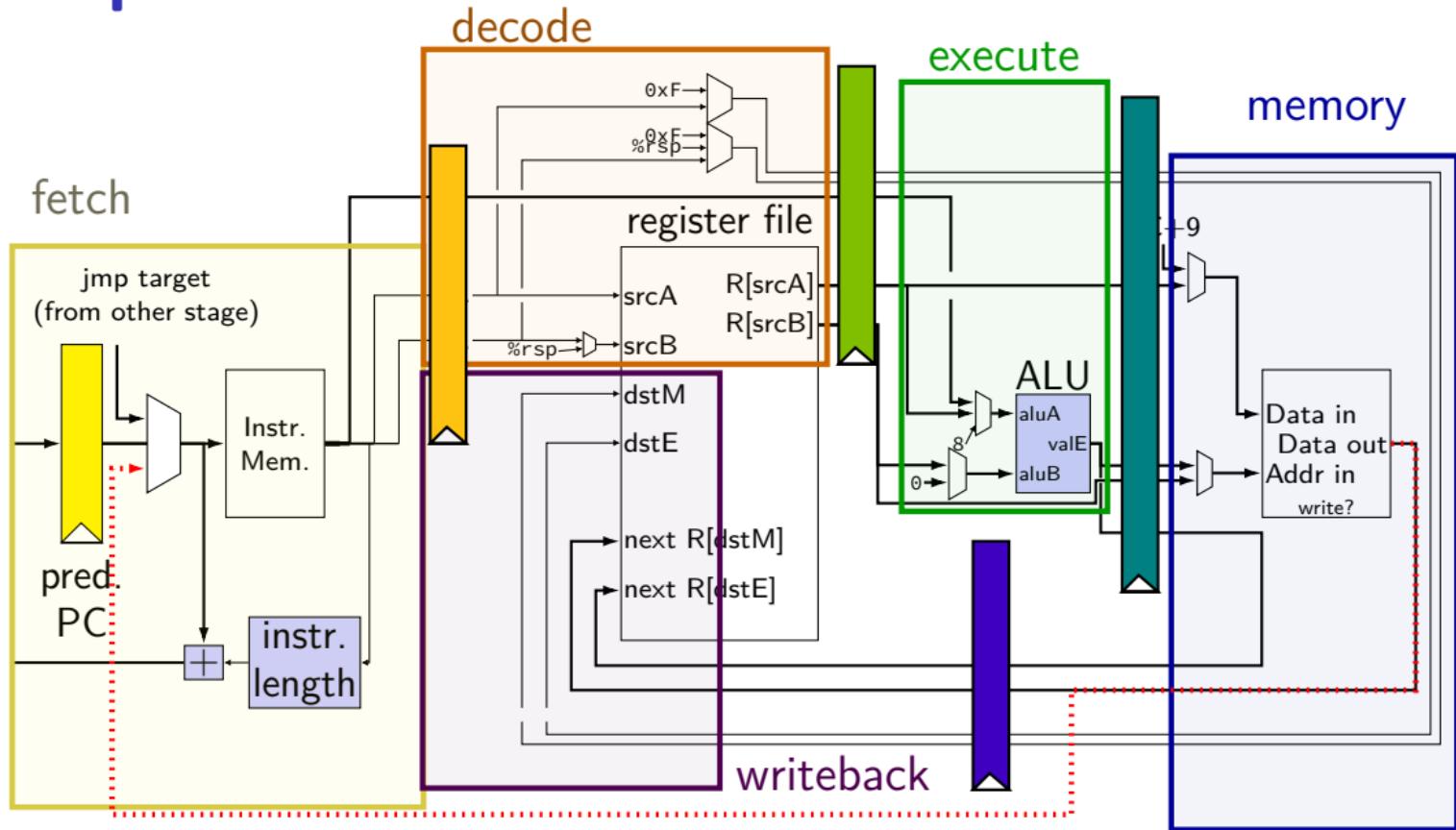
- A. 2.00x
- B. 1.70x to 1.99x
- C. 1.60x to 1.69x
- D. 1.50x to 1.59x
- E. less than 1.50x

$$\frac{1}{135} \div \frac{1}{210} = 1.56x — D$$

ret paths



ret paths



ret paths

