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Collaborators:

Collaboration Policy: For this homework only! You may collaborate with other students in this class. As an exception to the usual collaboration policy, you do not need to tell us about casual interactions of the "I got $X$, what did you get?" variety. But do cite any close collaboration or major corrections; for example if the answer to the above hypothetical was "I think $X$ is wrong, here's why" and then you change your answer, add a note like "mst3k suggested this answer" next to your answer. However, we expect that everyone will work on the assignment to better understand circuits, so you may not directly copy another student's answer.

PROBLEM I 4-input adder
We have discussed both a 2-input and 3-input adders for single-bit values as we were building our ripple carry adder. Draw a 4 -input adder for single-bit values: that is, a set of logic gates with 4 input wires (no need to name them) each representing a number between 0 and 1 and a multi-bit output $z$, composed of wires $z_{0}$ through $z_{\ldots}$ (where $z_{0}$ is the low-order bit, $z_{1}$ the next, etc., up to the number of wires needed for this task). The gates should ensure that $z=$ the sum of all four inputs.

PROBLEM 24 -bit increment to 15
In class we considered an increment circuit that adds 1 to its input value. How can we change our circuit to "stop" at $\mathrm{x}=0 \mathrm{~b} 1111$ ? That is, if x is not all 1 s , then increment by 1 . If x is all 1 s , then increment by o, i.e., $\mathrm{z}=0 \mathrm{~b} 1111$. Draw a circuit that does not use more than twice the number of gates in the original.
problem 3 4-bit decrement
Now, rather than our 4-bit increment circuit that adds 1 to its input value, we want a circuit that subtracts 1 (i.e., $z=x-1$ ). Draw a 4-bit decrement circuit that does not use not ( ${ }^{\sim}$ ) gates.

PROblem 4 Fancy adder
Given two 4 -bit inputs $x$ and $y$, draw a circuit that output the value $z$ such that $z=x+x+y$. As a special property of this circuit only, we do not want overflow, so we have decided that $z$ may have more than 4 bits to represent its value. Draw the corresponding circuit; label the output bits of $z$ and state the number of bits needed in the output. Hint: is there a fast way to calculate $x+x$ without using many gates?

