## Boolean Algebra

CS 2130: Computer Systems and Organization 1 January 20, 2023 Welcome

If you need to switch labs:

- $\cdot$  Form will be coming soon
- Must be justified (i.e. class conflicts)
- Very limited space to make swaps

Quiz 0 opens tonight, due Sunday 11:59pm

### Where to start?

Where to start? 0 and 1

#### Why only 0 and 1?

#### Claude Shannon





#### Why only 0 and 1?



• ...

- bit either a 0 or 1
- binary a system that has only two positions
- trinary a system that has only three positions
- **quadrinary** a system that has only four positions

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• ...

· decinary - ...

- bit either a 0 or 1
- binary a system that has only two positions
- trinary a system that has only three positions
- quadrinary a system that has only four positions
- ...
- decinary ...
- decimal system that has ten positions

#### Boolean Algebra

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|)

George Boole



Photo Public Domain

#### Overall idea:

- Only need two things (Shannon)
- We can do math with two things (Boole)

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Now we need a physical device that deals in two levels

#### Transistors



Electricity (conceptually) - involves flow of electrons or other charged carriers through a conductive material

- $\cdot \ current$  rate of flow
- **voltage** pressure of flow

Examples in water

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Examples in water

- High pressure, low flow squirt gun
- Low pressure, high flow bucket of water

#### Transistors



Transistors act like an electrically-triggered switch

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- $\cdot$  Apply voltage to allow current to flow

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- No voltage, no current
- $\cdot$  Apply voltage to allow current to flow
- The amount of voltage needed to open the gate is boundary between 0 and 1
- Central technique for how we are going to build binary computers

#### Transistors



### Circuit Diagram



### Circuit Diagram



### Circuit Diagram



# Other Gates (reading)

Where we are now

- World with only 2 states: 0 and 1
- Re-developed Boolean logic: and, or, not

Gives us everything Boole talked about

- We can do a lot of interesting things!
- Next: build higher level ideas: the **trinary operator**

### Trinary Operator

General idea
if ( ... ) {
 ...
} else {
 ...
}

Trinary operator (expression if)

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General idea
if ( ... ) {
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Trinary operator (expression if)

- Python: x = b if a else c
- · Java: x = a? b : c

## Multiplexer (mux)

How can we build a mux out of what we have learned so far?

x = a ? b : c

Can be built from and, or, and not

- Can be built using transistors
- Can physically put it in silicon!

Mux will be the key when constructing a computer out of gates and circuits!

# **Questions?**

# More bits!

### 2-bit Multiplexer (mux)

2-bit values instead of 1-bit values