

Circuits and Code

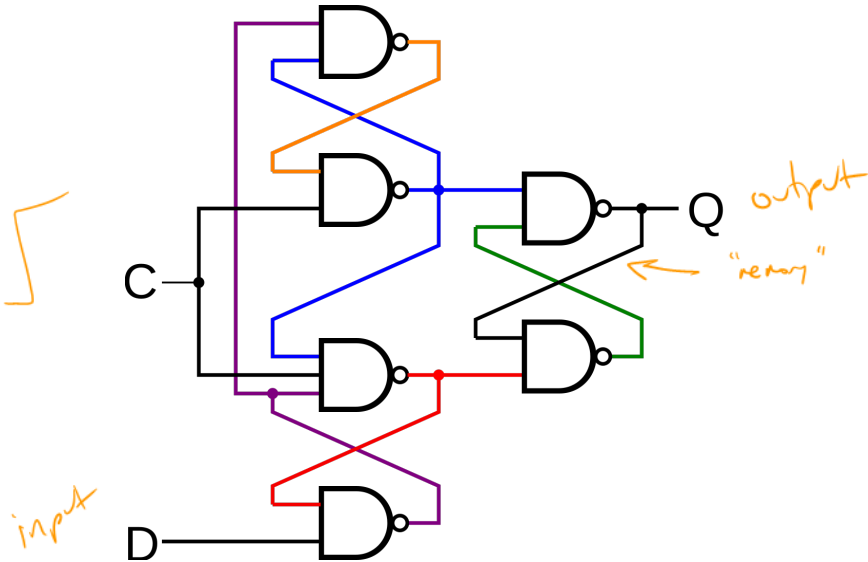
CS 2130: Computer Systems and Organization 1

February 6, 2023

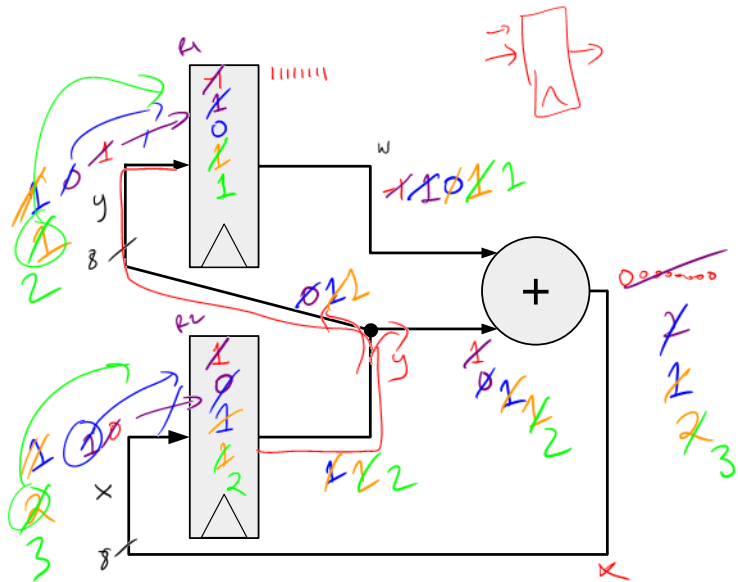
Announcements

- Homework 1 due tonight
- Homework 2 available today online, due next Monday
 - Please react to the Discord message in #general today if you want me to bring a paper copy for you on Wednesday!

1-bit Register Circuit

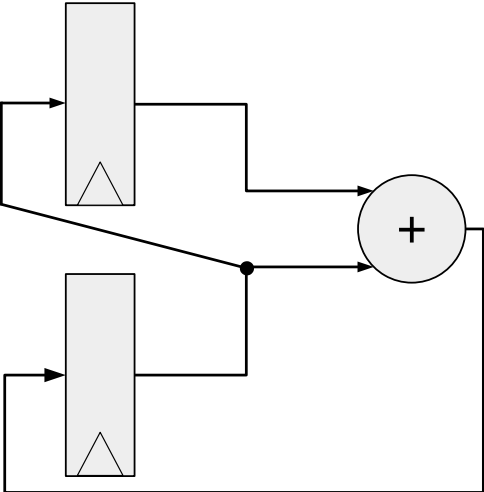


Another Circuit

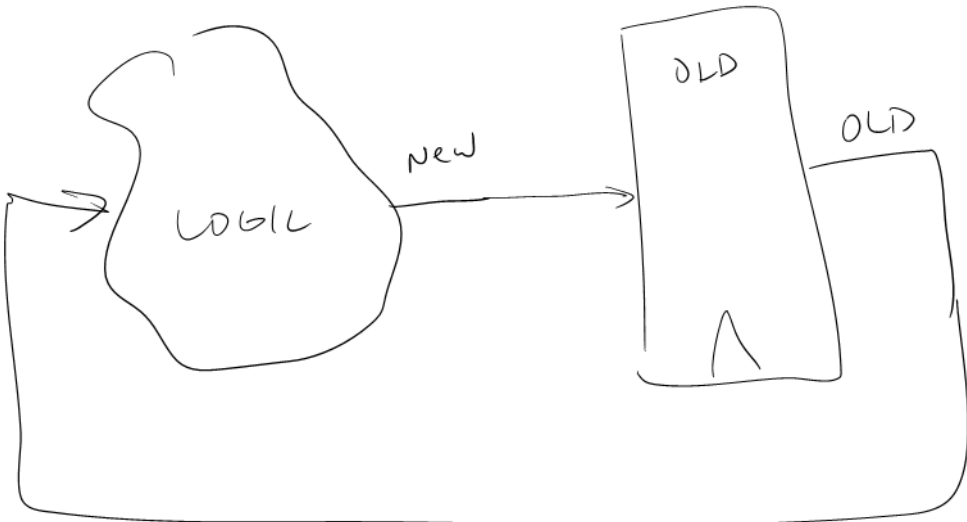


| bit | x | y | R_1 | R_2 |
|-----|----|---|-------|-------|
| 0 | 0 | 1 | -1 | 1 |
| 1 | 1 | 0 | 1 | 0 |
| 2 | 1 | 1 | 0 | 1 |
| 3 | 2 | 1 | 1 | 1 |
| 4 | 3 | 2 | 1 | 2 |
| 5 | 5 | 3 | | |
| 6 | 8 | 5 | | |
| 7 | 13 | 8 | | |

Another Circuit



Common Model in Computers



We can write code to build circuits

Code to Build Circuits from Gates

Write code to build circuits from gates

- Gates we *already* know: $\&$, $|$, \wedge , \sim
- Operations we can build from gates: $+$, $-$
- Others we can build: $*$

$x \& y$

$$\begin{array}{r} 2130 \\ \times 1001 \\ \hline 2130 \\ 0000 \\ 213000 \\ 2130000 \\ \hline \end{array}$$

Handwritten annotations: a green checkmark to the right of the first line, a green double arrow to the right of the second line, and a green checkmark below the final result.

$/$, $\%$

Code to Build Circuits from Gates

Write code to build circuits from gates

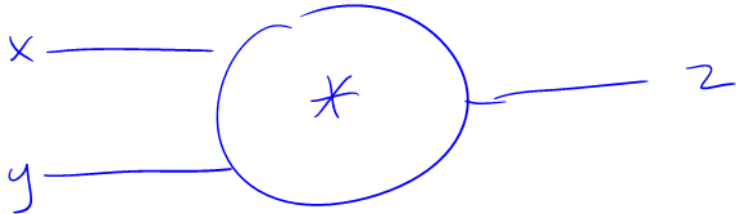
- Gates we *already* know: $\&$, $|$, \wedge , \sim
- Operations we can build from gates: $+$, $-$
- Others we can build:
- Ternary operator: $? :$

$$z = (a == b ? x : y) * w$$

Equals

Equals: =

- Attach with wire (i.e., connect things)
- Ex: $z = x * y$



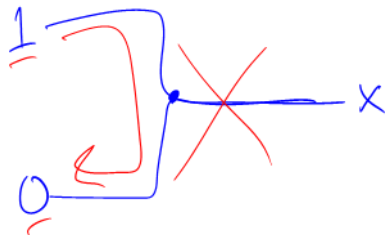
Equals

Equals: =

- Attach with wire (i.e., connect things)
- Ex: $z = x * y$
- What about the following?

$$x = 1$$

$$x = 0$$



Equals

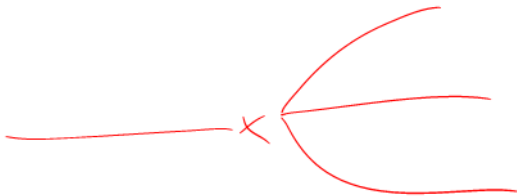
Equals: =

- Attach with wire (i.e., connect things)
- Ex: $z = x * y$
- What about the following?

$$x = 1$$

$$x = 0$$

- **Single assignment:** each variable can only be assigned a value once



Subtraction

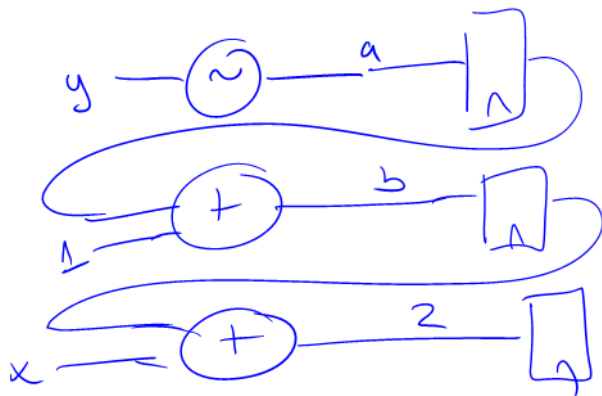
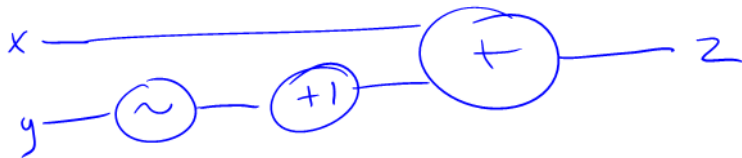
$$z = x - y$$

$$z = x + \overbrace{\sim y}^{-y} + 1$$

$$a = \sim y$$

$$b = a + 1$$

$$z = x + \underline{b}$$



Comparisons

Each of our comparisons in code are straightforward to build:

- == - xor then nor bits of output

$$x == y$$

$$\sim(\text{orbits})$$
$$!(x \wedge y)$$

Comparisons

Each of our comparisons in code are straightforward to build:

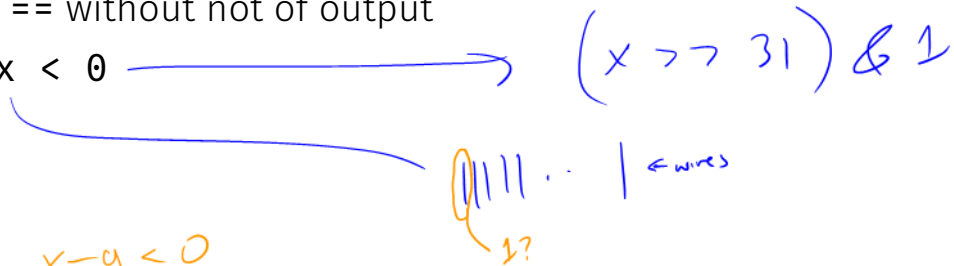
- `==` - xor then nor bits of output
- `!=` - same as `==` without not of output

Comparisons

Each of our comparisons in code are straightforward to build:

- == - xor then nor bits of output
- != - same as == without not of output
- < - consider $x < 0$

$$x < y \quad x - y < 0$$



Comparisons

Each of our comparisons in code are straightforward to build:

- `==` - xor then nor bits of output
- `!=` - same as `==` without not of output
- `<` - consider $x < 0$
- `>`, `<=`, `=>` are similar

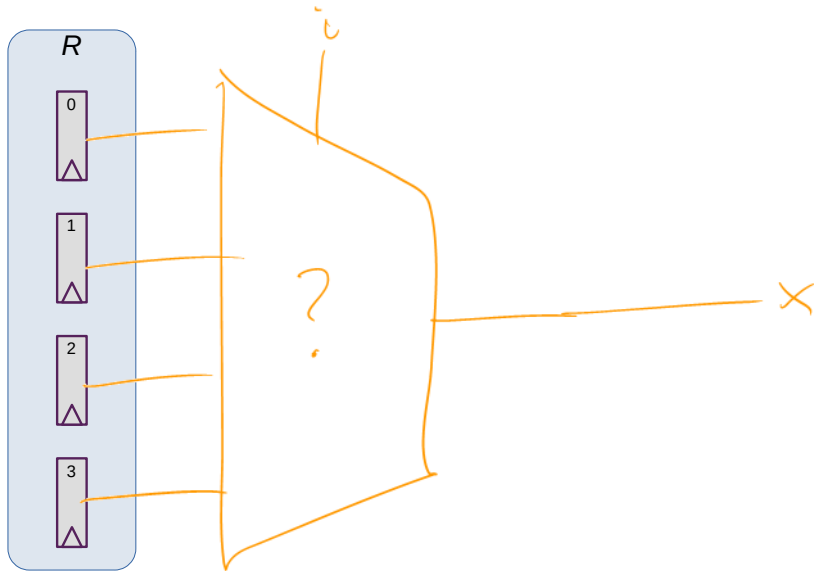
Indexing

Indexing with square brackets: []

- **Register bank** (or **register file**) - an array of registers
 - Can programmatically pick one based on index
 - I.e., can determine which register while running
- Two important operations:
 - $x = R[i]$ - Read from a register
 - $R[j] = y$ - Write to a register

Reading

$x = R[\underline{i}]$ - connect output of registers to x based on index i

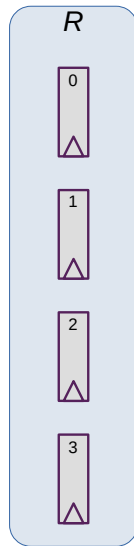


Aside: 4-input Mux

How do we build a 4-input mux? How many wires should i be?

Writing

$R[j] = y$ - connect y to input of registers based on index j



Aside: Creating $==0$ gates

How do we build gates that check for $j == w$?

Need one more thing to build computers

Memory and Storage

Registers

≈ KiB

- 6 gates each, ≈ 24 transistors
- Efficient, fast
- Expensive!
- Ex: local variables

Memory

≈ GiB

- Two main types: SRAM, DRAM
- DRAM: 1 transistor, 1 capacitor per bit
- DRAM is cheaper, simpler to build
- Ex: data structures, local variables

These do not persist between power cycles

Memory and Storage

Disk

≈ GiB-TiB

- Two main types: flash (solid state), magnetic disk
- Magnetic drive
 - Platter with physical arm above and below
 - Cheap to build
 - Very slow! Physically move arm while disk spins

- Ex: files

Data on disk does persist between power cycles

Putting it all together
Next time!