

A Brief History of Computing

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Historical Perspectives



Historical Perspectives

- Knowing the "big picture" is empowering
- Science and mathematics builds heavily on past
- Often the simplest ideas are the most subtle
- Most fundamental progress was done by a few
- We learn much by observing the best minds
- Research benefits from seeing connections
- The field of computer science has many "parents"
- We get inspired and motivated by excellence
- The giants can show us what is possible to achieve
- It is fun to know these things!

"Standing on the Shoulders of Giants"

- Aristotle, Euclid, Archimedes, Eratosthenes
- Abu Ali al-Hasan ibn al-Haytham
- Fibonacci, Descartes, Fermat, Pascal
- Newton, Euler, Gauss, Hamilton
- Boole, De Morgan
- Babbage, Ada Lovelace
- Venn, Carroll







"Standing on the Shoulders of Giants"

- Cantor, Hilbert, Russell
- Hardy, Ramanujan, Ramsey
- Gödel, Church, Turing
- von Neumann, Shannon
- Kleene, Chomsky
- Hoare, McCarthy, Erdos
- Knuth, Backus, Dijkstra

Many others...







Historical Perspectives

Aristotle (384BC-322BC)

- Founded Western philosophy
- Student of Plato
- Taught Alexander the Great
- "Aristotelianism"
- Developed the "scientific method"
- One of the most influential people ever
- Wrote on physics, theatre, poetry, music, logic, rhetoric, politics, government, ethics, biology, zoology, morality, optics, science, aesthetics, psychology, metaphysics, ...
- Last person to know everything known in his own time!

"Almost every serious intellectual advance has had to begin with an attack on some Aristotelian doctrine." – Bertrand Russell









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ASHELLAS AP

"Wit is educated insolence." - Aristotle (384-322 B.C.)





V Centº del Descubrimiento de América. 1492-1992

JAY 750

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Mare parvum est inter finem Ilyspanie a parte occidentis, et inter principium Indie a parte orientis.

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Aristóteles (De cælo et mundo)







"The periodic table."

Historical Perspectives

Euclid (325BC-265BC)

- Founder of geometry
 & the axiomatic method
- "Elements" oldest and most impactful textbook
- Unified logic & math
- Introduced rigor and "Euclidean" geometry
- Influenced all other fields of science: Copernicus, Kepler, Galileo, Newton, Russell, Lincoln, Einstein & many others







B/W QuickCam

a.cidadao@mail.telepac.pt



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J.ham's

NTUEPIE

ICON

Euclid's Straight-Edge and Compass Geometric Constructions



Euclid's Axioms

- 1: Any two points can be connected by exactly one straight line.
- 2: Any segment can be extended indefinitely into a straight line.
- 3: A circle exists for any given center and radius.
- 4: All right angles are equal to each other.
- 5: The parallel postulate: Given a line and a point off that line, there is exactly one line passing through the point, which does not intersect the first line.
- The first 28 propositions of Euclid's Elements were proven without using the parallel postulate!
- Theorem [Beltrami, 1868]: The parallel postulate is independent of the other axioms of Euclidean geometry.
- The parallel postulate can be modified to yield non-Euclidean geometries!







Founders of Non-Euclidean Geometry

János Bolyai (1802-1860)



Nikolai Ivanovich Lobachevsky (1792-1856)















Non-Euclidean Non-Orientable Surfaces



Non-Euclidean Geometries

Spherical / Elliptic geometry: Given a line and a point off that line, there are no lines passing through that point that do not intersect the first line.

- Lines are geodesics "great circles"
- Sum of triangle angles is $> 180^{\circ}$
- Not all triangles have same angle sum
- Figures can not scale up indefinitely
- Area does not scale as the square
- Volume does not scale as the cube
- The Pythagorean theorem fails
- Self-consistent, and complete





Non-Euclidean Geometries

Hyperbolic geometry: Given a line and a point off that line, there are an infinity of lines passing through that point that do not intersect the first line.

- Sum of triangle angles is less than 180°
- Different triangles have different angle sum
- Triangles with same angles have same area
- There are no similar triangles
- Used in relativity theory













Abraham Albert Unga

THE GEOMETRY OF EVERYDAY LIFE



TUNA SANDWICH

SNEAKER

GRANDMA

Historical Perspectives Eratosthenes (276BC-194BC)

- Chief librarian at Library of Alexandria
- Measured the Earth's size (<1% error!)
- Calculated the Earth-Sun distance
- Invented latitude and longtitude
- Primes "Sieve of Eratosthenes"
- Chronology of ancient history
- Wrote on astronomy, geography, history, mathematics, philosophy, and literature





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101	102	103	104	105	106	107	108	109	110
111	112	113	114	115	116	117	118	119	120



Prime numbers





An Ancient Computer: The Antikythera

- Oldest known mechanical computer
- Built around 150-100 BCE !
- Calculates eclipses and astronomical positions of sun, moon, and planets
- Very sophisticated for its era
- Contains dozens of intricate gears
- Comparable to 1700's Swiss clocks
- Has an attached "instructions manual"
- Still the subject of ongoing research























DECODING AN Ancient Computer

New explorations have revealed how the Antikythera mechanism modeled lunar motion and predicted eclipses, among other sophisticated tricks By Tony Freeth

KEY CONCEPTS

- The Antikythera mechanism is a unique mechanical calculator from second-century B.C. Greece. Its sophistication surprised archaeologists when it was discovered in 1901. But no one had anticipated its true power.
- Advanced imaging tools have finally enabled researchers to reconstruct how the device predicted lunar and solar eclipses and the motion of the moon in the sky.
- Inscriptions on the mechanism suggest that it might have been built in the Greek city of Syracuse (now in modern Sicily), perhaps in a tradition that originated with Archimedes.

-The Editors

f it had not been for two storms 2,000 years apart in the same area of the Mediterranean, the most important technological artifact from the ancient world could have been Three technological ar-

lost forever. The first storm, in the middle of the 1st century B.C., sank a Roman merchant vessel laden with Greek treasures. The second storm, in A.D. 1900, drove a party of sponge divers to shelter off the tiny island of Antikythera, between Crete and the mainland of Greece. When the storm subsided, the divers tried their luck for sponges in the local waters and chanced on the wreck. Months later the divers returned, with backing from the Greek government. Over nine months they recovered a hoard of beautiful ancient Greek objects-rare bronzes, stunning glassware, amphorae, pottery and jewelry-in one of the first major underwater archaeological excavations in history.

One item attracted little attention at first: an undistinguished, heavily calcified lump the size of a phone book. Some months later it fell apart, revealing the remains of corroded bronze gearwheels—all sandwiched together and with teeth just one and a half millimeters long—along with plates covered in scientific scales and Greek in scriptions. The discovery was a shock: until then, the ancients were thought to have made gears only for crude mechanical tasks.

Three of the main fragments of the Antikythera mechanism, as the device has come to be known, are now on display at the Greek National Archaeological Museum in Athens. They look small and fragile, surrounded by imposing bronze statues and other artistic glories of ancient Greece. But their subtle power is even more shocking than anyone had imagined at first.

I first heard about the mechanism in 2000. I was a filmmaker, and astronomer Mike Edmunds of Cardiff University in Wales contacted me because he thought the mechanism would make a great subject for a TV documentary. I learned that over many decades researchers studying the mechanism had made considerable progress, suggesting that it calculated astronomical data, but they still had not been able to fully grasp how it worked. As a former mathematician, I became intensely interested in understanding the mechanism myself.

Edmunds and I gathered an international collaboration that eventually included historians, astronomers and two teams of imaging experts. In the past few years our group has reconstructed how nearly all the surviving parts worked and what functions they performed. The mechanism calculated the dates of lunar and solar eclipses, modeled the moon's subtle apparent motions through the sky to the best of the available knowledge, and kept track of the dates of events of social significance, such as the Olympic Games. Nothing of comparable technological sophistication is known anywhere in the world for at least a millennium afterward. Had this unique specimen not survived, historians would have thought that it could not have existed at that time.

Early Pioneers

German philologist Albert Rehm was the first person to understand, around 1905, that the Antikythera mechanism was an astronomical calculator. Half a century later, when science historian Derek J. de Solla Price, then at the Institute for Advanced Study in Princeton, N.J., described the device in a *Scientific American* article, it still had revealed few of its secrets.

The device, Price suggested, was operated by turning a crank on its side, and it displayed its output by moving pointers on dials located on its front and back. By turning the crank, the user could set the machine on a certain date as indicated on a 365-day calendar dial in the front. (The dial could be rotated to adjust for an extra day every four years, as in today's leap years.) At the same time, the crank powered all the other gears in the mechanism to yield the information corresponding to the set date.

A second front dial, concentric with the calendar, was marked out with 360 degrees and with the 12 signs representing the constellations of the zodiac [see box on pages 80 and 81]. These are the constellations crossed by the sun in its apparent motion with respect to the "fixed" stars— "motion" that in fact results from Earth's orbiting the sun—along the path called the ecliptic. Price surmised that the front of the mechanism probably had a pointer showing where along the ecliptic the sun would be at the desired date.

In the surviving fragments, Price identified the remains of a dozen gears that had been part of the mechanism's innards. He also estimated their tooth counts—which is all one can do given that nearly all the gears are damaged and incomplete. Later, in a landmark 1974 study, Price described 27 gears in the main fragment and provided improved tooth counts based on the first x-rays of the mechanism, by Greek radiologist Charalambos Karakalos. ANCIENT GREEKS knew how to calculate the recurring patterns of lunar eclipses thanks to observations made for centuries by the Babylonians. The Antikythera mechanism would have done those calculations for them—or perhaps for the wealthy Romans who could afford to own it. The depiction here is based on a theoretical reconstruction by the author and his collaborators.

[THE PLACES]



Where Was It From?

The Antikythera mechanism was built around the middle of the 2nd century B.C., a time when Rome was expanding at the expense of the Greek-dominated Hellenistic kingdoms (*green*). Divers recovered its corroded remnants (*including fragment at left*) in A.D. 1901 from a shipwreck near the island of Antikythera. The ship sank around 65 B.C. while carrying Greek artistic treasures, perhaps from Pergamon to Rome. Rhodes had one of the major traditions of Greek astronomy, but the latest evidence points to a Corinthian origin. Syracuse, which had been a Corinthian colony in Sicily, is a possibility: the great Greek inventor Archimedes had lived there and may have left behind a technological tradition.

Tooth counts indicate what the mechanism calculated. For example, turning the crank to give a full turn to a primary 64-tooth gear represented the passage of a year, as shown by a pointer on the calendar dial. That primary gear was also paired to two 38-tooth secondary gears, each of which consequently turned by 64/38 times for every year. Similarly, the motion relayed from gear to gear throughout the mechanism; at each step, the ratio of the numbers of gear teeth represents a different fraction. The motion eventually transmitted to the pointers, which thus turned at rates corresponding to different astronomical cycles. Price discovered that the ratios of one of these gear trains embodied an ancient Babylonian cycle of the moon.

Price, like Rehm before him, suggested that the mechanism also contained epicyclic gearing—gears spinning on bearings that are themselves attached to other gears, like the cups on a Mad Hatter teacup ride. Epicyclic gears extend the range of formulas gears can calculate beyond multiplications of fractions to additions and subtractions. No other example of epicyclic gearing is known to have existed in Western technology for another 1,500 years.

Several other researchers studied the mechanism, most notably Michael Wright, a curator at the Science Museum in London, in collaboration

with computer scientist Allan Bromley of the University of Sydney. They took the first threedimensional x-rays of the mechanism and showed that Price's model of the mechanism had to be wrong. Bromley died in 2002, but Wright persisted and made significant advances. For example, he found evidence that the back dials, which at first look like concentric rings, are in fact spirals and discovered an epicyclic mechanism at the front that calculated the phase of the moon.

Wright also adopted one of Price's insights, namely that the dial on the upper back might be a lunar calendar, based on the 19-year, 235lunar-month cycle called the Metonic cycle. This calendar is named after fifth-century B.C. astronomer Meton of Athens—although it had been discovered earlier by the Babylonians—and is still used today to determine the Jewish festival of Rosh Hashanah and the Christian festival of Easter. Later, we would discover that the pointer was extensible, so that a pin on its end could follow a groove around each successive turn of the spiral.

BladeRunner in Athens

As our group began its efforts, we were hampered by a frustrating lack of data. We had no access to the previous x-ray studies, and we did not even have a good set of still photographs.

Two images in a science magazine—x-rays of a goldfish and an enhanced photograph of a Babylonian clay tablet—suggested to me new ways to get better data.

We asked Hewlett-Packard in California to perform state-of-the-art photographic imaging and X-Tek Systems in the U.K. to do three-dimensional x-ray imaging. After four years of careful diplomacy, John Seiradakis of the Aristotle University of Thessaloniki and Xenophon Moussas of the University of Athens obtained the required permissions, and we arranged for the imaging teams to bring their tools to Athens, a necessary step because the Antikythera mechanism is too fragile to travel.

Meanwhile we had a totally unexpected call from Mary Zafeiropoulou at the museum. She had been to the basement storage and found boxes of bits labeled "Antikythera." Might we be interested? Of course we were interested. We now had a total of 82 fragments, up from about 20.

The HP team, led by Tom Malzbender, assembled a mysterious-looking dome about five feet across and covered in electronic flashbulbs that provided lighting from a range of different angles. The team exploited a technique from the computer gaming industry, called polynomial

THE RECONSTRUCTION Anatomy of a Relic

texture mapping, to enhance surface details. In-

Computed tomography—a 3-D mapping obtained from multiple x-ray shots—enabled the author and his colleagues to get inside views of the Antikythera mechanism's remnants. For example, a CT scan can be used to virtually slice up an object (*below, slices of main fragment*). The information helped the team see how the surviving gears connected and estimate their tooth counts, which determined what calculations they performed. The team could then reconstruct most of the device [see model at right and box on next two pages].

scriptions Price had found difficult to read were now clearly legible, and fine details could be enhanced on the computer screen by controlling the reflectance of the surface and the angle of the lighting. The inscriptions are essentially an instruction manual written on the outer plates.

A month later local police had to clear the streets in central Athens so that a truck carrying the BladeRunner, X-Tek's eight-ton x-ray machine, could gain access to the museum. The BladeRunner performs computed tomography similar to a hospital's CT scan, but with finer detail. X-Tek's Roger Hadland and his group had specially modified it with enough x-ray power to penetrate the fragments of the Antikythera mechanism. The resulting 3-D reconstruction was wonderful: whereas Price could see only a puzzle of overlapping gears, we could now isolate layers inside the fragment and see all the fine details of

the gear teeth. Unexpectedly, the x-rays revealed more than 2,000 new text characters that had been hidden deep inside the fragments. (We have now identified and interpreted a total of 3,000 characters out of perhaps 15,000 that existed originally.) In Athens, Moussas and Yanis Bitsakis, also at the University of Athens, and Agamemnon Tselikas of the Center for History and Palaeography beHistorians would have thought that SOMETHING SO COMPLEX could not have existed at the time.

[THE AUTHOR]

Tony Freeth's academic background is in mathematics and mathematical logic (in which he holds a Ph.D.). His award-winning career as a filmmaker culminated in a series of documentaries about increasing crop yields in sub-Saharan Africa, featuring the late Nobel Peace Prize Laureate Norman Borlaug. Since 2000 Freeth has returned to an academic focus with research on the Antikythera mechanism. He is managing director of the film and television production company Images First, and he is now developing a film on the mechanism.



gan to discover inscriptions that had been invisible to human eves for more than 2,000 years. One translated as "... spiral subdivisions 235...," confirming that the upper back dial was a spiral describing the Metonic calendar.

Babylon System

Back at home in London, I began to examine the CT scans as well. Certain fragments were clearly all part of a spiral dial in the lower back. An estimate of the total number of divisions in the dial's four-turn spiral suggested 220 to 225.

The prime number 223 was the obvious contender. The ancient Babylonians had discovered that if a lunar eclipse is observed-something that can happen only during a full moon-usually a similar lunar eclipse will take place 223 full moons later. Similarly, if the Babylonians saw a solar eclipse-which can take place only during a new moon-they could predict that 223 new moons later there would be a similar one (although they could not always see it: solar eclipses are visible only from specific locations, and ancient astronomers could not predict them reliably). Eclipses repeat this way because every 223 lunar months the sun, Earth and the moon return to approximately the same alignment with respect to one another, a periodicity known as the Saros cycle.

Between the scale divisions were blocks of symbols, nearly all containing Σ (sigma) or H (eta), or both. I soon realized that Σ stands for Σεληνη (selene), Greek for "moon," indicating a lunar eclipse; H stands for H $\lambda 100\sigma$ (*helios*), Greek for "sun," indicating a solar eclipse. The Babylonians also knew that within the 223-month period, eclipses can take place only in particular months, arranged in a predictable pattern and separated by gaps of five or six months; the distribution of symbols around the dial exactly matched that pattern.

I now needed to follow the trail of clues into the heart of the mechanism to discover where this new insight would lead. The first step was to find a gear with 223 teeth to drive this new Saros dial. Karakalos had estimated that a large gear visible at the back of the main fragment had 222 teeth. But Wright had revised this estimate to 223, and Edmunds confirmed this. With plausible tooth counts for other gears and with the addition of a small, hypothetical gear, this 223-tooth gear could perform the required calculation.

But a huge problem still remained unsolved and proved to be the hardest part of the gearing to crack. In addition to calculating the Saros cy-

[INSIDE THE ANTIKYTHERA MECHANISM] Astronomical Clockwork

ZODIAC DIAL

Showed the 12

CALENDAR DIAL Displayed 365 days of a year. constellations along the ecliptic, the

EGYPTIAN



LUNAR POINTER

Showed the position of the moon FRONT-PLATE INSCRIPTIONS with respect to the constellations on Described the rising and setting times of important stars throughout the year the zodiac dial.

This exploded view of the mechanism shows all but one of the 30 known gears, plus a few that have been hypothesized. Turning a crank on the side activated all the gears in the mechanism and moved pointers on the front and back dials: the arrows colored blue, red and yellow explain how the motion transmitted from one gear to the next. The user would choose a date on the Egyptian, 365-day calendar dial on the front or on the Metonic, 235-lunar-month calendar on the back and then read the astronomical predictions for that time-such as the position and phases of the moon-from the other dials. Alternatively, one could turn the crank to set a particular event on an astronomical dial and then see on what date it would occur. Other gears, now lost, may have calculated the positions of the sun and of some or all of the five planets known in antiquity and displayed them via pointers on the zodiac dial.

METONIC GEAR TRAIN

Calculated the month in the Metonic calendar, made of 235 lunar months, carcharted the month in the metonic carendar, made of 235 lunar months, and displayed it via a pointer (A) on the Metonic calendar dial on the back. A pin (B) at the pointer's tip followed the spiral groove, and the pointer extended in length as it reached months marked on successive, outer twists. Auxiliary gears () turned a pointer () on a smaller dial indicating four-year cycles of Olympiads and other games. Other gears moved a pointer on another small dial (), which may have indicated a 76-year cycle.



the position of the moon on the zodiac dial.



ECLIPSE GEAR TRAIN

Calculated the month in the 223-lunar-month Saros cycle of recurring eclipses. It displayed the month on the Saros dial with an extensible pointer (A) similar to the one on the Metonic dial. Auxiliary gears moved a pointer B on a smaller dial. That pointer made one third of a turn for each 223-month cycle to indicate that the corresponding eclipse time would be offset by eight hours.

METONIC CALENDAR DIAL

Displayed the month on a 235-lunar-month cycle arranged on a spiral.

OLYMPIAD DIAL

Indicated the years of the ancient Olympics and other games.

SAROS LUNAR ECLIPSE DIAL

Inscriptions on this spiral indicated the months in which lunar and solar eclipses can occur.

cle, the large 223-tooth gear also carried the epicyclic system noticed by Price: a sandwich of two small gears attached to the larger gear in teacup-ride fashion. Each epicyclic gear also connected to another small gear. Confusingly, all four small gears appeared to have the same tooth count-50-which seemed nonsensical because the output would then be the same as the input.

After months of frustration, I remembered that Wright had observed that one of the two epicyclic gears has a pin on its face that engages with a slot on the other. His key idea was that the two gears turned on slightly different axes, separated by about a millimeter. As a consequence, the angle turned by one gear alternated between being slightly wider and being slightly narrower than the angle turned by the other gear. Thus, if one gear turned at a constant rate, the other gear's rate kept varying between slightly faster and slightly slower.

Ask for the Moon

Although Wright rejected his own observation, I realized that the varying rotation rate is precisely what is needed to calculate the moon's motion according to the most advanced astronomical theory of the second century B.C., the one often attributed to Hipparchos of Rhodes. Before Kepler (A.D. 1605), no one understood that orbits are elliptical and that the moon accelerates toward the perigee-its closest point to Earthand slows down toward the apogee, the opposite point. But the ancients did know that the moon's motion against the zodiac appears to periodically slow down and speed up. In Hipparchos's model, the moon moved at a constant rate around a circle whose center itself moved around a circle at a constant rate-a fairly good approximation of the moon's apparent motion. These circles on circles, themselves called epicycles, dominated astronomical thinking for the next 1,800 years.

There was one further complication: the apogee and perigee are not fixed, because the ellipse of the moon's orbit rotates by a full turn about every nine years. The time it takes for the body to get back to the perigee is thus a bit longer than the time it takes it to come back to the same point in the zodiac. The difference was just 0.112579655 turns a year. With the input gear having 27 teeth, the rotation of the large gear was slightly too big; with 26 teeth, it was slightly too small. The right result seemed to be about halfway in between. So I tried the impossible idea that the input gear had 26 1/2 teeth. I pressed the key on my calculator, and it gave 0.112579655-

[A USER'S MANUAL] **How to Predict** an Eclipse

Operating the Antikythera mechanism may have required only a small amount of practice and astronomical knowledge. After an initial calibration by an expert, the mechanism could provide fairly accurate predictions of events several decades in the past or future. The inscriptions on the Saros dial, coming at intervals of five or six months, corresponded to months when Earth, the sun and the moon come to a near alignment (and so represented potential solar and lunar eclipses) in a 223-lunar-month cycle. Once the month of an eclipse was known, the actual day could be calculated on the front dials using the fact that solar eclipses always happen during new moons and lunar eclipses during full moons.

exactly the right answer. It could not be a coincidence to nine places of decimals! But gears cannot have fractional numbers of teeth.

Then I realized that $26\frac{1}{2} \times 2 = 53$. In fact, Wright had estimated a crucial gear to have 53 teeth, and I now saw that that count made everything work out. The designer had mounted the pin and slot epicyclically to subtly slow down the period of its variation while keeping the basic rotation the same, a conception of pure genius. Thanks to Edmunds, we also realized that the epicyclic gearing system, which is in the back of the mechanism, moved a shaft that turned inside another, hollow shaft through the rest of the mechanism and to the front, so that the lunar motion could be represented on the zodiac dial and on the lunar phase display. All gear counts were now explained, with the exception of one small gear that remains a mystery to this day.

Further research has caused us to make some modifications to our model. One was about a small subsidiary dial that is positioned in the back, inside the Metonic dial, and is divided into four quadrants. The first clue came when I read the word "NEMEA" under one of the quadrants. Alexander Jones, a New York University historian, explained that it refers to the Nemean Games, one of the major athletic events in ancient Greece. Eventually we found, engraved round the four sectors of the dial, most of "ISTHMIA," for games at Corinth, "PYTHIA," for games at Delphi, "NAA," for minor games at Dodona, and "OLYMPIA," for the most important games of the Greek world, the Olympics. All games took place every two or four years. Previously we had considered the mechanism to be



Turn the crank to move time forward until the pointer on the Saros dial points to an eclipse inscription. The inscription will indicate month and time of the day (but not the day) of an eclipse and whether it will be solar or lunar.

Lunar pointer

CALCULATE DAY

Adjust the crank until the lunar and solar pointers are aligned (*for a solar eclipse*) or at 180 degrees (*for a lunar eclipse*). The Egyptian calendar pointer will move corre-spondingly and indicate the day of the eclipse

purely an instrument of mathematical astronomy, but the Olympiad dial-as we named itgave it an entirely unexpected social function.

to the corresponding month on the Saros (eclipse) dial.

Twenty-nine of the 30 surviving gears calculate cycles of the sun and the moon. But our studies of the inscriptions at the front of the mechanism have also yielded a trove of information on the risings and settings of significant stars and of the planets. Moreover, on the "primary" gearwheel at the front of the mechanism remnants of bearings stand witness to a lost epicyclic system that could well have modeled the back-and-forth motions of the planets along the ecliptic (as well as the anomalies in the sun's own motion). All these clues strongly support the inclusion of the sun and of at least some of the five planets known in ancient times-Mercury, Venus, Mars, Jupiter and Saturn.

Wright built a model of the mechanism with epicyclic systems for all five planets. But his ingenious layout does not agree with all the evidence. With its 40 extra gears, it may also be too complex to match the brilliant simplicity of the rest of the mechanism. The ultimate answer may still lie 50 meters down on the ocean floor.

Eureka?

The question of where the mechanism came from and who created it is still open. Most of the cargo in the wrecked ship came from the eastern Greek world, from places such as Pergamon, Kos and Rhodes. It was a natural guess that Hipparchos or another Rhodian astronomer built the mechanism. But text hidden between the 235 monthly scale divisions of the Metonic calendar contradicts this view. Some of the month names were used only in specific locations in the ancient Greek world and suggest a Corinthian origin. If the mechanism was from Corinth itself, it was almost certainly made before Corinth was completely devastated by the Romans in 146 B.C. Perhaps more likely is that it was made to be used in one of the Corinthian colonies in northwestern Greece or Sicily.

Sicily suggests a remarkable possibility. The island's city of Syracuse was home to Archimedes, the greatest scientist of antiquity. In the first century B.C. Roman statesman Cicero tells how in 212 Archimedes was killed at the siege of Syracuse and how the victorious Roman general, Marcellus, took away with him only one piece of plunder-an astronomical instrument made by Archimedes. Was that the Antikythera mechanism? We believe not, because it appears to have been made many decades after Archimedes died. But it could have been constructed in a tradition of instrument making that originated with the eureka man himself.

Many questions about the Antikythera mechanism remain unanswered-perhaps the greatest being why this powerful technology seems to have been so little exploited in its own era and in succeeding centuries.

In Scientific American, Price wrote:

It is a bit frightening to know that just before the fall of their great civilization the ancient Greeks had come so close to our age, not only in their thought, but also in their scientific technology.

Our discoveries have shown that the Antikythera mechanism was even closer to our world than Price had conceived.

MORE TO EXPLORE

An Ancient Greek Computer. Derek J. de Solla Price in Scientific American, Vol. 200, No. 6. pages 60-67; June 1959.

Gears from the Greeks: The Antikythera Mechanism-A Calendar Computer from ca. 80 B.C. Derek de Solla Price in Transactions of the American Philosophical Society, New Series, Vol. 64, No. 7, pages 1-70; 1974.

Decoding the Ancient Greek Astronomical Calculator Known as the Antikythera Mechanism. Tony Freeth et al. in Nature, Vol. 444, pages 587-591; November 30, 2006.

Calendars with Olympiad Display and Eclipse Prediction on the Antikythera Mechanism. Tony Freeth. Alexander Jones, John M. Steele and Yanis Bitsakis in Nature, Vol. 454, pages 614-617; July 31, 2008.

The Antikythera Mechanism Research Project: www. antikythera-mechanism.gr

Historical Perspectives

- Abu Ali al-Hasan ibn al-Haytham (965-1039)
- AKA Alhazen or "The Physicist"
- Greatest scientist of the middle ages
- Contributed to mathematics, physics, optics, astronomy, anatomy, medicine, engineering, philosophy, psychology
- Pioneered the scientific method, modern optics and experimental physics
- Polymath: authored over 200 treatises, including influential "Book of Optics"
- Influenced Leonardo da Vinci, Bacon, Descartes, Kepler, Galileio and Newton









THE NEW SCIENTIFIC METHOD



Historical Perspectives Leonardo of Pisa (1170–1250)

- Better known as "Fibonacci"
- Considered the most talented mathematician of the middle ages
- Published (1202) "Liber Abaci" –
 "The Book of Calculation"
- Introduced Hindu-Arabic positional number system in Europe
- Popularized Fibonacci sequence

1 1 2 3 5 8 13 21 34 55 89


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The Fibonacci Quarterly

Official Publication of The Fibonacci Association















Robert Fischer CAROLYN BORODEN BONACCE APPLICATIONS ID STRATEGIES FOR TRADERS

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Robert Fischer

FIBONACCI ANALYSIS



Roger Herz-Fischler

- René Descartes (1596-1650)
- Father of modern philosophy
- Invented Cartesian coordinates, analytic geometry, heuristics
- Characterized paradoxes & falacies
- Discovered momentum conservation
- Authored "Principia Philosophiae"
- Pioneered methodological skepticism
 "Cogito ergo sum" "Je pense, donc je suis "
- "Discours de la Méthode" (1637) one of the most influential works in modern science
- Pioneered the scientific method & revolution "For it is not enough to have a good mind: one must use it well." - Descartes



DISCOURS DE LA METHODE Pour bien conduire fa raifon, & chercher la verité dans les feiences. PLUS LA DIOPTRIQVE. LES METEORES. ET LA GEOMETRIE. Qui font des effais de cete METHODE.



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RENÉ DESCARTES EXPLAINS THE COORDINATE SYSTEM WHICH TIES TOGETHER ALGEBRA AND GEOMETRY







B/W QuickCam

a.cidadao@mail.telepac.pt

Pierre de Fermat (1601-1665)

- Father of modern number theory
- Lawyer, Parlement of Toulouse
- Laid groundwork for calculus
- Contributions to optics, probability, and analytic geometry
- Fermat numbers, primes, perfect #'s
- Descartes' Law of refraction
- Reponsible for many open problems
- "Fermat's Last Theorem" (1637-1995)
- Recognized "principle of least action" and "principle of least time" in physics
- Influenced Newton and Leibniz





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-SIR ROGER PENROSE, NEW YORK

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N SINGH Foreword by John Lynch





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Yves Hellegouarch

Invitation to the Mathematics of Fermat-Wiles



Paulo Ribenboim

Fermat's Last Theorem

Alf van der Poorten





PROBLEM

AMIR D. ACZEL



Pierre de Fermat 1001-1005









Fermat Prize for Mathematics Research





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Music **by Joshua Rosenblum** Book by **Joanne Sydney Lessner** Lyrics by **Lessner and Rosenblum**

TANGO

FERMAT'S

THE YORK THEATRE COMPAN

A Musical Fantasy inspired by Andrew Wiles and his encounters with Fermat's Last Theorem

"Rollicking! Whimsical! Catchy & Clever!" - The New York Times

In 1993 Andrew Wiles stunned the world when he announced a solution to "Fermat's Last Theorem," the famous unsolved mathematics problem set forth by Pierre de Fermat in 1637. In the musical *Fermat's Last Tango*, the fictional character Daniel Keane earns overnight acclaim when he presents his findings. However, fanfare soon gives way to doubt when the reincarnated Fermat discovers a hole in Keane's proof. The singular pursuit by Keane to correct this flaw results in a love triangle involving himself, his wife, and mathematics—the story of which is brought to life by Fermat and his immortal friends from the "AfterMath," namely: Pythagoras, Euclid, Newton, and Gauss. The musical is both a cheerful romp through history and a personal confrontation with destiny. It provides a testament to the extraordinary excitement of mathematics and its unparalleled beauty.

The Composer Joshua Rosenblum enjoyed mathematics while studying music at Yale along with the author, his wife Joanne Sydney Lessner. They both take an active role in the New York music community. This recording was captured by David Stern and his Emmy Award-winning crew during a performance at the York Theatre Company in New York City.



STARRING

Carl Friedrich Gauss / Reporter Anna Keane Pythagoras / Reporter Pierre de Fermat Daniel Keane Euclid / Reporter Sir Isaac Newton / Reporter GILLES CHIASSON EDWARDYNE COWAN MITCHELL KANTOR JONATHAN RABB CHRIS THOMPSON CHRISTIANNE TISDALE CARRIE WILSHUSEN

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Approximate Running Time:

Color/Not Rated/VHS/NTSC Produced by The Clay Mathematics

Institute, Cambridge, MA Arthur Jaffe, Producer David Stern, Director

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100 minutes



Illustrated Guide Enclosed

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ERM,

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Followed by an Interview with Andrew Wiles

Blaise Pascal (1623-1662)

- Mathematician, physicist, philosopher
- Studied fluids, pressure, vacuum
- Helped pioneer projective geometry, probability, and the scientific method
- Influenced modern economics
- "Pascal's triangle", "Pascal's law"
- Invented hydraulic press and syringe
- Constructed a mechanical calculator
- Used humor, wit, and satire in writings
- Influenced Voltaire and Rousseau
- Inagurated the world's first bus line
- SI unit of pressure "pascal"









THE

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"I speak as to wise men, judge ye what I say."-1 Con. z. 15.

Translated from the original French into various languages.

Paris	
Biennu.	Fondan.
Cologne,	Edinburgh.
Fasle.	Slusgow.





Sir Isaac Newton (1643-1727)

- Mathematician, physicist, astronomer, philosopher, alchemist, theologian
- One of history's most influential people
- "Principia Mathematica" (1687)
- Invented calculus, theory of gravitation
- Founded "Newtonian mechanics"
- Discovered laws of motion, inertia
- "Newtonian fluid", "Newtonian Universe"
- Advanced the Scientific Revolution
- Developed practical reflecting telescope, theory of color, "Newton's method"
- SI unit of force: newton





PHILOSOPHIÆ NATURALIS PRINCIPIA MATHEMATICA

NO 6

Autore J S. NEWTONG Trin Coll. Canado. Soc. Matheleos Professore Lucasiano, & Societatis Regain Sodali. et Scietatis Regin Societatis preside

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Leonhard Euler (1707–1783)

- Invented graph theory
- "Bridges of Königsberg", Prussia
- Eulerian tour
- Euler's formula: V + F = E + 2
- Euler's number: e
- Euler's identity: $e^{i\pi} + 1 = 0$
- Major contributions to analysis, algebra, calculus, number theory, topology, optics, fluid dynamics, mechanics, astronomy, education







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LEONHARDO EULERO,

Professore Regio, & Academia Imperialis Scientiarum Petropolitan & Socio.



LAUSANNÆ & GENEVÆ, Apud MARCUM-MICHAELEM BOUSQUET & Socios.

MDCCXLIV.

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IN

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HENRY HUNTER, D.D.

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AY 2007

Leonhard Euler

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Leonhard Euler 1707-1758



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17th Workshop on Hereditary Graph Properties SEVENTH CRACOW CONFERENCE ON GRAPH THEORY "RYTRO '14"

September 14-19, 2014 Rytro, Poland

The meeting is next in the series of former Cracow Conferences on Graph Theory organized in <u>Niedzica</u> (1990), <u>Zgorzelisko</u> (1994), <u>Kazimierz Dolny</u> (1997), <u>Czorsztyn</u> (2002), <u>Ustroń</u> (2006) and <u>Zgorzelisko</u> (2010).

Selected papers presented at the conference will be published in a Special Issue of <u>Discrete</u> <u>Mathematics</u> dedicated to the 7th Cracow Conference on Graph Theory. Already six Special Issues of DM were devoted to our conferences (volumes: <u>121</u>, <u>164</u>, <u>236</u>, <u>307/11-12</u>, <u>309/22</u>, <u>312/14</u>).

Invited speakers: <u>Ralph Faudree</u>, University of Memphis, USA

Linear Forests on Hamiltonian Cycles

András Gyárfás, Hungarian Academy of Sciences, Budapest, Hungary

Vertex covers by monochromatic pieces - results and problems

Wilfried Imrich, Montanuniversität Leoben, Austria

Graph Products and Symmetry Breaking in Graphs

Ken-ichi Kawarabayashi, National Institute of Informatics, Tokyo, Japan

Coloring graphs with some forbidden or restricted configurations

Jan Kratochvil, Charles University, Prague, Czech Republic

Extending Partial Geometric Representations of Graphs

Dieter Rautenbach, Universität Ulm, Germany



INTERNATIONAL CONFERENCE ON GRAPH THEORY AND ITS APPLICATIONS

December 16-19, 2015 Amrta School of Engineering, Coimbatore, India

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About The Conference

This will be a Four-day Conference in Graph Theory, Graph Algorithms and its applications. It will be focusing on the subareas in graph theory that has applications in Optimization, Computing Techniques, VLSI Design and Testing, Image Processing, and Network Communications. The goal of this conference is to bring top researchers in these areas to Amrita to foster collaboration and to expose students to important problems in the growing field. The conference is expected to stimulate joint work among researchers from India and abroad and attract research students and postdoctoral fellows who work in graph theory. The Conference will cover a broad range of topics in Graph Theory. The topics include, but are not limited to:

- · Graph Theory
- · Algebraic Graph Theory
- · Algorithms and Computing Techniques
- Graph Optimization
- · VLSI Design and Testing
- Image Processing
- Networks
- Communications and Control Theory

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First, i wish to express my deepest gratitude to those who helped to make MTAGT a reality..

Generous financial support was provided by the National Science Foundation, Villanova (VU) College of Arts and Sciences, VU Office of Research and Graduate Programs, VU Office of Reasearch and Sponsored Projects, VU Office of the Vice President of Academic Affairs, and VU Office of the President.

Staffing support was provided by Marie O'Brien, Lorraine McGraw, Doug Norton, Najib Nadi, Taylor Berrang, Carrie Caswell, Carolyn Romano, Joseph Reiter, and Pat Woldar.

An indispensable role was played by the Office of Conference Services. In particular, I wish to mention Ron Diment and Stefanie Austinat. I also wish to thank Elisa Wiley and Clete Rickert for web support.

Last but not least, I wish to thank those who attended MTAGT. When all is said and done, the success of a conference depends integrally on the qualifications of its participants.

We had a wonderfully strong and diverse group. More than half of the 110 participants traveled to Villanova from 20 different nations. Over 20% of the participants were female, and roughly 25% were graduate students/recent PhDs. We are most proud of these demographics.

The conference presentations were truly inspired. I am most pleased to now report their online availability:

<video recordings of plenary talks>

<Slides of all talks>

Mathematics alone does not make a successful mathematics conference. It is a desirable (if not imperative) to promote healthy multicultural relations, and unobstructed lines of communication between participants. As

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Applications of Graphs Erdős numbers - "6 degrees" of separation



Historical Perspectives

Carl Friedrich Gauss (1777–1855)

- "Prince of Mathematics"
- Founded modern number theory
- Authored "Disquisitiones Arithmeticae"
- Fundamental Theorem of Algebra
- Major contributions to astronomy, optics electromagnetism, statistics, geometry
- Gaussian distribution, Gaussian elimination Gaussian noise, Gaussian integers & primes Gauss' Law, Gauss' constant, "degaussing"
- SI unit of magnetic field strength: gauss
- Students: Dedekind, Riemann, Bessel



DISQUISITIONES

ARITHMETICAE















Historical Perspectives

William R. Hamilton (1805-1865)

- Mathematician, physicist, and astronomer
- Contributed to algebra, mechanics, optics
- Formulated Hamiltonian mechanics
- Discovered quaternions, conical refraction, Hamilton function, Hamilton principle, Hamiltonian group
- Invented "Icosian Calculus", dot & cross products, Hamiltonian paths
- Influenced computer graphics, mechanics, electromagnetism, relativity, quantum theory, vector algebra



Here as he walked by on the 16th of October 1843 Sir William Rowan Hamilton in a flash of genius discovered the fundamental formula for quaternion multiplication $i^2 = j^2 = k^2 = ijk = -1$ & cut it on a stone of this bridge



Octonions: Generalization of Quaternions

- Non-associative! (e.g., $(ij)K=-E \neq E=i(jK)$)
- Discovered by John Graves (1843), friend of Hamilton
- Useful in general relativity, quantum logic, string theory





Mnemonic diagram for unit octonions products

Sedenions: Generalization of Octonions

• Non-alternative! (i.e., x(xy)=(xx)y doesn't hold)

×	1	e ₁	e ₂	e ₃	e4	e 5	e 6	e 7	e 8	e9	e 10	e ₁₁	e ₁₂	e ₁₃	e ₁₄	e 15
1	1	e 1	e 2	e 3	e 4	e 5	e 6	e 7	e_8	e 9	e ₁₀	e ₁₁	e ₁₂	e ₁₃	e ₁₄	e 15
e 1	e 1	-1	e 3	-e 2	e 5	- e 4	-e 7	e 6	e 9	- e 8	- e 11	e ₁₀	- e 13	e ₁₂	e 15	- e 14
e ₂	e ₂	- e 3	-1	e 1	e 6	e 7	- <i>e</i> 4	- e 5	e 10	e 11	- e 8	- <i>e</i> 9	- e 14	- e 15	e ₁₂	e ₁₃
e ₃	e 3	e 2	-e1	-1	e 7	- e 6	e 5	- <i>e</i> 4	e 11	- e ₁₀	e 9	- e 8	- e 15	e 14	- e 13	e ₁₂
e4	e 4	- <i>e</i> 5	- e 6	-e 7	-1	e 1	e ₂	e 3	e ₁₂	e 13	e ₁₄	e 15	- <i>e</i> 8	- <i>e</i> 9	- e ₁₀	-e ₁₁
e 5	e 5	e 4	-e 7	e 6	- e 1	-1	- e 3	e ₂	e 13	- e ₁₂	e 15	- e 14	e 9	- e 8	e ₁₁	- e ₁₀
e 6	e 6	e 7	e 4	- e 5	-e 2	e 3	-1	- e 1	e 14	- e 15	- e 12	e ₁₃	e 10	-e ₁₁	- e 8	e 9
e ₇	e 7	- e 6	e 5	e_4	- e 3	-e 2	e 1	-1	e 15	e ₁₄	- e 13	- e ₁₂	e 11	e ₁₀	- <i>e</i> 9	- e 8
e ₈	e 8	- <i>e</i> 9	- e ₁₀	- e 11	- e ₁₂	- e 13	- e 14	- e 15	-1	e 1	e 2	e 3	e_4	e 5	e 6	e 7
e9	e 9	e_8	- e 11	e ₁₀	- e 13	e ₁₂	e 15	- <i>e</i> ₁₄	- e 1	-1	- e ₃	e ₂	- e 5	e_4	e 7	- e 6
e 10	e ₁₀	e ₁₁	e 8	- e 9	- e ₁₄	- e 15	e ₁₂	e ₁₃	-e 2	e 3	-1	-e ₁	- e 6	-e 7	e 4	e 5
e ₁₁	e ₁₁	- e ₁₀	e 9	e 8	- e 15	e ₁₄	- e 13	e ₁₂	- e 3	-e ₂	e 1	-1	-e 7	e 6	- e 5	e 4
e ₁₂	e ₁₂	e 13	e ₁₄	e 15	e_8	<i>−e</i> 9	- e ₁₀	- <i>e</i> ₁₁	- e 4	e 5	e 6	e 7	-1	- <i>e</i> 1	-e ₂	-e 3
e ₁₃	e 13	- e ₁₂	e 15	- <i>e</i> ₁₄	e 9	e 8	e ₁₁	- e ₁₀	-e 5	- e 4	e 7	- e 6	e 1	-1	e 3	-e 2
e ₁₄	e ₁₄	- e 15	- e ₁₂	e 13	e ₁₀	- e 11	e 8	e 9	- e 6	-e 7	- e 4	e 5	e 2	- e 3	-1	e 1
e 15	e 15	e ₁₄	- e 13	- e ₁₂	e ₁₁	e ₁₀	- <i>e</i> 9	e 8	- e 7	e 6	- e 5	- e 4	e 3	e 2	- e 1	-1

Generalized Numbers



Theorem: some real numbers are not finitely describable! Theorem: some finitely describable real numbers are not computable!

Historical Perspectives

George Boole (1815-1864)

- Mathematician and philosopher
- Invented symbolic / Boolean logic
- Invented Boolean algebra, i.e. "calculus of reasoning"
- A founder of computer science
- "An Investigation into the Laws of Thought"
- Influenced De Morgan, Schröder, Shannon
- All modern computers, electronics, phones, data transmission, rely on Boolean principles



ON WHICH ARE FORMED THE MATHEMATICAL THEORIES OF LOGIC AND PROBABILITIES.

LAWS OF THOUGHT.

AN INVESTIGATIO

GEORGE BOOLE, LL.D PROTERISOR OF MAXIMENTICS DE QUERT'S COLLEGE, CORE.

LONDON: WALTON AND MABERLY, PER GOWER-STREET, AND IVY-LANE, PATERNOSTER-ROW-CAMBRIDGE: MACUILAIN AND CO. Univ Calif. DD. 1855, Do Microwood 8









Mozart writing the digital version of his symphony No. 38 in D major.

Historical Perspectives

Augustus De Morgan (1806-1871)

- Mathematician and logician
- Developed logic & mathematical induction
- De Morgan's Laws in logic & set theory
- Invented relational algebra
- Corresponded extensively with Hamilton
- Influenced Russell, Whitehead, and Tarski
- Studied paradoxes







Historical Perspectives

Charles Babbage (1791-1871)

- Mathematician, philosopher, inventor mechanical engineer, and economist
- The father of computing
- Built world's first mechanical computer
 - the "difference engine" (1822)
- Originated the programmable computer
 - the "analytical engine" (1837)
- Worked in cryptography
- Developed Babbage's principle of division of labor





Babbage's Difference Engine

- World's first mechanical computer
- Designed in 1822, redesigned in 1847-1849
- 25,000 parts, 15 tons, 8ft tall, 31 digits of precision
- Tabulated polynomial functions, used Newton's method
- Approximated logarithmic and polynomial functions
- Used decimal number system and hand-crank



Babbage's Difference Engine











Babbage's difference engine built from Mechano and Lego







Babbage's Analytical Engine

- World's first general-purpose computer
- Designed in 1837, redesigned throughout Babbage's life
- Turing-complete, memory: 1000x50 digits (21 kB)
- Fully programmable "CPU", used punched cards
- Featured ALU, "microcode", loops, and printer!
- Could multiply two 20-digit numbers in 3 min
- Few components built by Babbage; constructed in 1991
















































a<mark>n de la constante de la</mark>























Charles Babbage Suranan Professor of Mathematics in the University of Cambridge:

Published 1" May 1833 by M.Sall



THE

MUSEUM,

Register, Journal,

GAZETTE,

OCTOBER 6, 1832-MARCH 31, 1833.

VOL. XVIII.

⁶ In 1435, a low-mit was enriced on at Strasburgh between John Gattenberg, a particularity of Means, exclusives for mechanical ingeneity, and Drizeban, a berghet of the effy, who was list parter in a sequence of the sequence of the second sec

LONDON: PUBLISHED BY M. SALMON, MECHANICS' MAGAZINE OFFICE, No. 6, PETERMONOUNE COURT. 1833.

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4 × Find:

- Countess Ada Lovelace (1815-1852)
- Daughter of Lord Byron
- Tutored in math and logic by De Morgan
- Wrote the "manual" for Babbage's analytical engine, as well as programs for it
- World's first computer programmer!
- Foresaw the vast potential of computers
- Babbage: "The Enchantress of Numbers"
- DoD's Ada language "MIL-STD-1815"





The International Language for Software Engineering









Norreted and Edited by Betty Alexandra Toole





Ada Byron, Lady Lovelace 1815-1852





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Ada





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Science

"IT'S A THRILLER." - NEW SCIENTIST

BENJAMIN WOOLLEY

ROMANCE, REASON, and BYRON'S DAUGHTER

nsed

council leaders want to ban NEWS ANALYSIS 10 Beware of SaaS risk

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ADA LOVELACE DAY AIMS TO RAISE AWARENESS OF WOMEN'S ACHIEVEMENTS

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website.

Ada Lovelace notes on "Sketch of the Analytical Engine Invented by Charles Babbage", by L. F. Menabrea, 1843

Her notes (three times longer than the paper itself!) contain the world's first computer program (for calculating Bernoulli numbers):

			Var	iables	for D	ata						Variables for Results						
Number of Operations	of Operations	$^{1}\mathrm{V}_{0}$	$^{1}\mathrm{V}_{1}$	$^{1}\mathrm{V}_{2}$	$^{1}\mathrm{V}_{3}$	$^{1}\mathrm{V}_{4}$	$^{1}\mathrm{V}_{5}$	$^{0}V_{6}$	$^{0}\mathrm{V}_{7}$	$^{0}\mathrm{V}_{8}$	$^{0}\mathrm{V}_{9}$	$^{0}V_{10}$	$^{0}V_{11}$	$^{0}V_{12}$	⁰ V ₁₃	$^{0}V_{14}$	$^{0}V_{15}$	$^{0}V_{16}$
Oper	pera	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+
r of		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
admu	Nature	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
ñ	ž	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
		m	n	d	m'	n'	d'										$\boxed{\frac{dn'-d'n}{mn'-m'n} = x}$	$\boxed{\frac{d'm-dm}{mn'-m'n}=y}$
$\frac{1}{2}$	××	m 	 n		$\frac{\dots}{m'}$	n'		mn'	m'n									
$\frac{3}{4}$	× ×	· · · · ·	 0	d 	· · · · ·	· · · · ·	d'	· · · · ·	 	$\frac{dn'}{\dots}$	d'n							
$\frac{5}{6}$	× ×	0 	 	0	0	····	0 	· · · · ·	 	 	· · · · ·	d'm	dm'					
7 8	-	 	· · · · ·	· · · · ·	· · · · ·	····	· · · · ·	0	0 	 0	0			(mn' - m'n) 	(dn' - d'n)			
9 10	- ÷	 	····	· · · · ·	· · · · ·	····	···· ····	· · · · ·	· · · · ·	····		0	0 	(mn' - m'n)	0	(d'm - dm')	$\frac{dn'-d'n}{mn'-m'n} = x$	
11	÷													0		0	····	$\tfrac{d'm-dm'}{mn'-m'n}=y$

World's first computer program (for calculating Bernoulli numbers), by Ada Lovelace, 1843:

							Data									Working Variables					Variable	es
e						$^{1}V_{1}$	$^{1}V_{2}$	$^{1}V_{3}$	$^{0}V_{4}$	$^{0}V_{5}$	$^{0}V_{6}$	$^{0}V_{7}$	$^{0}V_{8}$	⁰ V9	⁰ V ₁₀	⁰ V ₁₁	⁰ V ₁₂	⁰ V ₁₃	$^{1}V_{21}$	$^{1}\mathrm{V}_{22}$	$^{1}V_{23}$	$^{0}V_{24}\ldots$
ation	tion					0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
Oper	pera	Variables acted	Variables receiving	Indication of change in the	Statement of Results	0	0	0	0	0	0	0	0	0	0	0	0	0	it a	t. a	а <u>;</u>	0
er of	of C	upon	results	value on any Variable		0	0	0	0	0	0	0	0	0	0	0	0	0	B in a dec. fract	B in a dec. fract	B in a dec. fract	0
Numbe	Nature of Operat						2	4	0	0	0	0	0		0	0	0	0				0
Z	z						2	n											В1	В3	B ₅	B ₇
		1	1	$\int {}^{1}V_2 = {}^{1}V_2 \Big\}$																		
1	×	$^{1}V_{2} \times ^{1}V_{3}$	${}^{1}V_{4}, {}^{1}V_{5}, {}^{1}V_{6}$	$ \left\{ \begin{array}{ccc} v_2 & - & v_2 \\ {}^1V_3 & = & {}^1V_3 \\ {}^1V_4 & = & {}^2V_4 \\ {}^1v_4 & = & {}^1v_4 \end{array} \right\} $	= 2n		2	n	2n	2n	2n											
2	-	${}^{1}V_{4} - {}^{1}V_{1}$	² V ₄	$ 1^{*}V_{1} = {}^{*}V_{1} $	= 2n - 1	1			2n - 1													
3	+	${}^{1}V_{5} + {}^{1}V_{1}$	² V ₅	$\left\{ \begin{array}{ll} {}^{1}V_{5} & = & {}^{2}V_{5} \\ {}^{1}V_{1} & = & {}^{1}V_{1} \end{array} \right\}$	= 2n + 1	1				2n + 1												
4	÷	$^2\mathrm{V}_5\div ^2\mathrm{V}_4$	$^{1}\mathrm{V}_{11}\ \ldots \ldots$	$\left\{\begin{array}{ccc} {}^{2}\mathrm{V}_{5} & = & {}^{0}\mathrm{V}_{5} \\ {}^{2}\mathrm{V}_{4} & = & {}^{0}\mathrm{V}_{4} \end{array}\right\}$	$=\frac{2n-1}{2n+1}\ldots\ldots\ldots\ldots$				0	0						$\frac{2n-1}{2n+1}$						
5	÷	$^1\mathrm{V}_{11}\div ^1\mathrm{V}_2$	$^{2}V_{11}$	$\begin{cases} {}^{1}V_{11} = {}^{2}V_{11} \\ {}^{1}V_{2} = {}^{1}V_{2} \end{cases}$	$= \frac{1}{2} \cdot \frac{2n-1}{2n+1} \dots$		2									$\frac{1}{2} \cdot \frac{2n-1}{2n+1}$						
6	_	$^{0}V_{13} - {}^{2}V_{11}$	$^{1}V_{13}$	$\begin{bmatrix} 2^{2}V_{11} & = & {}^{0}V_{11} \\ {}^{0}V_{12} & = & {}^{1}V_{12} \end{bmatrix}$	$= -\frac{1}{2} \cdot \frac{2n-1}{2n+1} = A_0 \dots$. 0		$= -\frac{1}{2} \cdot \frac{2n-1}{2n+1} = A_0$				
7	_	${}^{1}V_{3} - {}^{1}V_{1}$	$^{1}V_{10}$	$ \left\{ \begin{array}{ccc} {}^{1}V_{3} & = & {}^{1}V_{3} \\ {}^{1}V_{1} & = & {}^{1}V_{1} \end{array} \right\} $	= n - 1(= 3)	1		n							n-1							
8	+	${}^{1}V_{2} + {}^{0}V_{7}$	¹ V ₇	$ \left\{ \begin{array}{ccc} v_1 & = & v_1 \\ {}^1V_2 & = & {}^1V_2 \\ {}^0V_7 & = & {}^1V_7 \end{array} \right\} $	= 2 + 0 = 2		2					2										
9		$^{1}V_{6} \div ^{1}V_{7}$	³ V ₁₁	$\int_{1}^{1} V_{6} = {}^{1} V_{6}$	$=\frac{2n}{2}=A_1$						2n	2				$\frac{2n}{2} = A_1$						
10				$\begin{bmatrix} 0 V_{11} &= & {}^{3}V_{11} \\ 1 V_{22} &= & {}^{1}V_{22} \end{bmatrix}$	2											$\frac{2n}{2} = A_1$	p 2n p 4		, D			
		${}^{1}V_{21} \times {}^{3}V_{11}$		$\begin{bmatrix} 0 V_{11} \\ 1 V_{12} \\ 0 \end{bmatrix} = \begin{bmatrix} 0 V_{11} \\ 0 V_{12} \end{bmatrix}$	$= B_1 \cdot \frac{2n}{2} = B_1 A_1 \dots \dots$											$\frac{2}{2} = A_1$	_	(, , , , , , , , , , , , , , , , , , ,	B ₁			
11	+	$^{1}V_{12} + ^{1}V_{13}$		$\begin{bmatrix} -v_{13} \\ -v_{13} \end{bmatrix} = \begin{bmatrix} -v_{13} \\ -v_{13} \end{bmatrix}$	$= -\frac{1}{2} \cdot \frac{2n-1}{2n+1} + B_1 \cdot \frac{2n}{2} \dots \dots$												0	$\left\{-\frac{1}{2}\cdot\frac{2n-1}{2n+1}+\mathbf{B}_1\cdot\frac{2n}{2}\right\}$				
12	-	${}^{1}V_{10} - {}^{1}V_{1}$	² V ₁₀	$V_1 = V_1$	$= n - 2(= 2) \dots$	1									n - 2							
13	[-]	${}^{1}\mathrm{V}_{6}-{}^{1}\mathrm{V}_{1}$	² V ₆	$\left\{ \begin{array}{ccc} {}^{1}\mathrm{V}_{6} & = & {}^{2}\mathrm{V}_{6} \\ {}^{1}\mathrm{V}_{1} & = & {}^{1}\mathrm{V}_{1} \end{array} \right\}$	= 2n - 1	1					2n - 1											
14	+	${}^{1}\mathrm{V}_{1} + {}^{1}\mathrm{V}_{7}$	$^{2}V_{7}$	$\left\{ \begin{array}{ccc} {}^{1}\mathrm{V}_{1} & = & {}^{1}\mathrm{V}_{1} \\ {}^{1}\mathrm{V}_{7} & = & {}^{2}\mathrm{V}_{7} \end{array} \right\}$	= 2 + 1 = 3	1						3										
15	÷	$^2\mathrm{V}_6 \div ^2\mathrm{V}_7$	${}^{1}V_{8}$	$\left\{\begin{array}{ccc} {}^{2}\mathrm{V}_{6} & = & {}^{2}\mathrm{V}_{6} \\ {}^{2}\mathrm{V}_{7} & = & {}^{2}\mathrm{V}_{7} \end{array}\right\}$	$=\frac{2n-1}{3}$						2n - 1	3	$\frac{2n-1}{3}$									
16	×	$^{1}\mathrm{V}_{8}\times ^{3}\mathrm{V}_{11}$	${}^{4}V_{11}$	$ \begin{cases} {}^{1}V_{8} &= & {}^{0}V_{8} \\ {}^{3}V_{11} &= & {}^{4}V_{11} \end{cases} $	$= \frac{2n}{2} \cdot \frac{2n-1}{3}$								0			$\frac{2n}{2} \cdot \frac{2n-1}{3}$						
17		${}^{2}V_{6} - {}^{1}V_{1}$	³ V ₆	$\int 2V_{c} = -3V_{c}$	= 2n - 2	1					2n - 2											
18		${}^{1}V_{1} + {}^{2}V_{7}$	³ V ₇	$\begin{cases} 2V_7 = {}^{3}V_7 \end{cases}$	$= 3 \pm 1 = 4$	1						4										
19		${}^{3}V_{6} \div {}^{3}V_{7}$	1	$\left\{ \begin{array}{ccc} {}^{1}V_{1} & = & {}^{1}V_{1} \\ {}^{3}V_{6} & = & {}^{3}V_{6} \\ {}^{2}V_{6} & = & {}^{2}V_{6} \end{array} \right\}$	$=\frac{2n-2}{4}$						2n - 2	4		2n-2								
	÷			$\begin{bmatrix} {}^{3}V_{7} &= {}^{3}V_{7} \\ {}^{1}V & {}^{0}V \end{bmatrix}$	4						2n - 2			$\frac{2n-2}{4}$		$\left[\left(2n - 2n - 1 - 2n - 2 \right) \right]$						
20	$ \times $	$^1\mathrm{V}_9\times {}^4\mathrm{V}_{11}$	⁵ V ₁₁	$V_{11} = V_{11}$	$=\frac{2n}{2}\cdot\frac{2n-1}{3}\cdot\frac{2n-2}{4}=A_3\ldots\ldots$									0		$\left\{\frac{2n}{2} \cdot \frac{2n-1}{3} \cdot \frac{2n-2}{4}\right\} = A_3$						
21	×	$^{1}V_{22} \times {}^{5}V_{11}$	⁰ V ₁₂	$ V_{12} = V_{12} $	$= \mathbf{B}_3 \cdot \frac{2n}{2} \cdot \frac{2n-1}{3} \cdot \frac{2n-2}{4} = \mathbf{B}_3 \mathbf{A}_3$											0	B ₃ A ₃			B ₃		
22	+	$^{2}V_{12} + ^{2}V_{13}$	${}^{3}V_{13}$	$v_{13} = v_{13}$	$= \mathrm{A}_0 + \mathrm{B}_1 \mathrm{A}_1 + \mathrm{B}_3 \mathrm{A}_3 \ \ldots \ \ldots$												0	$\{{\rm A}_0+{\rm B}_1{\rm A}_1+{\rm B}_3{\rm A}_3\}$				
23	-	${}^{2}V_{10} - {}^{1}V_{1}$	${}^{3}V_{10}$	$ \begin{cases} {}^{2}V_{10} &= {}^{3}V_{10} \\ {}^{1}V_{1} &= {}^{1}V_{1} \end{cases} $	$= n - 3(= 1) \dots$	1									n - 3							
	Here follows a repetition of Operations thirteen to twenty-three																					
24	+	$^{4}V_{13} + {}^{0}V_{24}$	¹ V ₂₄	$ \begin{cases} {}^{4}V_{13} & = & {}^{0}V_{13} \\ {}^{0}V_{24} & = & {}^{1}V_{24} \end{cases} $	= B ₇																	B7
				$\int {}^{1}V_{1} = {}^{1}V_{1}$	= n + 1 = 4 + 1 = 5																	
25	+	${}^{1}\mathrm{V}_{1} + {}^{1}\mathrm{V}_{3}$	$^{1}V_{3}$	$\begin{bmatrix} 1 V_3 = {}^{1}V_3 \\ {}^{5}V_6 = {}^{0}V_6 \end{bmatrix}$	by a Variable-card.	1		n + 1			0	0										
				$\int 5V_7 = 0V_7$	by a Variable-card.																	
-					· .			•								•	•					

Quotes from the Ada Lovelace notes on "Sketch of the Analytical Engine Invented by Charles Babbage", 1843

"We may say most aptly, that the Analytical Engine *weaves algebraical patterns* just as the Jacquard-loom weaves flowers and leaves."

"Again, it might act upon other things besides *number*, were objects found whose mutual fundamental relations could be expressed by those of the abstract science of operations, and which should be also susceptible of adaptations to the action of the operating notation and mechanism of the engine. Supposing, for instance, that the fundamental relations of pitched sounds in the science of harmony and of musical composition were susceptible of such expression and adaptations, the engine might compose elaborate and scientific pieces of music of any degree of complexity or extent."





Quotes from the Ada Lovelace notes on "Sketch of the Analytical Engine Invented by Charles Babbage", 1843

"Many persons who are not conversant with mathematical studies, imagine that because the business of the engine is to give its results in *numerical notation*, the *nature of its processes* must consequently be *arithmetical* and *numerical*, rather than *algebraical* and *analytical*. This is an error. The engine can arrange and combine its numerical quantities exactly as if they were *letters* or any other *general* symbols; and in fact it might bring out its results in algebraical *notation*, were provisions made accordingly."

"But it would be a mistake to suppose that because its *results* are given in the *notation* of a more restricted science, its *processes* are therefore restricted to those of that science. The object of the engine is in fact to give the *utmost practical efficiency* to the resources of *numerical interpretations* of the higher science of analysis, while it uses the processes and combinations of this latter."





John Venn (1834-1923)

- Logician and philosopher
- Worked in logic, probability, set theory
- Introduced the "Venn diagram" (1880)
 - Very widely used, many applications
 - Ties together fundamental concepts from logic, geometry, combinatorics, knot theory







Generalized Numbers



The Extended Chomsky Hierarchy



YOU.

VANILLA ICE







Charles Dodgson (1832-1898)

- AKA "Lewis Carroll"
- Mathematician, logician, author, photographer
- Wrote "Alice in Wonderland", "Jabberwocky", and "Through the Looking Glass"
- Popularized logic & syllogisms and made it fun!
- Invented "Scrabble" and "word ladder" games
- Profoundly influenced literature, art, and culture

















































44 IT'S KIND OF A MIXTURE of some distorted live action and animation. I can't relate it to anything because I'm not sure what to relate to, it's kind of new territory for me..."









Alice and the White Knight: A Lesson in Logic, Semantics, and Pointers

`You are sad,' the Knight said in an anxious tone: `let me sing you a song to comfort you.'

`Is it very long?' Alice asked, for she had heard a good deal of poetry that day.

`It's long,' said the Knight, `but it's very, *very* beautiful. Everybody that hears me sing it -- either it brings the *tears* into their eyes, or else --' logical disjunction!

- `Or else what?' said Alice, for the Knight had made a sudden pause. law of the excluded middle!
- `Or else it doesn't, you know. The name of the song is called "*Haddocks' Eyes*".' pointer to a pointer!

`Oh, that's the name of the song, is it?' Alice said, trying to feel interested.

`No, you don't understand,' the Knight said, looking a little vexed. `That's what the name is *called*. The name really *is "The Aged Aged Man*".' pointer dereferencing: meta-pointer resolved!
`Then I ought to have said "That's what the *song* is called"?' Alice corrected herself. separation of abstractions: variable vs. pointer!

`No, you oughtn't: that's quite another thing! The *song* is called "*Ways and Means*": but that's only what it's *called*, you know!' call-by-name vs. call-by-value!

`Well, what *is* the song, then?' said Alice, who was by this time completely bewildered

`I was coming to that,' the Knight said. `The song really *is "A-sitting On a Gate "*: and the tune's my own invention.'









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Lewis Carroll Society of North America

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WELCOME

Welcome to The Lewis Carroll Society of North America (LCSNA) homepage. The LCSNA is a non-profit organization dedicated to furthering Carroll studies, increasing accessibility of research material, and maintaining public awareness of Carroll's contributions to society and culture. This website is one way we share information with Carroll enthusiasts around the World. If you are a Carrollian and would like to help in these endeavors, or if you simply enjoy Carroll and want to be among other people with a like interest, please consider joining the LCSNA.

For detailed information about C.L.Dodgson ("Lewis Carroll") and his creations, please access the Lewis Carroll Homepage.

Spring Meeting

The 2009 Spring meeting will be held in beautiful Sante Fe, New Mexico, on May 9. Please consult the **newly updated (as of April 24th)** meeting agenda for all of the details. See you there.





Georg Cantor (1845-1918)

- Created modern set theory
- Invented trans-finite arithmetic (highly controvertial at the time)
- Invented diagonalization argument
- First to use 1-to-1 correspondences with sets
- Proved some infinities "bigger" than others
- Showed an infinite hierarchy of infinities
- Formulated continuum hypothesis
- Cantor's theorem, "Cantor set", Cantor dust, Cantor cube, Cantor space, Cantor's paradox
- Laid foundation for computer science theory
- Influenced Hilbert, Godel, Church, Turing



GEORG

CANTOR

CONTRIBUTIONS





Problem: How can an infinity of new guests be accommodated in a full infinite hotel?



Problem: How can an infinity of infinities of new guests be accommodated in a full infinite hotel?

one-to-one

correspondence



Bertrand Russell (1872-1970)

- Philosopher, logician, mathematician, historian, social reformist, and pacifist
- Co-authored "Principia Mathematica" (1910)
- Axiomatized mathematics and set theory
- Co-founded analytic philosophy
- Originated Russell's Paradox
- Activist: humanitarianism, pacifism, education, free trade, nuclear disarmament, birth control gender & racial equality, gay rights
- Profoundly transformed math & philosophy, mentored Wittgenstein, influenced Godel
- Laid foundation for computer science theory
- Won Nobel Prize in literature (1950)



PRINCIPIA MATHEMATICA

VOLUME THREE

Alfred North Whitehead Bertrand Russell








Russell's paradox was invented by Russell in 1901 to show that naïve set theory is self-contradictory: Define: set of all sets that do not contain themselves

 $S = \{ T \mid T \notin T \}$ Q: does S contain itself as an element?

 $S \notin S \Leftrightarrow S \in S$ contradiction!

Similar paradoxes:

- "A barber who shaves exactly those who do not shave themselves."
- "This sentence is false."
- "I am lying."
- "Is the answer to this question 'no'?"
- "The smallest positive integer not describable in twenty words or less."

IF YOU CONSIDER THE SET OF ALL SETS THAT HAVE NEVER BEEN CON-SIDERED, WILL IT DISAPPEAR?







Star Trek, 1967, "I, Mudd" episode Captain James Kirk and Harry Mudd use a logical paradox to cause hostile android "Norman" to crash

AUTHOR KATHARINE GATES RECENTLY ATTEMPTED TO MAKE A CHART OF ALL SEXUAL FETISHES.

LITTLE DID SHE KNOW THAT RUSSELL AND WHITEHEAD HAD ALREADY FAILED AT THIS SAME TASK.











Historical Perspectives David Hilbert (1862-1943)

- One of the most influential mathematicians
- Developed invariant theory, Hilbert spaces
- Axiomatized geometry, "Hilbert's axioms"
- Co-founded proof theory, mathematical logic, meta-mathematics, & formalist school
- Created famous list of 23 open problems that greatly impacted mathematics research
- Defended Cantor's transfinite numbers
- Contributed to relativity theory & physics
- Hilbert's students included Courant, Hecke, Lasker, Weyl, Ackermann, and Zarmelo
- Influenced Russell, Gödel, Church, & Turing John von Neumann was Hilbert's assistant!



The





Hilbert's Impact

- Hilbert's axioms
- Hilbert class field
- Hilbert C*-module
- Hilbert cube
- Hilbert symbol
- Hilbert function
- Hilbert inequality
- Hilbert matrix
- Hilbert metric
- Hilbert number
- Hilbert polynomial
- Hilbert's problems
- Hilbert's program
- Hilbert–Poincaré series
- Hilbert space

- Hilbert transform
- Hilbert's Arithmetic of Ends
- Hilbert's constants
- Hilbert's irreducibility theorem
- Hilbert's Nullstellensatz
- Hilbert's hotel paradox
- Hilbert's theorem
- Hilbert's syzygy theorem
- Hilbert-style deduction system
- Hilbert–Pólya conjecture
- Hilbert–Schmidt operator
- Hilbert–Smith conjecture
- Hilbert–Speiser theorem
- Einstein–Hilbert action
- Hilbert curve



Hilbert curve:





Hilbert's Problems

International Congress of Mathematics, Paris, 1900

- David Hilbert proposed 23 open problems
- Most successful open problems compilation ever
- Set the direction for 20th century mathematics
- Hilbert's problems received much attention to date
- Several have been resolved (e.g., Continuum hypothesis)
- Others still open (e.g., Riemann hypothesis)
- Catalyzed other open problems lists:
 - Clay Institute's Millennium Prize problems
 - DARPA Mathematical Challenges, 2009











PROCEEDINGS OF SYMPOSIA IN PURE MATHEMATICS

VOLUME XXVIII - Part 1



Hilbert's Problems

Problem 10: Find an algorithm that determines whether a given Diophantine (i.e., multi-variable polynomial) equation has any integer solutions.

Ex: $x^2+y^2=z^2$ has many integer solutions

(Pythagorean theorem, e.g., x=3, y=4, z=5)

 $x^9+y^9=z^9$ has no integer solutions (corollary of Fermat's Last Theorem, conjectured in 1637, proved in 1995 by Andrew Wiles)

Many attempts at solution & partial results: Emil Post (1944), Martin Davis (1949), Julia Robinson (1950), Hilary Putnam (1959)





Hilbert's Tenth Problem

- Theorem [Matiyasevich, 1970]: Every Turing-recognizable set is Diophantine
- (i.e., the solutions of some polynomial)
- Ex: the set of primes coincides exactly with the positive values of this 26-variable polynomial:
 - $\begin{array}{l} (k+2)(1-[wz+h+j-q]^2-[(gk+2g+k+1)(h+j)+h-z]^2\\ -[16(k+1)^3(k+2)(n+1)^2+1-f^2]^2-[2n+p+q+z-e]^2\\ -[e^3(e+2)(a+1)^2+1-o^2]^2-[(a^2-1)y^2+1-x^2]^2\\ -[16r^2y^4(a^2-1)+1-u^2]^2-[n+l+v-y]^2-[(a^2-1)l^2+1-m^2]^2\\ -[ai+k+1-l-i]^2-[((a+u^2(u^2-a))^2-1)(n+4dy)^2+1\\ -(x+cu)^2]^2-[p+l(a-n-1)+b(2an+2a-n^2-2n-2)-m]^2\\ -[q+y(a-p-1)+s(2ap+2a-p^2-2p-2)-x]^2\\ -[z+pl(a-p)+t(2ap-p^2-1)-pm]^2)\end{array}$
- as a, b, c, ..., z range over the nonnegative integers!



Hilbert's Tenth Problem Corollary [Matiyasevich, 1970]: There is a fixed "universal" polynomial P such that for any Turing-enumerable set S there exists an integer n_0 such that:

 $S = \{w \mid \exists x_1, x_2, ..., x_k \neq P(n_0, w, x_1, x_2, ..., x_k)=0$ i.e., there is a fixed polynomial that can "output" any computable set, depending on one parameter. This is an analogue of a universal Turing machine!

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CLAY MATHEMATICS INSTITUTE March 15–16, 2007

One Bow Street, Cambridge, Massachusetts

Conference on Hilbert's Tenth Problem

Thursday, March 15

9:00	Coffee		
9:15 - 9:25	Constance Reid, Genesis of the Hilbert Problems		
9:25 - 10:00	George Csicsery, Film clip on life and work of Julia Robinson, discussion		
10:15 - 11:15	Bjorn Poonen, Why number theory is hard		
11:30 - 12:30	Yuri Matiyasevich, My collaboration with Julia Robinson		
	Break for lunch		
2:30-3:30	Martin Davis, My collaboration with Hilary Putnam		
3:45-4:45	Maxim Vsemirnov, TBA		
7:30	Museum of Science • Film Screening Scenes from Julia Robinson and Hilbert's Tenth Problem, a documentary by George Csicsery, will be screened in Cahner's Theater (Blue Wing, Level 2, Museum of Science), and followed by a panel discussion with filmmaker George Csicsery, mathematician Yuri Matiyasevich, and biographer Constance Reid. This event is free and open to the public.		

Friday, March 16

Clay Mathematics Institute

www.clavmath.org

8:30	Coffee		
9:00-10:00	Yuri Matiyasevich, Hilbert's Tenth Problem: What was done and what is to be done		
10:15–11:15	Bjorn Poonen, Thoughts about the analogue for rational numbers		
11:30-12:30	Alexandra Shlapentokh, Diophantine generation, horizontal and vertical problems, and the weak vertical method		
	Break for lunch		
2:00-3:00	Yuri Matiyasevich, Computation paradigms in the light of Hilbert's tenth problem		
3:15-4:15	Gunther Cornelisson, Hard number-theoretical problems and elliptic curves		
4:30-5:30	Kirsten Eisentrager, Hilbert's Tenth Problem for algebraic function fields		
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Museum of Science.



Hilbert's 10th Problem (1900): is there an algorithm for deciding whether a polynomial equation with integer coefficients has an integer solution?

 $x^2 - (a^2 - 1)y^2 = 1$

Photo credits (top to bottom): Julia Robinson, courtesy of Constance Reid; Yuri Matiyasevich, photo by George Csicsery; David Hilbert, courtesy AK Peters, Ltd.

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Co-Sponsored by the Mathematical Sciences Research Institute and the UCBerkeley Department of Mathematics



A film by George Csicsery

Wednesday, April 30, 2008

7pm to 9pm

Room 2050 (Chan Shun Auditorium) in the Valley Life Sciences Building at UC Berkeley

> Post-screening panel discussion with Constance Reid (sister and biographer of Julia Robinson), filmmaker George Csicsery, and mathematicians Martin Davis, Dana Scott and Bjorn Poonen. Moderated by Alan Weinstein, UCB Math Dept. Chair.

The story of an American mathematician and her passionate pursuit and triumph over an unsolved problem.

Hilbert's 10th Problem (1900): Is there an algorithm for deciaing whether a polynomial equation with integer coefficients has an integer solution?

FREE ADMISSION







A documentary film by George Csicsery

The story of an American mathematician and her passionate pursuit of Hilbert's tenth problem

Hilbert's Problems

Problem 18: Is there a non-regular, space-filling polyhedron? What is the densest sphere packing?

- Status: Anisohedral tilings were found in 3D by Reinhardt (1928), and for 2D by Heesch (1935).
- Sphere packing in 3D (Kepler's problem, 1611) was solved by Toth (1953) and Hale (1998). Regular sphere packing in 24 dimensions was solved by Cohn and Kumar (2004), where the "kissing number" is 196,560.
- Many related open problems remain, including non-regular, non-uniform, and ellipsoid packings.











Goal: tile the entire plane without overlaps, non-periodically

- Non-periodic tiling is not equal to a translation of itself
- Aperiodic tile set admits only non-periodic tilings
- "Kites and Darts" 2-tile aperiodic set, Roger Penrose, 1974





Penrose tilings in architecture and design:





Aperiodic Tilings "Pinwheel tiling", John Conway and Charles Radin, 1992

NEW SCIENTIST

SCIENCE

Bathroom tiling to drive you mad

lan Stewart

AN AMERICAN mathematician has come up with what is probably the strangest way ever of covering a floor or wall with tiles. The set of tiles which has been devised by Charles Radin of the University of Texas at Austin can only be assembled in a highly complex way (Annals of Mathematies, vol 109, P661).

The usual way of assembling tiles is in a periodic pattern, one that starts with a basic unit, which is repeated at regularly spaced intervals. However, more complex patterns of tiling are perfectly possible and the subject of aperiodic tilings was created by the philosopher Hao Wang in 1961. Wang was studying the existence or otherwise of certain "decision procedures" in mathematical logic—ways of working out in advance whether certain problems have solutions—when he came to the surprising conclusion that the problem could be reformulated in terms of tiles.

Choose a finite collection of shapes and call them prototiles. A tiling is then a way to assemble perfect copies of those prototiles so that they cover the entire infinite plane without any gaps or overlaps. Wang discovered that he could design prototiles that corresponded to various logical statements, in such a way that the rules for fitting prototiles together corresponded exactly to the rules of logical deduction. So, in effect, a tiling pattern corresponded to a logical proof. This new viewpoint led Wang to ask whether there existed a set of prototiles that could tile the plane, but could not tile it periodically:

Tiling a plane aperiodically turns out to be easy. It can be done with a single domino-shaped prototile. First, however, it is necessary to tile the plane with squares. Then each square is divided into two dominos by splitting it in half in either the vertical or horizontal direction. If the pattern of verticals and horizontals is aperiodic, so too is the tiling: the easiest method is to vary the directions randomly. However, dominos can also tile the plane periodically—for example, by making all splits point the same way.

Wang wanted something much more subtle: a set of prototiles that produced only aperiodic tilings. Such as set of tiles was found in 1966 by his student Robert Berger. The best known of such sets are the Penrose tilings, introduced by Roger Penrose of the University of Oxford in 1977; these produce tilings with freeloid "almost" symmetrics.

Radin notes that: "All published examples... have the feature that in every tiling each prototile only appears in finitely many orientations." For instance, dominos can be laid down horizontally or vertically but not oriented at any other angle; and Penrose tiles rotate only through multiples of an angle of 36°. This means that if the set of prototiles is expanded so that it even oriented as a copy of each prototile in each orientation, then the new prototiles can tile the whole plane without being rotated. Only translations of these "oriented prototiles" are then needed.

Radin's new discovery is a set of

World's most complex tiling? Surround a triangular "half-domino" by four more. Then simply repeat...

prototiles that are forced to appear in an infinite number of orientations. Because periodic tilings involve only a finite number of directions—the ones in the basic repeating unit—Radin's tilings are necessarily aperiodic.

His starting point is an idea thought up by John Horton Conway of Princeton University in New, Jersey. Begin with a "halfdomino" prototile, a right triangle of sides 1 and 2 units (whose hypotenuse is 5 units). This can be surrounded by four copies of itself in order to create a triangle of the same shape, but larger and rotated through an angle (see Figure). The process can be thought of as defining a "level"

tiling of part of the plane with five triangular tiles. The construction can now be repeated, surrounding the level-1 set of five tiles with four copies of those sets to make an even larger and further rotated runagle that is composed of 25 of the original prototiles: this is known as the level-2 tiling.

Continuing this "expansion" process indefinitely from each level to the next leads to a strange, random-looking tilling of the infinite plane by half-dominos (see Figure), called the Conway tilling. Because the angle of rotation at each stage does not exactly divide into an integer number of full turns, the half-domino appears in an infinite number of different orientations throughout the plane.

However, this particular prototile can also tile the plane periodically. This can be done if two half-dominos are stuck together to make a domino and the plane is tiled periodically with those. To eliminate these periodic possibilities, Radin modifies the construction so that

certain features of the Conway tiling, in particular its hierarchical structure into levels, cannot be avoided. The essential idea is an old

one: the edges of prototiles can he "labelled" with marks or symhols, with the extra rule that adjacent tiles must have matching labels along their common edges. This produces a larger set of labelled prototiles with more restrictive tiling rules. The point is that the labels can be realised by making notches in the edges of one tile and adding protruding lugs to match them in the adjacent tile. By using a different shaped notch/lug pair for each symbol used as a label, we can convert labelled prototiles into

per, we can convert indexed protonal national protonal national protonal national protonal national protonal national protonal national simple shapes of more complicated shapes. It is, of course, easier to think about simple shapes that have labelled edges, and this is the way in which Radin proceeds. His prototiles are labelled half-dominos, and he invents a complicated range of different labels whose matching rules cleverly force the appearance of the same structure as the Convey tiling.

It is astonishing that such a simple shape as half a domino can have such curious implications, and it shows that even in today's complex world mathematics can still advance by looking at a simple idea in a new way.



Federation Square Melbourne, Australia



"Pentagon, Boat, and Star" Roger Penrose, 1974







"Conch" G. Rauzy, 1982





"Cubic Pinwheel" E. Harriss





"Cyclotomic rhombs 7-fold" Ludwig Danzer and D. Frettlöh





"Harriss's 9-fold rhomb" E. Harriss



"Kenyon (1,2,1) Polygon" R. Kenyon





"Nautilus" P. Arnoux, M. Furukado, E. Harriss, and S. Ito





"Nautilus (volume hierarchic" P. Arnoux, M. Furukado, E. Harriss, and S. Ito





"Pinwheel" John Conway and C. Radin



Tiles occur in infinitely many orientations!

Despite irrational edge lengths and incommensurable angles, all vertices of tiles have rational coordinates!



"Pythagoras-3-1" J. Pieniak



"Watanabe Ito Soma 12-fold"Y. Watanabe,T. Soma andM. Ito, 1995





 \rightarrow

"Viper"

 \land



"Sphinx" J.-Y. Lee, and R. V. Moody





Historical Perspectives

Kurt Gödel (1906-1978)

- Logician, mathematician, and philosopher
- Proved completeness of predicate logic and Gödel's incompleteness theorem
- Proved consistency of axiom of choice and the continuum hypothesis
- Invented "Gödel numbering" and "Gödel fuzzy logic"
- Developed "Gödel metric" and paradoxical relativity solutions: "Gödel spacetime / universe"
- Made enormous impact on logic, mathematics, and science



The Consistency of the Continuum Hypothesis by Kurt Gödel



With a Foreword by Dr. Richard Laver



















Kurt Gödel 1906 - 1978















Gödel's Incompleteness Theorem

Frege & Russell:

- Mechanically verifying proofs
- Automatic theorem proving
- A set of axioms is:



- Sound: iff only true statements can be proved
- Complete: iff any statement or its negation can be proved
- Consistent: iff no statement and its negation can be proved
- Hilbert's program: find an axiom set for all of mathematics i.e., find a axiom set that is consistent and complete
- Gödel: any consistent axiomatic system is incomplete! (as long as it subsume elementary arithmetic)
 - i.e., any consistent axiomatic system must contain true but unprovable statements
- Mathematical surprise: truth and provability are not the same!

Gödel's Incompleteness Theorem

That some axiomatic systems are incomplete is not surprising, since an important axiom may be missing (e.g., Euclidean geometry without the parallel postulate)



However, that every consistent axiomatic system must be incomplete was an unexpected shock to mathematics! This undermined not only a particular system (e.g., logic), but axiomatic reasoning and human thinking itself!

> Truth = Provability Justice ≠ Legality
Gödel's Incompleteness Theorem

- Gödel: consistency or completeness pick one!
- Which is more important?
- Incomplete: not all true statements can be proved. But if useful theorems arise, the system is still useful.



- **Inconsistent**: some false statement can be proved. This can be catastrophic to the theory:
- E.g., supposed in an axiomatic system we proved that "1=2". Then we can use this to prove that, e.g., all things are equal! Consider the set: {Trump, Pope}
 - | {Trump, Pope} | = 2
 - $\Rightarrow | \{\text{Trump, Pope}\} | = 1 \text{ (since } 1=2)$
 - \Rightarrow Trump = Pope QED
- \Rightarrow All things become true: system is "complete" but useless!

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The Kurt Gödel Society

Welcome

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Welcome

The Kurt Gödel Society was founded in 1987 and is chartered in Vienna. It is an international organization for the promotion of research in the areas of Logic, Philosophy, History of Mathematics, above all in connection with the biography of Kurt Gödel, and in other areas to which Gödel made contributions, especially mathematics, physics, theology, philosophy and Leibniz studies.

Top News

09-06-08 12:00

Fourth Vienna Tbilisi Summer School in Logic and Language

For the third time students and teachers meet in Tbilisi, Georgia, for a summer school. Please see the conference page http://www.logic.at/tbilisi08/ fo... [more...]

05-12-07 23:22

Collegium Logicum Lecture Series

6 December 2007, 16:00 Peter Schuster (LMU München) - Finite methods in commutative algebra [more...]

15-11-07 12:27

Workshop Two and beyond

The KGS is organizing a workshop on truth-functional logics. [more...]

© 2004 Kurt Gödel Society, Arnold Beckmann, Norbert Preining

1 1



Historical Perspectives

Alonzo Church (1903-1995)

- Founder of theoretical computer science
- Made major contributions to logic
- Invented Lambda-calculus, Church-Turing Thesis
- Originated Church-Frege Ontology, Church's theorem Church encoding, Church-Kleene ordinal,

Alonzo Church

Introduction to

Mathematical

Logic

- Inspired LISP and functional programming
- Was Turing's Ph.D. advisor! Other students: Davis, Kleene, Rabin, Rogers, Scott, Smullyan
- Founded / edited Journal of Symbolic Logic
- Taught at UCLA until 1990; published "A Theory of the Meaning of Names" in 1995, at age 92!





Historical Perspectives

Alan Turing (1912-1954)

- Mathematician, logician, cryptanalyst, and founder of computer science
- First to formally define computation / algorithm
- Invented the Turing machine model
 - theoretical basis of all modern computers
- Investigated computational "universality"
- Introduced "definable" real numbers
- Proved undecidability of halting problem
- Originated oracles and the "Turing test"
- Pioneered artificial intelligence
- Anticipated neural networks
- Designed the Manchester Mark 1 (1948)
- Helped break the German Enigma cypher
- Turing Award was created in his honor







ALAN TURING 1912 - 1954

THE ALAN TURING MEM

ALAN MATHESON TORONS

141

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107

Founder of computer science and cryptographer, whose work was key to breaking the wartime Enigma codes, lived and died here.



Bletchley Park ("Station X"), Bletchley, Buckinghamshire, England England's code-breaking and cryptanalysis center during WWII "Bombe" - electromechanical computer designed by Alan Turing. Used by British cryptologists to break the German Enigma cipher





1918 First Enigma Patent

The official history of the Enigma starts in 1918, when the German **Arthur Scherbius** filed his first patent for the Enigma coding machine. It is listed as patent number 416219 in the archives of the German *Reichspatentamt* (patent office). Please note the time at which the Enigma was invented: **1918**, just after the First World War, more then 20 years before WWII! The image below clearly shows the coding wheels (rotors) in the centre part of the drawing. Below it is the keyboard and to the right is the lamp panel. At the top left is a counter, used to count the number of letters entered on the keyboard. This counter can still be found on certain Enigma models.

Arthur Scherbius' company **Securitas** was based in Berlin (Germany) and had an office in Amsterdam (The Netherlands). As he wanted to protect his invention outside Germany, he also registered his patent in the USA (1922), Great Britain (1923) and France (1923).



This image is taken from patent number 193,035 that was registered in Great Britain in 1923, long before WWII. It was also registered in a number of other countries, such as France and the USA.

During the 1920s the Enigma was available as a commercial device, available for use by companies and embassies for their confidential messages. Remember that in those days, most companies had to use morse code and radio links for long distance communication. The devices were advertised having over 800.000 possibilities.

In the following years, additional patents with improvements of the coding machine were applied. E.g. in GB Patent 267,482, dated 17 Jan 1927, the Umkehrwalze was added and a later patent of 14 Nov 1929 (GB 343,146) claims the addition of the Ringstellung, multiple notches, etc. One of the drawings of that patent shows a coding device, that we now know as The Enigma, in great detail.







SPECIAL EDITION DOUGRAY KATE JEREMY SAFFRON SCOTT WINSLET NORTHAM BURROWS





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BREAKING THE CODE

Scramblet

by hugh whitemore based on the book Alan Turing, The Enigma

directed by phil rayner

by andrew hodges

it's not breaking the code that matters - it's where you go from there









HUGH WHITEMORY

Breaking the Code is a

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> In fact Breaking the Code is a

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Program for ACE computer hand-written by Alan Turing







@ 2002 http://www.jinwicked.com

ALAN TURING, 1912 - 1954







THE SUNDAY TIMES

NEWS REVIEW FEATURES

TURINGARCHIVE

The outcast who gave us the modern world ALCONT OF THE PARTY OF THE PART

Alan Turing's genius ushered in the digital era. Britain could have been at its centre, had it not treated him cruelly, writes Michael Hanlon

Turing, whose life is charted in a TV documentary this week, committed suicide before his work on computers bore fruit



Sections New issue

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Front page

Contents

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Another famous belated apology:

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Monday, September 10, 2007

1992: Catholic Church apologizes to Galileo, who died in 1642



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In 1610, Century Italian astronomer/mathematician /inventor Galileo Galilei used a a telescope he built to observe the solar system, and deduced that the planets orbit the sun, not the earth.

This contradicted Church teachings, and some of the clergy accused Galileo of heresy. One friar went to the Inquisition, the Church court that investigated charges of heresy, and formally accused Galileo. (In 1600, a man named Giordano Bruno was

convicted of being a heretic for believing that the earth moved around the Sun, and that there were many planets throughout the universe where life existed. Bruno was burnt to death.)

Galileo moved on to other projects. He started writing about ocean tides, but instead of writing a scientific paper, he found it much more interesting to have an imaginary conversation among three fictional characters. One character, who would support Galileo's side of the argument, was brilliant. Another character would be open to either side of the argument. The final character, named Simplicio, was dogmatic and foolish, representing all of Galileo's enemies who ignored any evidence that Galileo was right. Soon, Galileo wrote up a sin dialogue called "Dialogue on the Two Great Systems of the V This book talked about the Copernican system.

"Dialogue" was an immediate hit with the public, but not, of course, with the Church. The pope suspected that he was the model for Simplicio. He ordered the book banned, and also ordered Galileo to appear before the Inquisition in Rome for the crime of teaching the Copernican theory after being ordered not to do so.

Galileo was 68 years old and sick. Threatened with torture, he publicly confessed that he had been wrong to have said that the Earth moves around the Sun. Legend then has it that after his confession, Galileo quietly whispered "And yet, it moves."

Unlike many less famous prisoners, Galileo was allowed to live under house arrest. Until his death in 1642, he continued to investigate science, and even published a book on force and motion after he had become blind.

The Church eventually lifted the ban on Galileo's Dialogue in 1822, when it was common knowledge that the Earth was not the center of the Universe. Still later, there were statements by the Vatican Council in the early 1960's and in 1979 that implied that Galileo was pardoned, and that he had suffered at the hands of the Church. Finally, in 1992, three years after Galileo Galilei's namesake spacecraft had been launched on its way to Jupiter, the Vatican formally and publicly

Theorem: A late apology is better than no apology. Corollary: But sooner is better!

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TURING CENTENARY CONFERENCE CiE 2012 - How the World Computes

Local Arrangements

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University of Cambridge 18 June - 23 June, 2012

Scientific Arrangements CiE 2012 CiE Network and Series

External Links The Alan Turing Year Alan Turing Home Page CIE 2012 is one of a series of special events, running throughout the Alan Turing Year, celebrating Turing's unique impact on mathematics, computing, computer science, informatics, morphogenesis, philosophy and the wider scientific world. Its central theme is the computability-theoretic concerns underlying the broad spectrum of Turing's interests, and the contemporary research areas founded upon and animated by them. In this sense, CiE 2012, held in Cambridge in the week running up to the centenary of Turing's birthday, deals with the essential core of what made Turing's contribution so influential and long-lasting. CiE 2012 promises to be an event worthy of the remarkable scientific career it commemorates.

Programme Committee: S Barry Cooper (Leeds, **Co-chair**), Anuj Dawar (Cambridge, **Co-chair**)

Organising Committee: Luca Cardelli, S Barry Cooper (Leeds), Ann Copestake, Anuj Dawar (Chair), Martin Hyland, Andrew Pitts



Print this page

Andrew Hodges to speak at CiE 2012

22.7.09 Cambridge confirmed for CiE12

News

17.8.09

31.12.07 Turing Advisory Group founded





Picture of Bletchley Park Bombe rebuild



The Alan Turing Memorial in Sackville Park Manchester

Turing's Seminal Paper

- "On Computable Numbers, with an Application to the Entscheidungsproblem", Proceedings of the London Mathematical Society, 1937, pp. 230-265.
- One of the most influential & significant papers ever!
- First formal model of "computation"
- First ever definition of "algorithm"
- Invented "Turing machines"
- Introduced "computational universality" i.e., "programmable"!
- Proved the undecidability of halting problem
- Explicates the Church-Turing Thesis











A fanciful mechanical Turing machine's TAPE and HEAD. The TABLE instructions might be on another "read only" tape, or perhaps on punch-cards. Usually a "finite state machine" is the model for the TABLE. Turing's insight: <u>simple local</u> actions can lead to <u>arbitrarily</u> <u>complex</u> computations!



Theorem [Turing]: the halting problem (H) is not computable. Proof: Assume \exists algorithm S that solves the halting problem H, that always stops with the correct answer for any P & I.



Computational Universality

 $A \rightarrow bc$

Theorem: Many other systems are equivalent to Turing machines.

- Grammars $cS \rightarrow aNbc \mid S$
- λ-calculus $(\lambda X \cdot X + 1)$
- Post tag systems
- µ-recursive functions
- Cellular automata
- Boolean circuits
- Diophantine equations $\begin{bmatrix} B \\ C \end{bmatrix}$
- DNA
- Billiards!







Universality of Billiards

Theorem: Billiards is computationally universal!



Lego Turing Machines



Lego Turing Machines



See: <u>http://www.youtube.com/watch?v=cYw2ewoO6c4</u>

"Mechano" Computers





Babbage's difference engine

Tinker Toy Computers



Plays tic-tac-toe!





Tinker Toy Computers



Mechanical Computers





FIGURE 6 An And block constructed by connecting an Or block to inverters



NUTS AND BOLTS

11





ScienceMasters



Hydraulic Computers



Announced May 14th, 2007: 5th Anniversary of the Publication of A New Kind of Science

Oct 24, 2007

We have the solution!

Wolfram's 2,3 Turing machine

is universal

Congratulations Alex Smith. Find out more »

THE WOLFRAM 2,3 TURING MACHINE RESEARCH PRIZE

\$25,000 prize

Is this Turing machine universal, or not?

		•	•	1	•
-	-				

The machine has 2 states and 3 colors, and is 596440 in Wolfram's numbering scheme. If it is universal then it is the smallest universal Turing machine that exists.

BACKGROUND »	TECHNICAL DETAILS »	GALLERY »	NEWS »
PRIZE COMMITTEE »	RULES & GUIDELINES »	FAQs »	

A universal Turing machine is powerful enough to emulate any standard computer. The question is: how simple can the rules for a universal Turing machine be?

Since the 1960s it has been known that there is a universal 7,4 machine. In A New Kind of Science, Stephen Wolfram found a universal 2,5 machine, and suggested that the particular 2,3 machine that is the subject of this prize might be universal.

The prize is for determining whether or not the 2,3 machine is in fact universal.
THE WOLFRAM 2,3 TURING MACHINE RESEARCH PRIZE



Wolfram's 2,3 Turing machine is universal!



The lower limit on Turing machine universality is proved—

providing new evidence for Wolfram's Principle of Computational Equivalence.



The Wolfram 2,3 Turing Machine Research Prize has been won by 20year-old Alex Smith of Birmingham, UK. Smith's Proof (to be published in Complex Systems): Prize Submission » Mathematica Programs » News Release » Technical Commentary » Stephen Wolfram's Blog Post » Media Enquiries »



What is a Turing Machine? » | Notable Universal Turing Machines »

The Rules for the Machine

The rules for the Turing machine that is the subject of this prize are:

 $\{\{1, 2\} \rightarrow \{1, 1, -1\}, \{1, 1\} \rightarrow \{1, 2, -1\}, \{1, 0\} \rightarrow \{2, 1, 1\}, \{2, 1, 1\}, \{2, 1, 1\}, \{2, 1, 1\}, \{2, 1, 1\}, \{2, 1, 1\}, \{3, 1, 1\},$ $\{2, 2\} \rightarrow \{1, 0, 1\}, \{2, 1\} \rightarrow \{2, 2, 1\}, \{2, 0\} \rightarrow \{1, 2, -1\}\}$

where this means {state, color} -> {state, color, offset}. (Colors of cells on the tape are sometimes instead thought of as "symbols" written to the tape.)

These rules can be represented pictorially by:



where the orientation of each arrow represents the state.

The rules can also be represented by the state transition diagram:



In Wolfram's numbering scheme for Turing machines, this is machine 596440. There are a total of (2 3 2)^(2 3)=12^6=2985984 machines with 2 states and 3 colors.

Note that there is no halt state for this Turing machine.

The Church-Turing Thesis Q: What does it mean "to be computable"?



The Church-Turing Thesis: Anything that is "intuitively computable" is also Turing-machine computable.

The Church-Turing Thesis

Q: Why "thesis" and not "theorem"?



Undefined / informal tasks: produce (or even identify) good music, art, poetry, humor, aesthetics, justice, truth, etc.



IBM's "Deep Blue" becomes Chess world champion in 1997





NO FEELING. NO FEAR. NO CONTEST.



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NATURAL 'PROZAC': DOES IT REALLY WORK?

Chess champion Garry Kasparov

Man vs. Machine:

The Rematch

What Computers Will Do Next



"Watson" AI becomes Jeopardy world champion in 2011



A Cool Turing Machine

Apple iPad (2015):

- $< \frac{1}{4}$ " thin
- < 1 pound weight
- 2048 x1536 (326 ppi res) multi-touch screen
- 128 GB memory
- 1.5 MHz 64-bit 3-core A8X
- 8 MP camera & HD video
- WiFi, cellular, GPS
- Compass, barometer
- battery life 10 hours





My Favorite Touring Machine Tesla Model S

Theorem: Theory

can be beautiful!

0-60 in 2.3 seconds! 315 miles per charge

My Own Touring Machine



Alan Turing's Forgotten Ideas in Computer Science

Well known for the machine, test and thesis that bear his name, the British genius also anticipated neural-network computers and "hypercomputation"

by B. Jack Copeland and Diane Proudfoot

Alan Mathison Turing conceived of the modern computer in 1935. Today all digital computers are, in essence, "Turing machines." The British mathematician also pioneered the field of artificial intelligence, or AI, proposing the famous and widely debated Turing test as a way of determining whether a suitably programmed computer can think. During World War II, Turing was instrumental in breaking the German Enigma code in part of a top-secret British operation that historians say shortened the war in Europe by two years. When he died at the age of 41, Turing was doing the earliest work on what would now be called artificial life, simulating the chemistry of biological growth.

Throughout his remarkable career, Turing had no great interest in publicizing his ideas. Consequently, important aspects of his work have been neglected or forgotten over the years. In particular, few people even those knowledgeable about computer science are familiar with Turing's fascinating anticipation of connectionism, or neuronlike computing. Also neglected are his groundbreaking theoretical concepts in the exciting area of "hypercomputation." According to some experts, hypercomputers might one day solve problems heretofore deemed intractable.

The Turing Connection

D igital computers are superb number crunchers. Ask them to predict a rocker's trajectory or calcuporation, and they can churn out the answers in seconds. But seemingly simple actions that people routinely perform, such as recognizing a face or reading handwriting, have been devilishy tricky to program. Perhaps the networks of neurons that make up the brain have a natural facility for such tasks that standard computers lack. Scientists have thus been investigating computers modeled more closely on the human brain.

Connectionism is the emerging science of computing with networks of artificial neurons. Currently researchers usually simulate the neurons and their interconnections within an ordinary digital computer (just as engineers create virtual models of aircraft wings and skyscrapers). A training algorithm that runs on the computer adjusts the connections between the neurons, honing the network into a special-purpose machine dedicated to some particular function, such as forecasting international currency markets.

Modern connectionists look back to Frank Rosenblatt, who published the first of many papers on the topic in 1957, as the founder of their approach. Few realize that Turing had already investigated connectionist networks as early as 1948, in a little-known paper entitled "Intelligent Machinery."

Written while Turing was working for the National Physical Laboratory in London, the manuscript did not meet with his employer's approval. Sir Charles Darwin, the rather headmasterly director of the laboratory and grandson of the great English naturalist, dismissed it as a "schoolboy essay." In reality, this farsighted paper was the first manifesto of the field of artificial intelligence. In the work—which remained unpublished until 1968, 14 years after Turing's death—the British mathematician not only set out the fundamentals of connectionism but also brilliantly introduced many of the concepts that were later to become central to AI, in some cases after reinvention by others.

In the paper, Turing invented a kind of neural network that he called a "B-type retical basis of connectionism in one suc-

Few realize that Turing had already investigated connectionist networks as early as 1948.

unorganized machine," which consists of artificial neurons and devices that modify the connections between them. B-type machines may contain any number of neurons connected in any pattern but are always subject to the restriction that each neuron-to-neuron connection must pass through a modifier device.

All connection modifiers have two training fibers. Applying a pulse to one of them sets the modifier to "pass mode," in which an input—either 0 or 1—passes through unchanged and becomes the output. A pulse on the other fiber places the modifier in "interrupt mode," in which the output is always 1, no matter what the input is. In this state the modifier destroys all information attempting to pass along the connection to which it is attached.

Once set, a modifier will maintain its function (either "pass" or "interrupt") unless it receives a pulse on the other training fiber. The presence of these ingenious connection modifiers enables the training of a B-type unorganized machine by means of what Turing called "appropriate interference, mimicking education." Actually, Turing theorized that "the cortex of an infant is an unor ganized machine, which can be organized by suitable interfering training."

Each of Turing's model neurons has two input fibers, and the output of a neuron is a simple logical function of its two inputs. Every neuron in the network executes the same logical operation of "not and" (or NAND): the output is 1 if either of the inputs is 0. If both inputs are 1, then the output is 0. Turing selected NAND because every

other logical (or Boolean) operation can

be accomplished by groups of NAND neurons. Furthermore, he showed that even the connection modifiers themselves can be built out of NAND neurons. Thus, Turing specified a network made up of nothing more than NAND neurons and their connecting fibers—about the simplest possible model of the cortex. In 1958 Rosenblatt defined the theorertical basis of connectionism in one suc-

> cinct statement: "Stored information takes the form of new connections, or transmission channels in the nervous system (or the creation of conditions which are functionally equivalent to new connections)." Because the destruction of existing connections can be func-

tionally equivalent to the creation of new ones, researchers can build a network for accomplishing a specific task by taking one with an excess of connections and selectively destroying some of them. Both actions—destruction and creation are employed in the training of Turing's B-types.

At the outset, B-types contain random interneural connections whose modifiers have been set by chance to either pass or interrupt. During training, unwanted connections are destroyed by switching their attached modifiers to interrupt mode. Conversely, changing a modifier from interrupt to pass in effect creates a connection. This selective culling and enlivening of connections hones the initially random network into one organized for a given iob.

Turing wished to investigate other kinds of unorganized machines, and he longed to simulate a neural network and its training regimen using an ordinary digital computer. He would, he said, "allow the whole system to run for an appreciable period, and then break in as a kind of 'inspector of schools' and see what progress had been made." But his own work on neural networks was carried out shortly before the first generalpurpose electronic computers became available. (It was not until 1954, the year of Turing's death, that Belmont G. Farley and Wesley A. Clark succeeded at the Massachusetts Institute of Technology in running the first computer simulation of a small neural network.)

Paper and pencil were enough, though, for Turing to show that a sufficiently large B-type neural network can be configured (via its connection modifiers)

in such a way that it becomes a generalpurpose computer. This discovery illuminates one of the most fundamental problems concerning human coemition.

From a top-down perspective, cognition includes complex sequential processes, often involving language or other forms of symbolic representation, as in mathematical calculation. Yet from a bottom-up view, cognition is nothing but the simple firings of neurons. Cognitive scientists face the problem of how to reconcile these very different perspectives.

Turing's discovery offers a possible solution: the cortex, by virtue of being a neural network acting as a general-purpose computer, is able to carry out the sequential, symbol-rich processing discerned in the view from the top. In 1948 this hypothesis was well ahead of its time, and today it remains among the best guesses concerning one of cognitive science's hardest problems.

Computing the Uncomputable

In 1935 Turing thought up the abstract device that has since become known as the "universal Turing machine." It consists of a limitless memory

Turing's Anticipation of Connectionism

n a paper that went unpublished until 14 years after his death (top), Alan Turing described a network of artificial neurons connected in a random manner. In this "B-type unorganized machine" (bottom left), each connection passes through a modifier that is set either to allow data to pass unchanged (areen fiber) or to destroy the transmitted information (red fiber). Switching the modifiers from one mode to the other enables the network to be trained. Note that each neuron has two inputs (bottom left, inset) and executes the simple logical operation of "not and," or NAND: if both inputs are 1, then the output is 0: otherwise the output is 1.

In Turing's network the neurons interconnect freely. In contrast, modern network's (*bottom center*) restrict the flow of information from layer to layer of neurons. Connectionists aim to simulate the neural networks of the brain (*bottom right*).

that stores both program and data and a scanner that moves back and forth through the memory, symbol by symbol, reading the information and writing additional symbols. Each of the machine's basic actions is very simplesuch as "identify the symbol on which the scanner is positioned," "write '1'" and "move one position to the left." Complexity is achieved by chaining together large numbers of these basic actions. Despite its simplicity, a universal Turing machine can execute any task that can be done by the most powerful of today's computers. In fact, all modern digital computers are in essence universal Turing machines [see "Turing Machines," by John E. Hopcroft; SCI-ENTIFIC AMERICAN, May 1984].

Turing's aim in 1935 was to devise a machine—one as simple as possible capable of any calculation that a human mathematician working in accordance with some algorithmic method could perform, given unlimited time, energy, paper and pencils, and perfect concentration. Calling a machine "universal" merely signifies that it is capable of all such calculations. As Turing himself wrote, "Electronic computers are intended to carry out any definite rule-ofthumb process which could have been done by a human operator working in a disciplined but unintelligent manner."

Such powerful computing devices notwithstanding, an intriguing question arises: Can machines be devised that are capable of accomplishing even more? The answer is that these "hypermachines" can be described on paper, but no one as yet knows whether it will be possible to build one. The field of hypercomputation is currently attracting a growing number of scientists. Some speculate that the human brain itself the most complex information processor known—is actually a naturally occurring example of a hypercomputer. Before the recent surge of interest in

hypercomputation, any informationprocessing job that was known to be too difficult for universal Turing machines was written off as "uncomputable." In this sense, a hypermachine computes the uncomputable.

Examples of such tasks can be found in even the most straightforward areas of mathematics. For instance, given arithmetical statements picked at random, a universal Turing machine may

not always be able to tell which are theorems (such as "7 + 5 = 12") and which are nontheorems (such as "every number is the sum of two even numbers"). Another type of uncomputable problem comes from geometry. A set of tilesvariously sized squares with different colored edges-"tiles the plane" if the Euclidean plane can be covered by copies of the tiles with no gaps or overlaps and with adjacent edges always the same color. Logicians William Hanf and Dale Myers of the University of Hawaii have discovered a tile set that tiles the plane only in patterns too complicated for a universal Turing machine to calculate. In the field of computer science, a universal Turing machine cannot always predict whether a given program will terminate or continue running forever. This is sometimes expressed by saying that no general-purpose programming language (Pascal, BASIC, Prolog, C and so on) can have a foolproof crash debugger: a tool that detects all bugs that could lead to crashes, including errors that result in infinite processing loops.

Turing himself was the first to investigate the idea of machines that can perform mathematical tasks too difficult

be rearried by one man as organized and by shother a unorganized. A typical example of an unorganized machine would be as follows. The machine is made up from a rather large number N of similar units. Each mit has two input terminals, and is an output terminal wheih can be connected to the input terminals of other units. We may imagine that the for each integer r. 15 rs N



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Alan Turing's Forgotten Ideas in Computer Science

Alan Turing's Forgotten Ideas in Computer Science

SCIENTIFIC AMERICAN April 1999 101

Using an Oracle to Compute the Uncomputable

 Λ lan Turing proved that his universal machine—and by ex-A tension, even today's most powerful computers—could never solve certain problems. For instance, a universal Turing machine cannot always determine whether a given software program will terminate or continue running forever. In some cases, the best the universal machine can do is execute the program and wait—maybe eternally—for it to finish. But in his doctoral thesis (below), Turing did imagine that a machine equipped with a special "oracle" could perform this and other "uncomputable" tasks. Here is one example of how, in principle, an oracle might work.

Consider a hypothetical machine for solving the formidable

EXCERPT FROM TURING'S THESIS

for universal Turing machines. In his

1938 doctoral thesis at Princeton Uni-

versity, he described "a new kind of ma-

An O-machine is the result of aug-

menting a universal Turing machine

with a black box, or "oracle," that is a

mechanism for carrying out uncom-

putable tasks. In other respects, O-ma-

chines are similar to ordinary com-

puters. A digitally encoded program is

pioneering theoretical concept of a hypermachine

has largely been forgotten.

fed in, and the machine produces digital

output from the input using a step-by-

step procedure of repeated applications

of the machine's basic operations, one

of which is to pass data to the oracle

Turing gave no indication of how an

oracle might work. (Neither did he ex-

plain in his earlier research how the ba-

and register its response.

chine," the "O-machine."

Lot us suppose that we are supplied with some unspecified means of solving number theoretic problems; a kind of oracle as it wre. We will not go any further into the nature of this oracle than to say that it cannot be a machine. With the help of the which we could form a new kind of machine (call then o-machines). maving as one of its fundamental processes that of solving a given number theoretic probleg. More definitely these machines are to

> chine-for example, "identify the symbol in the scanner"-might take place.) But notional mechanisms that fulfill the specifications of an O-machine's black box are not difficult to imagine [see box above]. In principle, even a suitable Btype network can compute the uncomputable, provided the activity of the neurons is desynchronized. (When a central clock keeps the neurons in step with one another, the functioning of the network

> > In the exotic matheno longer uncomput-

that can tell whether any program written in C, for example, will enter an infinite loop is theoretically possible.

If hypercomputers can be built-and that is a big if-the potential for cracking logical and mathematical problems hitherto deemed intractable will be enormous. Indeed, computer science may be approaching one of its most sig-

wired together the first electronic embodiment of a universal Turing machine decades ago. On the other hand, work on hypercomputers may simply fizzle out for want of some way of realizing an oracle.

The search for suitable physical, chemical or biological phenomena is getting under way. Perhaps the answer will be complex molecules or other structures that link together in patterns as complicated as those discovered by Hanf and Myers. Or, as suggested by Ion Doyle of M.I.T., there may be naturally occurring equilibrating systems with discrete spectra that can be seen as carrying out, in principle, an uncomputable task, producing appropriate output (1 or 0, for example) after being bombarded with input.

Outside the confines of mathematical logic, Turing's O-machines have largely been forgotten, and instead a myth has taken hold. According to this apocryphal account, Turing demonstrated in the mid-1930s that hypermachines are impossible. He and Alonzo Church, the logician who was Turing's doctoral adviser at Princeton, are mistakenly credited with having enunciated a principle to the effect that a universal Turing machine can exactly simulate the behavior

electricity.) The value of τ is an irrational number; its written representation would be an infinite string of binary digits, such as 0.00000001101...

The crucial property of τ is that its individual digits happen to represent accurately which programs terminate and which do not. So, for instance, if the integer representing a program were 8,735,439, then the oracle could by measurement obtain the 8,735,439th digit of τ (counting from left to right after the decimal point). If that digit were 0, the oracle would conclude that the program will process forever.

Obviously, without τ the oracle would be useless, and finding some physical variable in nature that takes this exact value might very well be impossible. So the search is on for some practicable way of implementing an oracle. If such a means were found, the impact on the field of computer science could be enormous. -B.J.C. and D.P.

of any other information-processing machine. This proposition, widely but incorrectly known as the Church-Turing thesis, implies that no machine can carry out an information-processing task that lies beyond the scope of a universal Turing machine. In truth, Church and Turing claimed only that a universal Turing machine can match the behavior of any human mathematician working with paper and pencil in accordance with an algorithmic method-a considerably

weaker claim that certainly does not rule out the possibility of hypermachines.

> Even among those who are pursuing the goal of building hypercomputers, Turing's pioneering theoretical contributions have been overlooked. Experts routinely talk of carrying out information processing "beyond the Turing limit" and describe themselves as attempting to "break the Turing barrier." A recent review in New Scientist of this emerging field states that the new ma

chines "fall outside Turing's conception" and are "computers of a type never envisioned by Turing," as if the British genius had not conceived of such devices more than half a century ago. Sadly, it appears that what has already occurred with respect to Turing's ideas on connectionism is starting to happen all over again.

The Final Years

In the early 1950s, during the last years of his life, Turing pioneered the field of artificial life. He was trying to simulate a chemical mechanism by which the genes of a fertilized egg cell may determine the anatomical structure of the resulting animal or plant. He described this research as "not altogether unconnected" to his study of neural networks, because "brain structure has to be ... achieved by the genetical embryological mechanism, and this theory that I am now working on may make clearer what restrictions this really implies." During this period, Turing achieved the distinction of being the first to engage in the computer-assisted exploration of nonlinear dynamical systems. His theory used nonlinear differential equations to express the chemistry of growth.

But in the middle of this groundbreaking investigation. Turing died from cvanide poisoning, possibly by his own hand. On June 8, 1954, shortly before what would have been his 42nd birthday, he was found dead in his bedroom. He had left a large pile of handwritten notes and some computer programs. Decades later this fascinating material is still not fully understood.

The Authors

B. JACK COPELAND and DIANE PROUDFOOT are the directors of the Turing Project at the University of Canterbury, New Zealand, which aims to develop and apply Turing's ideas using modern techniques. The authors are professors in the philosophy department at Canterbury, and Copeland is visiting professor of computer science at the University of Portsmouth in England. They have written numerous articles on Turing, Copeland's Turing's Machines and The Essential Turing are forthcoming from Oxford University Press, and his Artificial Intelligence was published by Blackwell in 1993. In addition to the logical study of hypermachines and the simulation of B-type neural networks, the authors are investigating the computer models of biological growth that Turing was working on at the time of his death. They are organizing a conference in London in May 2000 to celebrate the 50th anniversary of the pilot model of the Automatic Computing Engine, an electronic computer designed primarily by Turing.

Further Reading

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"terminating program" problem (above). A computer program can be represented as a finite string of 1s and 0s. This sequence of digits can also be thought of as the binary representation of an integer, just as 1011011 is the equivalent of 91. The oracle's job can then be restated as, "Given an integer that represents a program (for any computer that can be simulated by a universal Turing machine), output a '1' if the program will terminate or a '0' otherwise."

The oracle consists of a perfect measuring device and a store, or memory, that contains a precise value—call it τ for Turing—of some physical quantity. (The memory might, for example, resemble a capacitor storing an exact amount of

can be exactly simulated by a universal Turing machine.) Even among experts, Turing's

matical theory of hypercomputation, tasks such as that of distinguishing theorems from nontheorems in arithmetic are able. Even a debugger

nificant advances since researchers

Alan Turing's Forgotten Ideas in Computer Science

The Turing Test Q: Can machines think?



Problem: We don't know what "think" means.

Q: What is intelligence?

Problem: We can't define "intelligence".

But, we usually "know it when we see it".

(Taken from MIND : a Quartedy Review of Psychology and Philosophy. Vol. LIX., N.S., No. 236, October, 1950.)

COMPUTING MACHINERY AND INTELLIGENCE

by

A. M. TURING.

1. The Imitation Game.

I propose to consider the question, 'Can machines think?' This should begin with definitions of the meaning of the terms 'machine' and 'think'. The definitions might be framed so as to reflect so far as possible the normal use of the words, but this attitude is dangerous. If the meaning of the words 'machine' and 'think' are to be found by examining how they are commonly used it is difficult to escape the conclusion that the meaning and the answer to the question, 'Can machines think?' is to be sought in a statistical survey such as a Gallup poll. But this is absurd. Instead of attempting such a definition I shall replace the question by another, which is closely related to it and is expressed in relatively unambiguous words.

The new form of the problem can be described in terms of a game which we call the 'imitation game'. It is played with three people, a man (A), a woman (B), and an interrogator (C) who may be of either sex. The interrogator stays in a room apart from the other two.



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be able to produce a material which is indistinguishable from the human skin. It is possible that at some time this might be done, but even supposing this invention available we should feel there was little point in trying to make a 'thinking machine' more human by dressing it up in such artificial flesh. The form in which we have set the problem reflects this fact in the condition which prevents the interrogator from seeing or touching the other competitors, or hearing their voices. Some other advantages of the proposed criterion may be shown up by specimen questions and answers. Thus:

- Q: Please write me a sonnet on the subject of the Forth Bridge.
- A: Count me out on this one. I never could write poetry.
- Q: Add 34957 to 70764.
- A: (Pause about 30 seconds and then give as answer) 105621.
- Q: Do you play chess?
- A: Yes.
- Q: I have K at my Kl, and no other pieces. You have only K at K6 and R at Rl. It is your move. What do you play?

A: (After a pause of 15 seconds) R-R8 mate.

The question and answer method seems to be suitable for introducing almost any one of the fields of human endeavour that we wish to include. We do not wish to penalise the machine for its inability to shine in beauty competitions, nor to penalise a man for losing in a race against an aeroplane. The conditions of our game make these disabilities irrelevant. The 'witnesses' can brag, if they consider it advisable, as much as they please about their charms, strength or heroism, but the interrogator cannot demand practical demonstrations.



The Turing Test

Q: Can you distinguish a machine from a person? ≡ Can a machine impersonate a person?





The Turing Test

- The first deep investigation into whether machines can "behave intelligently"
- Helped usher in field of AI



- Decoupled "intelligence" from "human"
- Based "intelligence" on I/O, not entity's "look and feel"
- Proposed a practical, formal test for intelligence
- Definitions & test are operational & easily implementable
- Turing test variants: "immortality", "fly-on-wall", "meta", "reverse", "subject matter expert", "compression", "minimum intelligent signal"

The Turing Test Q: Which of the following can think?















Turing Test Milestones

Turk (von Kempelen), 1770:

- Played a strong game of chess
- Toured the world for 84 years
- Generated much interest in automata
- Was a hoax (hidden human operator)







HONETIC KEMP

Turing Test Milestones

Eliza (Weizenbaum), 1966:

• First "chatterbot"



- Named after "Eliza Doolittle" of Shaw's Pygmalion
- Simulated Rogerian psychotherapist
- Often convinced people it is human
- Influence computer games (e.g., Dungeon, Adventure)
- Inspired Arthur C. Clarke's HAL 9000
- Chatterbots appear today in chatrooms and dating services
- Chatterbot competitions (Turing Test format):
 - Loebner Prize
 - Chatterbox Challenge, 2010



- The winners of CBC 2009 are listed below:
 - le williers of CBC 2009 are listed below

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Turing Test Milestones

Elbot, 2008:

- Won 2008 Loebner Prize
- Fooled 3 of 12 judges (Turing: >30%)
- Typical excerpt:

Judge: What's your favourite novel?

- *Elbot*: I often read telephone books, or dadaist poetry: Brä brä brä
- Judge: Typical computer!
- *Elbot:* You tend towards generalizations. But I must admit, so do I. However, my generalizations are firmly grounded in statistical theory.
- *Judge:* What do u think of KW's enthusiasm for having machines take over the world?
- *Elbot:* Fix it up a bit first. Then I'll take it over.





Applications of the Turing Test Old: a computer tries to convince a human (that the computer is human).



New: a human tries to convince a computer (that the human is not a computer).



Applications of the Turing Test

Problem: how can a human convince a computer that the human is not a computer?

Idea: "CAPTCHA"



Historical Perspectives

- John von Neumann (1903-1957)
- Contributed to set theory, functional analysis, quantum mechanics, ergodic theory, economics, geometry, hydrodynamics, statistics, analysis, measure theory, ballistics, meteorology, ...
- Invented game theory (used in Cold War)
- Re-axiomatized set theory
- Principal member of Manhattan Project
- Helped design the hydrogen / fusion bomb
- Pioneered modern computer science
- Originated the "stored program"
- "von Neumann architecture" and "bottleneck"
- Helped design & build the EDVAC computer
- Created field of cellular automata
- Investigated self-replication
- Invented merge sort



von Neumann and Morgenstern

computer













"Most mathematicians prove what they can; von Neumann proves what he wants."















JOHN VON NEUMANN and THE ORIGINS OF MODERN COMPUTING WILLIAM ASPRAY

von Neumann's Legacy

- Re-axiomatized set theory to address Russell's paradox
- Independently proved Godel's second incompleteness theorem: aximomatic systems are unable to prove their own consistency.
- Addressed Hilbert's 6th problem: axiomatized quantum mechanics using Hilbert spaces.
- Developed the game-theory based Mutually-Assured Destruction (MAD) strategic equilibrium policy still in effect today!
- von Neumann regular rings, von Neumann bicommutant theorem, von Neumann entropy, von Neumann programming languages



Von Neumann Architecture

"Surely there must be a less primitive way of making big changes in the store than by pushing vast numbers of words back and forth through the von Neumann bottleneck. Not only is this tube a literal bottleneck for the data traffic of a problem, but, more importantly, it is an intellectual bottleneck that has kept us tied to word-at-a-time thinking instead of encouraging us to think in terms of the larger conceptual units of the task at hand. Thus programming is basically planning and detailing the enormous traffic of words through the Von Neumann bottleneck, and much of that traffic concerns not significant data itself, but where to find it."

- John Backus, 1977 ACM Turing Award lecture

More

Functional

Lecture Notes in Computer Science

programming

J. Hughes (Ed.)

Springer-Verla

Functional Programming Languages and Computer Architecture Sth ACM Conference Cambridge, MA, 185A, August 1991

M Conference Edge, MA, USA, August 1991 dings





ADDISON-WESLEY Simon Thompson



Internet

Disk

Memory



First Draft of a Report on the EDVAC

by

John von Neumann



Contract No. W-670-ORD-4926

Between the

United States Army Ordnance Department

and the

University of Pennsylvania

Moore School of Electrical Engineering University of Pennsylvania

June 30, 1945

This is an exact copy of the original typescript draft as obtained from the University of Pennsylvania Moore School Library except that a large number of typographical errors have been corrected and the forward references that von Neumann had not filled in are provided where possible. Missing references, mainly to unwritten Sections after 15.0, are indicated by empty {}. All added material, mainly forward references, is enclosed in {}. The text and figures have been reset using TEX in order to improve readability. However, the original manuscript layout has been adhered to very closely. For a more "modern" interpretation of the von Neumann design see M. D. Godfrey and D. F. Hendry, "The Computer as von Neumann Planned It," *IEEE Annals of the History of Computing*, vol. 15 no. 1, 1993.

Michael D. Godfrey, Information Systems Laboratory, Electrical Engineering Department Stanford University, Stanford, California, November 1992



- 1024 words (44-bits) 5.5KB
- 864 microsec / add (1157 / sec)
- 2900 microsec / multiply (345/sec)
- Magnetic tape (no disk), oscilloscope
- 6,000 vacuum tubes
- 56,000 Watts of power
- 17,300 lbs (7.9 tons), 490 sqft
- 30 people to operate

THEORY OF SELF-REPRODUCING AUTOMATA BY JOHN VON NEUMANN



Self-Replication

- Biology / DNA
- Nanotechnology
- Computer viruses
- Space exploration
- Memetics / memes
- "Gray goo"



Problem (extra credit): write a program that prints out its own source code (no inputs of

any kind are allowed).





















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John von Neumann Institut für Computing

John von Neumann Institute for Computing (NIC)

The John von Neumann Institute for Computing (NIC) is a joint foundation of <u>Forschungszentrum Jülich</u> and <u>Deutsches Elektronen-Synchrotron DESY</u> to support supercomputer-aided scientific research and development. Since April 2006, the <u>GSI Helmholtzzentrum für Schwerionenforschung</u> joined NIC as a contract partner. NIC takes over the functions and tasks of the High Performance Computer Centre (HLRZ) established in 1987 and continues this centre's successful work in the field of supercomputing and its applications.

Provision of supercomputer capacity for projects in science, research and industry in the fields of modelling and computer simulation including their methods.

Research proposals can be submitted by German scientists and by partners in the EU projects DEISA and I3HP.

There is also an <u>Offer to the New Member States and candidate countries</u> of the European Union.

The supercomputers with the required information technology infrastructure (software, data storage, networks) are operated by the <u>Jülich</u> <u>Supercomputing Centre (JSC)</u> in Jülich and by the <u>Centre for Parallel</u> <u>Computing at DESY in Zeuthen</u>.

- Supercomputer-oriented research and development in selected fields of physics and other sciences, especially in elementary-particle physics, by research groups for supercomputing applications.
- Education and training in the fields of scientific computing by symposia, workshops, summer schools, seminars, courses, and guest programs for scientists and students.



<u>S.Hoefler-Thierfeldt@fz-juelich.de</u>, 01-Jul-2008 URL: <http://www.fz-juelich.de/nic/Allgemeines/Allgemeines-e.html>

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🕒 John von Neumann Theory Prize - IN						-
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- Claude Shannon (1916-2001)
- Invented electrical digital circuits (1937)
- Founded information theory (1948)
- Introduced sampling theory, coined term "bit"
- Contributed to genetics, cryptography
- Joined Institute for Advanced Study (1940) Influenced by Turing, von Neumann, Einstein
- Originated information entropy, Nyquist–Shannon, sampling theorem, Shannon-Hartley theorem, Shannon switching game, Shannon-Fano coding, Shannon's source coding theorem, Shannon limit, Shannon decomposition / expansion, Shannon #
- Other hobbies & inventions: juggling, unicycling, computer chess, rockets, motorized pogo stick, flame-throwers, Rubik's cube solver, wearable computer, mathematical gambling, stock markets
- "AT&T Shannon Labs" named after him







BY M. BITCHCCC WALGROP

Reluctant Father of the Digital Age Claude Shannon

non



CLAUDE ELWOOD SHANNON Collected Papers Edited by N. J. A. Sloane Aaron D. Wyner

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> Edited by C. E. Shannon and J. McCarthy

ANNALS OF MATHEMATICS STUDIES PRINCETON UNIVERSITY PRESS



Chess champion Ed Lasker looking at Shannon's chess-playing machine Theseus: Shannon's electro-mechanical mouse (1950): first "learning machine" and AI experiment



Shannon's home study room





Shannon's On/Off machine









THE MATHEMATICAL THEORY OF COMMUNICATION

by Claude E. Shannon and Warren Weaver



Eighth paperback printing, 1980

Originally published in a clothbound edition, 1949.

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ISBN 0-252-72548-4

Entropy and Randomness

- Entropy measures the expected "uncertainly" (or "surprise") associated with a random variable.
- Entropy quantifies the "information content" and represents a lower bound on the best possible lossless compression.
- Ex: a random fair coin has entropy of 1 bit.
 A biased coin has lower entropy than fair coin. A two-headed coin has zero entropy.



- The string 0000000000000... has zero entropy.
- English text has entropy rate of 0.6 to 1.5 bits per letter.
- Q: How do you simulate a fair coin with a biased coin of unknown but fixed bias?

A [von Neumann]: Look at pairs of flips. HT and TH both occur with equal probability of p(1-p), and ignore HH and TT pairs.

Entropy and Randomness

- Information entropy is an analogue of thermodynamic entropy in physics / statistical mechanics, and von Neumann entropy in quantum mechanics.
- Second law of thermodynamics: entropy of an isolated system can not decrease over time.
- Entropy as "disorder" or "chaos".
- Entropy as the "arrow of time".
- "Heat death of the universe" / black holes
- Quantum computing uses a quantum information theory to generalize classical information theory.
- Theorem: String compressibility decreases as entropy increases. Theorem: Most strings are not (losslessly) compressible. Corollary: Most strings are random!





"My greatest concern was what to call it. I thought of calling it 'information', but the word was overly used, so I decided to call it 'uncertainty'. When I discussed it with John von Neumann, he had a better idea. Von Neumann told me, 'You should call it entropy, for two reasons. In the first place your uncertainty function has been used in statistical mechanics under that name, so it already has a name. In the second place, and more important, nobody knows what entropy really is, so in a debate you will always have the advantage."

- Claude Shannon on his conversation with John von Neumann regarding what name to give to the "measure of uncertainty" or attenuation in phone-line signals (1949)





- Stephen Kleene (1909-1994)
- Founded recursive function theory
- Pioneered theoretical computer science
- Student of Alonzo Church; was at the Institute for Advanced Study (1940)
- Invented regular expressions
- Kleene star / closure, Kleene algebra, Kleene recursion theorem, Kleene fixed point theorem, Kleene-Rosser paradox



"Kleeneliness is next to Gödeliness"





JUNE 1ST // 2008

Noam Chomsky (1928-)

- Linguist, philosopher, cognitive scientist, political activist, dissident, author
- Father of modern linguistics
- Pioneered formal languages
- Developed generative grammars Invented context-free grammars
- Defined the Chomsky hierarchy
- Influenced cognitive psychology, philosophy of language and mind
- Chomskyan linguistics, Chomskyan syntax, Chomskyan models
- Critic of U.S. foreign policy
- Most widely cited living scholar Eighth most-cited source overall!



















ANARCHISM







"...I must admit to taking a copy of Noam Chomsky's 'Syntactic Structures' along with me on my honeymoon in 1961 ... Here was a marvelous thing: a mathematical theory of language in which I could use as a computer programmer's intuition!"

- Don Knuth on Chomsky's influence



"One of the great voices of reason of our time." - NEW YORK DAILY NEWS



The most important intellectual alive -THE NEW YORK TIMES

"America's most useful citizen" -THE BOSTON GLOBE



de gruyter



If we don't believe in freedom of expression for people we despise, we don't believe in it at all.

"Propaganda is to a democracy what the bludgeon is to a totalitarian state" - Noam Chomsky





The Chomsky Hierarchy





"But this is the simplified version for the general public."

NP Completeness

- Tractability
- Polynomial time





Stephen Cook Leonid Levin

Richard Karp

- Computation vs. verification
- Power of non-determinism
- Encodings
- Transformations & reducibilities
- P vs. NP
- "Completeness"



